Package 'LRMoE'

March 2, 2020

```
Type Package
Title LRMoE for actuarial loss modelling
Version 0.1.0
Date 2020-02-29
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Description This package is based on the Logit-
     Weighted Reduced Mixture of Experts (LRMoE) proposed by Fung et al. (2019),
     which is a flexible framework actuarial loss modelling.
License GPL-3
URL https://github.com/sparktseung/LRMoE
BugReports https://github.com/sparktseung/LRMoE/issues
Encoding UTF-8
LazyData false
Depends R (>= 3.5.1)
Imports actuar,
     copula,
     expint,
     EnvStats,
     ggplot2,
     matrixStats,
     NMOF,
     reshape2,
     rmutil,
     statmod,
     stats
RoxygenNote 7.0.2
R topics documented:
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cluster.mm.frequency Initializes parameter for frequency distributions using CMM.

Description

Initializes parameter for frequency distributions using CMM.

Usage

```
cluster.mm.frequency(Y, cluster)
```

Arguments

Y A vector of response variables.

cluster The cluster list vector returned by kmeans

Value

A list of parameter initialization.

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cluster.mm.severity Initializes parameter for severity distributions using CMM.

Description

Initializes parameter for severity distributions using CMM.

Usage

```
cluster.mm.severity(Y, cluster)
```

Arguments

Y A vector of response variables.

cluster The cluster list vector returned by kmeans

Value

A list of parameter initialization.

dataset.simulator Simulate y, given a fixed covariate matrix X and a model

Description

Simulate y, given a fixed covariate matrix X and a model

Usage

```
dataset.simulator(X, alpha, comp.dist, zero.prob, params.list)
```

Arguments

X A N*P matrix of of covariates	The first column must be 1. Each row may be
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different.

alpha A g*P matrix of logit regression coefficients.

comp.dist A d*g matrix of strings, describing component distributions by dimension and

by component.

zero.prob A d*g matrix of numbers between 0 and 1, describing zero probability masses

by dimension and by component.

paramas.list A list of length d, where each element is a sublist of length g. Each sublist

contains one numeric vector, which is the initial parameter guess for the corre-

sponding comp.dist.

Value

A matrix of simulated values, where each row represents a policyholder and each column a dimension of the response variable.

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DemoData

Demo data for LRMoE.

Description

- X: A matrix of covariates required by the LRMoE fitting function (complete).
- Y: A matrix of response required by the LRMoE fitting function (complete).
- X.obs: A matrix of covariates required by the LRMoE fitting function (after truncation and censoring).
- Y. obs: A matrix of response required by the LRMoE fitting function (after truncation and censoring).

dgammacount.new

Modified GammaCount pmf for better numerical accuracy.

Description

Modified GammaCount pmf for better numerical accuracy.

Usage

```
dgammacount.new(y, m, s, log = FALSE)
```

Arguments

y Vector of gamma count values.

m, s Paramaters of Gamma count distribution.

See Also

GammaCount.

LRMoE.fit

Fit an LRMoE model.

Description

Fit an LRMoE model.

LRMoE.fit 5

Usage

