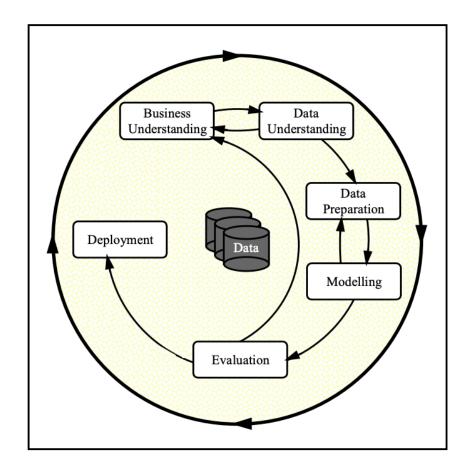
# What drives the price of a car?



#### **OVERVIEW**

In this application, you will explore a dataset from kaggle. The original dataset contained information on 3 million used cars. The provided dataset contains information on 426K cars to ensure speed of processing. Your goal is to understand what factors make a car more or less expensive. As a result of your analysis, you should provide clear recommendations to your client -- a used car dealership -- as to what consumers value in a used car.

#### **CRISP-DM Framework**



To frame the task, throughout our practical applications we will refer back to a standard process in industry for data projects called CRISP-DM. This process provides a framework for working through a data problem. Your first step in this application will be to read through a brief overview of CRISP-DM <a href="https://mo-pcco.s3.us-east-1.amazonaws.com/BH-PCMLAI/module 11/readings starter.zip">here (https://mo-pcco.s3.us-east-1.amazonaws.com/BH-PCMLAI/module 11/readings starter.zip</a>). After reading the overview, answer the questions below.

# **Business Understanding**

From a business perspective, we are tasked with identifying key drivers for used car prices. In the CRISP-DM overview, we are asked to convert this business framing to a data problem definition. Using a few sentences, reframe the task as a data task with the appropriate technical vocabulary.

## 1.1) Business Question

Given a dataset containing used cars attributes, identify the key drivers behind prices of used cars.

## 1.2) Understanding of Business

In order to estimate the price of used car, the deal would be interested in predicting the price of a car based on its attributes. Answers to the following questions may help the dealer determine the price of the used car.

- 1) Do used cars with less age cost more/less?
- 2) Do used cars with electric fuel cost more?
- 3) List top 5 states with highest used car sales.
- 4) Do used cars with automatic transmission cost more?
- 5) Which fuel type is preferred more compared to the other?
- 6) Do used cars with more cylinders cost more?
- 7) Which make and type are most predominant in the used car market?
- 8) Which transmission type is the most sold?

# **Data Understanding**

After considering the business understanding, we want to get familiar with our data. Write down some steps that you would take to get to know the dataset and identify any quality issues within. Take time to get to know the dataset and explore what information it contains and how this could be used to inform your business understanding.

In order to understand the data, some required libraries are imported to run few basic stats about the data. Navigating through the dataset using shape to determine the number of rows and columns and using the describe and info function to determine the mean, std and count along with the type of columns will help in next steps.

## 2.1) Data Collection - Imports

```
In [1]: import pandas as pd
        import numpy as np
        import plotly.express as px
        import matplotlib.pyplot
                                     as plt
        import seaborn
                                     as sns
        import matplotlib.image
                                     as mpimg
        import plotly graph objects as go
        from sklearn.preprocessing import StandardScaler
        from sklearn.preprocessing import OneHotEncoder, LabelEncoder, OrdinalEncoder
        import category encoders as ce
        from sklearn.inspection import permutation importance
        from sklearn.feature selection import SequentialFeatureSelector
        from sklearn.preprocessing import PolynomialFeatures
        from sklearn.model selection import train_test_split
        from sklearn.linear model import LinearRegression, Ridge, Lasso
        from sklearn.metrics import mean squared error, median absolute error, mean absolute error, mean absolute percent
        from sklearn.pipeline import Pipeline
        from sklearn.neighbors import KNeighborsClassifier
        from sklearn.ensemble import RandomForestRegressor
        from sklearn.compose import make column transformer, TransformedTargetRegressor
        from sklearn.model selection import GridSearchCV, cross val score, KFold
        from sklearn.feature selection import RFE
        from scipy.special import exp10
        import warnings
        warnings.filterwarnings("ignore")
```

### 2.2 Data Collection - Load Data

```
In [3]: print('Exact number of entries/rows in vehicles: {}'.format(data_csv.shape[0]))
    print('Number of features/columns in vehicles: {}'.format(data_csv.shape[1]))
    print('Feature/Column-names in vehicles: {}'.format(data_csv.columns.values))
Exact number of entries/rows in vehicles: 426880
```

```
Exact number of entries/rows in vehicles: 426880

Number of features/columns in vehicles: 18

Feature/Column-names in vehicles: ['id' 'region' 'price' 'year' 'manufacturer' 'model' 'condition' 'cylinders' 'fuel' 'odometer' 'title_status' 'transmission' 'VIN' 'drive' 'size' 'type' 'paint_color' 'state']
```

### 2.3 Data Collection - Describe Data

```
In [4]: data_csv.describe()
```

### Out[4]:

	id	price	year	odometer
count	4.268800e+05	4.268800e+05	425675.000000	4.224800e+05
mean	7.311487e+09	7.519903e+04	2011.235191	9.804333e+04
std	4.473170e+06	1.218228e+07	9.452120	2.138815e+05
min	7.207408e+09	0.000000e+00	1900.000000	0.000000e+00
25%	7.308143e+09	5.900000e+03	2008.000000	3.770400e+04
50%	7.312621e+09	1.395000e+04	2013.000000	8.554800e+04
75%	7.315254e+09	2.648575e+04	2017.000000	1.335425e+05
max	7.317101e+09	3.736929e+09	2022.000000	1.000000e+07

## 2.4 Data Collection - Data Types

```
In [5]: data_csv.dtypes
Out[5]: id
                           int64
        region
                          object
        price
                           int64
                         float64
        year
                          object
        manufacturer
        model
                          object
        condition
                          object
        cylinders
                          object
                          object
        fuel
        odometer
                         float64
                          object
        title_status
        transmission
                          object
        VIN
                          object
        drive
                          object
        size
                          object
        type
                          object
        paint_color
                          object
        state
                          object
        dtype: object
```

### 2.5 Data Collection - Data Dimensions

```
In [6]: data_csv.shape
Out[6]: (426880, 18)
```

2.6 Data Collection - Check NA

```
In [7]: data csv.isna().sum()
Out[7]: id
                               0
         region
                               0
         price
                               0
                            1205
         year
        manufacturer
                           17646
        model
                            5277
         condition
                          174104
         cylinders
                          177678
         fuel
                            3013
         odometer
                            4400
         title status
                            8242
         transmission
                            2556
         VIN
                          161042
         drive
                          130567
         size
                          306361
         type
                           92858
         paint color
                          130203
         state
                               0
         dtype: int64
```

### **Data Preparation**

After our initial exploration and fine tuning of the business understanding, it is time to construct our final dataset prior to modeling. Here, we want to make sure to handle any integrity issues and cleaning, the engineering of new features, any transformations that we believe should happen (scaling, logarithms, normalization, etc.), and general preparation for modeling with sklearn.

## 3.1 Numerical and Categorical Attributes

```
In [8]: num_attributes = data_csv.select_dtypes( include=['float64','int64'] )
    cat_attributes = data_csv.select_dtypes( exclude=['float64', 'datetime64[ns]'] )
    num_attributes.sample()
```

#### Out[8]:

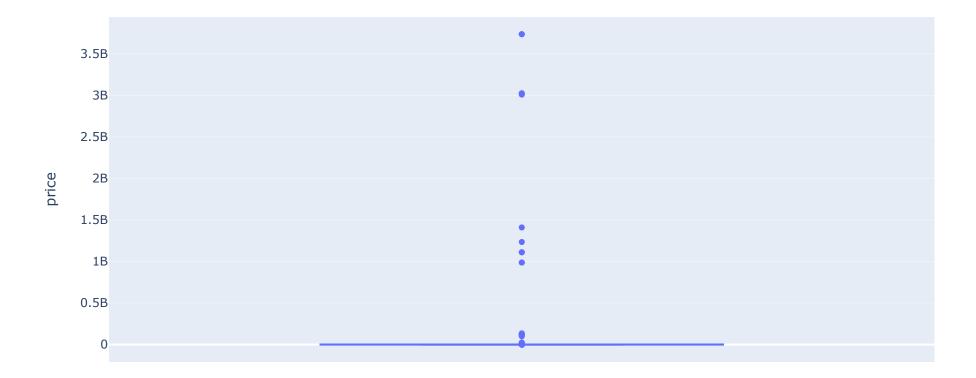
```
id price year odometer

341626 7317041317 14500 2008.0 165000.0
```

# 3.2 Clean Dataset by dropping rows and columns

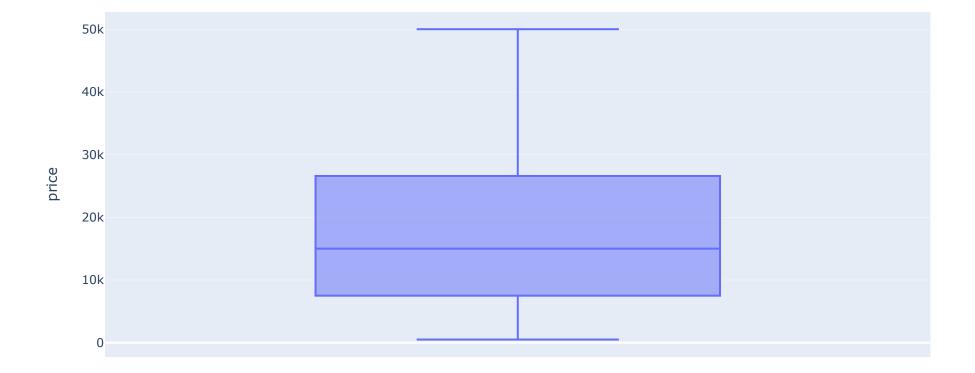
```
In [10]: #sns.boxplot( data_csv['price'] )
px.box(data_csv, y="price", title="Price of used cars")
```

# Price of used cars



```
In [11]: #From the above we see that outliers exist. For now, just remove the noise.
    data_csv = data_csv[(data_csv['price']>500) & (data_csv['price']<50000)]
    #sns.boxplot( data_csv['price'] )
    px.box(data_csv, y="price", title="Price of used cars after removing noise")</pre>
```

## Price of used cars after removing noise



```
In [12]: cat_attributes.apply( lambda x: x.unique().shape[0])
Out[12]: id
                         426880
         region
                            404
         price
                          15655
         manufacturer
                             43
         model
                          29650
         condition
                              7
         cylinders
                              9
         fuel
                              6
         title_status
         transmission
                              4
         VIN
                         118247
         drive
                              4
         size
                              5
         type
                             14
         paint_color
                             13
         state
                             51
         dtype: int64
```

