

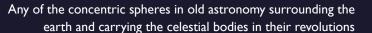
Black hole orbiter (Orb)

Samuel Amrich

Dominik Pavlov

Lukáš Randuška

Filip Stempel



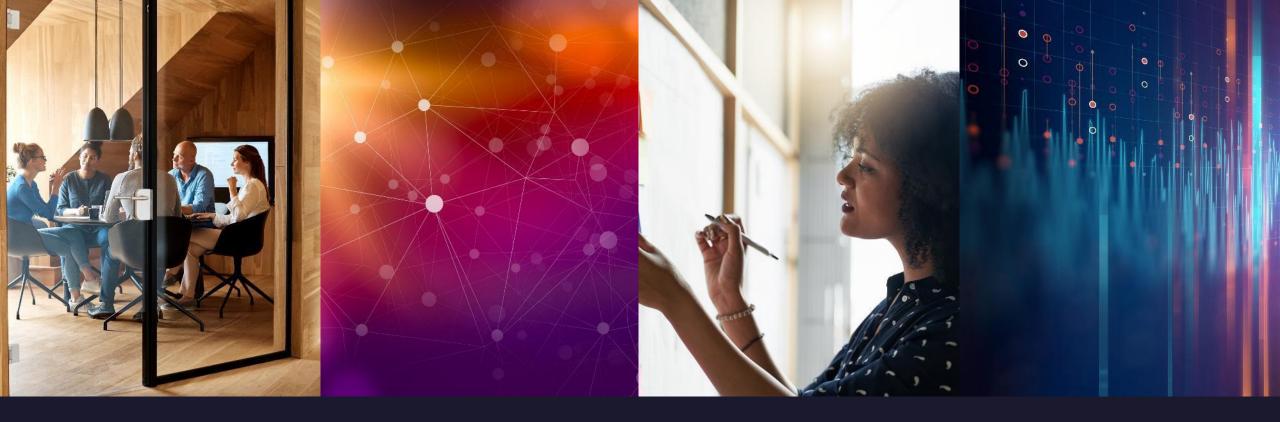
WHY?

- Dostali sme to ako zadanie
- Kvalitných simulátorov
 - GC je žalostne málo
- Je to výzva!









