

# Week 1- Introduction to model checking

B. Srivathsan

Chennai Mathematical Institute

*NPTEL-course*

July - November 2015

# Course overview

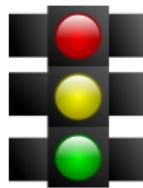
What are we **interested** in?

What are we **interested** in?

## Software Controllers

Code that controls the working of an

**Information and Communication (ICT) device**



*Traffic lights controller*



*Flight control*



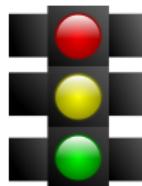
*Automatic gear control*



*ATM*



*Pacemaker*



*Traffic lights controller*



*Flight control*



*Automatic gear control*



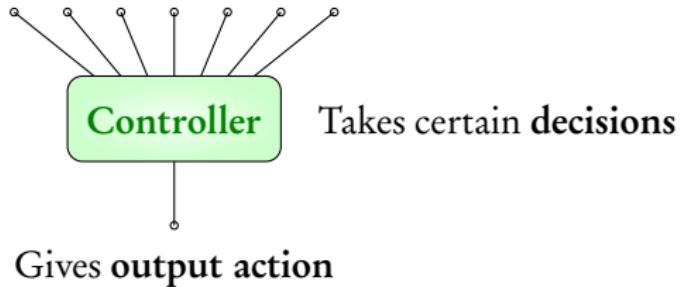
*ATM*



*Pacemaker*

*Lifts, Automatic doors, Hardware circuits, Netbanking ... and many more!*

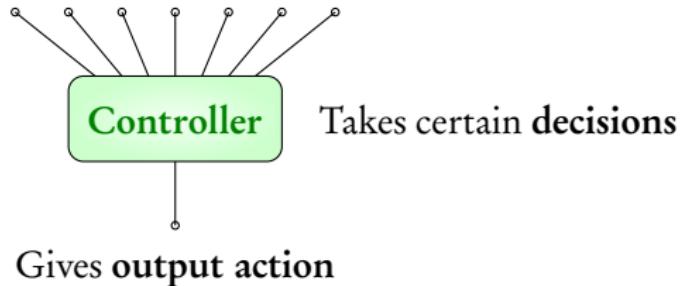
Listens to **various inputs**



Takes certain **decisions**

Gives **output action**

Listens to various inputs



Many **safety-critical** systems controlled by code

## How **reliable** is the controlling code?

- ▶ **decision making** should be correct
- ▶ **all possible scenarios** should be considered

# Bugs are costly

- ▶ Intel's Pentium II processor:
  - Error in floating point division code (1994)
    - ▶ Loss of 475 million US dollars
- ▶ Ariane 5 rocket:
  - Error in the control software (1996)
    - ▶ Crashed 36 seconds after launch
- ▶ Therac-25 radiation therapy machine:
  - Error in control software (1985 - 1987)
    - ▶ Death of 6 patients due to radiation overdose

## Goal: Make **low-defect** software controllers

Traditional testing **insufficient** for safety-critical systems

## Goal: Make low-defect software controllers

Traditional testing **insufficient** for safety-critical systems

→ A new **verification technology** called **Model-checking**



Edmund Clarke



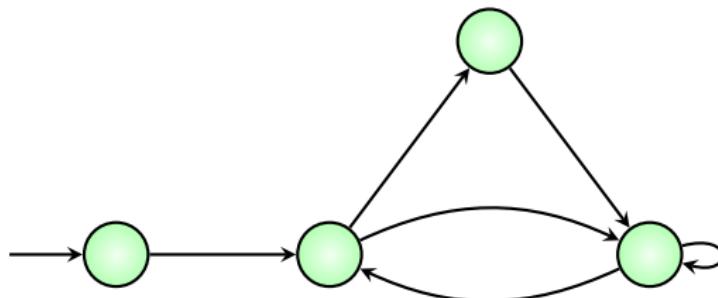
Allen Emerson



Joseph Sifakis

# Model Checking

Uses **finite state machines** to model and verify controllers



## Some places where **Model Checking** technology is used

- ▶ *Hardware:* Intel, IBM, Synopsys
- ▶ *Avionics:* Rockwell Collins, Honeywell
- ▶ *Automobiles:* Toyota
- ▶ *Space:* NASA, European Space Agency
- ▶ *Others:* Microsoft Research, Tata, Mathworks

## Some places where **Model Checking** technology is used

- ▶ *Hardware:* Intel, IBM, Synopsys
- ▶ *Avionics:* Rockwell Collins, Honeywell
- ▶ *Automobiles:* Toyota
- ▶ *Space:* NASA, European Space Agency
- ▶ *Others:* Microsoft Research, Tata, Mathworks

Backed by many **university groups** from all over the world!



Edmund Clarke



Allen Emerson



Joseph Sifakis

Turing Award'07 for their work on Model-checking

## Why do this course?

- ▶ Various industries **adopting** model-checking into their design cycle
- ▶ Need engineers **qualified** in model-checking technology
- ▶ Scope for **higher studies**

# In this course

Introduction to **techniques and tools** used in Model-Checking

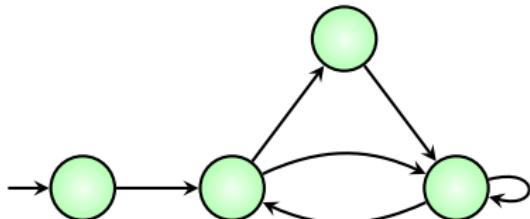
**Book:** Principles of Model Checking,  
*Christel Baier and Joost-Pieter Katoen*, MIT Press (2008)

# In this course

Introduction to **techniques and tools** used in Model-Checking

**Book:** Principles of Model Checking,

*Christel Baier and Joost-Pieter Katoen*, MIT Press (2008)



$(\{q_1, q_2, q_3, q_4\}, \delta)$

$\delta(q_1) = q_2, \delta(q_2) = \{q_3, q_4\}$

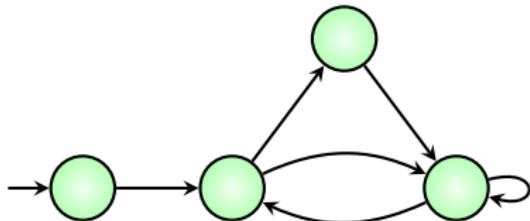
$\delta(q_3) = q_4, \delta(q_4) = \{q_2, q_4\}$

# In this course

Introduction to **techniques and tools** used in Model-Checking

**Book:** Principles of Model Checking,

*Christel Baier and Joost-Pieter Katoen*, MIT Press (2008)



$(\{q_1, q_2, q_3, q_4\}, \delta)$

$\delta(q_1) = q_2, \delta(q_2) = \{q_3, q_4\}$

$\delta(q_3) = q_4, \delta(q_4) = \{q_2, q_4\}$

Bachelors/Masters in CS/IT/EEE/ECE welcome!

Hope you'll **enjoy** the course!

# Week-1: Introduction to model checking

B. Srivathsan

Chennai Mathematical Institute

*NPTEL-course*

July - November 2015

# Module 1: **Modeling code behaviour**

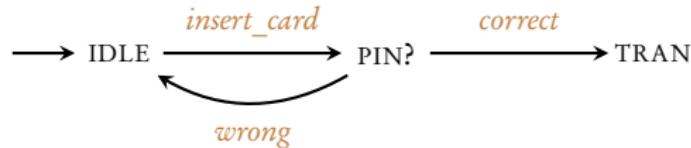


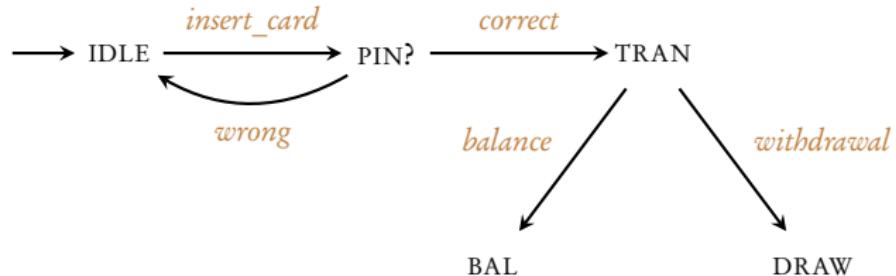


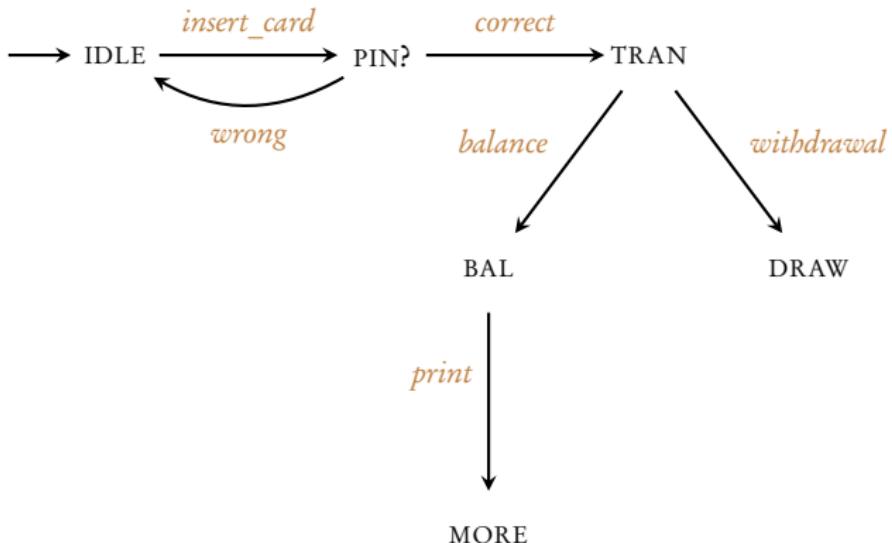
→ IDLE

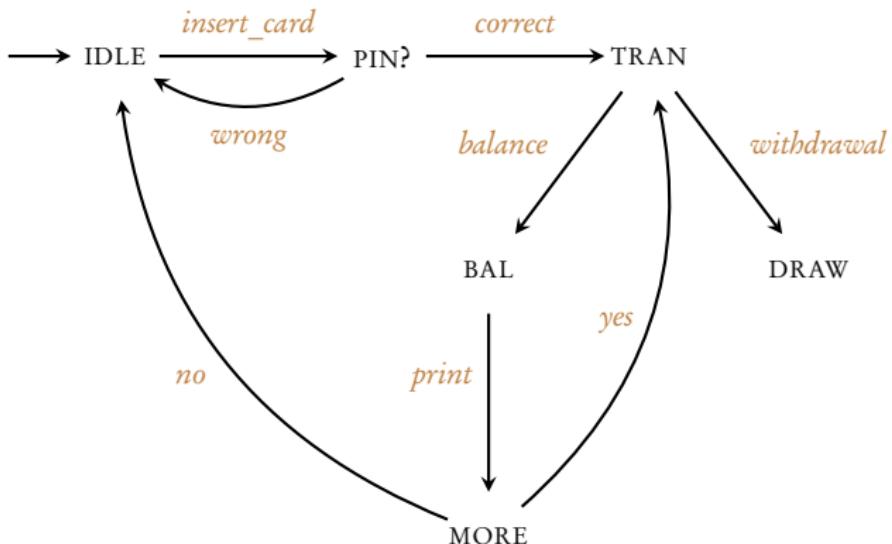


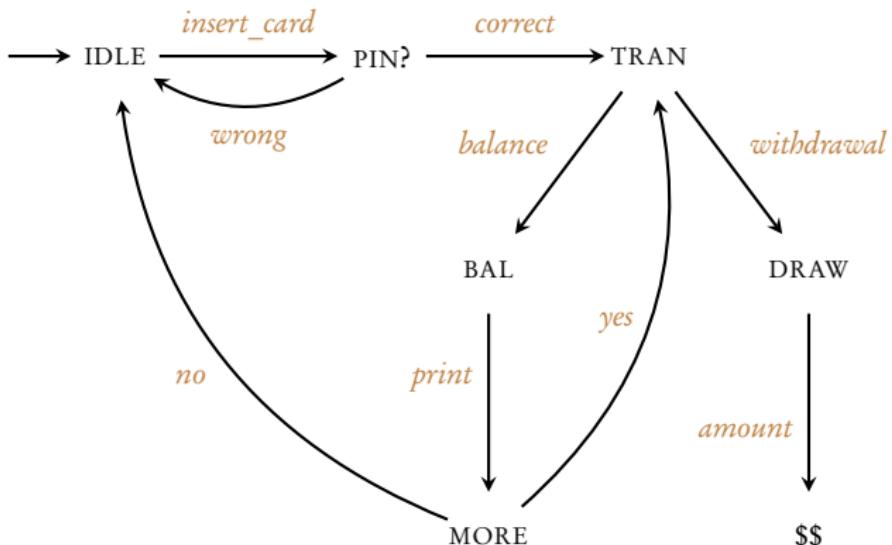
→ IDLE → *insert\_card* → PIN?