After dropping the noise, lets check the shape

```
In [13]: data_csv.shape
```

Out[13]: (370724, 18)

```
In [14]: | data_csv.isna().sum()
Out[14]: id
                                0
          region
                                0
                                0
          price
          year
                              863
         manufacturer
                            14146
          model
                             4045
          condition
                           136790
          cylinders
                           150132
          fuel
                             2509
          odometer
                             2009
          title status
                             6667
          transmission
                             1730
          VIN
                           144685
          drive
                           113470
          size
                           265007
          type
                            79520
         paint_color
                           106731
          state
                                0
         dtype: int64
```

From the above, we see a lot of Nan values. We will either drop these rows or replacing them with the mean values. We will start by evaluating the distinct values in categorical columns. The year, manufacturer, model and cylinders have Nan values. Without these the data will not be helpful. Dropping these rows with NAN values for those specific columns. Also, we will create a dictionary of model and other features to check for missing NAN values based on existing rows.

```
In [15]: #drop rows and columns
data_csv.drop(index=data_csv[data_csv['year'].isna() & data_csv['model'].isna() & data_csv['manufacturer'].isna()
#drop all the nan values which are missing in the year column
data_csv.drop(index=data_csv[data_csv['year'].isna()].index,inplace=True)
data_csv.drop(['VIN'], axis=1, inplace=True)
data_csv.drop(['id'],axis = 1, inplace= True)
```

```
In [16]: #apply lowercase first
data_csv['model'] = data_csv['model'].str.lower()
data_csv['type'] = data_csv['type'].str.lower()
data_csv.isna().sum()
```

```
Out[16]: region
                              0
         price
                              0
         year
                              0
         manufacturer
                          13284
         model
                           3984
         condition
                         135927
         cylinders
                         150065
         fuel
                           2283
         odometer
                           1947
         title_status
                           6445
         transmission
                           1669
         drive
                         113207
         size
                         264144
                         79366
         type
         paint_color
                         106612
         state
                              0
         dtype: int64
```

```
In [17]:
         #drop rows that have 'model' and 'manufacturer' with nan values at the same time.
         data csv.drop(index=data csv[data csv['manufacturer'].isna() & data csv['model'].isna()].index, inplace=True )
         #fill the odometer nan values with mean
         data csv['odometer'] = data csv['odometer'].fillna(data csv.groupby('year')['odometer'].transform('mean'))
         data_csv['title_status'].fillna( 'other', inplace=True )
         data csv['transmission'].fillna( 'other', inplace=True )
         data_csv['paint_color'].fillna( 'custom', inplace=True )
         data csv['fuel'].fillna( 'other', inplace=True )
         df manufacturer = data csv[data csv['manufacturer'].notna()]
         df model manufacturer = df manufacturer[df manufacturer['model'].notna()]
         df1 cylinders = data csv[data csv['cylinders'].notna()]
         df1 model cylinders = df1_cylinders[df1_cylinders['model'].notna()]
         df1 condition = data csv[data csv['condition'].notna()]
         df1 model condition = df1 condition[df1 condition['model'].notna()]
         df1 drive = data csv[data csv['drive'].notna()]
         df1 model drive = df1_drive[df1_drive['model'].notna()]
         df1 size = data csv[data csv['size'].notna()]
         df1 model size = df1 size[df1 size['model'].notna()]
         df1 type = data csv[data csv['type'].notna()]
         df1 model type = df1 type[df1 type['model'].notna()]
         condition dict = {}
         cylinders dict = {}
         manufacturer dict = {}
         drive dict = {}
         size dict = {}
         type dict = {}
         for model, manu in df_model_manufacturer[['model', 'manufacturer']].values:
             manufacturer dict[model] = manu
         for model, cylinder in df1_model_cylinders[['model', 'cylinders']].values:
             cylinders dict[model] = cylinder
         for model, condition in df1 model condition[['model', 'condition']].values:
             condition dict[model] = condition
         for model, drive in df1_model_drive[['model', 'drive']].values:
             drive dict[model] = drive
         for model, size in df1 model size[['model', 'size']].values:
             size dict[model] = size
```

```
(369861, 16)
(281765, 16)
```

### 3.3 Rename Columns

```
In [18]: data_formatted.rename( columns={"region": "city"}, inplace=True )
    data_formatted.head()
```

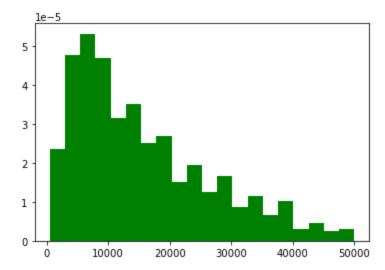
### Out[18]:

	city	price	year	manufacturer	model	condition	cylinders	fuel	odometer	title_status	transmission	drive	size	type	paint_color
28	auburn	22590	2010.0	chevrolet	silverado 1500	good	8 cylinders	gas	71229.0	clean	other	4wd	full-size	pickup	blue
30	auburn	30990	2017.0	toyota	tundra double cab sr	good	8 cylinders	gas	41124.0	clean	other	4wd	full-size	pickup	red
31	auburn	15000	2013.0	ford	f-150 xlt	excellent	6 cylinders	gas	128000.0	clean	automatic	rwd	full-size	truck	black
34	auburn	35000	2019.0	toyota	tacoma	excellent	6 cylinders	gas	43000.0	clean	automatic	4wd	compact	truck	grey
35	auburn	29990	2016.0	chevrolet	colorado extended cab	good	6 cylinders	gas	17302.0	clean	other	4wd	mid-size	pickup	red

# 3.4 Data Analysis

# 3.4.1 Univariate Analysis ( Descriptive Statistics)

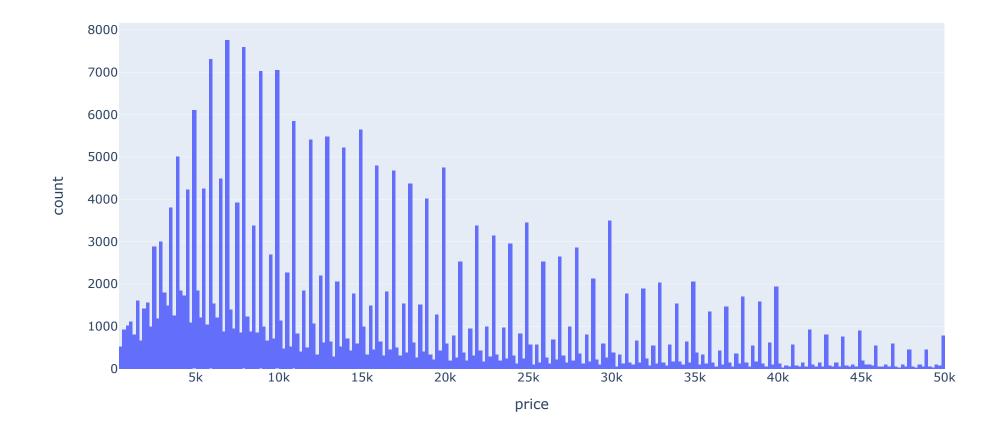
### 3.4.1.1 Response Variable



### 3.4.1.2 Numerical Variables

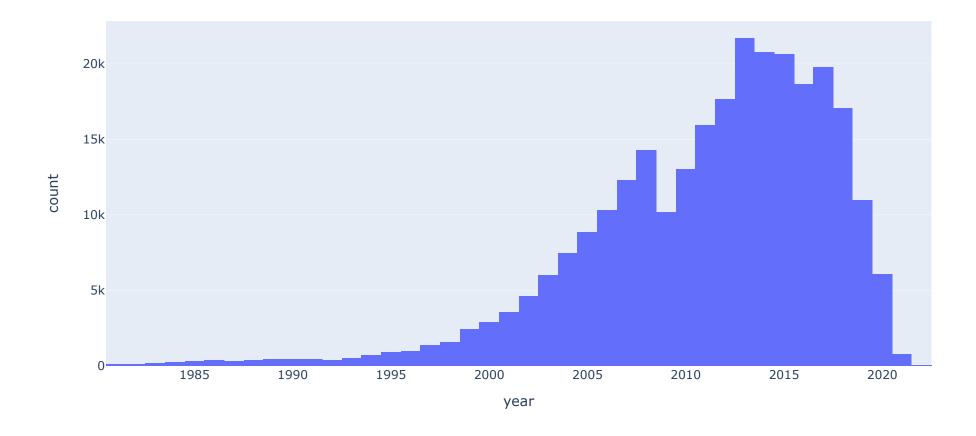
```
In [20]: px.histogram(data_formatted,x="price", title='Price of used cars by total count',)
```

# Price of used cars by total count



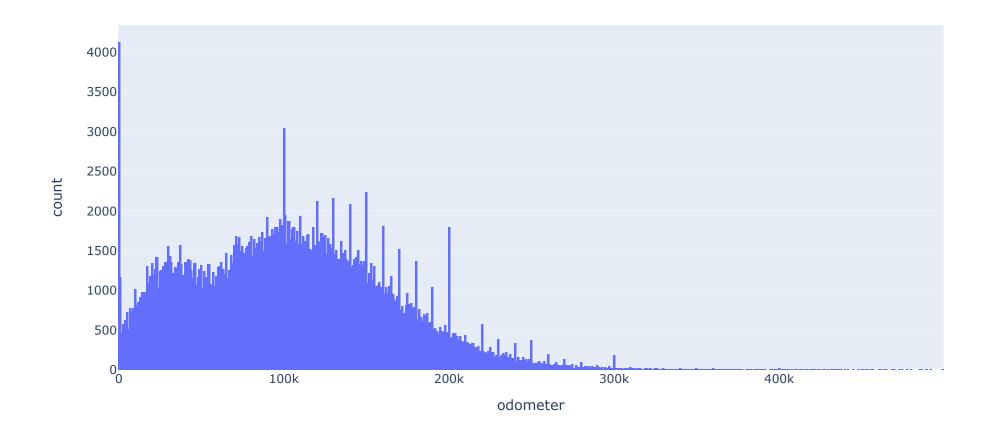
In [21]: px.histogram(data\_formatted[data\_formatted['year'] > 1980],x="year",title="Used Cars by year")

# Used Cars by year



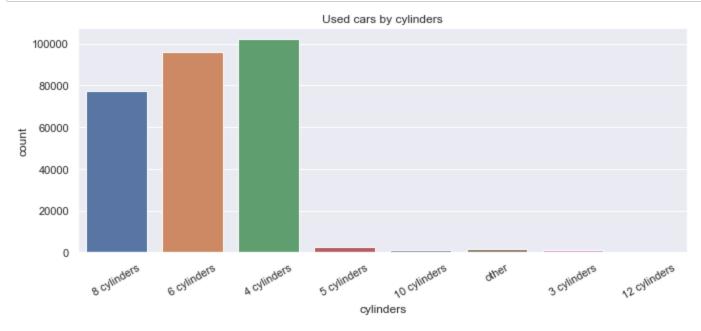
In [22]: px.histogram(data\_formatted[data\_formatted['odometer'] < 500000],x="odometer", title='Used cars with odometer les</pre>