```
LRMoE.fit(
  Υ,
  Χ,
  n.comp = 2,
  comp.dist = NULL,
  alpha.init = NULL,
  zero.init = NULL,
  params.init = NULL,
  penalty = TRUE,
  hyper.alpha = NULL,
  hyper.params = NULL,
  eps = 0.001,
  alpha.iter.max = 5,
  ecm.iter.max = 200,
  grad.jump = TRUE,
  grad.period = 5,
  grad.seq = 2^{(seq(8) - 1) - 1}
  print = TRUE
)
```

Arguments

Χ

comp.dist

zero.init

params.init

hyper.alpha

hyper.params

penalty

Y A N*4d matrix of numerics, where N is sample size and d is the dimension of each obsevation. Each block of four columns should be organized as (t1,y1,yu,tu), representing the truncation lower bound, censoring lower bound, censoring upper bound and truncation upper bound.

A N*P matrix of numerics, where P is the number of covariates. The first column of X should be 1, which is the intercept.

n.comp A numeric which indicates the number of experts desired to fit the data. Default value is 2.

A d*g matrix of strings, which specify the component distributions to fit. The rows represent the dimensions of Y, while the columns represent the component distributions. See below for more details.

alpha.init A g*P matrix of numerics, which contains initial guess of the logit regression coefficients. The last row should all be zero, representing the default latent class. If no initialization is provided, all coefficients are set to zero.

A d*g matrix of numerics in (0,1), which specify the probability mass at zero for component distributions. If the corresponding entry in comp.dist is not zero-inflated, zero value must by supplied.

A list of length d, where each element is a sublist of length g. Each sublist contains one numeric vector, which is the initial parameter guess for the corresponding comp.dist.

TRUE/FALSE: whether the parameters are penalized for their magnitude. Default (and recommended) is TRUE.

A g*P matrix of numerics, which contains penalties for alpha.init. If penalty=T but no hyper.alpha is provided, a constant is used.

A list of length d, where each element is a sublist of length g. Each sublist contains one numeric vector, which is the corresponding penalty for params.init.

LRMoE.loglik

eps	Stopping criteria for loglikelihood convergence. Default is 1e-03.		
alpha.iter.max	Maximum number of iterations for updating alpha. Defauls is 5. See also $alpha.m.recur.$		
ecm.iter.max	Maximum number of iterations for ECM. Default is 200.		
grad.jump	TRUE/FALSE: whether to use an approximated gradient jump to speed up convergence.		
grad.period	How often should grad. jump occur. Default is every 5 iterations.		
grad.seq	How are the gradient sequence selected. Default is 2^(seq(8)-1)-1.		
print	TRUE/FALSE: whether paramater updates are printed on screen. Default is TRUE.		

IKUL

LRMoE.loglik

Computes the loglikelihood of LRMoE, given X, Y and a fitted model.

Description

Computes the loglikelihood of LRMoE, given X, Y and a fitted model.

Usage

```
LRMoE.loglik(X, Y, model, penalty = TRUE, hyper.alpha, hyper.params)
```

Arguments

X A N*P matrix of covariates.
Y A N*d matrix of response.

model A list of parameters specifying an LRMoE model, including

- alpha: A g*P matrix, where g is the number of components and P is the number of covariates.
- comp.dist: A d*g matrix of strings, describing component distributions by dimension and by component.
- zero.prob: A d*g matrix of numbers between 0 and 1, describing zero probability masses by dimension and by component.
- params.list: A list of length d, where each element is a sublist of length g. Each sublist contains one numeric vector, which is the initial parameter guess for the corresponding comp.dist.

penalty TRUE/FALSE, which indicates whether parameter penalty should be applied.

Default (and recommended) is TRUE.

hyper.alpha A numeric, which penalizes the magnitude of alpha.

hyper.params A list of length d. Each element is a sublist of length g. Each element of a

sublist is a vector of numerics, which penalizes expert parameters. See also

expert.loglik.pen.dim.comp.

Value

Loglikelihood (with and without penalty), AIC and BIC.

mgammacount 7

mo	amı	mac	'OII	nt

Calculates moments of GammaCount using finite approximation.

Description

Calculates moments of GammaCount using finite approximation.

Usage

```
mgammacount(order, m, s, tol = 1e-10)
```

Arguments

order A vector of positive power indices.

m, s Paramaters of Gamma count distribution.

tol Cut-off probability threshold. Values above (1-tol) are discarded.

Value

A vector of Gamma count distribution moments.

See Also

GammaCount.

pgammacount.new

Modified GammaCount cdf for better numerical accuracy.

Description

Modified GammaCount cdf for better numerical accuracy.

Usage

```
pgammacount.new(q, m, s, log = FALSE)
```

Arguments

q Vector of quantiles.

m, s Paramaters of Gamma count distribution.

See Also

GammaCount.