Introduction

Aneb jak tím A* k Orbu došiel

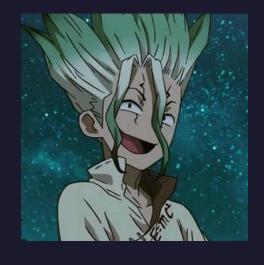
Tím



Team







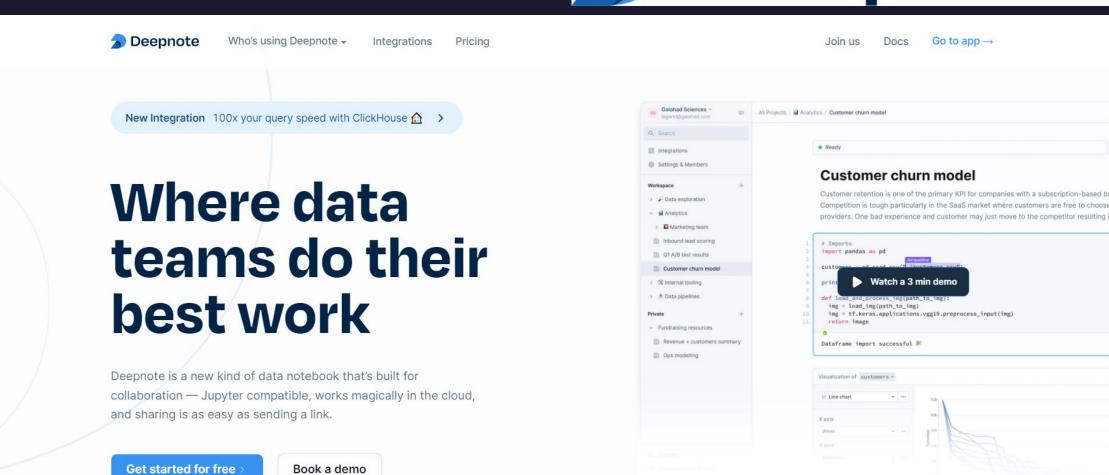


Dominik Pavlov Samuel Amrich Filip Stempel Lukáš Randuška

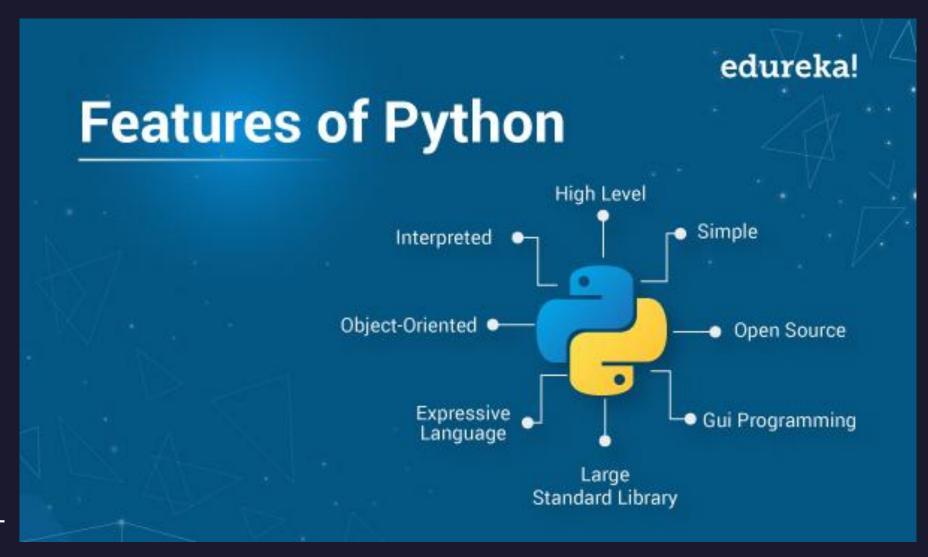
Prostredie







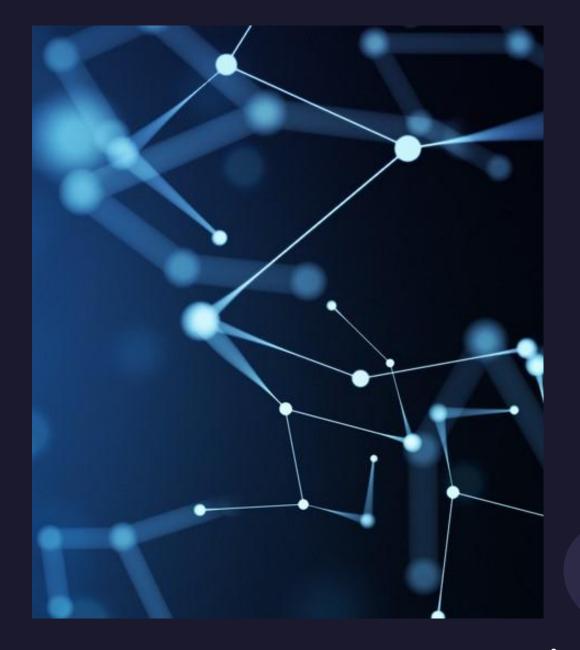
Python





Nie je to C++

Problém



Globular cluster (GC)