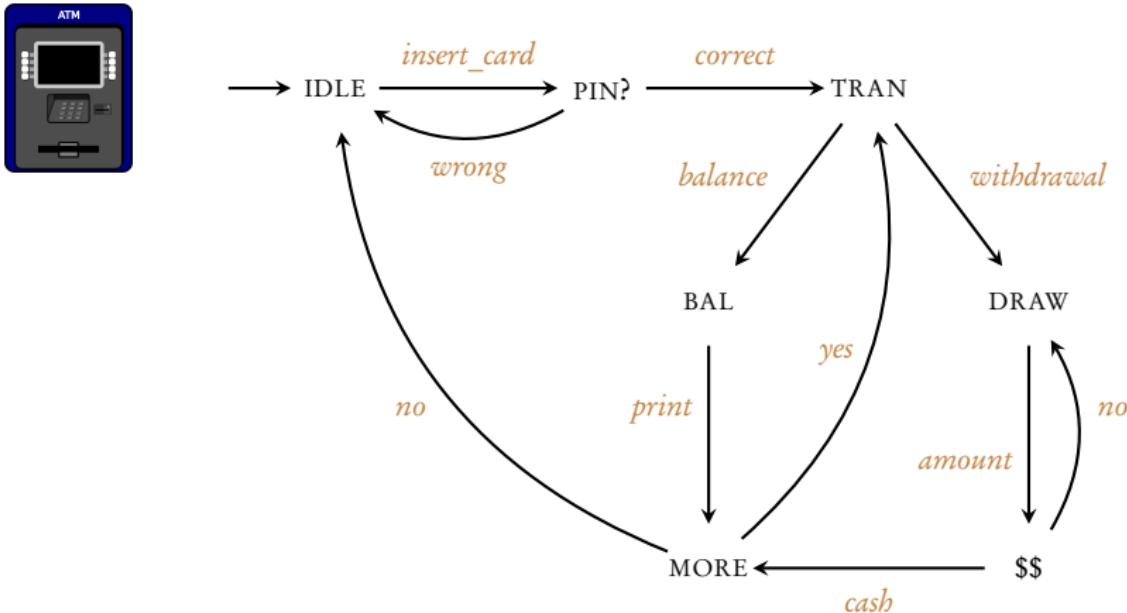


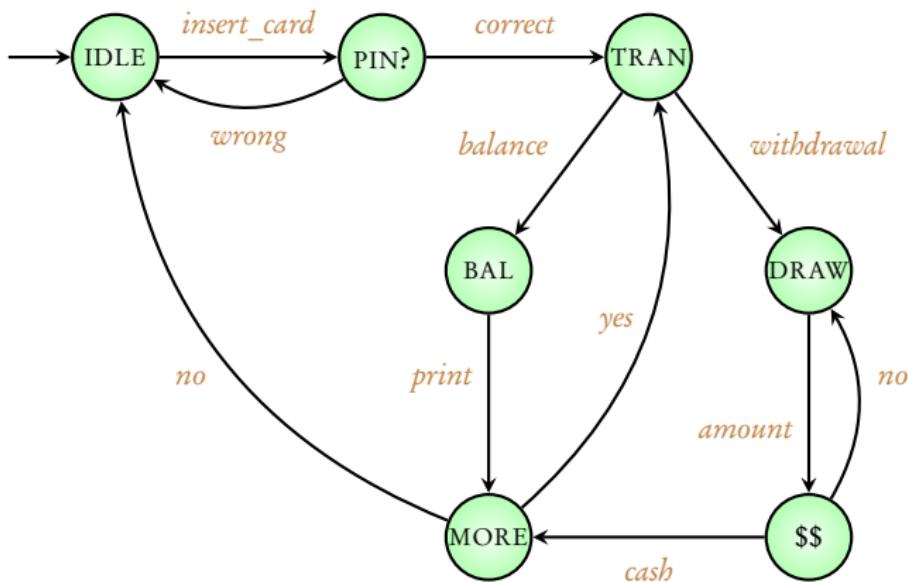


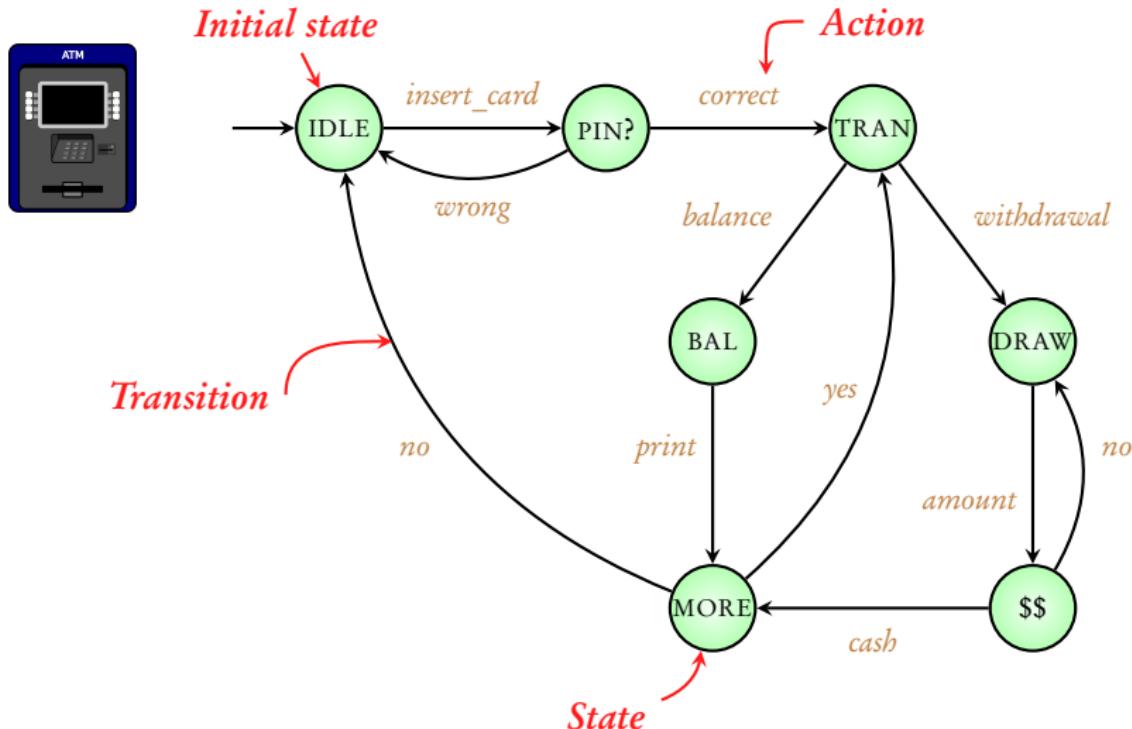




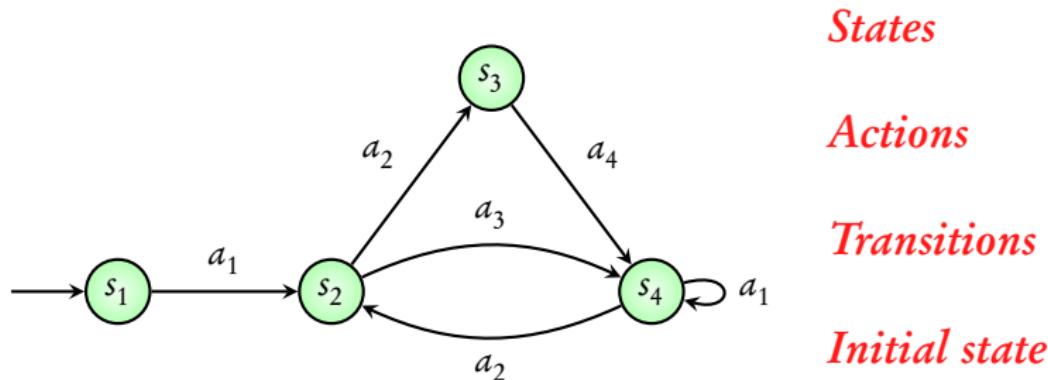






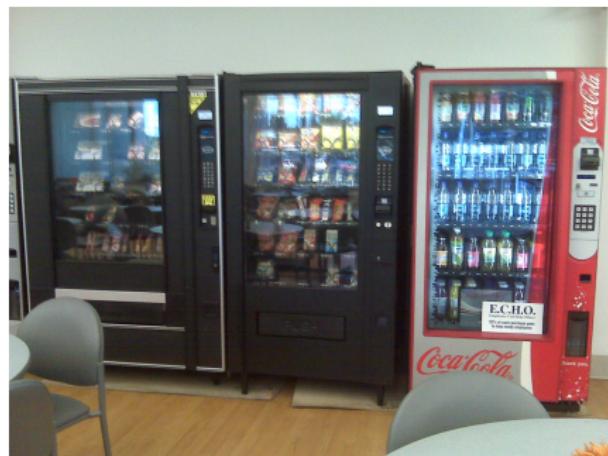


# Transition system



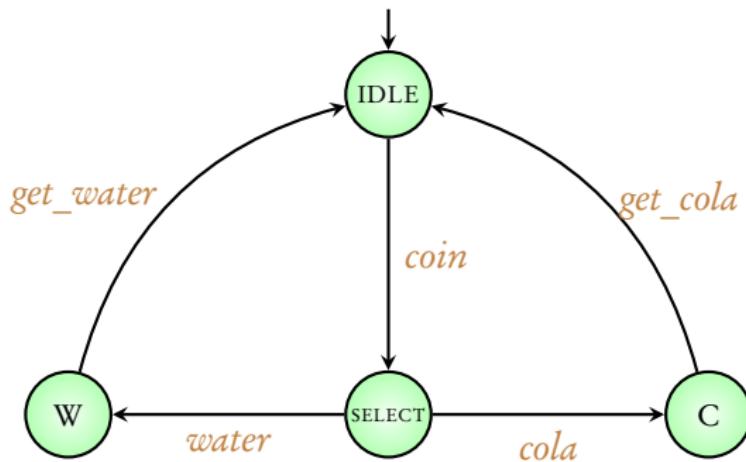
**Other names:** Finite-state machines, State-transition graphs

## Coming next: Modeling a vending machine

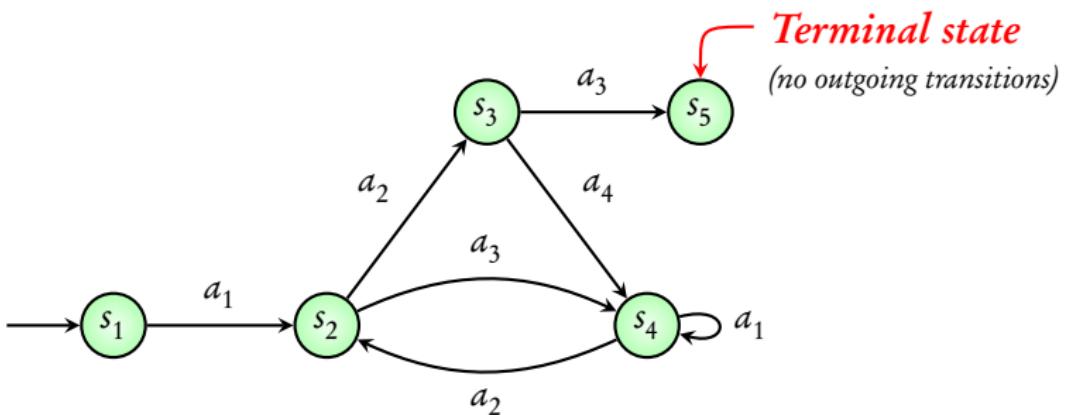


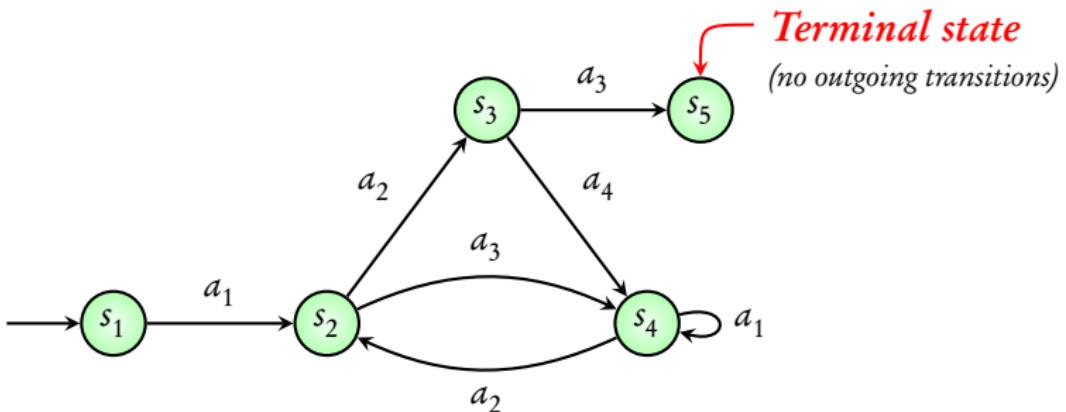
"Vending machines at hospital" by PCHS-NJROTC - Own work