```
plot.dataset.class.prob
```

Plots a stacked bar chart of most likely latent class proportion, given a matrix of covariates.

Description

Plots a stacked bar chart of most likely latent class proportion, given a matrix of covariates.

Usage

```
## S3 method for class 'dataset.class.prob'
plot(X, alpha, title = "Proportion of Latent Classes")
```

Arguments

X A matrix of covariates.

alpha A matrix of logit regression coefficients.

title A text string for plot title.

Value

A ggplot2 object.

See Also

```
LRMoE.fit, predict.class
```

```
plot.dataset.prob.posterior
```

Plots two stacked bar charts of most likely latent class proportions, which contrasts prior and posterior latent class proportions, given a covariate matrix.

Description

Plots two stacked bar charts of most likely latent class proportions, which contrasts prior and posterior latent class proportions, given a covariate matrix.

Usage

```
## S3 method for class 'dataset.prob.posterior'
plot(
    X,
    Y,
    alpha,
    comp.dist,
    zero.prob,
    params.list,
    title = "Proportion of Latent Classes"
)
```

plot.ind.class.prob 9

Arguments

X A matrix of covariates.

Y A matrix of observed responses for X.

A matrix of logit regression coefficients.

comp.dist A d*g matrix of strings, which specify the component distributions to fit. The

rows represent the dimensions of Y, while the columns represent the component

distributions.

zero.prob A d*g matrix of numerics in (0,1), which specify the probability mass at zero

for component distributions.

title A text string for plot title.

params.init A list of length d, where each element is a sublist of length g. Each sublist

contains one numeric vector, which is the parameter value for the corresponding

comp.dist.

Value

A ggplot2 object.

See Also

LRMoE.fit, predict.class.posterior

 $\verb|plot.ind.class.prob| Plots a stacked bar chart of latent class probabilities, given a covariate$

vector.

Description

Plots a stacked bar chart of latent class probabilities, given a covariate vector.

Usage

```
## S3 method for class 'ind.class.prob'
plot(X, alpha, title = "Prediction of Latent Classes")
```

Arguments

X A vector of covariates for one policyholder.

alpha A matrix of logit regression coefficients.

title A text string for plot title.

Value

A ggplot2 object.

```
LRMoE.fit, predict.class.prob
```

```
plot.ind.class.prob.posterior
```

Plots two stacked bar charts of latent class probabilities, which contrasts prior and posterior latent class probabilities, given a covariate vector.

Description

Plots two stacked bar charts of latent class probabilities, which contrasts prior and posterior latent class probabilities, given a covariate vector.

Usage

```
## S3 method for class 'ind.class.prob.posterior'
plot(
    X,
    Y,
    alpha,
    comp.dist,
    zero.prob,
    params.list,
    title = "Prediction of Latent Classes"
)
```

Arguments

X	A matrix of covariates.
Υ	A matrix of observed responses for X.

alpha A matrix of logit regression coefficients.

comp.dist A d*g matrix of strings, which specify the component distributions to fit. The

rows represent the dimensions of Y, while the columns represent the component

distributions.

zero.prob A d*g matrix of numerics in (0,1), which specify the probability mass at zero

for component distributions.

params.list A list of length d, where each element is a sublist of length g. Each sublist

contains one numeric vector, which is the parameter value for the corresponding

comp.dist.

title A text string for plot title.

Value

A ggplot2 object.

```
LRMoE.fit, predict.class.prob.posterior
```

plot.ind.fitted.dist

 ${\tt plot.ind.fitted.dist} \quad \textit{Plot the fitted density, given a vector of covariates and a model}$

Description

Plot the fitted density, given a vector of covariates and a model

Usage

```
## S3 method for class 'ind.fitted.dist'
plot(
    X,
    alpha,
    comp.dist,
    zero.prob,
    params.list,
    plot.dim = 1,
    plot.lim = NULL
)
```

Arguments

Χ	A vector of covariates.
alpha	A g*P matrix of numerics, which contains initial guess of the logit regression coefficients. The last row should all be zero, representing the default latent class.
comp.dist	A d*g matrix of strings, which specify the component distributions to fit. The rows represent the dimensions of Y, while the columns represent the component distributions.
zero.prob	A $d*g$ matrix of numerics in $(0,1)$, which specify the probability mass at zero for component distributions.
params.list	A list of length d, where each element is a sublist of length g. Each sublist contains one numeric vector, which is the parameter value for the corresponding comp.dist.
plot.dim	A numeric indicating which dimention of y to plot.
plot.lim	Upper bound of y for plotting. Default is 50, if no value is provided.

Value

A ggplot2 object.