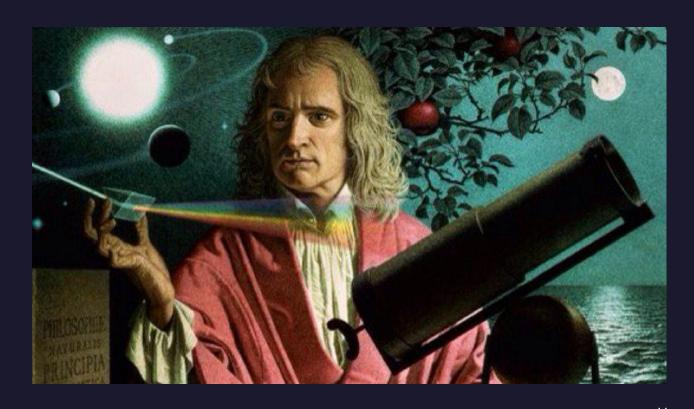
Newtonovská gravitácia

$$\vec{F} = -G \frac{M_1 \cdot M_2}{r^2} \vec{e_r}$$

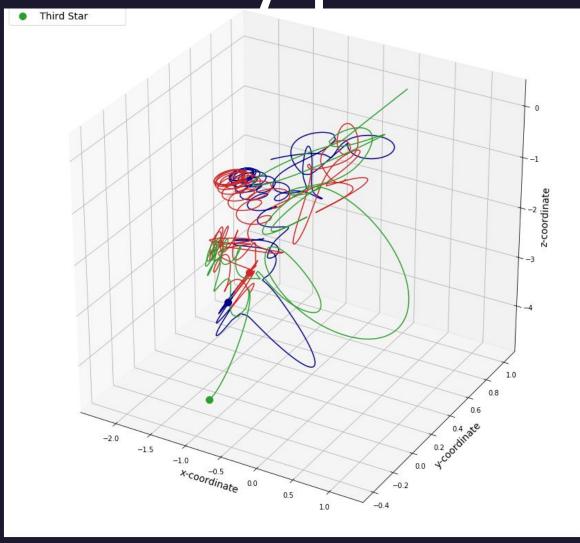
Okamžitý prenos informácie

Univerzálna sila

Jediná uvažovaná sila



N-body problem



Analyticky neriešiteľné

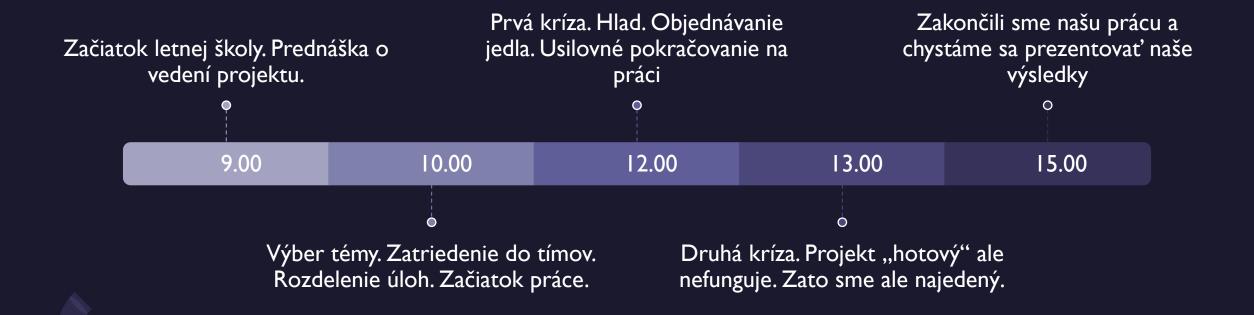
Výpočetne náročné

Vedecky podstatné

Riešenie



Timeline



24.08.2022 Black hole orbiter

Počiatočné podmienky

- Hmotnost' $M = 2 \cdot 10^5 M_{\odot}$
- Polomer R = 50 ly
- Počet hviezd $N = 330\ 000$
- Zgranulovanie gran = 1000
- Doba simulácie T = 1000 000
- Časový krok dt = 1000