Licensed under CC BY - SA 3.0 via Wikimedia Commons



Coming next: some **terminology**

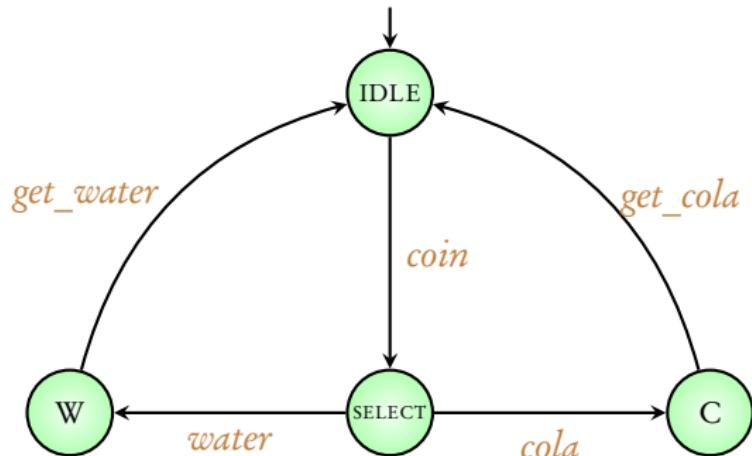




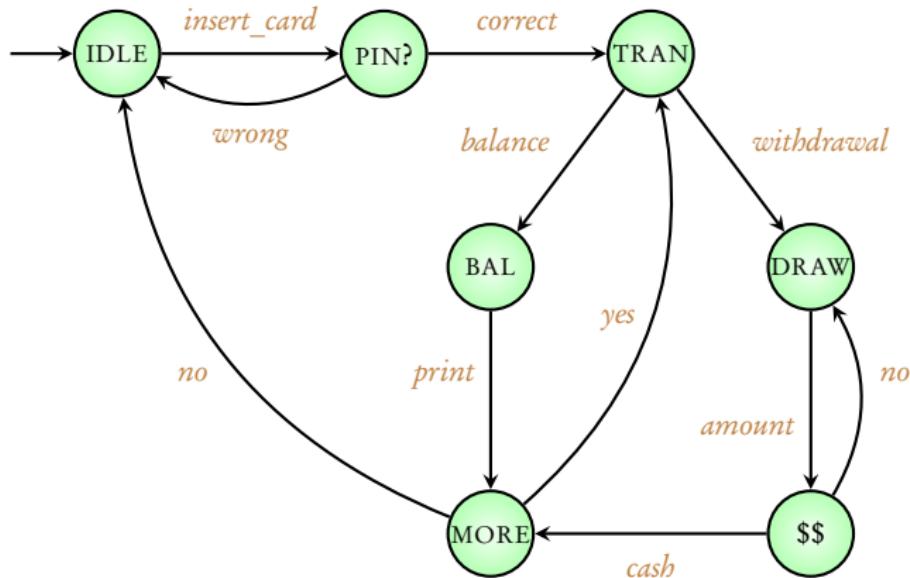
**Execution:**  $s_1 \xrightarrow{a_1} s_2 \xrightarrow{a_3} s_4 \xrightarrow{a_2} s_2 \xrightarrow{a_3} s_4 \xrightarrow{a_2} s_2 \xrightarrow{a_3} s_4 \dots$

$s_1 \xrightarrow{a_1} s_2 \xrightarrow{a_2} s_3 \xrightarrow{a_4} s_4 \xrightarrow{a_1} s_4 \xrightarrow{a_1} s_4 \xrightarrow{a_1} s_4 \dots$

$s_1 \xrightarrow{a_1} s_2 \xrightarrow{a_2} s_3 \xrightarrow{a_4} s_4 \xrightarrow{a_2} s_2 \xrightarrow{a_2} s_3 \xrightarrow{a_3} s_5$



**Execution:** IDLE  $\xrightarrow{\text{coin}}$  SELECT  $\xrightarrow{\text{water}}$  W  $\xrightarrow{\text{get\_water}}$  IDLE  $\xrightarrow{\text{coin}}$  SELECT  $\xrightarrow{\text{cola}}$  ...



**Execution:** IDLE  $\xrightarrow{\text{insert\_card}}$  PIN  $\xrightarrow{\text{wrong}}$  IDLE  $\xrightarrow{\text{insert\_card}}$  PIN ...

# Summary

## Transition Systems

States, actions, transitions

Executions

Reference: Principles of Model Checking, *Baier and Katoen*, MIT Press (2008)

Pages 19 - 26

# Week-1: Introduction to model checking

B. Srivathsan

Chennai Mathematical Institute

*NPTEL-course*

July - November 2015

# Module 2: **Modeling hardware circuits**



$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	1



$x_1$	$x_2$	$y$
0	0	0
0	1	0
1	0	0
1	1	1



$x$	$y$
0	1
1	0



$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



$$y = \text{NOT}(\text{XOR}(x_1, x_2))$$

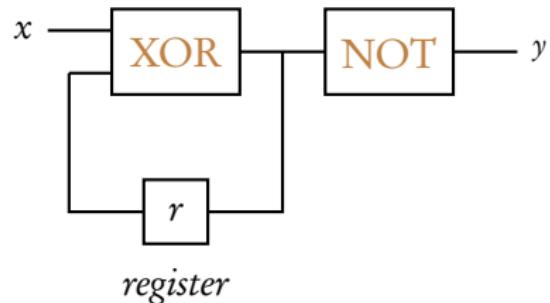


$$y = \text{NOT}(\text{XOR}(x_1, x_2))$$



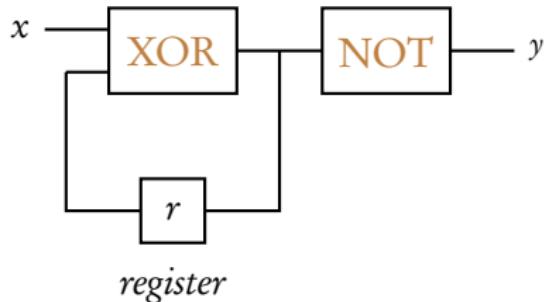
$x_1$	$x_2$	$y$
0	0	1
0	1	0
1	0	0
1	1	1

$$y = \text{NOT}(\text{XOR}(x, r))$$



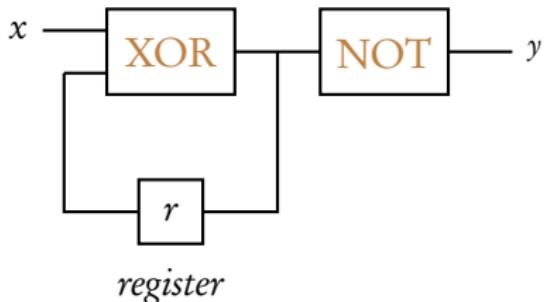
$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$



$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$



$$x \quad 1$$

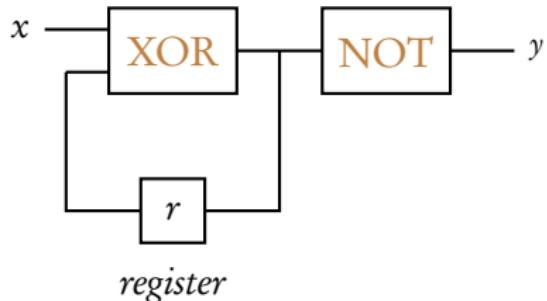
$$r \quad 0$$

$$y \quad 0$$



$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

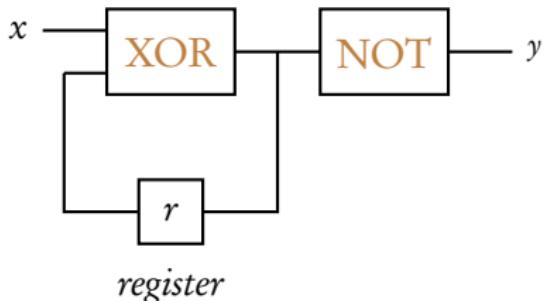


$x$	1
$r$	0      1
$y$	0



$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

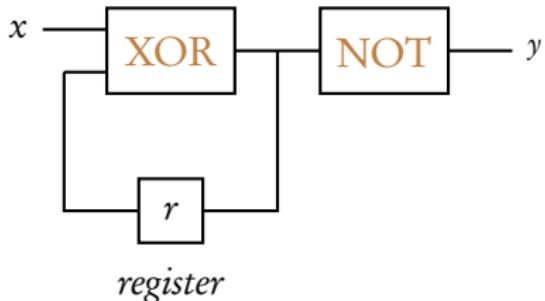


$x$	1	1
$r$	0	1
$y$	0	1



$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

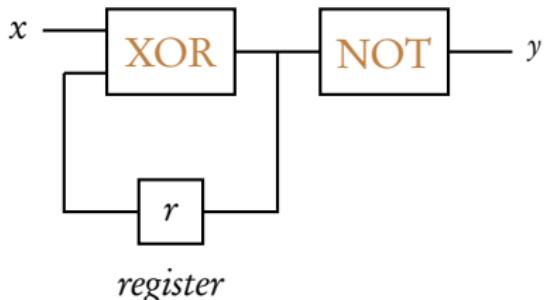


$x$	1	1
$r$	0	1
$y$	0	1



$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

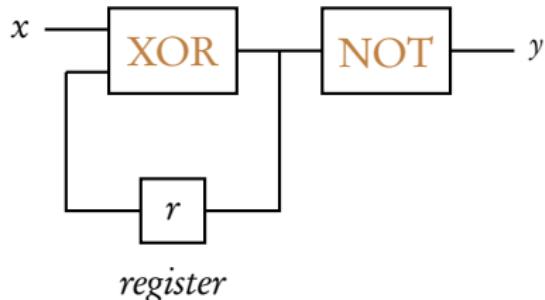


$x$	1	1	0
$r$	0	1	0
$y$	0	1	1



$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

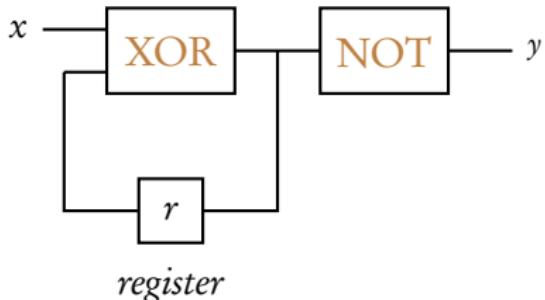


$x$	1	1	0
$r$	0	1	0
$y$	0	1	1



$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

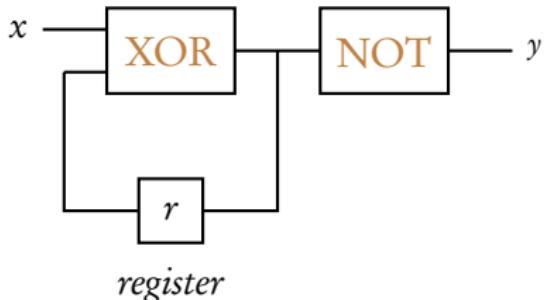


$x$	1	1	0	1
$r$	0	1	0	0
$y$	0	1	1	0



$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

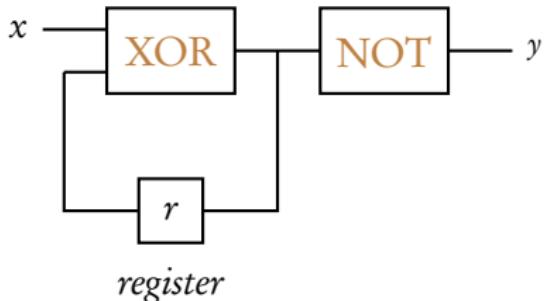


$x$	1	1	0	1
$r$	0	1	0	0
$y$	0	1	1	0



$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

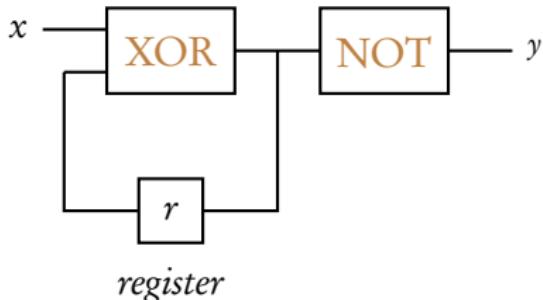


$x$	1	1	0	1	1
$r$	0	1	0	0	1
$y$	0	1	1	0	1



$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

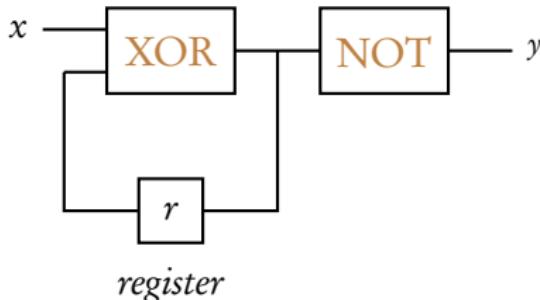


$x$	1	1	0	1	1	1	0	0	1	0	...
$r$	0	1	0	0	1	0	1	1	1	0	...
$y$	0	1	1	0	1	0	0	0	1	1	...

A horizontal bracket below the columns indicates the sequence of operations. Red checkmarks are placed under the first seven columns of the  $y$  row, indicating correct computation for those steps.

$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$



$$x = 0, r = 0, y = 1$$

$$x = 1, r = 0, y = 0$$

$$x = 0, r = 1, y = 0$$

$$x = 1, r = 1, y = 1$$

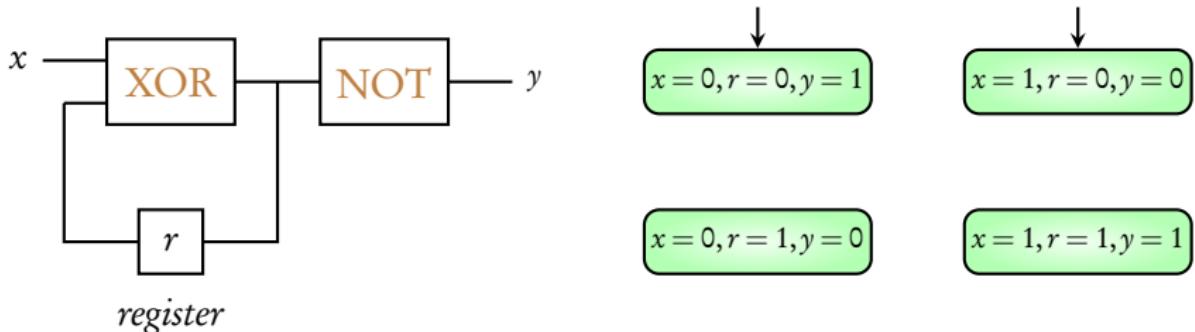
$$\begin{array}{ccccccccccccc} x & 1 & 1 & 0 & 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ r & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & \dots \end{array}$$

$$\begin{array}{ccccccccccccc} y & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 1 \\ \hline \end{array}$$



$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

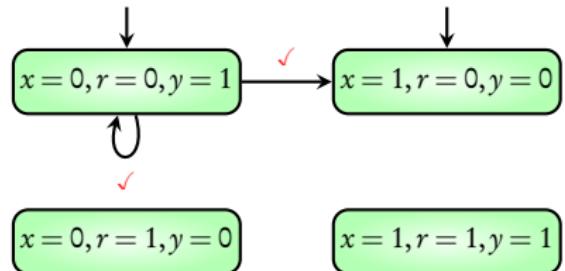
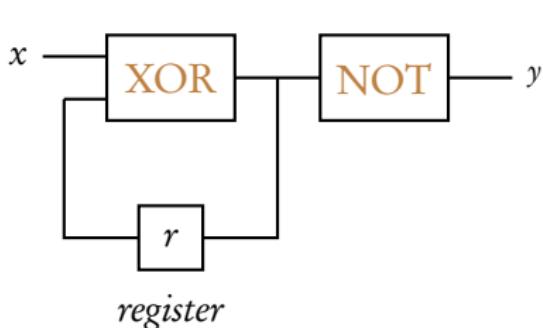


$x$	1	1	0	1	1	1	0	0	1	0	...
$r$	0	1	0	0	1	0	1	1	1	0	...
$y$	0	1	1	0	1	0	0	0	1	1	...