Used cars with odometer less than 500000



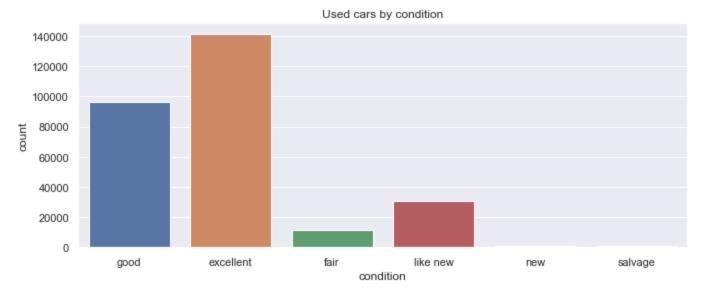
## 3.4.1.3 Categorical Variables

```
In [23]: sns.set(rc={'figure.figsize':(24,14)})
    plt.subplot( 3, 2, 5)
    fig1 = sns.countplot( data_formatted['cylinders'] )
    fig1.set_xticklabels(fig1.get_xticklabels(), rotation=30)
    fig1.title.set_text('Used cars by cylinders')
    plt.show()
```



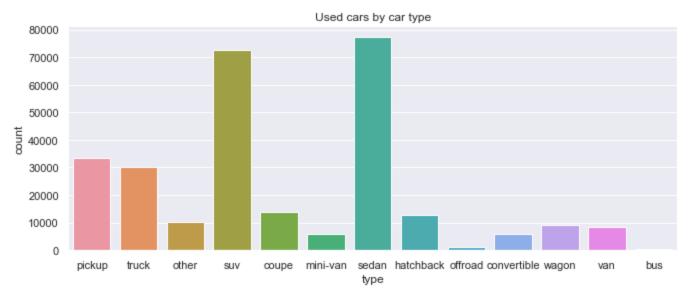
Cylinders do not have a direct. Correlation in determining the price.

```
In [24]: sns.set(rc={'figure.figsize':(24,14)})
plt.subplot( 3, 2, 5)
fig2 = sns.countplot( data_formatted['condition'] )
fig2.title.set_text('Used cars by condition')
plt.show()
```



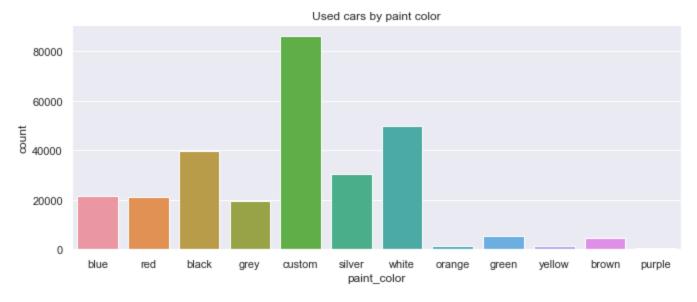
Cars with excellent condition cost more compared to other cars.

```
In [25]: sns.set(rc={'figure.figsize':(24,14)})
    plt.subplot( 3, 2, 3)
    fig3 = sns.countplot( data_formatted['type'] )
    fig3.title.set_text('Used cars by car type')
    plt.show()
```



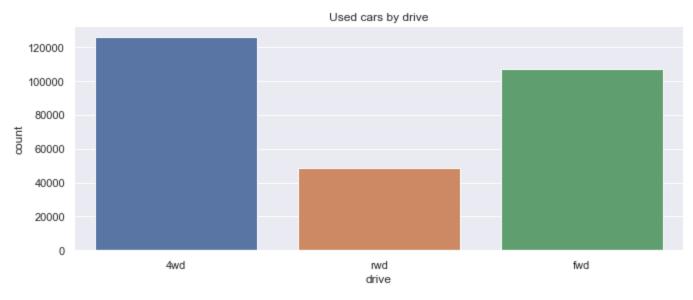
Cars of type SUV and sedan are sold more compared to other cars. The prices of these cars are driven by supply and demand.

```
In [26]: sns.set(rc={'figure.figsize':(24,14)})
plt.subplot( 3, 2, 5)
fig4 = sns.countplot( data_formatted['paint_color'] )
fig4.title.set_text('Used cars by paint color')
plt.show()
```



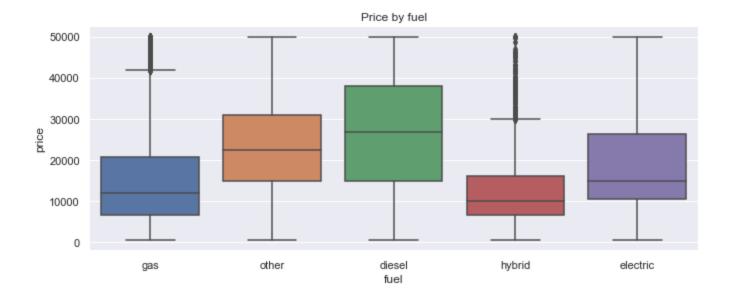
Cars with white, black and silver are sold more compared to the other car types. The custom column in the above may involve Nan values too.

```
In [27]: plt.subplot( 3, 2, 1)
fig5 = sns.countplot( data_formatted['drive'] )
fig5.title.set_text('Used cars by drive')
plt.show()
```



Cars with 4wd are priced higher compared to the other cars.

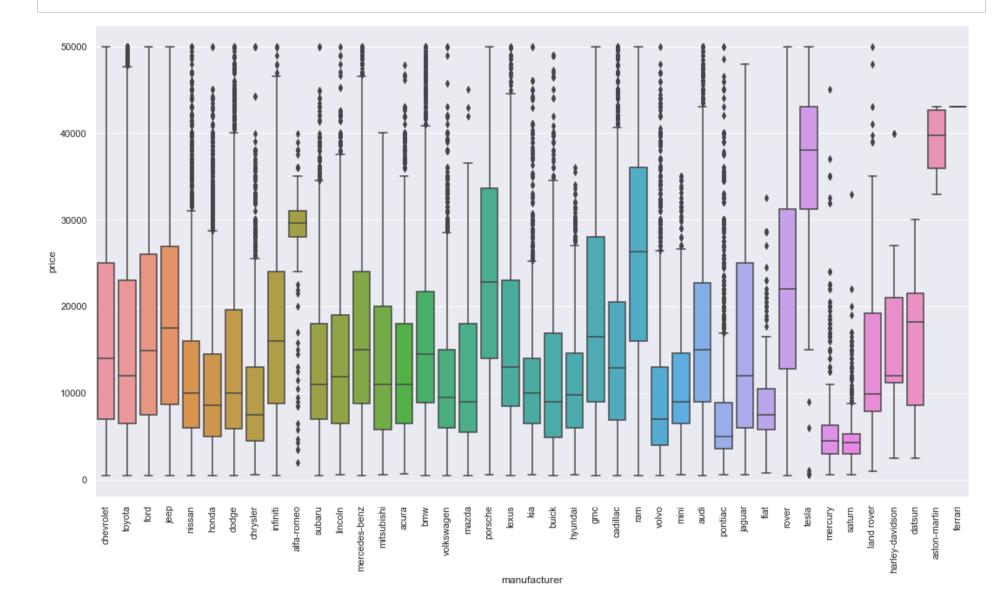
```
In [28]: plt.subplot( 3, 2, 4)
fig6 = sns.boxplot(data=data_formatted, x='fuel', y='price')
fig6.title.set_text("Price by fuel")
plt.show()
```



Cars with fuel type diesel are priced higher compared to the other car types.

Cars with fuel type diesel are priced higher compared to the other car types.

```
In [29]: # Visualization price vs manufacturer cars
fig = plt.figure(figsize=(18, 10))
sns.boxplot(data=data_formatted, x='manufacturer', y='price')
plt.xticks(rotation=90)
plt.show()
```



Tesla, Ferrari, Porsche and RAM are priced higher compared to other manufacturers.

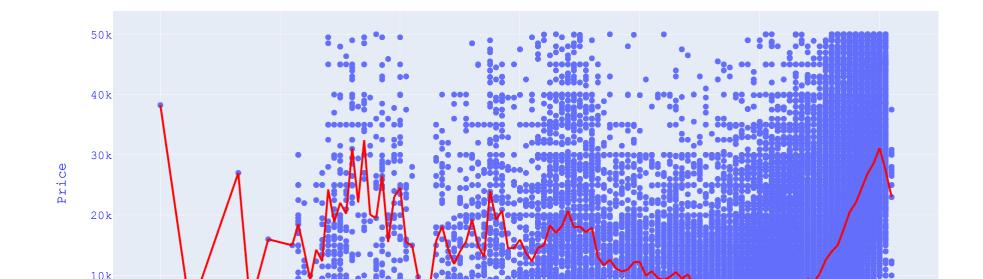
# 3.4.2 Bivariate analysis (inferential statistics)

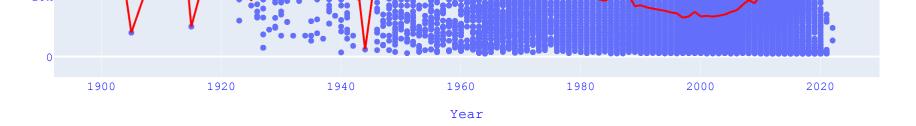
We will be answering some of the questions from the business understanding steps.

1) Do used cars with less age should cost more/less?

```
In [30]: data formatted['mean price'] = data formatted.groupby('year')['price'].transform('mean')
         data formatted = data formatted.sort values(by=['year'])
         fig1 = px.scatter(data formatted, x="year", y="price")
         fig2 = px.line(data formatted, x="year", y="mean price", title='Mean Price')
         fig3 = go.Figure(data=fig1.data + fig2.data, layout=go.Layout(
                 title=go.layout.Title(text="Price of used cars by age")
             ))
         fig3.update traces(line=dict(color = 'red'))
         fig3.update layout(
             showlegend=True,
             font family="Courier New",
             font color="blue",
             title font family="Times New Roman",
             title font color="black",
             legend title font color="green"
         fig3.update xaxes(title text = 'Year')
         fig3.update yaxes(title text = 'Price')
         fig3.show()
```

Price of used cars by age



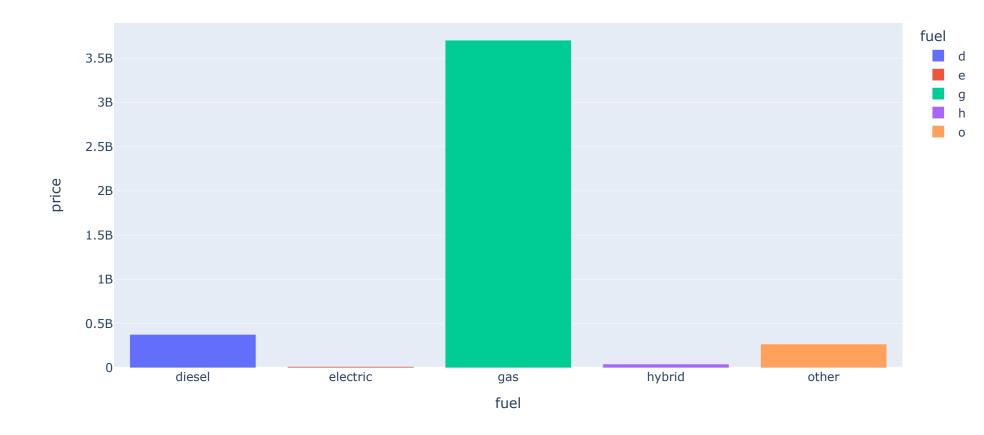


From the year 2000, we clearly see that the price of cars increases as age of the used car decreases.