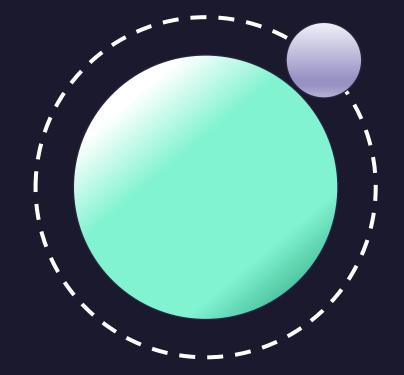
Rozdelenie hmotnosti a polôh

HUSTOTNÉ ROZDELENIE

• $\rho(r) = \frac{3M}{4\pi a^3 \left(1 + \frac{r^2}{a^2}\right)^{\frac{5}{2}}}$

PRIESTOROVÉ ROZDELENIE

 Prechod od spojitého rozdelenia hustoty k diskrétnym hmotnostiam

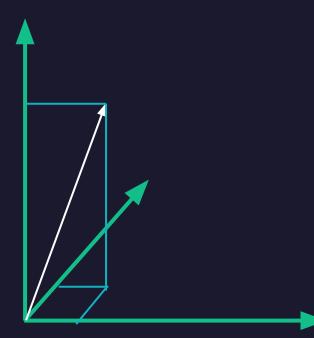


Náhodné rozdelenie rýchlosti

ROZDELENIE VEĽKOSTI RÝCHLOSTI

•
$$v(r) = \left(1 - \frac{r}{R + 0.5}\right) \cdot 15km/s$$

NÁHODNÝ PRIEMET





Black hole orbiter

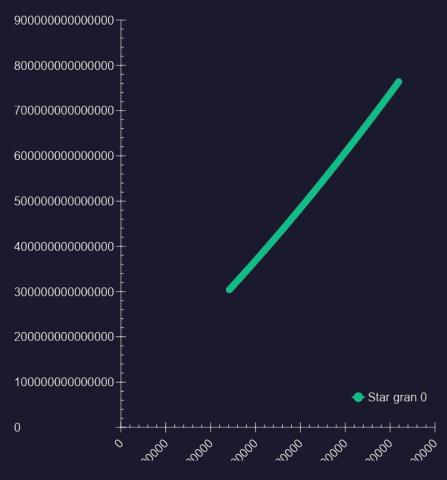
Kód

```
import random as rnd
 import numpy as np
import tensorflow as tf
Format dat
[[[x1, y1, z1], [x2, y2, z2], [x3, y3, z3], ..., [x1000, y1000, z1000]], v case 0
[[x1, y1, z1], [x2, y2, z2], [x3, y3, z3], ..., [x1000, y1000, z1000]], v case 1
[[x1, y1, z1], [x2, y2, z2], [x3, y3, z3], ..., [x1000, y1000, z1000]]] v case 100000
# Vygeneruje nahodne projekcie pre jednu zadanu rychlost
def vel_projection(vel):
    velx = rnd.randrange(np.floor(vel))
    vely = rnd.randrange(np.floor(np.sqrt(vel*vel - velx*velx)))
    velz = np.sqrt(vel*vel - velx*velx - vely*vely)
    return np.array([velx, vely, velz])
 # Vygeneruje nahodne projekcie pre numpy array rychlosti
def vel_projections(vel):
    velx = np.random.random()*np.floor(vel)
     vely = np.random.random()*np.floor(np.sqrt(vel*vel - velx*velx))
     velz = np.sqrt(vel*vel - velx*velx - vely*vely)
    return velx, vely, velz
```

```
# Pociatocne podmienky M92
M = 4*(10**35) # Hmotnost gulovej hviezdokopy v kg
R = 5*(10**16) # Polomer hviezdokopv v m
N = 330000 # Pocet hviezd v hviezdokope
gran = 1000 # Kolko hviezd reprezentuje jeden bod (granula)
n = N//gran # Prvy odhad Pocet bodov do simulacie
m = M/gran # Hmotnost jednej granule v kg
G = 6.6743*10**(-11) # Gravitacna konstanta
a = 0.6*R # Plumerova sfera
dt = 1000*365*24*60*60 # Casovy krok
T = 1000000*365*24*60*60 # Doba simulacie
Q = T//dt # Pocet krokov simulacie
# Generovanie pociatocnich dat
pos, n = gen_pos(M=M, R=R, n=n, m=m, a=a)
vel = gen_vel(R=R, n=n, pos=pos)
vel = vel_vari(vel, delta=0.05)
# get acceleration based on gravitational pull and update sub-clusters (granule) postions
def tf_delete(tensor,index,row=True):
    if row:
        sub = list(range(tensor.shape[0]))
    else:
        sub = list(range(tensor.shape[1]))
    sub.pop(index)
        return tf.gather(tensor, sub)
    return tf.transpose(tf.gather(tf.transpose(tensor), sub))
def acc_by_G_pull(pos, m, G, dt, vel):
```