A bracket below the first ten columns of the table has red checkmarks under each of the first ten entries in the  $y$  column.

$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

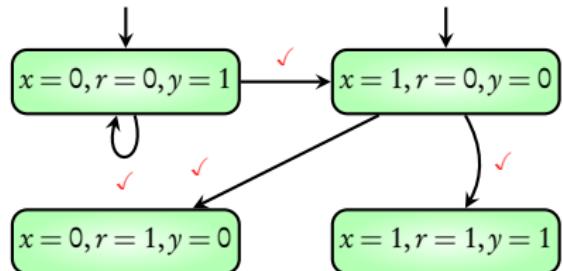
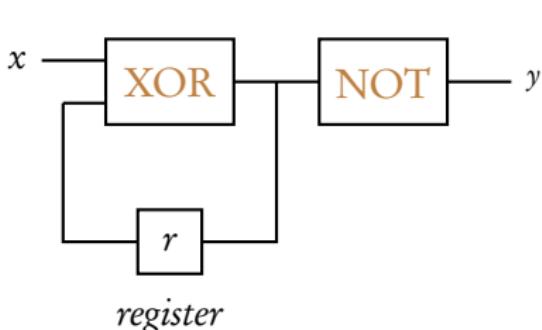


$x$	1	1	0	1	1	1	0	0	1	0	...
$r$	0	1	0	0	1	0	1	1	1	0	...
$y$	0	1	1	0	1	0	0	0	1	1	...

Below the table, a horizontal bracket spans all columns, and below it, nine red checkmarks are placed under the values 1, 1, 0, 1, 1, 0, 1, 0, and 1 respectively.

$$y = \text{NOT}(\text{XOR}(x, r))$$

$$r_{next} = \text{XOR}(x, r)$$

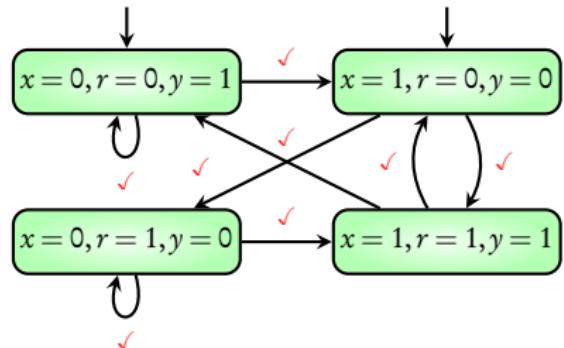
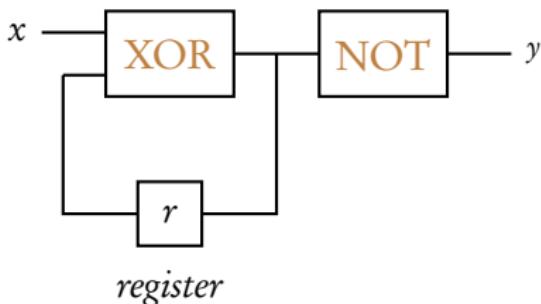


$x$	1	1	0	1	1	1	0	0	1	0	$\dots$
$r$	0	1	0	0	1	0	1	1	1	0	
$y$	0	1	1	0	1	0	0	0	1	1	

↙ ↘ ↗ ↙ ↘ ↗ ↙ ↘ ↗ ↙ ↘ ↗

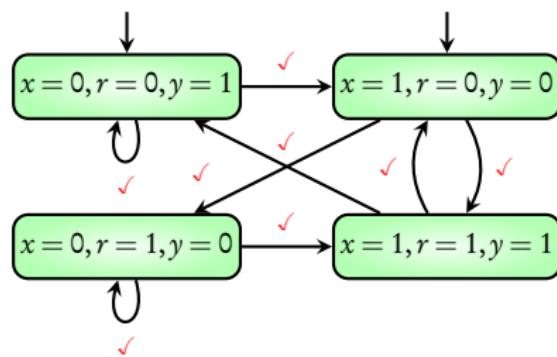
$$y = \text{NOT}(\text{XOR}(x, r))$$

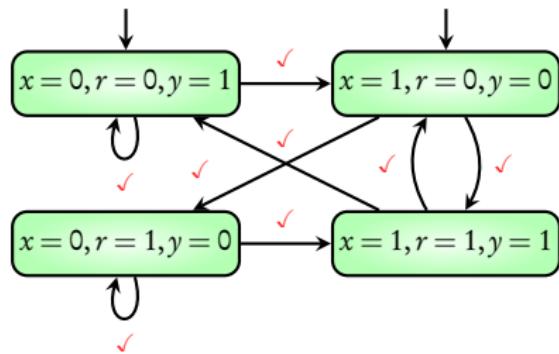
$$r_{next} = \text{XOR}(x, r)$$



$x$	1	1	0	1	1	1	0	0	1	0	$\dots$
$r$	0	1	0	0	1	0	1	1	1	0	
$y$	0	1	1	0	1	0	0	0	1	1	

Below the table, a horizontal bracket spans all columns from the second to the eleventh, with red checkmarks placed under each tick mark below it.

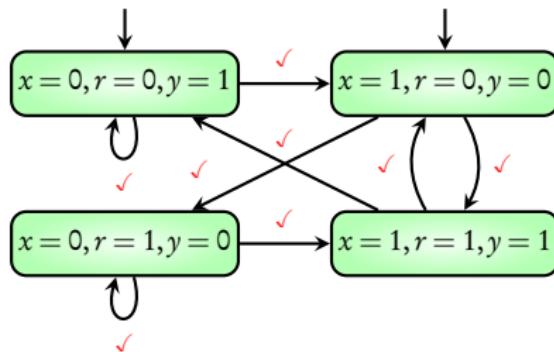




More than one initial state

States with **more than one transition** on an action

## *Non-deterministic transition system*



More than one initial state

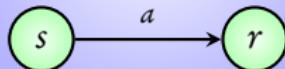
States with **more than one transition** on an action

# Transition Systems

## Deterministic

Single initial state

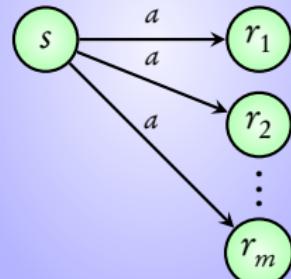
and



## Non-deterministic

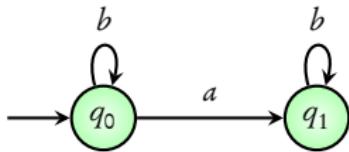
Multiple initial states

or

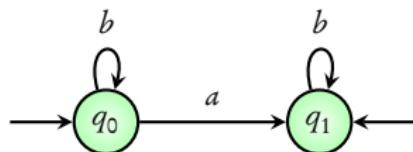
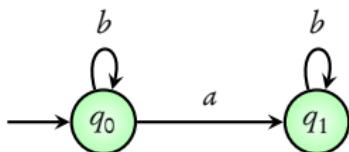
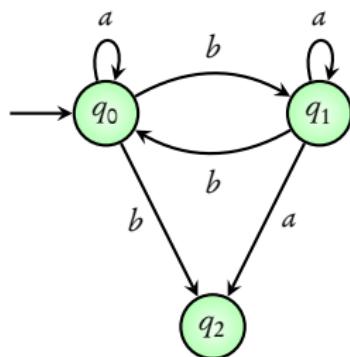
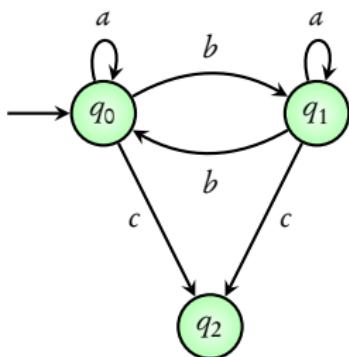
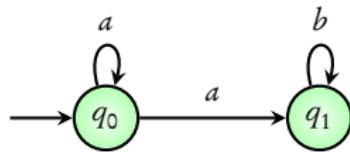


