# **Exploring Data**

September 26, 2017

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# Tentative Class Agenda

- Class 1 (9/12) Introduction to data science
- Class 2 (9/19) Python basic
- Class 3 (9/26) Introduction to data, HW#1
- Class 4 (10/3) More on data, OLAP
   No class on 10/10
- Class 5 (10/17) Python ML library scikit-learn, HW#2 (using scikit-learn)
- Class 6 (10/24) PCA/SVD, Text and Web data, project announcement
- Class 7 (10/31) Introduction to data mining: classification,

## Tentative Class Agenda (cont'd)

- Class 8 (11/7) Association mining
- Class 9 (11/14) Clustering, brief on Keras and Tensorflow HW#3 (using Keras and Tensorflow)
- Class 10 (11/21) Social network, (project abs. due on 11/19)
- Class 11 (11/28) R-1
- Class 12 (12/5) R-2, HW#4 (data mining with R)
- Class 13 –(12/12) Exam (in class, closed book)
- Class 14 (12/19) Cloud computing, Introduction to GPU programming, HW#5
- Class 15 (12/26) Project presentation I
- Class 16 (1/2) Project presentation II

Happy New Year!

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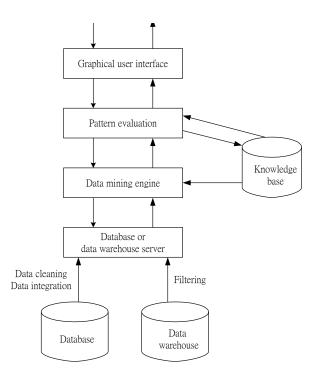
## Class Announcement

- A class Web page is ready
  - Ceiba
- TA: 謝有恒, 蔡仕竑; 吳齊軒 (for R)
- Grading (tentative):
  - HW 45%
    - 5 in total
  - Midterm 25% (in class, closed book)
  - Project 30% (including 5% on abstract, 5% on presentation)
  - Final grades will be adjusted based on overall scores.
  - Class performance +-...

## **Course Materials**

- Introduction to data science
- Exploring Data
- Mining data
  - Classification, association, and clustering
- Data manipulation at Scale

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# Description on Data (Chapter 2-3 in Vipin's book)

# What is Data?

• Collection of data objects and their attributes

- An attribute is a property or characteristic of an object
  - Examples: eye color of a person, temperature, etc.
  - Attribute is also known as variable, field, characteristic or feature
- A collection of attributes describe an object
  - Object is also known as record, point, case, sample, entity, or instance

#### **Attributes**

			$\sim$		
_	Tid	Refund	Marital Status	Taxable Income	Cheat
	1	Yes	Single	125K	No
	2	No	Married	100K	No
	3	No	Single	70K	No
	4	Yes	Married	120K	No
	5	No	Divorced	95K	Yes
١	6	No	Married	60K	No
	7	Yes	Divorced	220K	No
	8	No	Single	85K	Yes
	9	No	Married	75K	No
	10	No	Single	90K	Yes

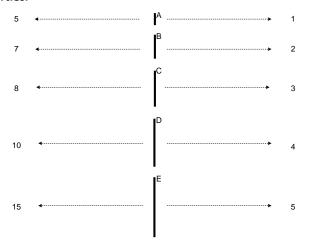
## **Attribute Values**

- Attribute values are numbers or symbols assigned to an attribute
- Distinction between attributes and attribute values
  - Same attribute can be mapped to different attribute values
    - Example: height can be measured in feet or meters
  - Different attributes can be mapped to the same set of values
    - Example: Attribute values for ID and age are integers
    - But properties of attribute values can be different
      - ID has no limit but age has a maximum and minimum value

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# Measurement of Length

 The way you measure an attribute may somewhat not match the attributes properties.



## Types of Attributes

- There are different types of attributes
  - Nominal
    - Examples: ID numbers, eye color, zip codes
  - Ordinal
    - Examples: rankings (e.g., taste of potato chips on a scale from 1-10), grades, height in {tall, medium, short}
  - Interval
    - Examples: calendar dates, temperatures in Celsius or Fahrenheit.
  - Ratio
    - Examples: temperature in Kelvin, length, time, counts

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## **Properties of Attribute Values**

- The type of an attribute depends on which of the following properties it possesses:
  - Distinctness:  $= \neq$
  - Order: < >
  - Addition: + ·
  - Multiplication: \* /
  - Nominal attribute: distinctness
  - Ordinal attribute: distinctness & order
  - Interval attribute: distinctness, order & addition
  - Ratio attribute: all 4 properties