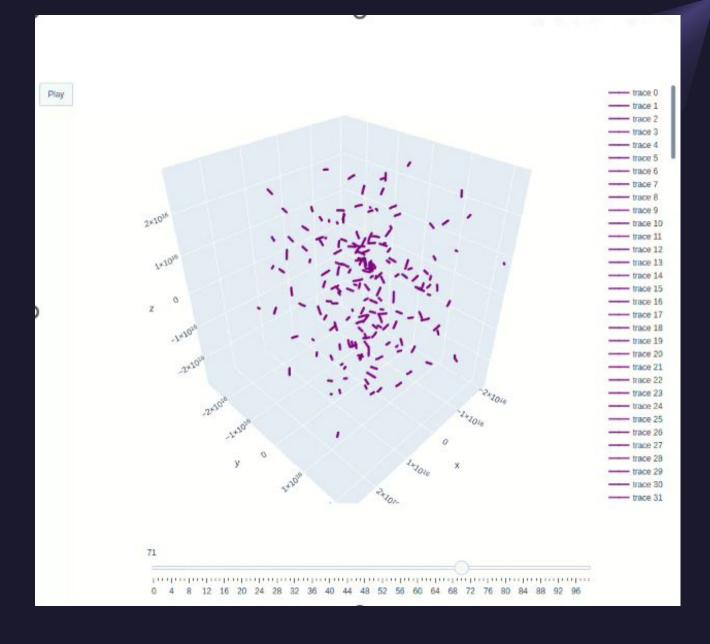
```
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       sub = list(range(tensor.shape[0]))
       sub = list(range(tensor.shape[1]))
   sub.pop(index)
   if row:
       return tf.gather(tensor, sub)
   return tf.transpose(tf.gather(tf.transpose(tensor),sub))
def acc_by_G_pull(pos, m, G, dt, vel):
   pos_tf = tf.convert_to_tensor(pos, dtype=tf.float64)
   trans_pos = tf.transpose(pos_tf)
   m_temp = tf.convert_to_tensor(m, dtype=tf.float64)
   m_tf = tf.fill(pos_tf.shape, m_temp)
   G_tf = tf.convert_to_tensor(G, dtype=tf.float64)
   vel_tf = tf.convert_to_tensor(vel, dtype=tf.float64)
   x = pos_tf[:, 0:1]
   y = pos_tf[:, 1:2]
   z = pos_tf[:, 2:3]
   dx = tf.transpose(x) - x
   dy = tf.transpose(y) - y
   dz = tf.transpose(z) - z
   inv_r3 = (dx ** 2 + dy ** 2 + dz ** 2 + 0.1 ** 2) ** (-1.5)
   ax = G_tf * (dx * inv_r3) @ m_tf
   ay = G_tf * (dy * inv_r3) @ m_tf
   az = G tf * (dz * inv r3) @ m tf
   ax = tf_delete(ax, 1, False)
   ax = tf_delete(ax, 1, False)
   ay = tf_delete(ay, 1, False)
   ay = tf_delete(ay, 1, False)
   az = tf_delete(az, 1, False)
   az = tf_delete(az, 1, False)
   a = tf.concat([ax, ay, az], axis=1)
   vel += a.numpy() * dt / 2.0
   pos += vel * dt
   return vel, pos
acc_by_G_pull(pos, m, G, dt, vel)
```