**Coming next: examples** of deterministic and non-deterministic transition systems

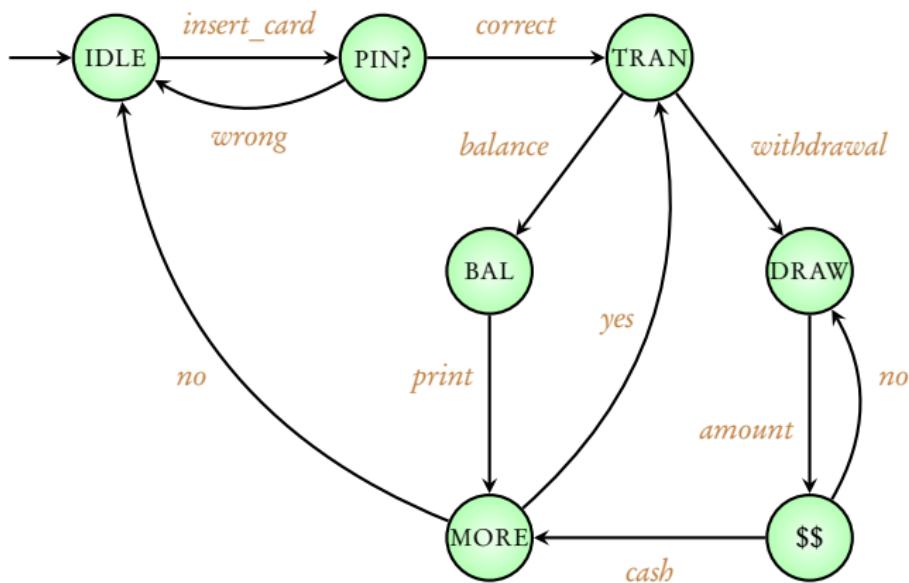
Deterministic



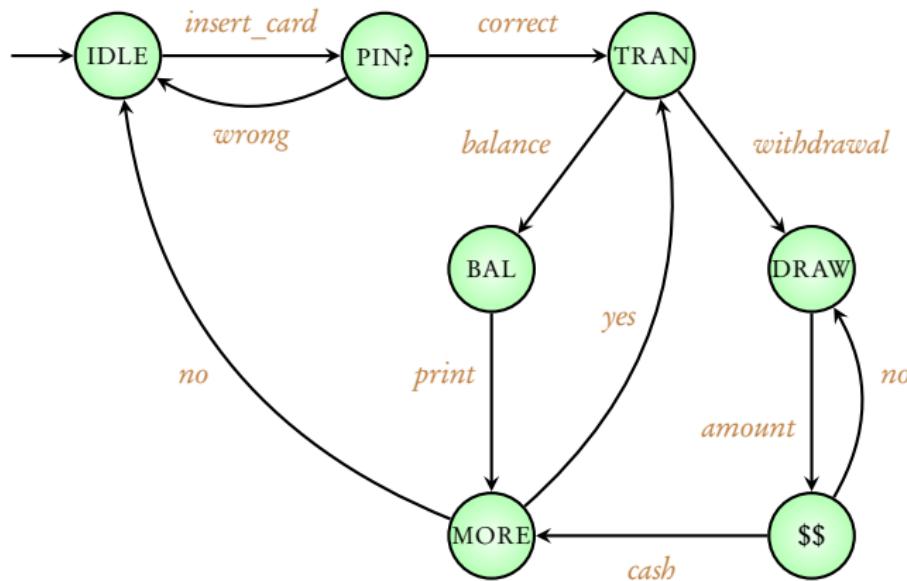
Non-deterministic



# Model of ATM

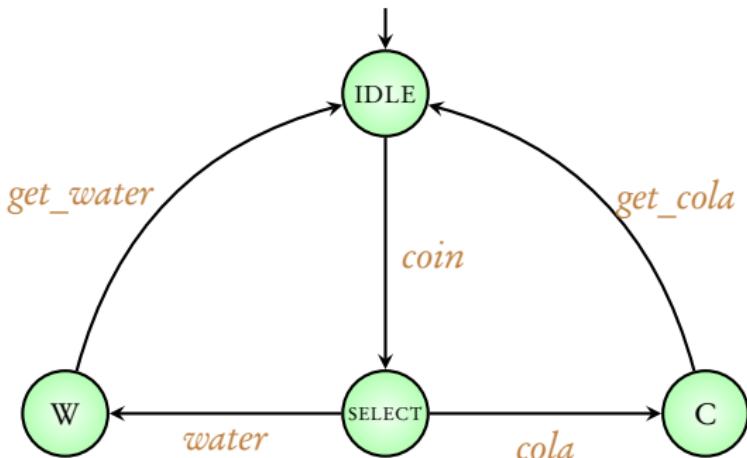


# Model of ATM

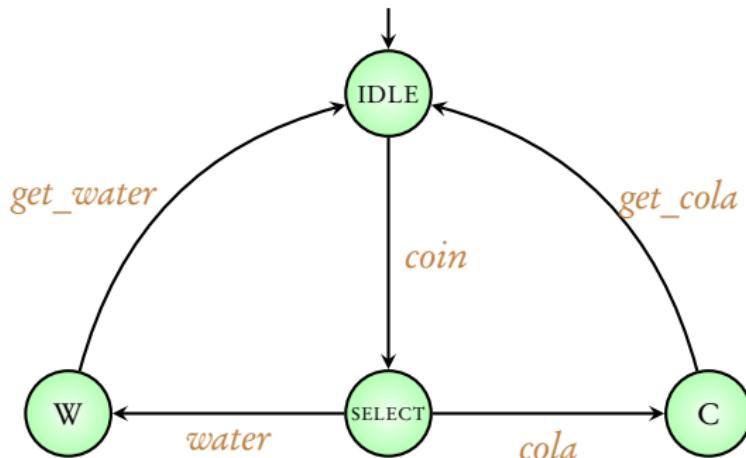


Deterministic transition system

# Model of vending machine

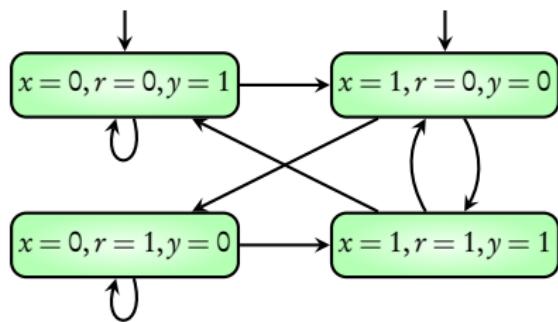


# Model of vending machine

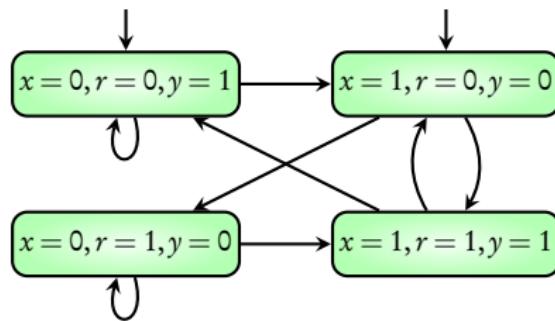


Deterministic transition system

# Model of hardware circuit

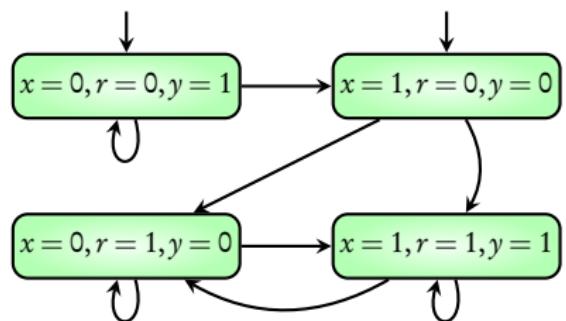
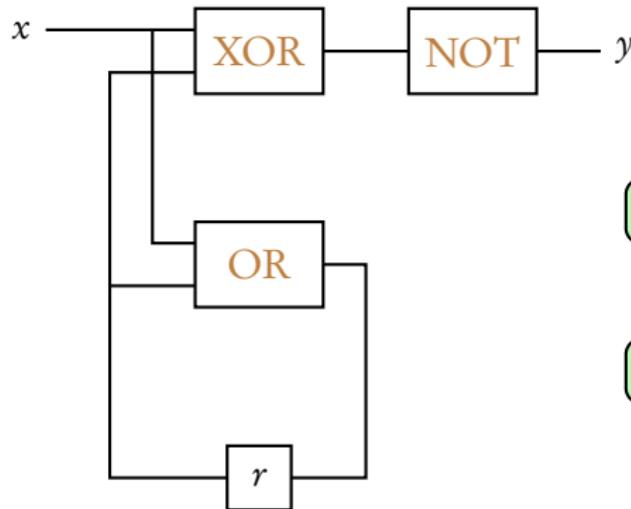


# Model of hardware circuit



Non-deterministic transition system: to model **incomplete information**

**Coming next:** Another example of hardware circuit



# Summary

## Hardware Circuits

Modeling using transition systems

Non-determinism

Reference: Principles of Model Checking, *Baier and Katoen*, MIT Press (2008)

Pages 26 - 29

# Week-1: Introduction to model checking

B. Srivathsan

Chennai Mathematical Institute

*NPTEL-course*

July - November 2015

# Module 3: Modeling data-dependent programs

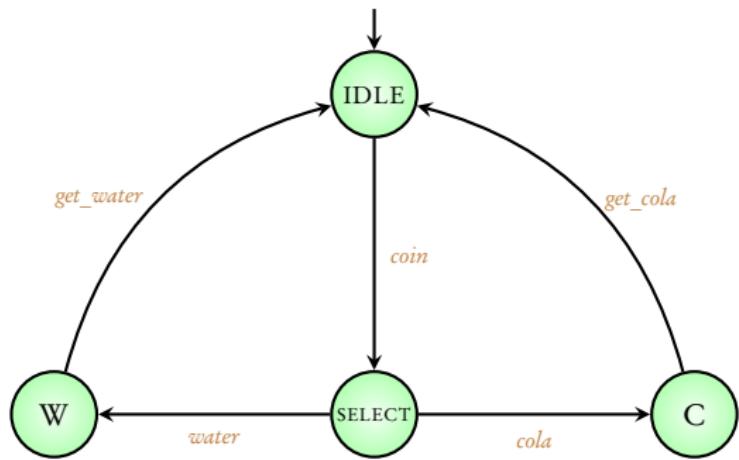
## Data-dependent programs:

Variables + Conditional branching + Assignments

## Data-dependent programs:

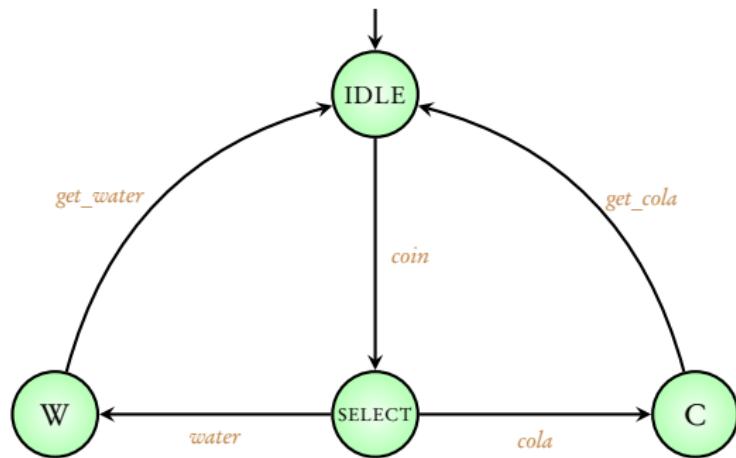
Variables + Conditional branching + Assignments

**Coming next:** vending machine revisited



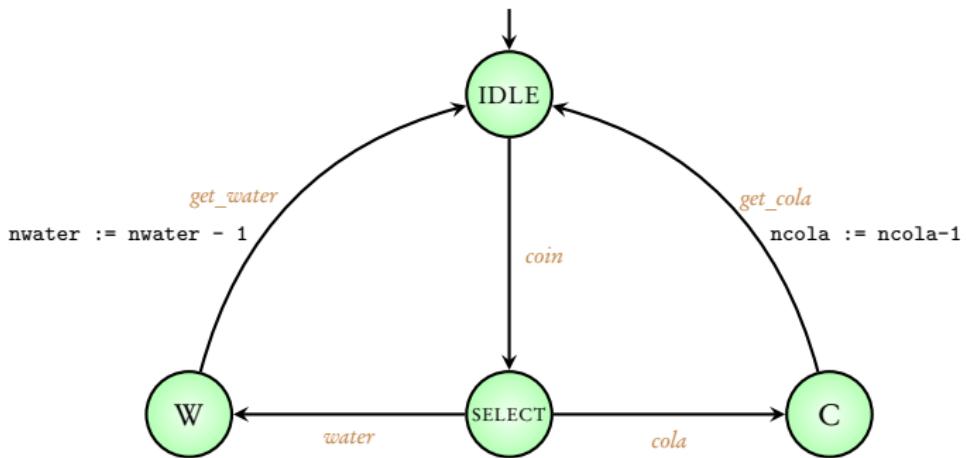
Variables:

nwater, ncola, max



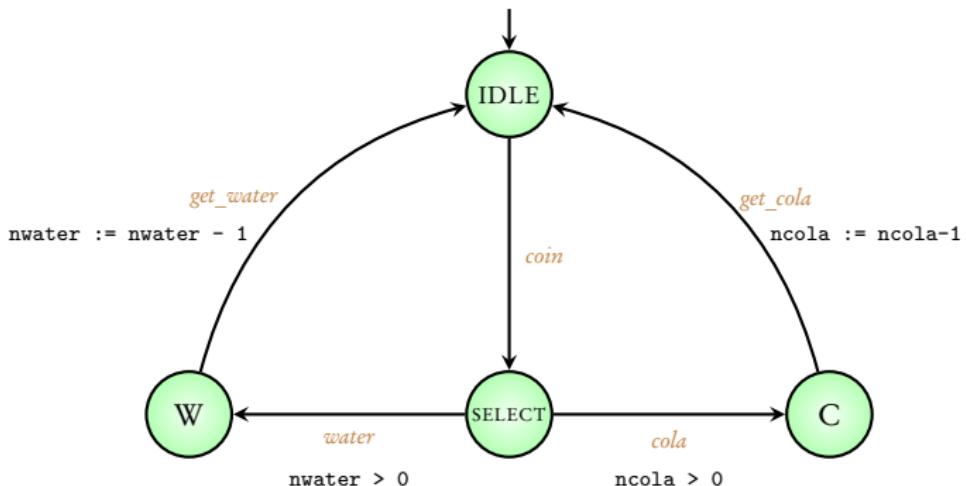
Variables:

nwater, ncola, max



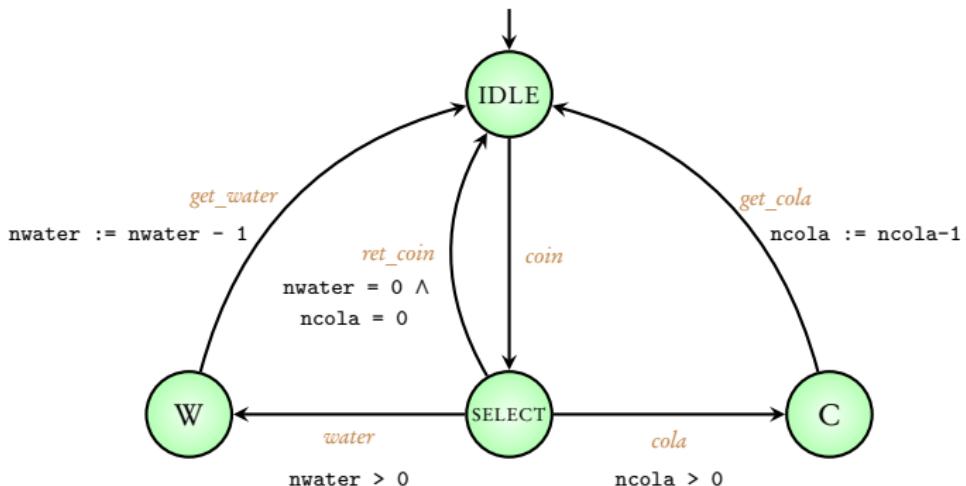
Variables:

nwater, ncola, max



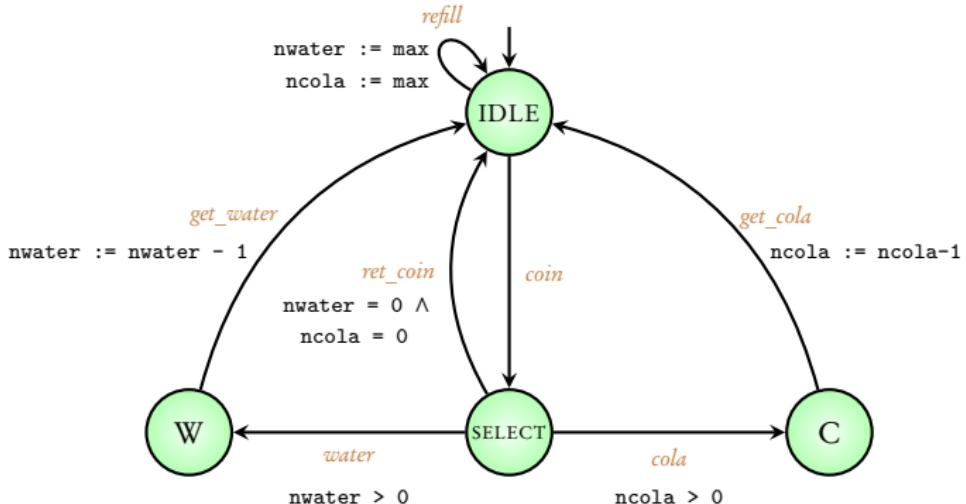
Variables:

nwater, ncola, max



Variables:

nwater, ncola, max

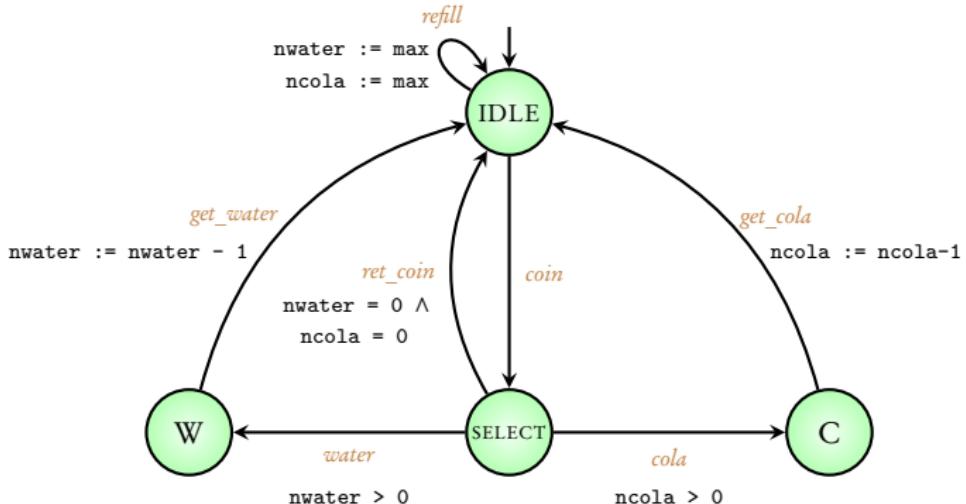


Initial condition:

```
nwater = max, ncola = max
```

Variables:

```
nwater, ncola, max
```

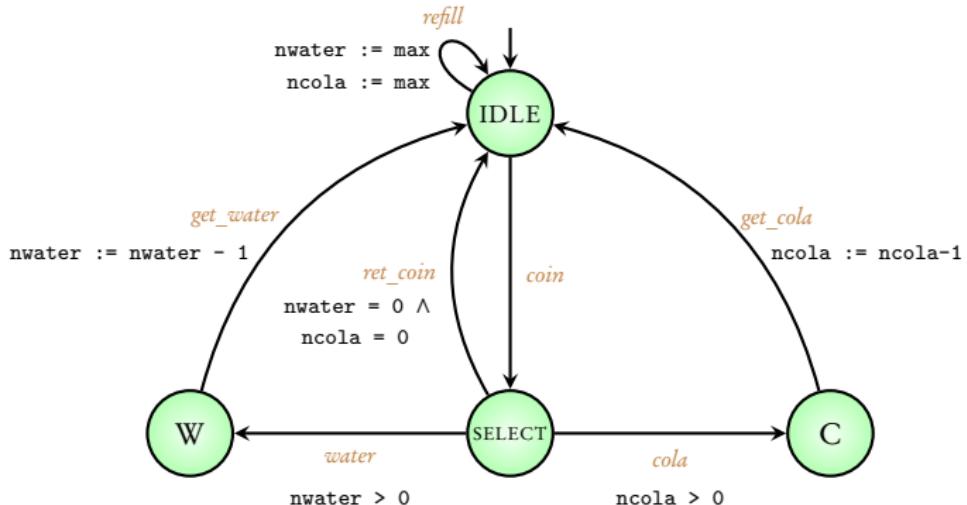


Initial condition:

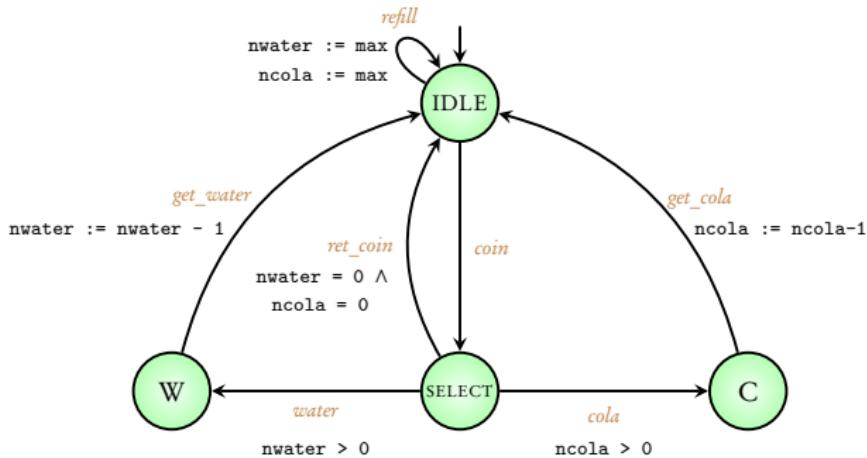
```
nwater = max, ncola = max
```

Variables:

```
nwater, ncola, max
```

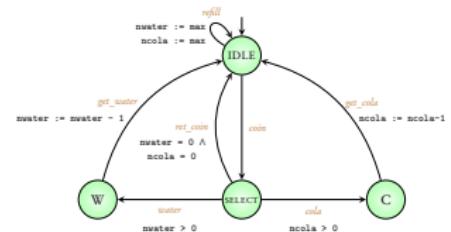


Program graph

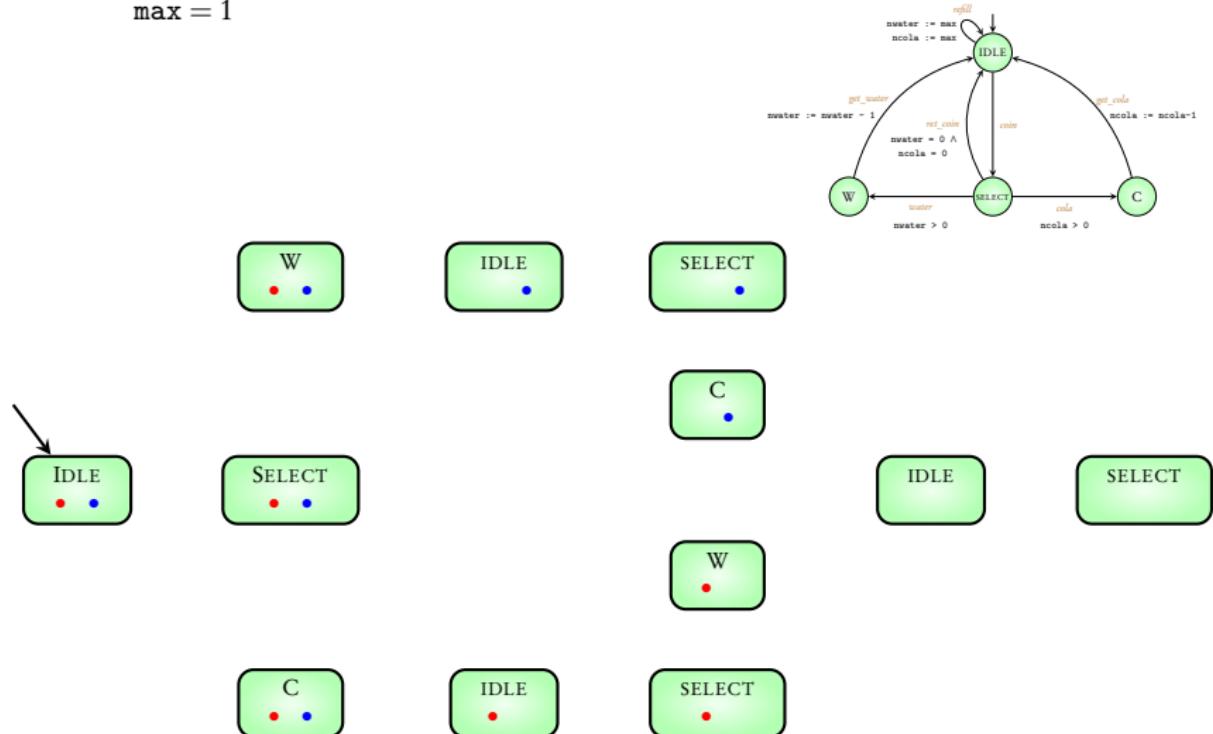


**Coming next:** Transition system corresponding to  $\text{max} = 1$

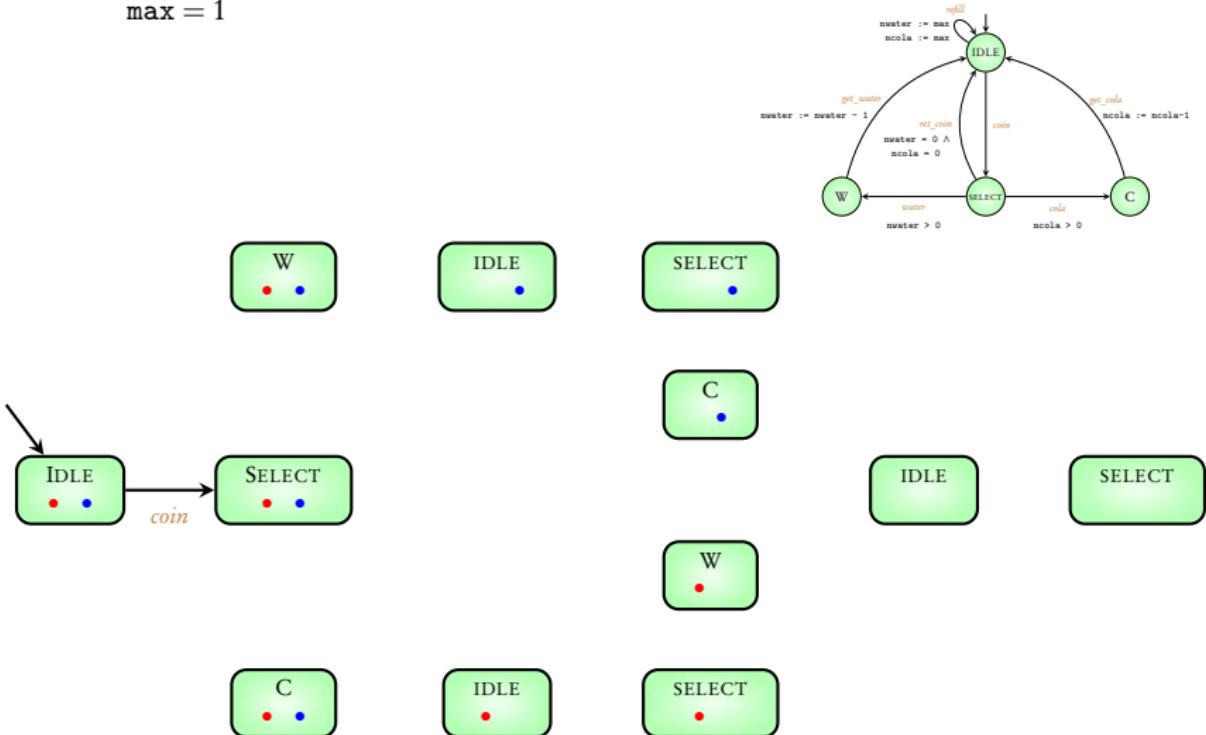
$\max = 1$



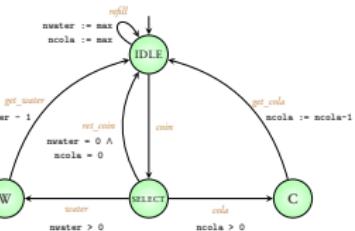
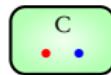
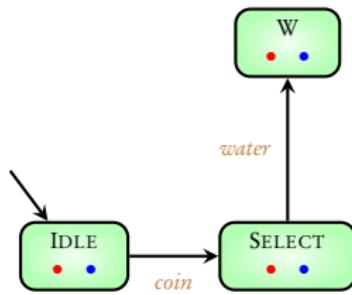
$\max = 1$



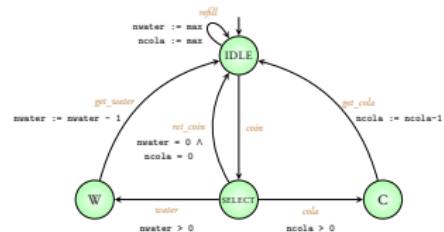
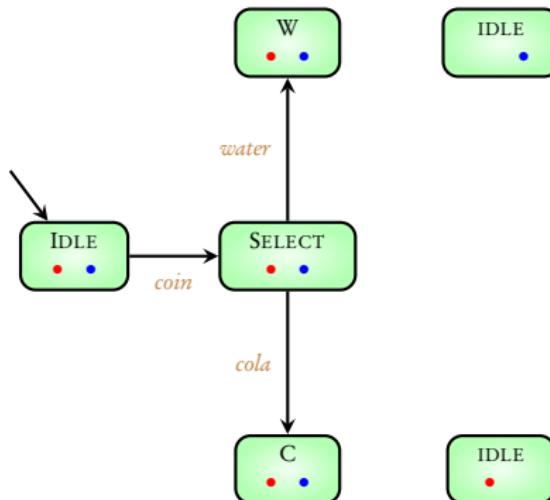
$\max = 1$



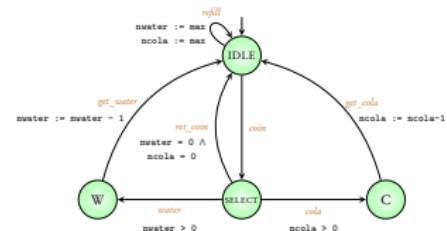
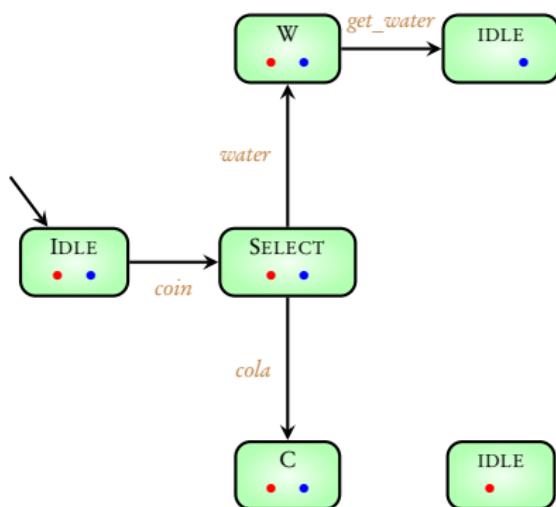
$\max = 1$