Attribute Type	Description	Examples	Operations
Nominal	The values of a nominal attribute are just different names, i.e., nominal attributes provide only enough information to distinguish one object from another. (=, \neq)	zip codes, employee ID numbers, eye color, sex: {male, female}	mode, entropy, contingency correlation, $\chi^2$ test
Ordinal	The values of an ordinal attribute provide enough information to order objects. (<, >)	hardness of minerals, {good, better, best}, grades, street numbers	median, percentiles, rank correlation, run tests, sign tests
Interval	For interval attributes, the differences between values are meaningful, i.e., a unit of measurement exists.	calendar dates, temperature in Celsius or Fahrenheit	mean, standard deviation, Pearson's correlation, <i>t</i> and <i>F</i> tests
Ratio	For ratio variables, both differences and ratios are meaningful. (*, /)	temperature in Kelvin, monetary quantities, counts, age, mass, length, electrical current	geometric mean, harmonic mean, percent variation

# Discrete and Continuous **Attributes**

#### Discrete Attribute

- Has only a finite or countably infinite set of values
- Examples: zip codes, counts, or the set of words in a collection of documents
- Often represented as integer variables.
- Note: binary attributes are a special case of discrete attributes

#### Continuous Attribute

- Has real numbers as attribute values
- Examples: temperature, height, or weight.
- Practically, real values can only be measured and represented using a finite number of digits.
- Continuous attributes are typically represented as floating-point variables.

# Types of data sets

#### Record

- Data Matrix
- Document Data
- Transaction Data

#### Graph

- World Wide Web
- Molecular Structures

#### Ordered

- Spatial Data
- Temporal Data
- Sequential Data
- Genetic Sequence Data

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## Important Characteristics of Structured Data

- Dimensionality
  - Curse of Dimensionality
- Sparsity
  - Only presence counts
- Resolution
  - Patterns depend on the scale

## **Record Data**

 Data that consists of a collection of records, each of which consists of a fixed set of attributes

Tid	Refund	Marital Status	Taxable Income	Cheat
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
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8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

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## Data Matrix

- If data objects have the same fixed set of numeric attributes, then the data objects can be thought of as points in a multidimensional space, where each dimension represents a distinct attribute
- Such data set can be represented by an m by n matrix, where there are m rows, one for each object, and n columns, one for each attribute

Projection of x Load	Projection of y load	Distance	Load	Thickness
10.23	5.27	15.22	2.7	1.2
12.65	6.25	16.22	2.2	1.1

## **Document Data**

- Each document becomes a 'term' vector,
  - each term is a component (attribute) of the vector,
  - the value of each component is the number of times the corresponding term occurs in the

locument.	team	coach	pla y	ball	score	game	n <u>¥</u> .	lost	timeout	season
Document 1	3	0	5	0	2	6	0	2	0	2
Document 2	0	7	0	2	1	0	0	3	0	0
Document 3	0	1	0	0	1	2	2	0	3	0

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### **Transaction Data**

- A special type of record data, where
  - each record (transaction) involves a set of items.
  - For example, consider a grocery store. The set of products purchased by a customer during one shopping trip constitute a transaction, while the individual products that were purchased are the items.

TID Items

1 Bread, Coke, Milk

2 Beer, Bread

3 Beer, Coke, Diaper, Milk

4 Beer, Bread, Diaper, Milk

5 Coke, Diaper, Milk

# Types of data sets

#### Record

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#### Graph

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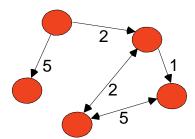
#### Ordered

- Spatial Data
- Temporal Data
- Sequential Data
- Genetic Sequence Data

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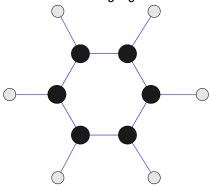
# **Graph Data**

- Many data could be represented by a graph structure
  - Examples: Web graph and HTML Links
- A directed graph with links labelled



## **Chemical Data**

• Benzene Molecule: C<sub>6</sub>H<sub>6</sub>



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# Types of data sets

#### Record

- Data Matrix
- Document Data
- Transaction Data

#### Graph

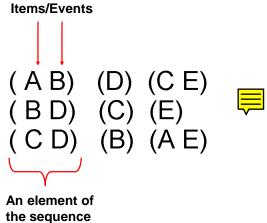
- World Wide Web
- Molecular Structures

#### Ordered

- Spatial Data
- Temporal Data
- Sequential Data
- Genetic Sequence Data

## **Ordered Data**

Sequences of transactions



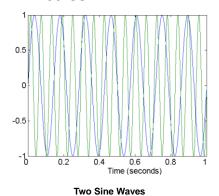
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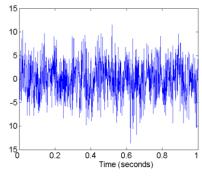
# **Data Quality**