2) Do used cars with electric fuel cost more?

```
In [31]: df_electric = data_formatted[['fuel','price']].groupby('fuel').sum().reset_index()
px.bar(df_electric,x='fuel', y='price',color="fuel", title="Price by car fuel injection type")
```

## Price by car fuel injection type

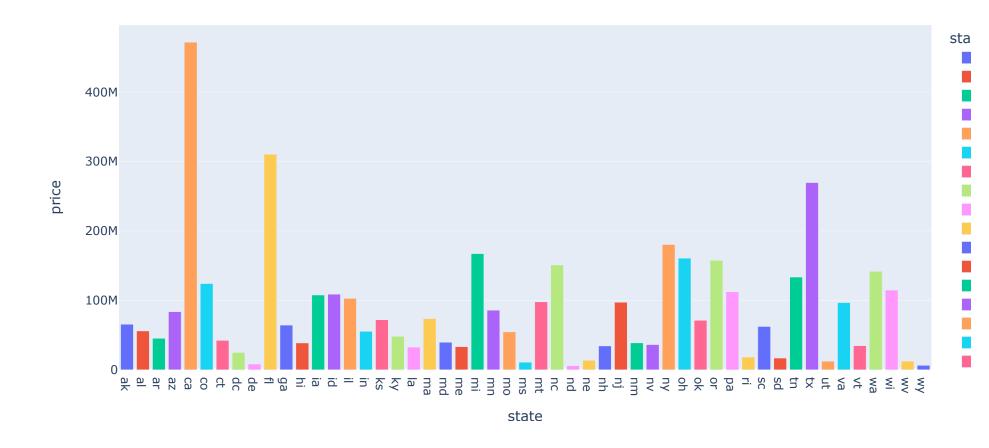


Based on the above plot, it is clear that used cars with fuel type gas are more sold compared to the other car types.

### 3) List top 5 states with highest used car sales.

```
In [32]: aux1 = data_formatted[['state', 'price']].groupby( 'state' ).sum().reset_index()
px.bar(aux1,x='state', y='price',color="state", title="Used cars total price by state")
```

### Used cars total price by state

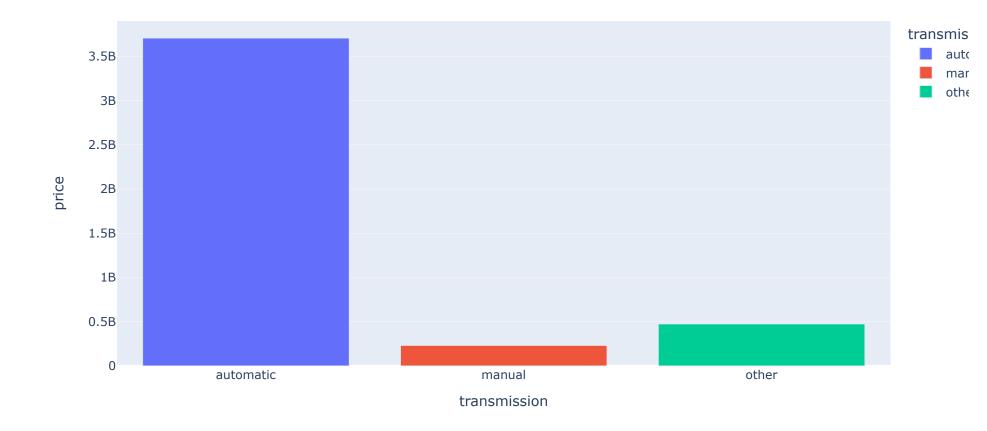


Based on the above plot, we can clearly see th top 5 states by total price. CA, FL, TX, NY and MI

#### 4) Do used cars with automatic transmission cost more?

```
In [33]: aux1 = data_formatted[['transmission', 'price']].groupby( 'transmission' ).sum().reset_index()
fig = px.bar(aux1,x='transmission', y='price',color="transmission", title="Total Price by transmission");
fig.show()
```

## Total Price by transmission

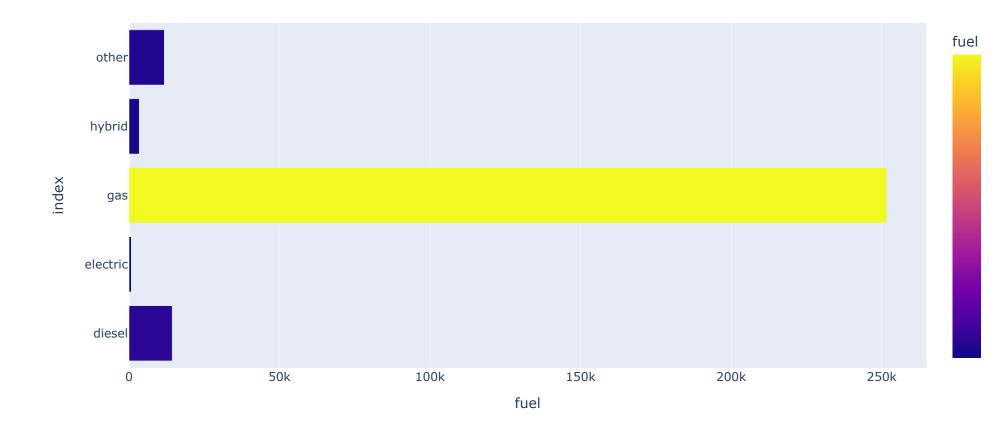


Based on the above plot, it clearly shows us that automatic transmission costs much more than manual and other transmissions.

#### 5) Which fuel type is preferred more compared to the other?

```
In [34]: aux1 = data_formatted.groupby('fuel')['fuel'].count()
fig = px.bar(aux1, x='fuel', color="fuel", title="Preferred fuel type by total count")
fig.show()
```

## Preferred fuel type by total count

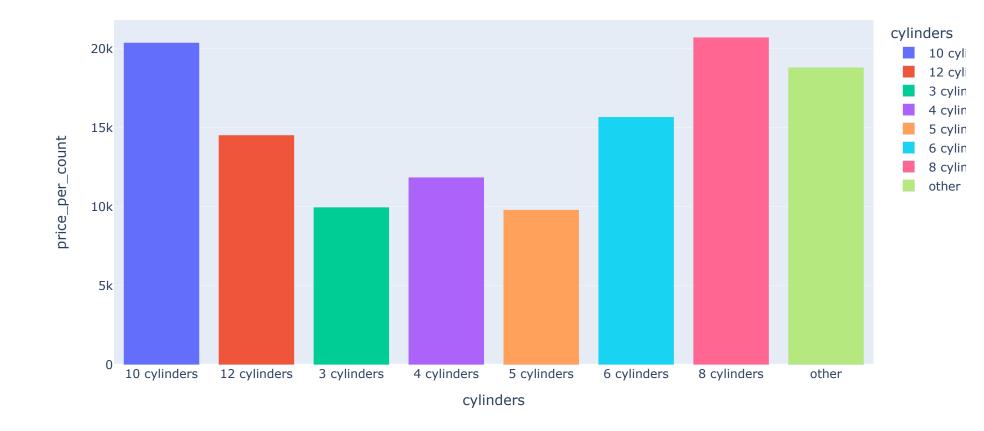


From the above plot, we can see that the gas is most preferred fuel type compared to other fuel types.

### 6) Do used cars with more cylinders cost more?

```
In [35]: #In order to find out the true cost of cylinder, lets divide the total price of used car by cylinder and divide
    # number of rows by cylinder
    aux1 = data_formatted[['cylinders', 'price']].groupby( 'cylinders').sum().reset_index()
    cylinder_count = data_formatted.groupby('cylinders')['cylinders'].count()
    cyl_count_frame = pd.Series.to_frame(cylinder_count)
    cyl_count_frame.columns = ['count']
    aux1 = aux1.set_index('cylinders')
    aux1['count'] = cyl_count_frame['count']
    aux1['price_per_count'] = aux1['price']/aux1['count']
    aux1 = aux1.reset_index()
    fig = px.bar(aux1,x='cylinders', y='price_per_count',color="cylinders", title="Total Price by cylinders");
    fig.show()
```

### Total Price by cylinders

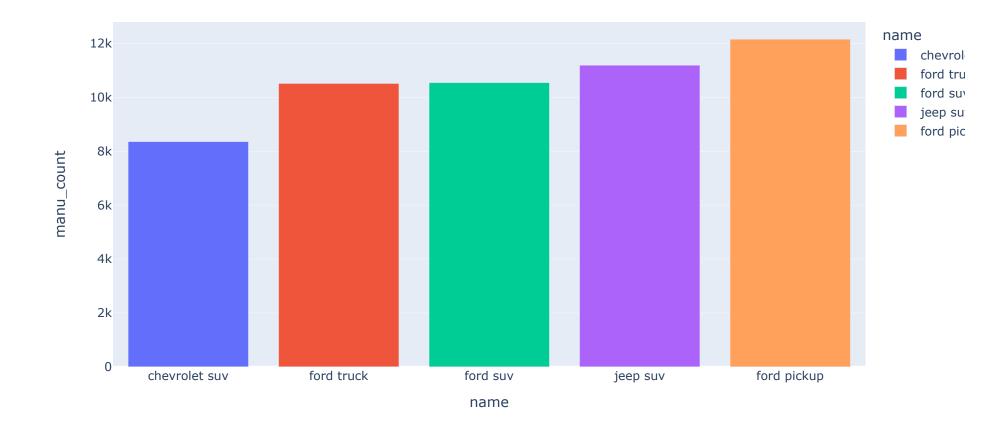


Based on the information provided and from the above plot, it is pretty clear that the cost of cylinder does not increase with increase in number of cylinders.