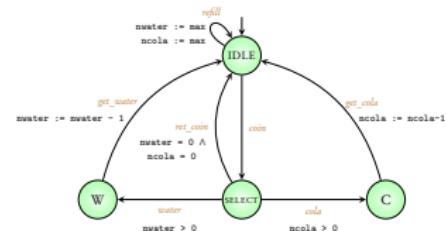
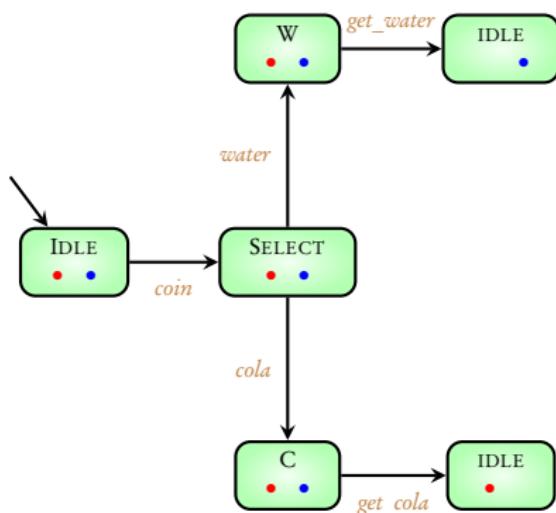
$\max = 1$



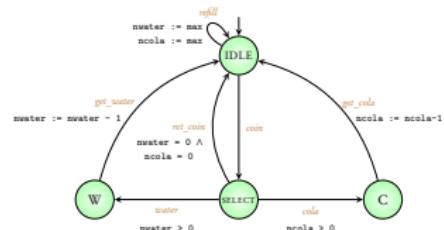
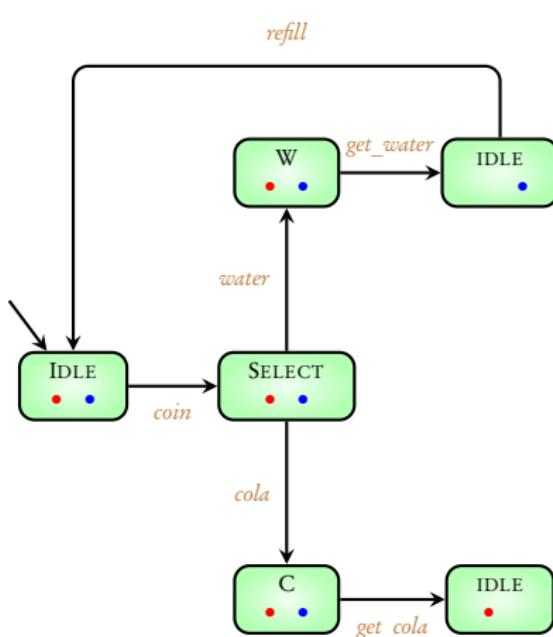
$\max = 1$



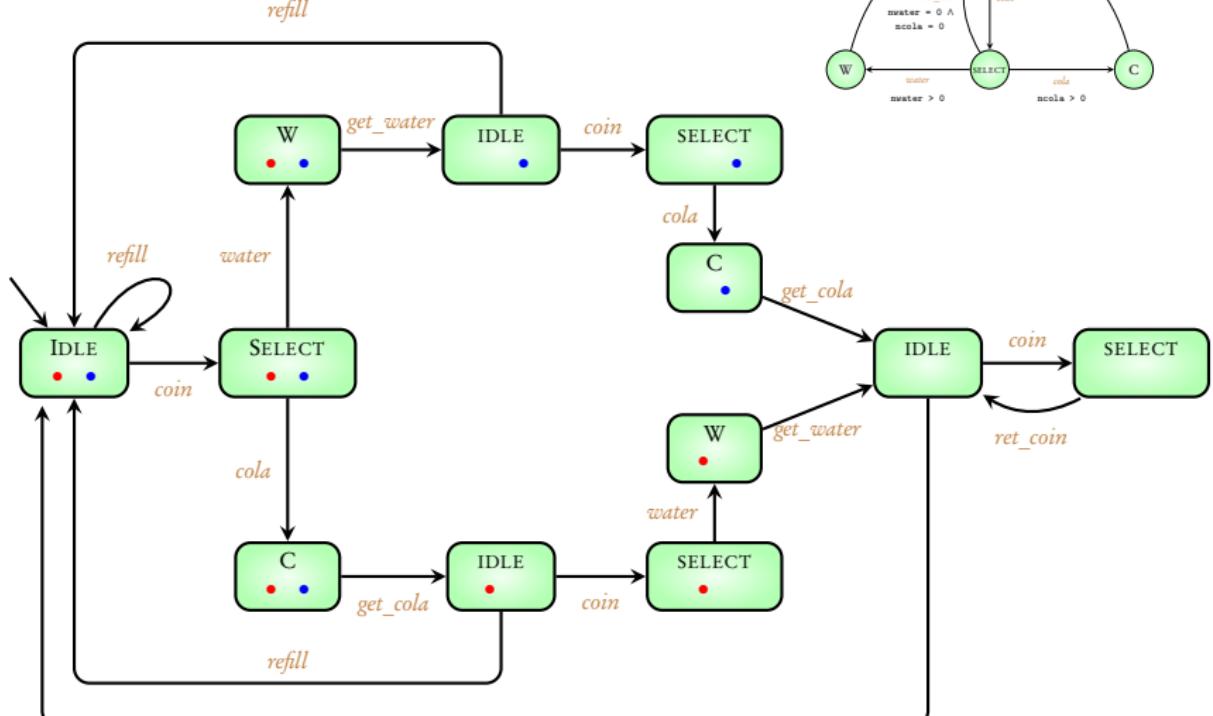
$\max = 1$



$\max = 1$



$\max = 1$



refill

• • •

**while** ( x > 0 )

**if** ( x mod 2 = 0)

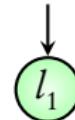
x := x - 2

**else** x := x - 1

• • •

• • •

$l_1:$  **while** ( $x > 0$ )



$l_3$

**if** ( $x \bmod 2 = 0$ )

$l_2:$        $x := x - 2$

**else**     $x := x - 1$

• • •

$l_3:$



• • •

$l_1:$  **while** ( $x > 0$ )

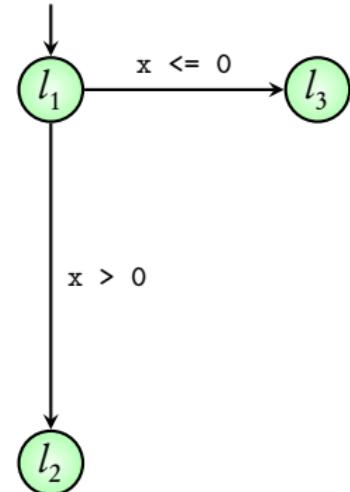
**if** ( $x \bmod 2 = 0$ )

$l_2:$         $x := x - 2$

**else**    $x := x - 1$

    • • •

$l_3:$



• • •

$l_1:$  **while** ( $x > 0$ )

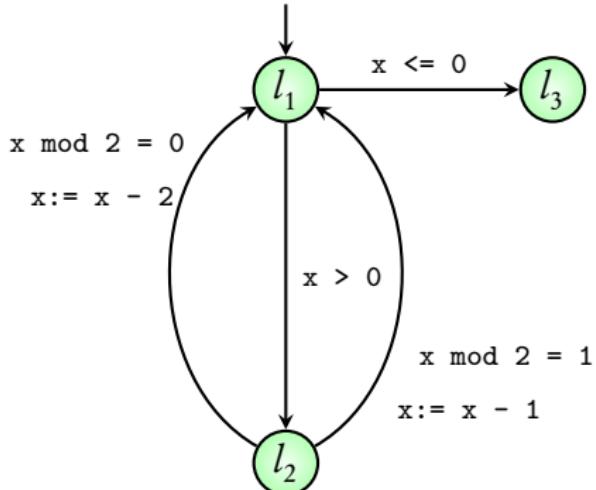
**if** ( $x \bmod 2 = 0$ )

$l_2:$             $x := x - 2$

**else**    $x := x - 1$

• • •

$l_3:$



• • •

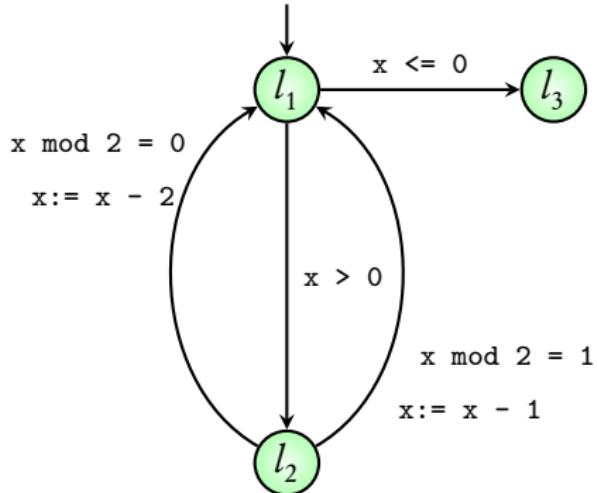
$l_1:$  **while** ( $x > 0$ )

**if** ( $x \bmod 2 = 0$ )

$l_2:$             $x := x - 2$

**else**    $x := x - 1$

$l_3:$



Program graph

$\dots$

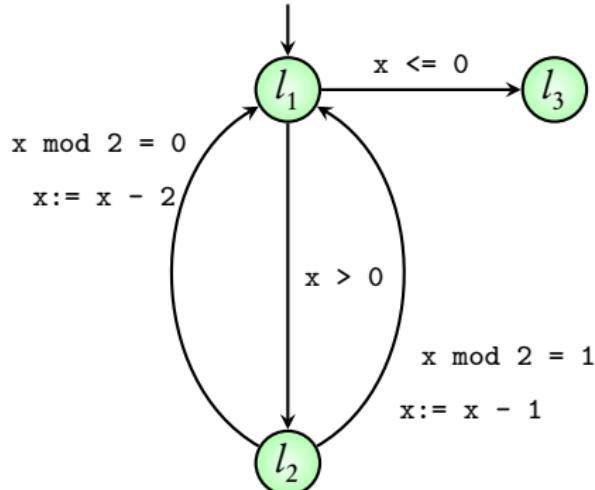
$l_1:$  **while** ( $x > 0$ )

**if** ( $x \bmod 2 = 0$ )

$l_2:$        $x := x - 2$

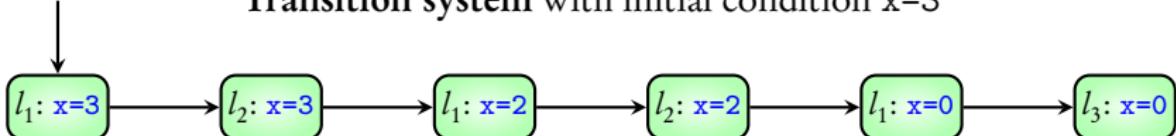
**else**  $x := x - 1$

$l_3:$   $\dots$



Program graph

Transition system with initial condition  $x=3$



# Summary

## Data-dependent programs

Program graphs

Transition systems of program graphs

Reference: Principles of Model Checking, *Baier and Katoen*, MIT Press (2008)

Pages 29 - 34

# Week-1: Introduction to model checking

B. Srivathsan

Chennai Mathematical Institute

*NPTEL-course*

July - November 2015

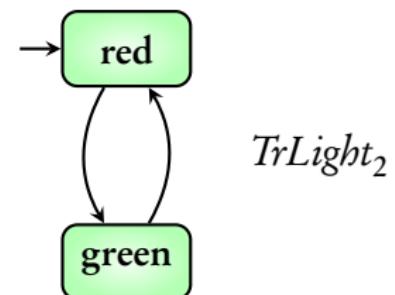
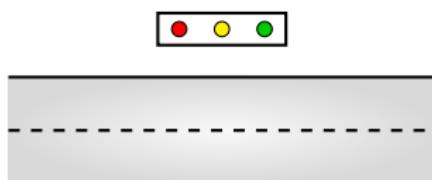
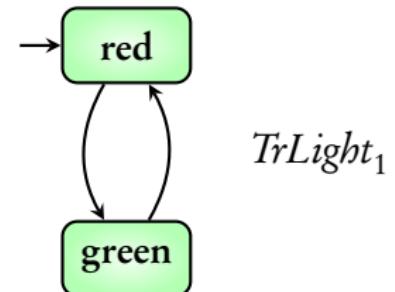
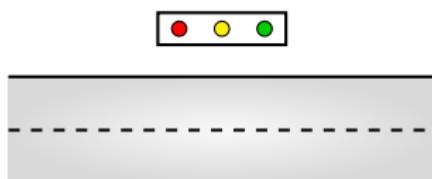
# Module 4: Modeling concurrent systems