- What kinds of data quality problems?
- How can we detect problems with the data?
- What can we do about these problems?
- Examples of data quality problems:
  - Noise and outliers
  - missing values
  - duplicate data

## Noise

- Noise refers to modification of original values
  - Examples: distortion of a person's voice when talking on a poor phone and "snow" on television screen



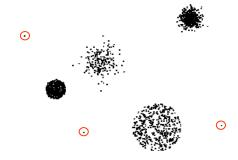


Two Sine Waves + Noise

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## **Outliers**

 Outliers are data objects with characteristics that are considerably different than most of the other data objects in the data set



## Missing Values

- · Reasons for missing values
  - Information is not collected (e.g., people decline to give their age and weight)
  - Attributes may not be applicable to all cases (e.g., annual income is not applicable to children)
- Handling missing values
  - Eliminate Data Objects
  - Estimate Missing Values
  - Ignore the Missing Value During Analysis
  - Replace with all possible values (weighted by their probabilities)

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# **Duplicate Data**

- Data set may include data objects that are duplicates, or almost duplicates of one another
  - Major issue when merging data from heterogeous sources
- Examples:
  - Same person with multiple email addresses
- Data cleaning
  - Process of dealing with duplicate data issues

## **Data Preprocessing**

- Aggregation
- Sampling
- Dimensionality Reduction
- Feature subset selection
- Feature creation
- Discretization and Binarization
- Attribute Transformation

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# Aggregation

- Combining two or more attributes (or objects) into a single attribute (or object)
- Purpose
  - Data reduction
    - · Reduce the number of attributes or objects
  - Change of scale
    - Cities aggregated into regions, states, countries, etc
  - More "stable" data
    - · Aggregated data tends to have less variability

## Sampling

- Sampling is the main technique employed for data selection.
  - It is often used for both the preliminary investigation of the data and the final data analysis.
- Statisticians sample because obtaining the entire set of data of interest is too expensive or time consuming.
- Sampling is used in data mining because processing the entire set of data of interest is too expensive or time consuming.

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## Sampling ...

- The key principle for effective sampling is the following:
  - using a sample will work almost as well as using the entire data sets, if the sample is representative
  - A sample is representative if it has approximately the same property (of interest) as the original set of data

## **Types of Sampling**

- · Simple Random Sampling
  - There is an equal probability of selecting any particular item
- Sampling without replacement
  - As each item is selected, it is removed from the population
- · Sampling with replacement
  - Objects are not removed from the population as they are selected for the sample. In sampling with replacement, the same object can be picked up more than once
- Stratified sampling
  - Split the data into several partitions; then draw random samples from each partition

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# Sample Size







8000 points

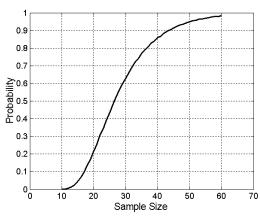
2000 Points

500 Points

## Sample Size

• What sample size is necessary to get at least one object from each of 10 groups.

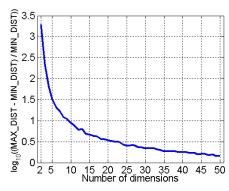




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# **Curse of Dimensionality**

- When dimensionality increases, data becomes increasingly sparse in the space that it occupies
- Definitions of density and distance between points, which is critical for clustering and outlier detection, become less meaningful



- · Randomly generate 500 points
- Compute difference between max and min distance between any pair of points

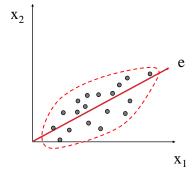
## **Dimensionality Reduction**

- Purpose:
  - Avoid curse of dimensionality
  - Reduce amount of time and memory required by data mining algorithms
  - Allow data to be more easily visualized
  - May help to eliminate irrelevant features or reduce noise
- Techniques
  - Principle Component Analysis
  - Singular Value Decomposition
  - Others: supervised and non-linear techniques

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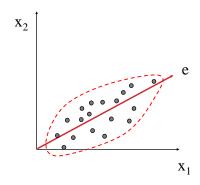
# **Dimensionality Reduction: PCA**

 Goal is to find a projection that captures the largest amount of variation in data



## **Dimensionality Reduction: PCA**

- Find the eigenvectors of the covariance matrix
- The eigenvectors define the new space



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### **Feature Subset Selection**

- Another way to reduce dimensionality of data
- Redundant features
  - duplicate much or all of the information contained in one or more other attributes
  - Example: purchase price of a product and the amount of sales tax paid
- Irrelevant features
  - contain no information that is useful for the data mining task at hand
  - Example: students' ID is often irrelevant to the task of predicting students' GPA