```
LRMoE.fit
```

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predict.class	Predict the most likely latent class, given a fixed covariate matrix X
	and a model.

Description

Predict the most likely latent class, given a fixed covariate matrix X and a model.

Usage

```
## S3 method for class 'class'
predict(X, alpha)
```

Arguments

X A matrix of covariates.

alpha A matrix of logit regression coefficients.

Value

A vector of the most likely latent class by observation.

See Also

```
LRMoE.fit.
```

```
predict.class.posterior
```

Predict the most likely latent class, given a fixed covariate matrix X and a model.

Description

Predict the most likely latent class, given a fixed covariate matrix X and a model.

Usage

```
## S3 method for class 'class.posterior'
predict(X, Y, alpha, comp.dist, zero.prob, params.list)
```

Arguments

X A matrix of covariates.

Y A matrix of observed responses for X. alpha A matrix of logit regression coefficients.

comp.dist A d*g matrix of strings, which specify the component distributions to fit. The

rows represent the dimensions of Y, while the columns represent the component

distributions.

predict.class.prob 13

zero.prob A d*g matrix of numerics in (0,1), which specify the probability mass at zero

for component distributions.

params.init A list of length d, where each element is a sublist of length g. Each sublist

contains one numeric vector, which is the parameter value for the corresponding

comp.dist.

Value

A vector of the most likely latent class by observation.

See Also

LRMoE.fit.

predict.class.prob

Predict the latent class probabilities, given a fixed covariate matrix X and a model.

Description

Predict the latent class probabilities, given a fixed covariate matrix X and a model.

Usage

```
## S3 method for class 'class.prob'
predict(X, alpha)
```

Arguments

X A matrix of covariates.

alpha A matrix of logit regression coefficients.

Value

A matrix of latent class probabilities by observation and by component.

```
LRMoE.fit.
```

14 predict.cte

```
predict.class.prob.posterior
```

Predict the posterior latent class probabilities, given a fixed covariate matrix X, Y and a model.

Description

Predict the posterior latent class probabilities, given a fixed covariate matrix X, Y and a model.

Usage

```
## S3 method for class 'class.prob.posterior'
predict(X, Y, alpha, comp.dist, zero.prob, params.list)
```

Arguments

,	V	٨	moteix	٥f	acresiates
	X	Α	maırıx	OL	covariates.

Y A matrix of observed responses for X. alpha A matrix of logit regression coefficients.

comp.dist A d*g matrix of strings, which specify the component distributions to fit. The

rows represent the dimensions of Y, while the columns represent the component

distributions.

zero.prob A d*g matrix of numerics in (0,1), which specify the probability mass at zero

for component distributions.

params.list A list of length d, where each element is a sublist of length g. Each sublist

contains one numeric vector, which is the parameter value for the corresponding

comp.dist.

Value

A matrix of latent class probabilities by observation and by component.

See Also

```
LRMoE.fit.
```

predict.cte

Predict the CTE of y, given a fixed covariate matrix X and a model.

Description

Predict the CTE of y, given a fixed covariate matrix X and a model.

Usage

```
## S3 method for class 'cte'
predict(X, alpha, comp.dist, zero.prob, params.list, prob = NULL)
```

predict.excess 15

Arguments

Χ A matrix of covariates. alpha A matrix of logit regression coefficients. A d*g matrix of strings, which specify the component distributions to fit. The comp.dist rows represent the dimensions of Y, while the columns represent the component distributions. zero.prob A d*g matrix of numerics in (0,1), which specify the probability mass at zero for component distributions. params.list A list of length d, where each element is a sublist of length g. Each sublist contains one numeric vector, which is the parameter value for the corresponding comp.dist. probs A vector of probabilities. Default is a vector of length d of 0.95, if no value is

Value

A matrix of CTE.

See Also

LRMoE.fit, predict.quantile.

provided.

predict.excess	Predict the excess mean of y, given a fixed covariate matrix X, a model
	and a vector of limits by dimension.

Description

Predict the excess mean of y, given a fixed covariate matrix X, a model and a vector of limits by dimension.

Usage