#### 7) Which make and type are most predominant in the used car market?

```
In [87]: aux1 = data_formatted.groupby(['manufacturer', 'type'])['manufacturer', 'type'].count()
    aux1.columns = ['manu_count','type_count']
    aux1 = aux1.sort_values(by=['type_count']).tail(5)
    aux1 = aux1.reset_index()
    aux1['name'] = aux1['manufacturer'] + " " + aux1['type']
    fig = px.bar(aux1,x='name', y='manu_count',color='name', title="Top 5 used cars");
    fig.show()
```

Top 5 used cars

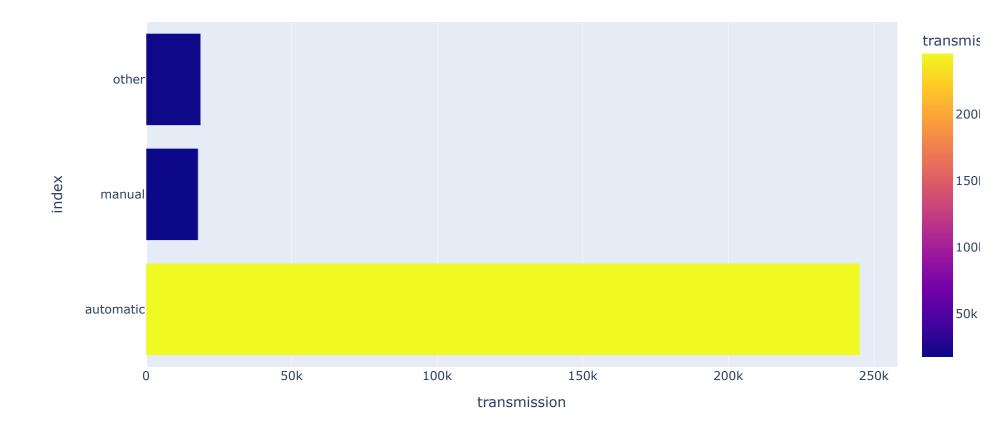


From the above, it is pretty clear that ford pick up is the most sold car.

#### 9) Which transmission type is the most sold?

```
In [37]: aux1 = data_formatted.groupby('transmission')['transmission'].count()
    fig = px.bar(aux1, x='transmission', color="transmission", title="Most sold used car by transmission")
    fig.show()
```

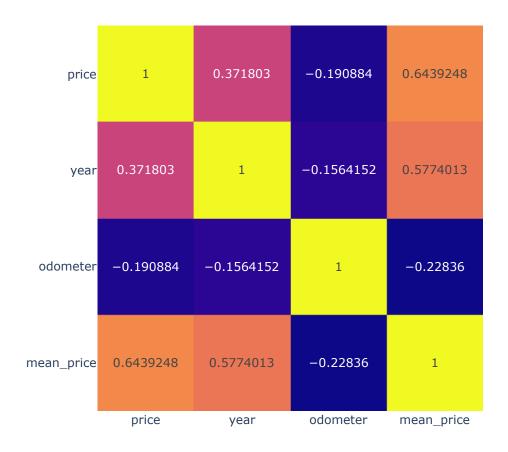
## Most sold used car by transmission



From the above plot, it is pretty clear that automatic transmission is the most sold among used cars.

# 3.4.2 Multivariate analysis

```
In [38]: #Lets take a look at the correlation matrix for numerical attributes
    #data.corr()
fig = px.imshow(data_formatted.corr(),text_auto=True)
fig.show()
```



```
In [39]: #type(cat_attributes)
    #d_cat_attributes = df_encoded.drop(['city', 'manufacturer','price', 'year','odometer','size', 'paint_color', 'd.
    #fig = px.imshow(d_cat_attributes.corr(),text_auto=True)
    #fig.show()
In []:
```

## Modeling

With your (almost?) final dataset in hand, it is now time to build some models. Here, you should build a number of different regression models with the price as the target. In building your models, you should explore different parameters and be sure to cross-validate your findings.

```
In [ ]:
```

# 4.1 Rescaling

```
In [40]: #Using Standard Scaler here to scale the numerical values.
    ss = StandardScaler()
    data_formatted['year'] = ss.fit_transform(data_formatted[['year']].values)
    data_formatted['odometer'] = ss.fit_transform(data_formatted[['odometer']].values)
In [41]: data_formatted.drop('mean_price', axis=1,inplace=True)
```

## 4.2 Transformation

Transformation of categorical values using One Hot Encoder, Ordinal Encoder. pd.get\_dummies is not being used here as it is not a simple analyzation

## 4.2.1 Encoding

```
In [43]: ohe = OneHotEncoder(sparse=False)
In [44]: #Transforming the fuel column with One-Hot Encoder
         ohe.fit(df scaled[['fuel']])
         temp df = pd.DataFrame(data=ohe.transform(df scaled[['fuel']]), columns=ohe.get feature names out())
         df scaled.drop(columns=['fuel'], axis=1, inplace=True)
         df scaled = pd.concat([df scaled.reset index(drop=True), temp df], axis=1)
         #Transforming the transmission column
         ohe.fit(df scaled[['transmission']])
         temp df2 = pd.DataFrame(data=ohe.transform(df scaled[['transmission']]), columns=ohe.get feature names out())
         df scaled.drop(columns=['transmission'], axis=1, inplace=True)
         df scaled = pd.concat([df scaled.reset index(drop=True), temp df2], axis=1)
         #Transforming the drive column
         ohe.fit(df scaled[['drive']])
         temp df3 = pd.DataFrame(data=ohe.transform(df scaled[['drive']]), columns=ohe.get feature names out())
         df scaled.drop(columns=['drive'], axis=1, inplace=True)
         df scaled = pd.concat([df scaled.reset index(drop=True), temp df3], axis=1)
In [45]: #OrdinalEncoding the condition column
         condition dict = {'col':'condition', 'mapping':{'other': 0, 'new': 6, 'like new': 5, 'excellent': 4, 'good': 3, '
         ordinal encoder1 = ce.OrdinalEncoder(cols=['condition'], return df=True, mapping=[condition dict])
         df scaled['condition'] = ordinal encoder1.fit transform(df scaled[['condition']])
         cylinders dict = {'col':'cylinders', 'mapping':{'other': 0, '12 cylinders': 12, '10 cylinders': 10, '8 cylinders'
         ordinal encoder2 = ce.OrdinalEncoder(cols=['cylinders'], return df=True, mapping=[cylinders dict])
         df scaled['cylinders'] = ordinal encoder2.fit transform(df scaled[['cylinders']])
         title status dict = {'col':'title status', 'mapping':{'other': 0, 'clean': 6, 'lien': 5, 'salvage': 4, 'rebuilt':
         ordinal encoder3 = ce.OrdinalEncoder(cols=['title status'], return df=True, mapping=[title status dict])
         df scaled['title status'] = ordinal encoder3.fit transform(df scaled[['title status']])
```

In [42]: df scaled = data formatted.copy()

```
In [46]: #label encoding the remaining columns.
label_encoder = LabelEncoder()
df_scaled['size']= label_encoder.fit_transform(df_scaled['size'])
df_scaled['manufacturer'] = label_encoder.fit_transform( df_scaled['manufacturer'] )
df_scaled['type'] = label_encoder.fit_transform( df_scaled['type'] )
df_scaled['paint_color'] = label_encoder.fit_transform( df_scaled['paint_color'] )
df_scaled['state'] = label_encoder.fit_transform(df_scaled['state'] )
df_scaled['city'] = label_encoder.fit_transform(df_scaled['city'] )
#Lets take a look at the info to see what columns remain
In [47]: #one last thing to do is to drop the model column as it is no more a determinant at this point.
```

```
In [4/]: #one last thing to do is to drop the model column as it is no more a determinant at this point.

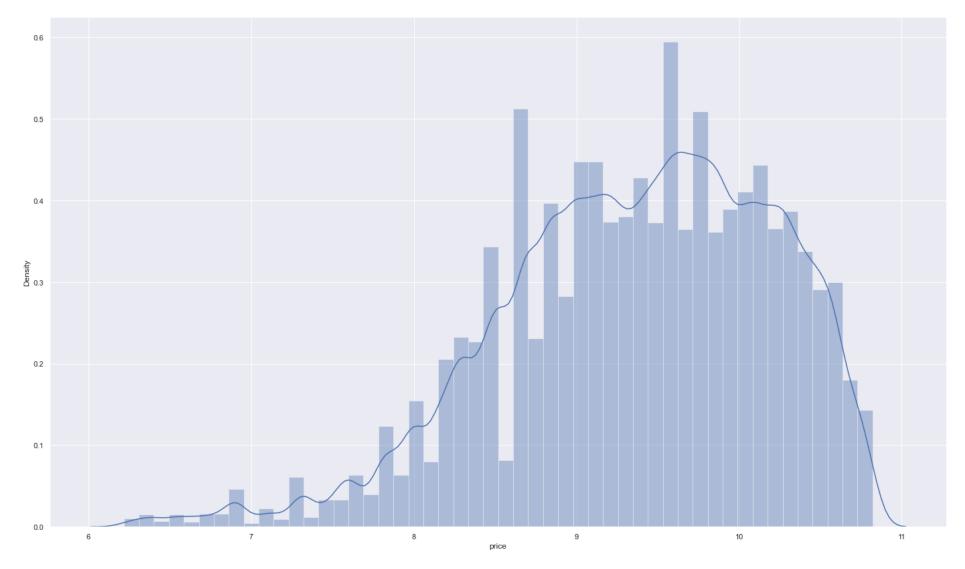
df_encoded = df_scaled.drop('model', axis = 1)
```

#### 4.2.2 Response Variable Transformation

```
In [48]: df_encoded['price'] = np.log1p( df_encoded['price'] )
In []:
```

```
In [49]: sns.distplot( df_encoded['price'] )
```

Out[49]: <AxesSubplot:xlabel='price', ylabel='Density'>



### 4.3 Feature Selection

#### 4.3.1 Feature Selection using KNN and SFS

```
In [50]: RANDOM SEED = 42
         knn = KNeighborsClassifier(n neighbors=4)
         X = df encoded.drop('price', axis=1)
         y = df encoded['price']
         X train, X test, y train, y test = train test split(X,y,test size=0.3)
         print(X train.shape, y train.shape)
         print(X test.shape, y test.shape)
         #Using KNN
         sfs1 = SequentialFeatureSelector(knn,
                    n features to select=12,
                    scoring='neg mean squared error'
         sfs1 = sfs1.fit(X, y)
         (197235, 22) (197235,)
         (84530, 22) (84530,)
In [51]: kcols = sfs1.get_feature_names_out()
```

