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Problem Set – Module 2
605.744.81 Information Retrieval
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1.) Character n-gram overlap is used for both automated spelling correction and personal name matching (i.e., deciding whether two names might be the same, a common database problem known as "record linkage"). Using a character 3- gram representation, how many distinct n-grams do "CHEONGSONG" and "CHEONMACHONG" have in common? What is the Dice-coefficient score for these two strings using 3-grams? What is the Dice score using 4-grams instead? Which score is higher?

## 3-grams

a.) Distinct 3-grams of CHEONGSONG:

CHE

**HEO** 

**EON** 

ONG

NGS

GSO

SON

**ONG** 

b.) Distinct 3-grams of CHEONMACHONG:

CHE

**HEO** 

**EON** 

**ONM** 

NMA

MAC

ACH

CHO

HON

**ONG** 

c.) Distinct 3-grams in common:

CHE

HEO

**EON** 

ONG

d.) Dice-coefficient score:

X = number of 3-grams for CHEONGSONG = 8

Y = number of 3-grams for CHEONMACHONG = 10

 $X \cap Y$  = number of 3-grams in common = 4

Dice – coefficient score = 
$$\frac{2|X \cap Y|}{|X| + |Y|} = \frac{2 * 4}{8 + 10} = \frac{8}{18} \approx 0.4444$$

## 4-grams

- a.) Distinct 4-grams of CHEONGSONG:
  - **CHEO**
  - **HEON**
  - **EONG**
  - ONGS
  - NGSO
  - GSON
  - SONG
- b.) Distinct 4-grams of CHEONMACHONG:
  - **CHEO**
  - **HEON**
  - **EONM**
  - **ONMA**
  - **NMAC**
  - MACH
  - **ACHO**
  - CHON
  - HONG
- c.) Distinct 4-grams in common:
  - CHEO
  - **HEON**
- d.) Dice-coefficient score:
  - X = number of 4-grams for CHEONGSONG = 7
  - Y = number of 4-grams for CHEONMACHONG = 9
  - $X \cap Y$  = number of 4-grams in common = 2

$$Dice-coefficient\ score = \frac{2|X \cap Y|}{|X|+|Y|} = \frac{2*2}{7+9} = \frac{4}{16} = 0.2500$$

## The dice-coefficient score using 3-grams is higher than the dice-coefficient score using 4-grams

- 2.) Compute the edit distance (or Levenshtein distance) for these two pairs of strings: (a) "CHEBYSHEV" and "TSCHEBYSCHEF"; and (b) "LEVINSTINE" and "LEVENSHTEIN". Then report a sequence of transformations for that cost that converts one string into the other. You should use unit costs for each operation: insertion, deletion, or substitution; that is, each step has a cost of 1.
  - a.) Edit Distance: Chebyshev and Tschebyschef

## Edit Distance Table:

	" "	С	Н	Ε	В	Y	S	Н	E	V
" "	0	1	2	3	4	5	6	7	8	9
T	1	1	2	3	4	5	6	7	8	9
S	2	2	2	3	4	5	5	7	8	9

С	3	2	3	3	4	5	6	6	7	8
Н	4	3	2	3	4	5	6	6	7	8
E	5	4	4	2	5	5	6	7	6	7
В	6	6	5	3	2	3	4	5	6	7
Y	7	7	7	6	4	2	3	4	5	6
S	8	8	8	8	7	3	2	3	4	5
С	9	8	9	9	9	4	3	3	4	5
Н	10	9	8	8	9	5	4	3	4	5
E	11	10	9	8	9	6	5	4	3	4
F	12	11	10	9	9	7	6	5	4	4

Based on the edit distance table above, we can see how that the edit distance between CHEBYSHEV and TSCHEBYSCHEF is 4. To convert CHEBYSHEV to TSCHEBYSCHEF we would need to perform the following steps:

- 1.) Insert T: Cost = 1
- 2.) Insert S: Cost = 1
- 3.) The letters "CHEBYS" are the same in both strings so there is no cost in keeping the letters as is.
- 4.) Insert C: Cost = 1
- 5.) Replace V to F: Cost = 1

The total cost after the three insert and one replace is 4.

b.) Edit Distance: Levinstine and Levenshtein

	" "	L	E	٧	ı	N	S	Т	ı	N	E
" "	0	1	2	3	4	5	6	7	8	9	10
L	1	0	1	2	3	4	5	6	7	8	9
E	2	2	0	1	2	3	4	5	6	7	7
٧	3	3	1	0	1	2	3	4	5	6	7
E	4	4	1	1	1	2	3	4	5	6	6
N	5	4	2	2	2	1	2	3	4	4	5
S	6	5	3	3	3	2	1	2	3	4	5
Н	7	6	4	4	4	3	2	2	3	4	5
Т	8	7	5	5	5	4	3	2	3	4	5
E	9	8	5	6	6	6	5	3	3	4	4
ı	10	9	6	6	6	7	6	4	3	4	5
N	11	10	7	7	7	6	7	5	4	3	4

Based on the edit distance table above, we can see how that the edit distance between LEVINSTINE and LEVENSHTEIN is 4. To convert LEVINSTINE to LEVENSHTEIN we would need to perform the following steps:

- 1.) The letters "Lev" are the same in both strings so there is no cost in keeping the letters as is.
- 2.) Replace I to E: Cost = 1
- 3.) The letters "NS" are the same in both strings so there is no cost in keeping the letters as is.

- 4.) Insert H: Cost = 1
- 5.) The letter, "t", is the same in both strings so there is no cost in keeping the letters as is.
- 6.) Insert E: Cost = 1
- 7.) The letter, "IN", is the same in both strings so there is no cost in keeping the letters as is.
- 8.) Delete E: Cost = 1

The total cost after one replace step, two inserts, and one delete step is 4.

- 3.) Following the method described in the textbook (or lecture materials), what are the Soundex codes for the strings: (a) "Daniels" and (b) "Hrabowski"? Show intermediate steps to produce the final code.
  - *a.*) *DANIELS = D542*

Steps to convert "DANIELS" to a Soundex code:

- I. D remains D since we retains the first letter of the word
- II. A becomes 0
- III. N becomes 5
- IV. I becomes 0
- V. E becomes 0
- VI. L becomes 4
- VII. S becomes 2
- VIII. We then have D050042. After removing all the zeroes from the resulting string, we are left with the 4-digit Soundex Code: D542
- *b.*) *HRABOWSKI* = *H612*

Steps to convert "HRABOWSKI" to a Soundex code:

- I. H remains H since we retains the first letter of the word
- II. R becomes 6
- III. A becomes 0
- IV. B becomes 1
- V. O becomes 0
- VI. W becomes 0
- VII. S becomes 2
- VIII. K becomes 2
- IX. I becomes 0
- X. We then have H60100220. After removing all the zeroes from the resulting string, we have: H6122
- XI. The code has two consecutive 2's which can be replaced with only the first 2. We then have the 4-digit Soundex code of: H612