```
## S3 method for class 'excess'
predict(X, alpha, comp.dist, zero.prob, params.list, limit)
```

Arguments

Χ	A matrix of covariates.
alpha	A matrix of logit regression coefficients.
comp.dist	A d*g matrix of strings, which specify the component distributions to fit. The rows represent the dimensions of Y, while the columns represent the component distributions.
zero.prob	A d*g matrix of numerics in (0,1), which specify the probability mass at zero for component distributions.
params.list	A list of length d, where each element is a sublist of length g. Each sublist contains one numeric vector, which is the parameter value for the corresponding comp.dist.
limit	A vector of limit to apply to each dimension of y.

16 predict.limit

Value

A matrix of excess mean values by observation and by dimension. This is equan to predict.mean -predict.limit.

See Also

```
LRMoE.fit, predict.limit.
```

predict.limit	Predict the limited mean of y, given a fixed covariate matrix X, a model
	and a vector of limits by dimension.

Description

Predict the limited mean of y, given a fixed covariate matrix X, a model and a vector of limits by dimension.

Usage

```
## S3 method for class 'limit'
predict(X, alpha, comp.dist, zero.prob, params.list, limit)
```

Arguments

Χ	A matrix of covariates.
alpha	A matrix of logit regression coefficients.
comp.dist	A d*g matrix of strings, which specify the component distributions to fit. The rows represent the dimensions of Y, while the columns represent the component distributions.
zero.prob	A d*g matrix of numerics in (0,1), which specify the probability mass at zero for component distributions.
params.list	A list of length d, where each element is a sublist of length g. Each sublist contains one numeric vector, which is the parameter value for the corresponding comp.dist.
limit	A vector of limit to apply to each dimension of y.

Value

A matrix of limited mean values by observation and by dimension. Calculation is done for severity distributions only. NA values are returned for frequency distributions.

```
LRMoE.fit, GammaSupp.
```

predict.mean 17

predict.mean	Predict the mean of y, given a fixed covariate matrix X and a model.

Description

Predict the mean of y, given a fixed covariate matrix X and a model.

Usage

```
## S3 method for class 'mean'
predict(X, alpha, comp.dist, zero.prob, params.list)
```

Arguments

Х	A matrix of covariates.
alpha	A matrix of logit regression coefficients.
comp.dist	A d*g matrix of strings, which specify the component distributions to fit. The rows represent the dimensions of Y, while the columns represent the component distributions.
zero.prob	A d*g matrix of numerics in (0,1), which specify the probability mass at zero for component distributions.

params.list A list of length d, where each element is a sublist of length g. Each sublist contains one numeric vector, which is the parameter value for the corresponding

comp.dist.

Value

A matrix of mean values by observation and by dimension.

See Also

```
LRMoE.fit.
```

predict.quantile Predict the VaR of y, given a fixed covariate matrix X and a model.

Description

Predict the VaR of y, given a fixed covariate matrix X and a model.

Usage

```
## S3 method for class 'quantile'
predict(X, alpha, comp.dist, zero.prob, params.list, prob = NULL)
```

18 predict.var

Arguments

X A matrix of covariates.

alpha A matrix of logit regression coefficients.

comp.dist A d*g matrix of strings, which specify the component distributions to fit. The

rows represent the dimensions of Y, while the columns represent the component

distributions.

zero.prob A d*g matrix of numerics in (0,1), which specify the probability mass at zero

for component distributions.

params.list A list of length d, where each element is a sublist of length g. Each sublist

contains one numeric vector, which is the parameter value for the corresponding

comp.dist.

probs A vector of probabilities. Default is a vector of length d of 0.95, if no value is

provided.

Value

A matrix of VaR.

See Also

LRMoE.fit, predict.cte.

predict.var

Predict the variance of y, given a fixed covariate matrix X and a model.

Description

Predict the variance of y, given a fixed covariate matrix X and a model.

Usage

```
## S3 method for class 'var'
predict(X, alpha, comp.dist, zero.prob, params.list)
```

Arguments

X A matrix of covariates.

alpha A matrix of logit regression coefficients.

comp.dist A d*g matrix of strings, which specify the component distributions to fit. The

rows represent the dimensions of Y, while the columns represent the component

distributions.

zero.prob A d*g matrix of numerics in (0,1), which specify the probability mass at zero

for component distributions.

params.list A list of length d, where each element is a sublist of length g. Each sublist

contains one numeric vector, which is the parameter value for the corresponding

comp.dist.

predict.var 19

Value

A matrix of variance by observation and by dimension.

See Also

LRMoE.fit.

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