## 4.3.2 Feature Selection using Permutation Importance

```
In [52]: from sklearn.pipeline import make pipeline
         preprocessor = make column transformer(
             (StandardScaler(),['year','odometer']),
             remainder="passthrough",
             verbose feature names out=False, # avoid to prepend the preprocessor names
         model = make pipeline(
                 preprocessor,
                 TransformedTargetRegressor(
                 regressor=Ridge(alpha=1e-10), func=np.log10, inverse func=exp10
         model.fit(X train, y train)
         y pred = model.predict(X train)
         mae = median absolute error(y train, y pred)
         string score = f"MAE on training set: {mae:.2f} $/hour"
         mse train = mean squared error(y train, y pred)
         y pred = model.predict(X test)
         mae = median absolute error(y test, y pred)
         string_score += f"\nMAE on testing set: {mae:.2f} $/hour"
         mse test = mean squared error(y test,y pred)
         print(f'The mean squared error on the trained data is : {mse train: .2f}')
         print(f'The mean squared error on the test data is : {mse test: .2f}')
```

The mean squared error on the trained data is: 0.42
The mean squared error on the test data is: 0.42

```
In [53]: r = permutation_importance(model, X_test, y_test,n_repeats=30,random_state=RANDOM_SEED)
for i in r.importances_mean.argsort()[::-1]:
    if r.importances_mean[i] - 2 * r.importances_std[i] > 0:
        print(f"{X_test.columns[i]:<8}"
        f" {r.importances_mean[i]:.3f}"
        f" +/- {r.importances_std[i]:.3f}")</pre>
```

```
drive fwd 0.399 +/- 0.003
         0.353 +/- 0.003
year
drive 4wd 0.087 +/- 0.001
cylinders 0.081 + - 0.001
transmission automatic 0.045 +/- 0.001
drive rwd 0.039 +/- 0.001
odometer 0.038 +/- 0.001
condition 0.035 +/- 0.001
fuel diesel 0.013 +/- 0.000
fuel gas 0.009 +/- 0.000
transmission manual 0.009 +/- 0.000
title status 0.004 +/- 0.000
type
         0.002 +/- 0.000
manufacturer 0.001 +/- 0.000
state
         0.001 +/- 0.000
paint color 0.001 + - 0.000
transmission other 0.001 +/- 0.000
fuel electric 0.001 +/- 0.000
fuel hybrid 0.000 +/- 0.000
size
        0.000 +/- 0.000
         0.000 +/- 0.000
city
```

```
----r2-----
drive fwd 0.399 +/- 0.003
year
       0.353 +/- 0.003
drive 4wd 0.087 +/- 0.001
cylinders 0.081 +/- 0.001
transmission automatic 0.045 +/- 0.001
drive rwd 0.039 +/- 0.001
odometer 0.038 +/- 0.001
condition 0.035 +/- 0.001
fuel diesel 0.013 +/- 0.000
fuel gas 0.009 +/- 0.000
transmission manual 0.009 +/- 0.000
title status 0.004 + /- 0.000
         0.002 +/- 0.000
type
manufacturer 0.001 + /- 0.000
state
         0.001 +/- 0.000
paint color 0.001 + - 0.000
transmission other 0.001 +/- 0.000
fuel electric 0.001 +/- 0.000
fuel hybrid 0.000 +/- 0.000
size
         0.000 +/- 0.000
city
         0.000 +/- 0.000
----neg mean absolute percentage error-----
drive fwd 0.020 +/- 0.000
        0.018 +/- 0.000
year
cylinders 0.004 +/- 0.000
drive 4wd 0.004 +/- 0.000
drive rwd 0.003 +/- 0.000
transmission automatic 0.002 +/- 0.000
odometer 0.002 +/- 0.000
condition 0.002 +/- 0.000
fuel diesel 0.001 + /- 0.000
transmission manual 0.001 +/- 0.000
fuel gas 0.001 +/- 0.000
title status 0.000 + /- 0.000
```

```
transmission other 0.000 + /- 0.000
paint color 0.000 +/- 0.000
manufacturer 0.000 +/- 0.000
state
         0.000 +/- 0.000
fuel electric 0.000 +/- 0.000
fuel hybrid 0.000 +/- 0.000
size
         0.000 +/- 0.000
city
         0.000 +/- 0.000
----neg mean squared error-----
drive fwd 0.284 +/- 0.002
year
         0.251 +/- 0.002
drive 4wd 0.062 +/- 0.001
cylinders 0.057 +/- 0.001
transmission automatic 0.032 +/- 0.001
drive rwd 0.028 +/- 0.000
odometer 0.027 +/- 0.000
condition 0.025 +/- 0.000
fuel diesel 0.009 +/- 0.000
fuel gas 0.007 +/- 0.000
transmission manual 0.007 +/- 0.000
title status 0.003 +/- 0.000
type
         0.001 +/- 0.000
manufacturer 0.001 + /- 0.000
state
         0.001 +/- 0.000
paint color 0.001 + - 0.000
transmission other 0.001 +/- 0.000
fuel electric 0.001 +/- 0.000
fuel hybrid 0.000 +/- 0.000
size
         0.000 +/- 0.000
city
         0.000 +/- 0.000
```

Looking at the above we can say the following columns will have an impact on the prediction results final\_columns = ['drive\_rwd','drive\_fwd','drive\_4wd', 'fuel\_gas','fuel\_diesel', 'odometer','year', 'cylinders', 'condition','transmission\_manual','type','title\_status']

#### 4.4 Models

```
rmse = np.sqrt( mean squared error( y, yhat ) )
             mse = mean squared error(y, yhat)
             return pd.DataFrame( { 'Model Name': model name,
                                     'MAE': mae,
                                     'MAPE': mape,
                                     'MSE': mse,
                                     'RMSE': rmse }, index=[0] )
         def mean percentage error( y, yhat ):
             return np.mean( ( y - yhat ) / y )
In [57]: # using final columns as features
         X = df encoded
         y = np.log1p(df encoded.price)
         X_train, X_test, y_train, y_test = train_test_split(X,y,test_size=0.3, random_state=RANDOM_SEED)
         x_train = X_train[final_columns ]
         x_test = X_test[final_columns ]
         #using KNN columns as features
         xk_train = X_train[kcols ]
         xk_test = X_test[kcols ]
 In [ ]:
```

### 4.4.1) Linear Regression

In [56]: def ml error( model name, y, yhat ):

mae = mean absolute error( y, yhat )

mape = mean\_absolute\_percentage\_error( y, yhat )

```
In [58]: # In the beginning I use the Linear Model to see how linear or non-linear our dataset is.
         # model
         lr = LinearRegression().fit( x train, y train )
         # prediction
         yhat lr = lr.predict( x test )
         # performance
         lr result1 = ml error( 'Linear Regression', np.expm1( y test ), np.expm1( yhat lr ) )
         lr result1
Out[58]:
                                            MSE
               Model Name
                             MAE
                                   MAPE
                                                   RMSE
          0 Linear Regression 0.475208 0.052931 0.431789 0.657106
In [59]: #using KNN
         # model
         lr = LinearRegression().fit( xk train, y train )
         # prediction
         yhat lr = lr.predict( x test )
         # performance
         lr result2 = ml error( 'Linear Regression with KNN Features', np.expm1( y test ), np.expm1( yhat lr ) )
         lr result2
```

#### Out[59]:

 Model Name
 MAE
 MAPE
 MSE
 RMSE

 0 Linear Regression with KNN Features
 1.689028
 0.19043
 3.661722
 1.913563

#### 4.4.2) Linear Regression Model - Cross Validation

```
In [60]: # k-fold CV (using all the 23 variables)
lm = LinearRegression()
scores = cross_val_score(lm, X_train, y_train, scoring='r2', cv=5)
scores
```

Out[60]: array([0.99682226, 0.99681473, 0.99687368, 0.99675945, 0.9967948 ])

## 4.4.2.1) Hyperparameter tuning

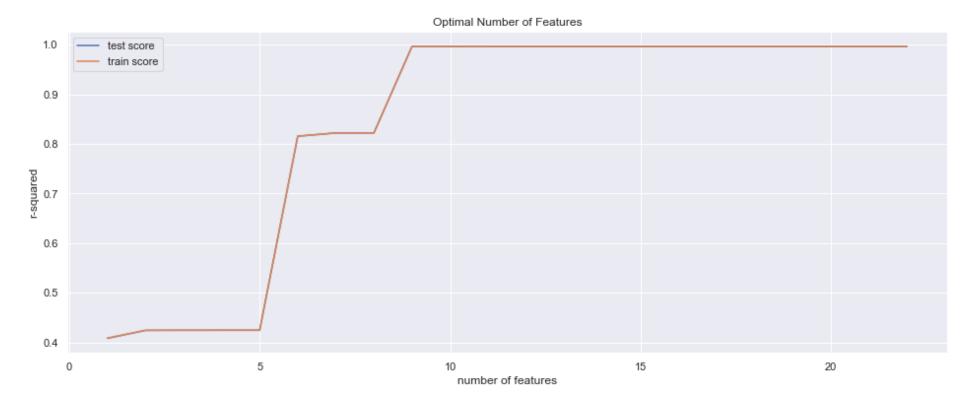
A common use of cross-validation is for tuning hyperparameters of a model. The most common technique is what is called grid search cross-validation.

```
In [63]: # step-1: create a cross-validation scheme
         folds = KFold(n splits = 5, shuffle = True, random state = 100)
         # step-2: specify range of hyperparameters to tune
         hyper params = [{'n features to select': list(range(1, 23))}]
         # step-3: perform grid search
         # 3.1 specify model
         lm = LinearRegression()
         lm.fit(X train, y train)
         rfe = RFE(lm)
         # 3.2 call GridSearchCV()
         model cv = GridSearchCV(estimator = rfe,
                                 param grid = hyper params,
                                 scoring= 'r2',
                                 cv = folds,
                                 verbose = 1,
                                 return train score=True)
         # fit the model
         model cv.fit(X train, y train)
```

```
In [64]: cv_results = pd.DataFrame(model_cv.cv_results_)
    plt.figure(figsize=(16,6))

    plt.plot(cv_results["param_n_features_to_select"], cv_results["mean_test_score"])
    plt.plot(cv_results["param_n_features_to_select"], cv_results["mean_train_score"])
    plt.xlabel('number of features')
    plt.ylabel('r-squared')
    plt.title("Optimal Number of Features")
    plt.legend(['test score', 'train score'], loc='upper left')
```

Out[64]: <matplotlib.legend.Legend at 0x7f9a73d07be0>



Looking at the above plot, it is clear that optimal number of features is 9.

```
In [65]: n_features_optimal = 9

lm = LinearRegression()
lm.fit(X_train, y_train)

rfe = RFE(lm, n_features_to_select=n_features_optimal)
rfe = rfe.fit(X_train, y_train)

# predict prices of X_test
y_pred = rfe.predict(X_test)
lr_result3 = ml_error( 'Linear Regression with with Kfold with 9 Features', np.expml( y_pred lr_result3)
```

MAPE

MSE

**RMSE** 

#### Out[65]:

**Model Name** 

**0** Linear Regression with with Kfold with 9 Features 0.034345 0.003776 0.002141 0.046276

MAE

In [ ]:

## 4.4.3) Linear Regression - Lasso

```
In [66]: # model
lrr = Lasso( alpha=0.00001 ).fit( x_train, y_train )

# prediction
yhat_lrr = lrr.predict( x_test )

# performance
lr_result4 = ml_error( 'Linear Regression - Lasso', np.expml( y_test ), np.expml( yhat_lrr ) )
lr_result4
```

#### Out[66]:

	Model Name	MAE	MAPE	MSE	RMSE
0	Linear Regression - Lasso	0.475231	0.052934	0.43179	0.657107

```
In [67]: # model
lrr = Lasso( alpha=0.00001 ).fit( xk_train, y_train )

# prediction
yhat_lrr = lrr.predict( xk_test )

# performance
lr_result5 = ml_error( 'Linear Regression - Lasso with KNN features', np.expml( y_test ), np.expml( yhat_lrr ) )
lr_result5
```

#### Out[67]:

Model Name MAE MAPE MSE RMSE

**0** Linear Regression - Lasso with KNN features 0.504285 0.056088 0.469406 0.685132

## 4.4.4) Ridge Regression

```
In [68]: rrr = Ridge()
    rrr.fit(x_train,y_train)
    yhat_rrr = rrr.predict(x_test)

lr_result6 = ml_error( 'Ridge Regression', np.expml( y_test ), np.expml( yhat_rrr ) )
    lr_result6
```

#### Out[68]:

Model Name MAE MAPE MSE RMSE

**0** Ridge Regression 0.475175 0.052928 0.431777 0.657097

```
In [69]: | rrr = Ridge()
         rrr.fit(xk train,y train)
         yhat rrr = rrr.predict(xk test)
         lr result7 = ml error( 'Ridge Regression with KNN Features', np.expml( y test ), np.expml( yhat rrr ) )
         lr result7
Out[69]:
                            Model Name
                                                 MAPE
                                                         MSE
                                                                RMSE
                                          MAE
          0 Ridge Regression with KNN Features 0.504236 0.056083 0.46939 0.685121
         4.4.5) Ridge Regression with GridSearchCV
In [70]: ridge param dict = {'ridge alpha': np.logspace(0, 10, 50) }
         ridge pipe = Pipeline([('scaler', StandardScaler()),
                                  ('ridge',Ridge())
                                 ])
```

#### Out[70]:

Model Name MAE MAPE MSE RMSE

0 Ridge Regression - Grid Search CV 0.475269 0.052938 0.431805 0.657119

#### Out[71]:

Model Name MAE MAPE MSE RMSE

## 4.5.6) Ridge Regression - Transformed Target Regressor

```
In [72]:
    preprocessor = make_column_transformer(
        (StandardScaler(),['year','odometer']),
        remainder="passthrough",
        verbose_feature_names_out=False, # avoid to prepend the preprocessor names
)

model = make_pipeline(
        preprocessor,
        TransformedTargetRegressor(
        regressor=Ridge(alpha=le-10), func=np.log10, inverse_func=exp10
        )
    )
    model.fit(x_train, y_train)
    y_pred = model.predict(x_test)

lr_result10 = ml_error( 'Ridge Regression - Transformed Target Regressor', np.expm1( y_test ), np.expm1( y_pred lr_result10)
```

#### Out[72]:

	Model Name	MAE	MAPE	MSE	RMSE
0	Ridge Regression - Transformed Target Regressor	0.475604	0.052896	0.428134	0.654319

#### **Evaluation**

With some modeling accomplished, we aim to reflect on what we identify as a high quality model and what we are able to learn from this. We should review our business objective and explore how well we can provide meaningful insight on drivers of used car prices. Your goal now is to distill your findings and determine whether the earlier phases need revisitation and adjustment or if you have information of value to bring back to your client.

### 5.1 Metric Evaluation

#### 5.1.2 Identification of Evaluation Metric

MAE: Absolute value of the difference between the real and the predicted number and divides it by the number of predictions, that is, for each value that the model predicts it varies the MAE value on average (both for more and for less). Due to the way the MAE is calculated, it is not sensitive to outliers.

MAPE: The MAPE simply represents the percentage of the MAE, that is, how much the error that the model has means in percentage of the real value.

RMSE: This is the error most used to measure the performance of the model and its value serves as a parameter in the process of trying to decrease the model error within the project. This high use of RMSE is due to the fact that it is sensitive to outliers and this helps data scientists to be more rigorous with model errors.

MSE: measures the amount of error in statistical models. It assesses the average squared difference between the observed and predicted values. When a model has no error, the MSE equals zero.

#### 5.1.2) Rationale behind use of evaluation metric

# Since the projects contains outliers, we will be using RMSE to determine the right model.

```
In [73]: modelling_result = pd.concat( [lr_result1, lr_result2, lr_result3, lr_result4, lr_result5, lr_result6, lr_result1
modelling_result.sort_values( 'RMSE' )
```

#### Out[73]:

	Model Name	MAE	MAPE	MSE	RMSE
0	Linear Regression with with Kfold with 9 Features	0.034345	0.003776	0.002141	0.046276
0	Ridge Regression - Transformed Target Regressor	0.475604	0.052896	0.428134	0.654319
0	Ridge Regression	0.475175	0.052928	0.431777	0.657097
0	Linear Regression	0.475208	0.052931	0.431789	0.657106
0	Linear Regression - Lasso	0.475231	0.052934	0.431790	0.657107
0	Ridge Regression - Grid Search CV	0.475269	0.052938	0.431805	0.657119
0	Ridge Regression with KNN Features	0.504236	0.056083	0.469390	0.685121
0	Linear Regression - Lasso with KNN features	0.504285	0.056088	0.469406	0.685132
0	Ridge Regression - Grid Search CV with KNN fea	0.504348	0.056095	0.469429	0.685149
0	Linear Regression with KNN Features	1.689028	0.190430	3.661722	1.913563

Linear Regression with K-fold seems to be the one with lowest RMSE. We will be taking that to move ahead with our evaulation

```
In [74]: n features optimal = 9
         lm = LinearRegression()
         lm.fit(X train, y train)
         rfe = RFE(lm, n_features_to_select=n_features_optimal)
         rfe = rfe.fit(X_train, y_train)
         # predict prices of X test
         y pred = rfe.predict(X test)
         mpe = mean_percentage_error( np.expm1( y_test ), np.expm1(y_pred) )
         mpe
```

Out[74]: -2.995707850959188e-05

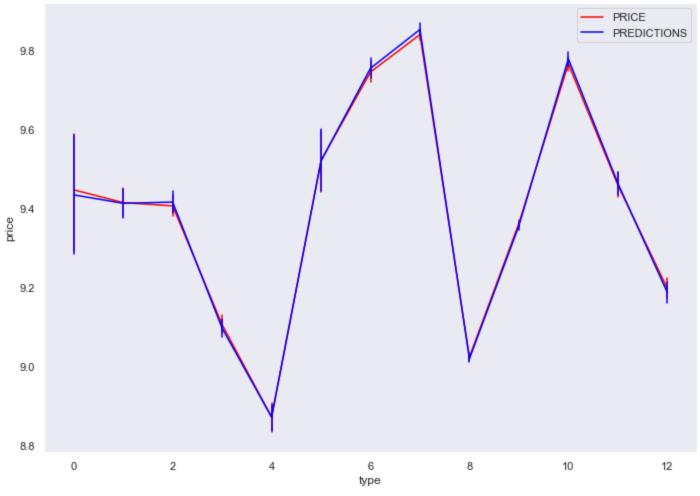
As the mean percentage error is closer to zero, it does not influence much.

```
In [75]: df_final = X_test[ final_columns_all ]
         # rescale
         #df final['price'] = np.expm1( df final['price'] )
         df final['predictions'] = np.expm1( y pred );
In [76]: df_final['error'] = df_final['price'] - df_final['predictions']
         df final['error rate'] = df final['predictions'] / df final['price']
```

In [ ]:

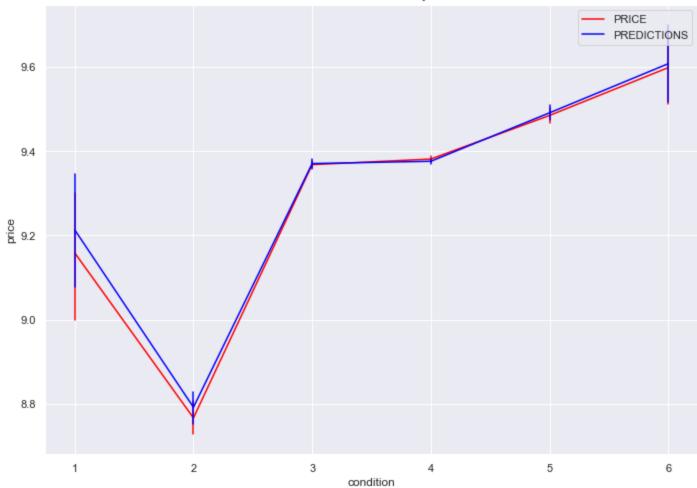
```
In [77]: sns.set_style("whitegrid", {'axes.grid': False})
    sns.set(rc={'figure.figsize':(11.7,8.27)})
    sns.lineplot( x='type', y='price', data=df_final, label='PRICE',color='red',err_style='bars' )
    fig = sns.lineplot( x='type', y='predictions', data=df_final, label='PREDICTIONS',color='blue',err_style='bars'
    fig.grid(False)
    fig.title.set_text('Model Price and Predictions by type')
```

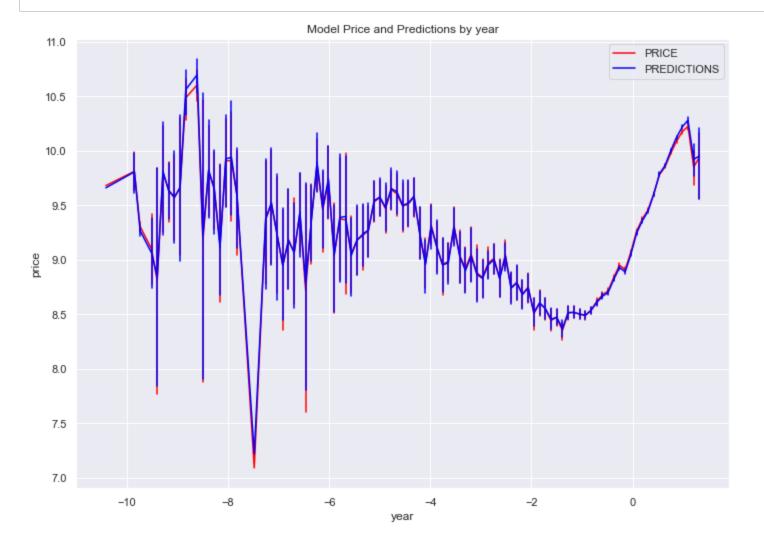




```
In [78]: sns.set_style("whitegrid", {'axes.grid': False})
sns.set(rc={'figure.figsize':(11.7,8.27)})
sns.lineplot( x='condition', y='price', data=df_final, label='PRICE', color='red',err_style='bars')
fig = sns.lineplot( x='condition', y='predictions', data=df_final, label='PREDICTIONS', color='blue',err_style='lately fig.title.set_text('Model Price and Predictions by condition')
```