Semi výsledky



24.08.2022

Lepšie výsledky



24.08.2022

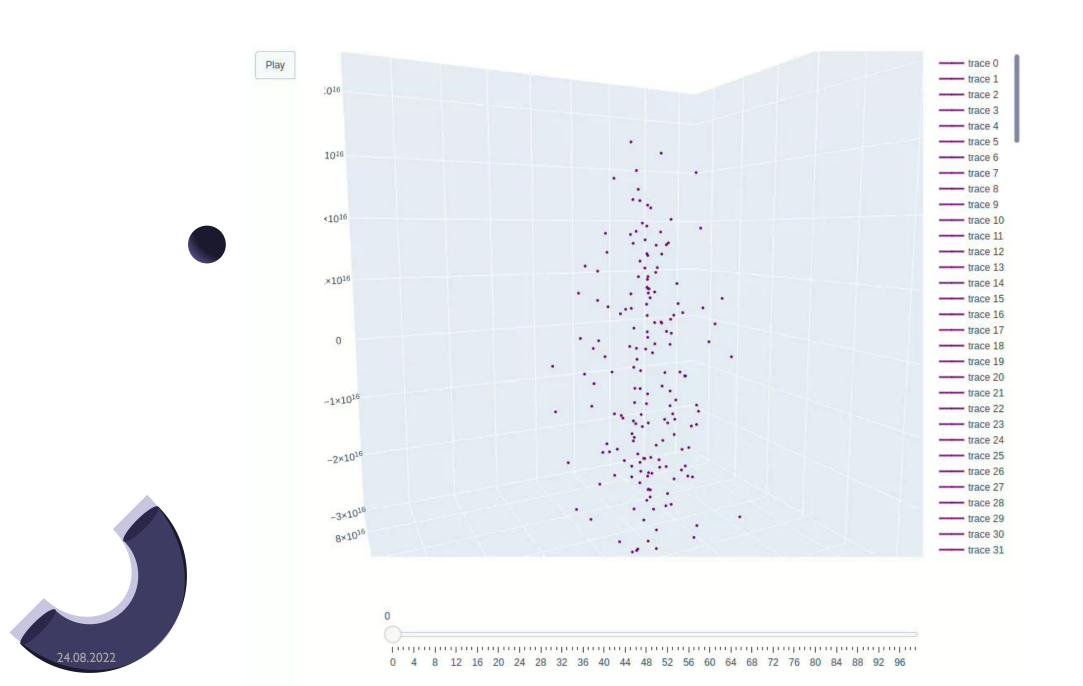
Play 24.08.2022



Play









For the future

ABY SIMULÁCIA FUNGOVALA

/

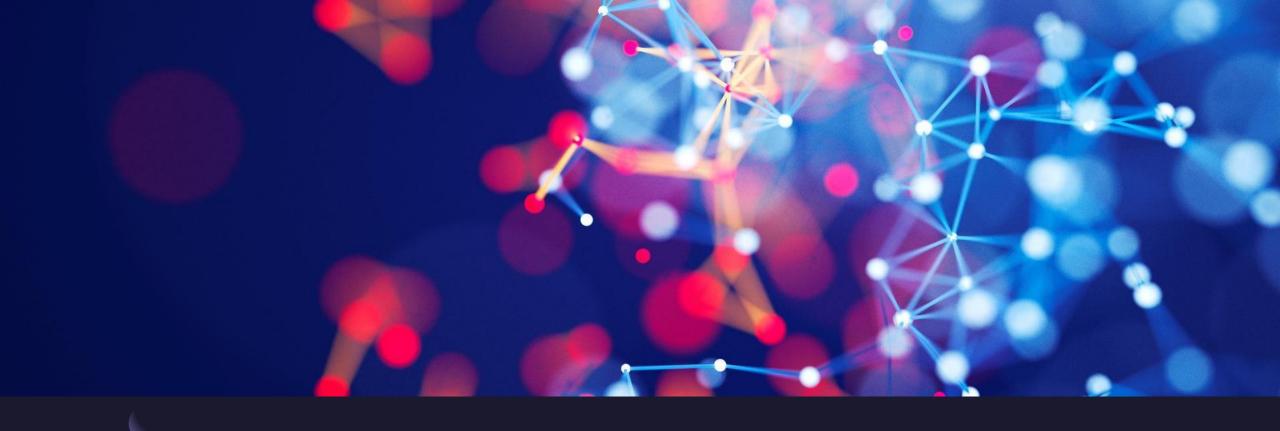
DASH VIZUALIZÁCIE

DODATOČNÉ VYLEPŠENIA









Záver

Ďakujem Vám za pozornosť