## **Feature Subset Selection**

- Techniques:
  - Brute-force approch:
    - Try all possible feature subsets as input to data mining algorithm
  - Embedded approaches:
    - Feature selection occurs naturally as part of the data mining algorithm
  - Filter approaches:
    - Features are selected before data mining algorithm is run
  - Wrapper approaches:
    - Use the data mining algorithm as a black box to find best subset of attributes

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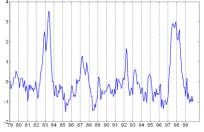
### **Feature Creation**

- Create new attributes that can capture the important information in a data set much more efficiently than the original attributes
- Three general methodologies:
  - Feature Extraction
    - · domain-specific
  - Mapping Data to New Space
  - Feature Construction
    - combining features

## **Attribute Transformation**

- A function that maps the entire set of values of a given attribute to a new set of replacement values such that each old value can be identified with one of the new values
  - Simple functions:  $x^k$ , log(x),  $e^x$ , |x|

- Standardization and Normalization



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## Similarity and Dissimilarity

- Similarity
  - Numerical measure of how alike two data objects are.
  - Is higher when objects are more alike.
  - Often falls in the range [0,1]
- Dissimilarity
  - Numerical measure of how different are two data objects
  - Lower when objects are more alike
  - Minimum dissimilarity is often 0
  - Upper limit varies
- Proximity refers to a similarity or dissimilarity

#### Similarity/Dissimilarity for Simple Attributes

p and q are the attribute values for two data objects.

Attribute	Dissimilarity	Similarity
Type		
Nominal	$d = \left\{ egin{array}{ll} 0 &  ext{if } p = q \ 1 &  ext{if } p  eq q \end{array}  ight.$	$s = \begin{cases} 1 & \text{if } p = q \\ 0 & \text{if } p \neq q \end{cases}$
Ordinal	$d = \frac{ \vec{p}-\vec{q} }{n-1}$ (values mapped to integers 0 to $n-1$ , where $n$ is the number of values)	$s = 1 - \frac{ p-q }{n-1}$
Interval or Ratio	d =  p - q	$s = -d,  s = \frac{1}{1+d}$ or
		$s = -d$ , $s = \frac{1}{1+d}$ or $s = 1 - \frac{d - min\_d}{max\_d - min\_d}$

Table 5.1. Similarity and dissimilarity for simple attributes

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#### **Euclidean Distance**

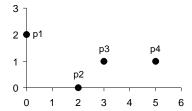
• Euclidean Distance

$$dist = \sqrt{\sum_{k=1}^{n} (p_k - q_k)^2}$$

Where n is the number of dimensions (attributes) and  $p_k$  and  $q_k$  are, respectively, the  $k^{th}$  attributes (components) or data objects p and q.

• Standardization is necessary, if scales differ.

#### **Euclidean Distance**



point	X	у
p1	0	2
p2	2	0
р3	3	1
p4	5	1

	p1	<b>p2</b>	р3	р4
p1	0	2.828	3.162	5.099
p2	2.828	0	1.414	3.162
р3	3.162	1.414	0	2
p4	5.099	3.162	2	0

**Distance Matrix** 

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## Minkowski Distance

 Minkowski Distance is a generalization of Euclidean Distance

$$dist = \left(\sum_{k=1}^{n} |p_k - q_k|^r\right)^{\frac{1}{r}}$$

Where r is a parameter, n is the number of dimensions (attributes) and  $p_k$  and  $q_k$  are, respectively, the kth attributes (components) or data objects p and q.

## **Minkowski Distance: Examples**

- r = 1. City block (Manhattan, taxicab,  $L_1$  norm) distance.
  - A common example of this is the Hamming distance, which is just the number of bits that are different between two binary vectors
- r = 2. Euclidean distance
- $r \rightarrow \infty$ . "supremum" (L<sub>max</sub> norm, L<sub> $\infty$ </sub> norm) distance.
  - This is the maximum difference between any component of the vectors
- Do not confuse *r* with *n*, i.e., all these distances are defined for all numbers of dimensions.

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## Minkowski Distance

point	X	y
p1	0	2
p2	2	0
р3	3	1
р4	5	1

L1	p1	<b>p2</b>	р3	p4
p1	0	4	4	6
<b>p2</b>	4	0	2	4
p3	4	2	0	2
p4	6	4	2	0

L2	p1	<b>p2</b>	р3	p4
p1	0	2.828	3.162	5.099
<b>p2</b>	2.828	0	1.414	3.162
р3	3.162	1.414	0	2
p4	5.099	3.162	2	0

$L_{\infty}$	p1	p2	р3	p4
p1	0	2	3	5
<b>p2</b>	2	0	1	3
р3	3	1	0	2
p4	5	3	2	0

**Distance Matrix**