Homework 4

April 8, 2018

Task 1

$$\begin{array}{l} \left(\left(\lambda a. (\lambda b.b\,b) \, (\lambda b.b\,b) \right) b \right) \left(\left(\lambda c. (c\,b) \right) \, (\lambda a.a) \right) \ \rightarrow_{\beta} \ \left(\left(\lambda b.b\,b \right) \, (\lambda b.b\,b) \right) \left(\left(\lambda c. (c\,b) \right) \, (\lambda a.a) \right) \ \rightarrow_{\beta} \\ \left(\left(\lambda b.b\,b \right) \, (\lambda b.b\,b) \right) \left(\left(\lambda a.a \right) b \right) \ \rightarrow_{\beta} \ \left(\left(\lambda b.b\,b \right) \, (\lambda b.b\,b) \right) b \end{array}$$

Task 2

S K K =
$$(\lambda x\,y\,z\,.x\,z\,(y\,z))$$
 $(\lambda x\,y.x)$ $(\lambda x\,y.x)$ \to $\lambda z.((\lambda x\,y.x)\,z\,((\lambda x\,y.x)\,z))$ \to $\lambda z.((\lambda x\,y.x)\,z\,z)$ \to $\lambda z.z$ = I