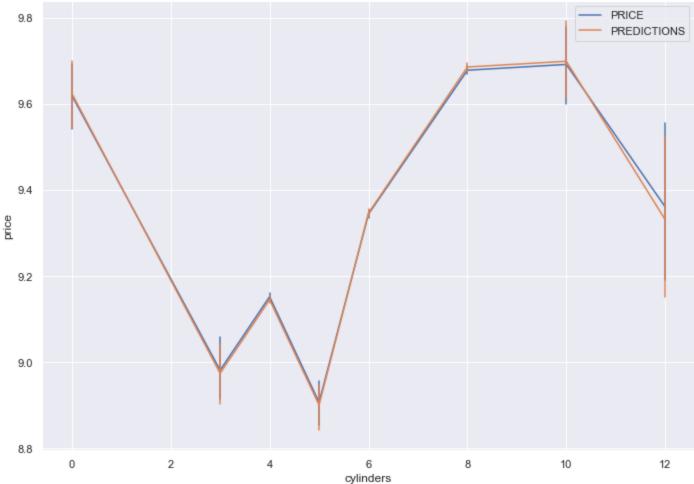




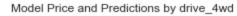


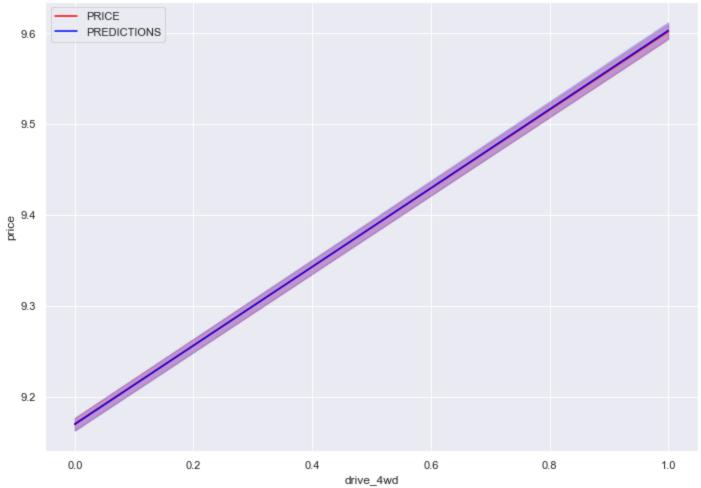
```
In [80]: sns.set(rc={'figure.figsize':(11.7,8.27)})
    sns.lineplot( x='cylinders', y='price', data=df_final, label='PRICE',err_style='bars' )
    fig = sns.lineplot( x='cylinders', y='predictions', data=df_final, label='PREDICTIONS' ,err_style='bars')
    fig.title.set_text('Model Price and Predictions by cylinders')
```



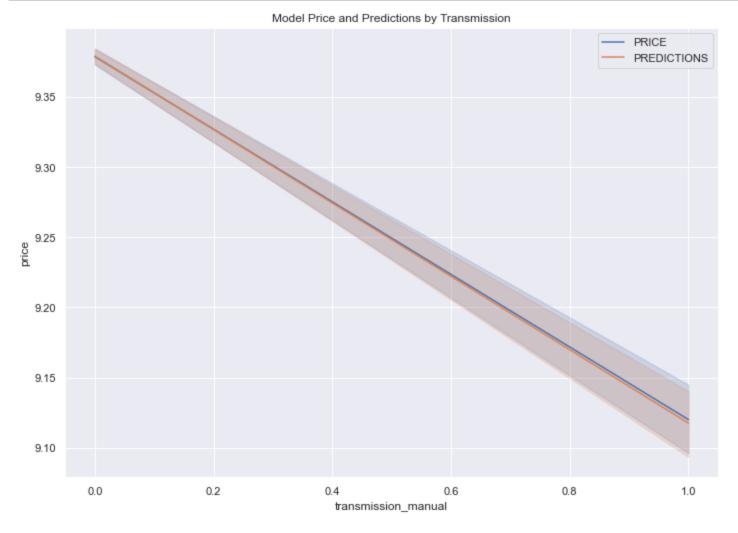


```
In [81]: sns.set(rc={'figure.figsize':(11.7,8.27)})
sns.lineplot( x='drive_4wd', y='price', data=df_final, label='PRICE',color='red' )
fig = sns.lineplot( x='drive_4wd', y='predictions', data=df_final, label='PREDICTIONS',color='blue' )
fig.title.set_text('Model Price and Predictions by drive_4wd')
```





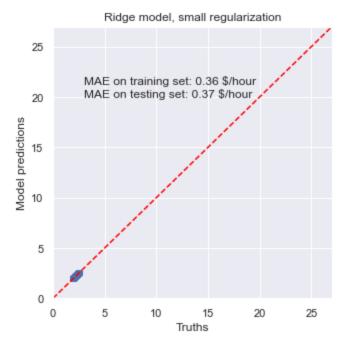
```
In [82]: sns.lineplot( x='transmission_manual', y='price', data=df_final, label='PRICE' )
fig = sns.lineplot( x='transmission_manual', y='predictions', data=df_final, label='PREDICTIONS')
fig.title.set_text('Model Price and Predictions by Transmission')
```



From the above plots, it is clear that the model is performing quite well. However, this is just the first cycle. We will have to do multiple cycles in order to determine the overall performance.

## **5.2 Interpretation of Coefficients**

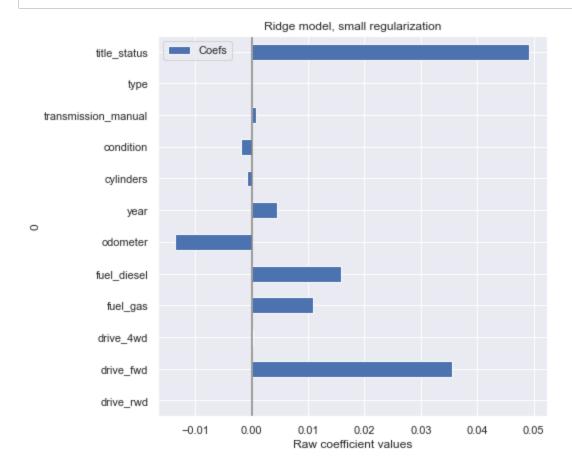
```
In [83]: fig, ax = plt.subplots(figsize=(5, 5))
    plt.scatter(y_test, y_pred)
    ax.plot([0, 1], [0, 1], transform=ax.transAxes, ls="--", c="red")
    plt.text(3, 20, string_score)
    plt.title("Ridge model, small regularization")
    plt.ylabel("Model predictions")
    plt.xlabel("Truths")
    plt.xlim([0, 27])
    _ = plt.ylim([0, 27])
```



```
In [84]: coef_table = pd.DataFrame(list(x_train.columns)).copy()
    coef_table.insert(len(coef_table.columns), "Coefs", rrr.coef_.transpose())
    coef_table = coef_table.set_index(0)
    print(coef_table)
```

	Coefs
0	
drive_rwd	-0.000007
drive_fwd	0.035584
drive_4wd	0.000238
fuel_gas	0.010833
fuel_diesel	0.015801
odometer	-0.013522
year	0.004481
cylinders	-0.000766
condition	-0.001850
transmission_manual	0.000717
type	-0.000131
title_status	0.049182

```
In [85]: coef_table.plot.barh(figsize=(9, 7))
    plt.title("Ridge model, small regularization")
    plt.axvline(x=0, color=".5")
    plt.xlabel("Raw coefficient values")
    plt.subplots_adjust(left=0.3)
    plt.show()
```



From the plot above, the most important factor in determining the prices is year. Vehicles with fuel type gas also play an important role in driving the prices of used cars. Drive with type rwd, manual transmission and fwd are other factors that have a correlation with the overall used car price.

In [ ]:

#### **Deployment**

Now that we've settled on our models and findings, it is time to deliver the information to the client. You should organize your work as a basic report that details your primary findings. Keep in mind that your audience is a group of used car dealers interested in fine tuning their inventory.

The goal here is to make the prediction model accessible to anyone. To achieve this, an API is created.

The architecture of the model in production:

AWS SageMaker provides an HTTPS endpoint for your model, availing it to provide inferences in three steps:

- 1) Create the model in SageMaker, including the relevant S3 path and Docker registry path
- 2) Create an endpoint configuration for an HTTPS endpoint
- 3) Create an HTTPS endpoint

**API** -> is the part that receives the requests and plays for the other parts so that the data is processed and then brings everything together, returning the final answer.

**Data Preparation** -> all the treatments and modifications we made to the data will be kept inside. When the Handler receives the raw data it will throw it here within this list of treatment codes so that they are prepared so that they can be ready to be used within the Machine Learning model.

**Model Training** -> this is our trained model that has been saved and will be placed inside this folder in our production architecture. The Handler will take the data processed within Data Preparation and play it inside the model so that it provides the prediction.

At the end of the construction of all this architecture and being put into production, the way it will be visualized can be through an App, Dashboard or a website.

In [ ]:

# 6) Recommendations to the dealer

#### **Summary**

Detailed summary is located <a href="https://github.com/spalakollu/Used-Cars/blob/main/Recommendations%20to%20the%20dealer.pdf">here (https://github.com/spalakollu/Used-Cars/blob/main/Recommendations%20to%20the%20dealer.pdf</a>)

Used vehicle market involves many factors when it comes to predicting the prices. Colors, vehicle type, manufacturer, model,price,transmission and vehicle ages are some of the significant factors we had a chance to analyze that affect the time a used vehicle stays in the lot. Few characteristics that are highly desirable among used vehicles that may help the dealer in determining the overall price.

- 1. Cars between 1980 and 2000 cost much lower compared to the cars from 2000.
- 2. Based on the data, the top 5 cars in the dataset are Chevrolet suv, ford truck, ford suv, jeep suv and ford pickup.
- 3. CA, NY and FL are the states where cars sales are more compared to the other states implying that price might be higher due to high demand.
- 4. Electric cars are expensive compared to gas, hybrid and diesel.
- 5. The price of cylinders is not directly correlated to the price of car.
- 6. Cars with color white, black, silver and grey are sold more compared to the other cars.
- 7. Cars with condition excellent are sold more compared to the cars good, new and like new.
- 8. SUVs and sedan-type vehicles are sold faster than Economy vehicles
- 9. Dealers should prefer to buy cars with low age with color black, while, or silver.
- 10. The top priced cars are tesla, Ferrari, ram and Porsche.

# 8) Next Steps

Future research is recommended to explore other factors that influence the sales period of a used vehicle. For example, the level of fuel-efficiency, level of discount from the original price. Incorporating these factors in the analysis can improve the accuracy to choose non-overage vehicles and have a positive impact on profit.