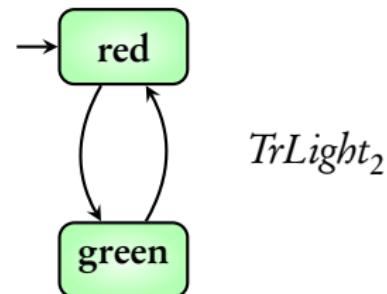
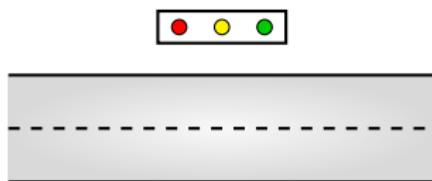
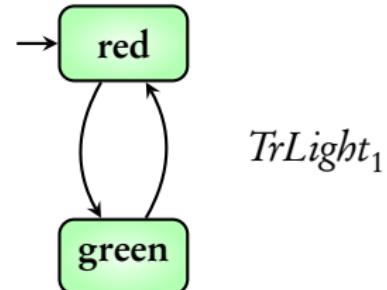
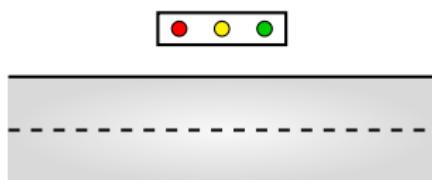
# Concurrent systems

Independent

Shared variables

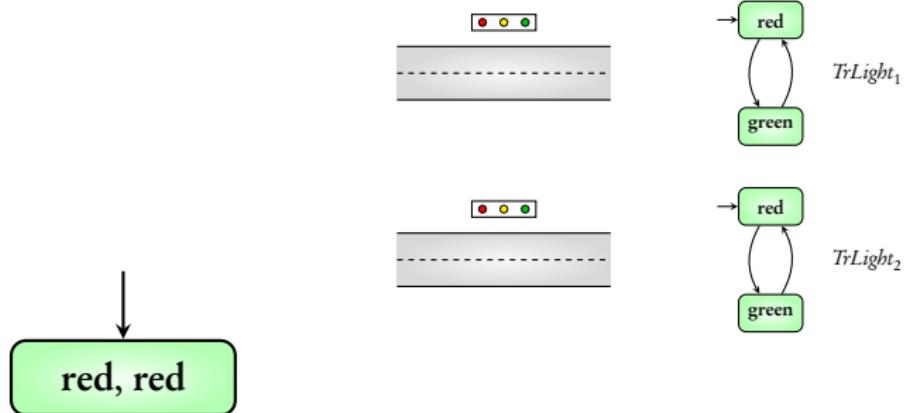
Shared actions

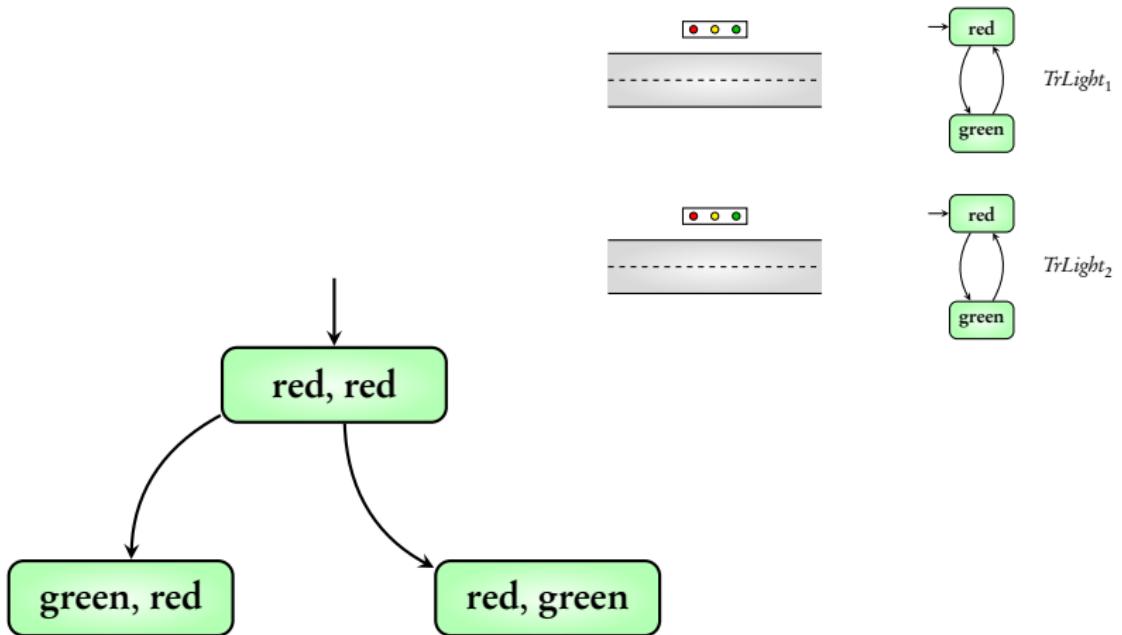


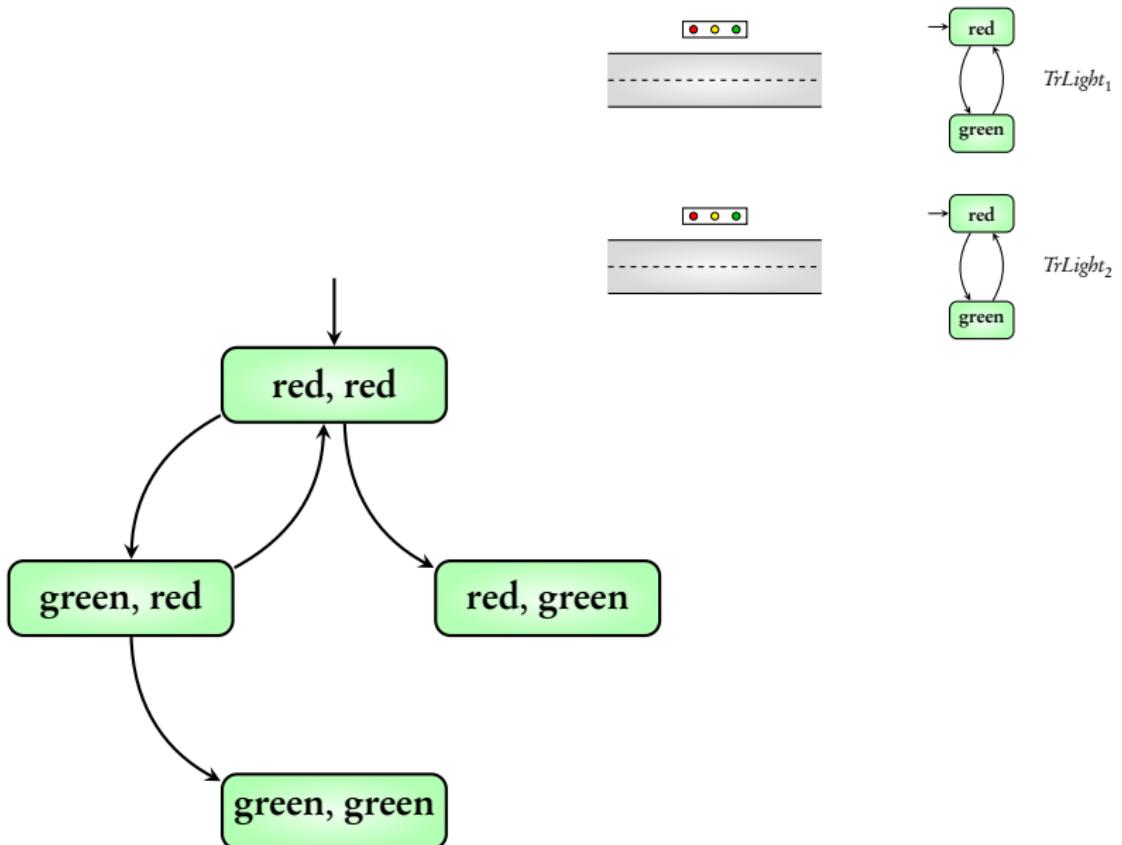


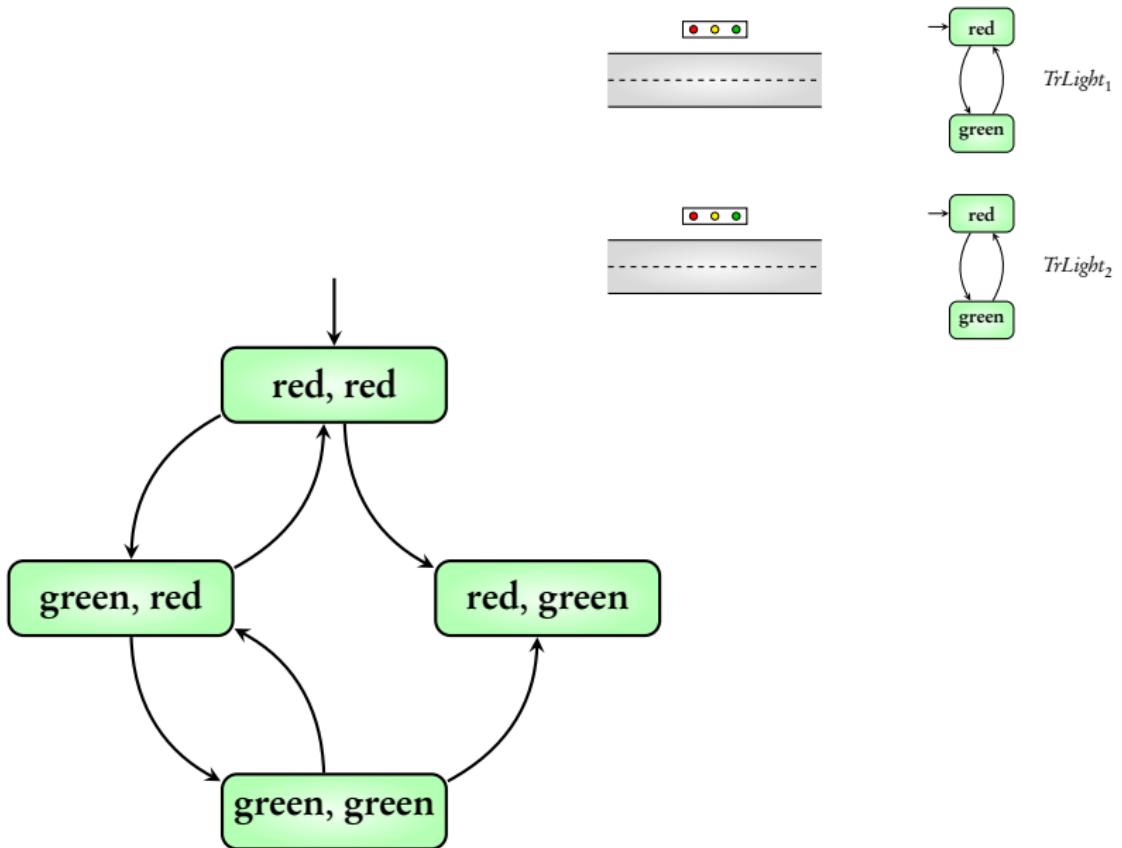
What is the transition system for the **joint behaviour**?

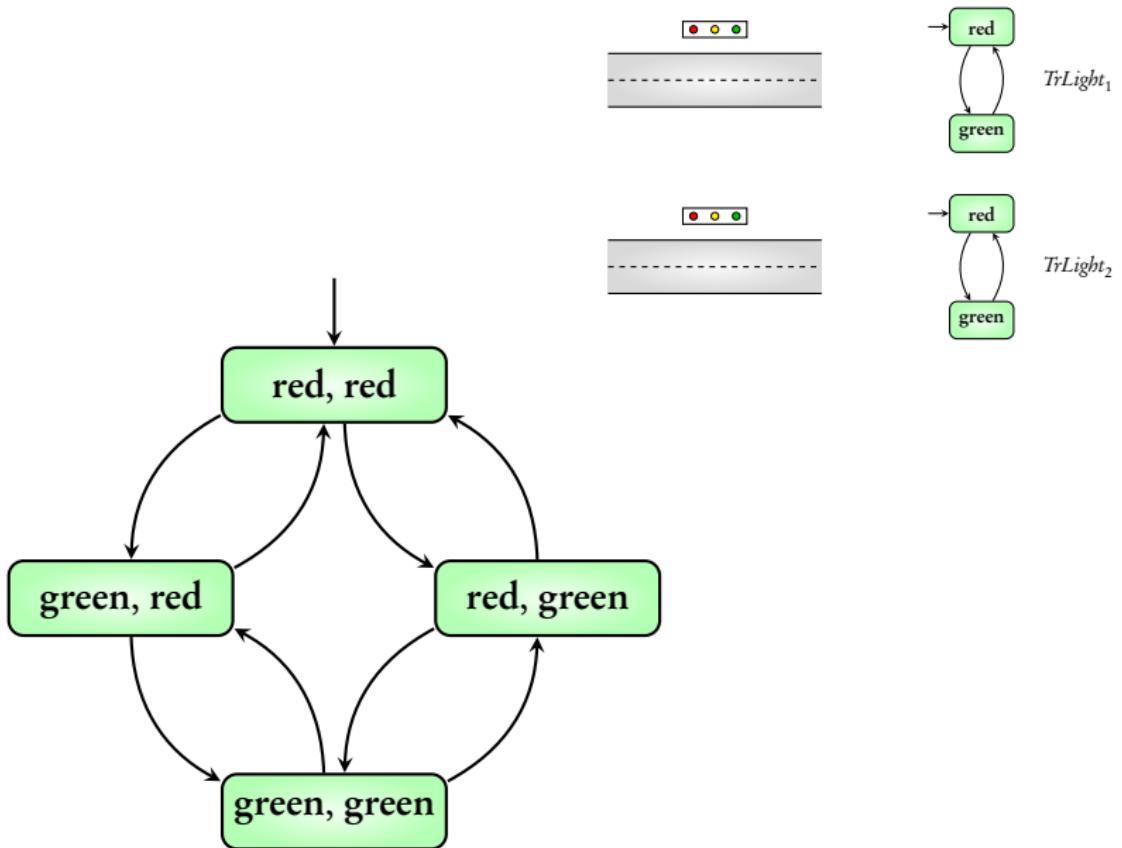


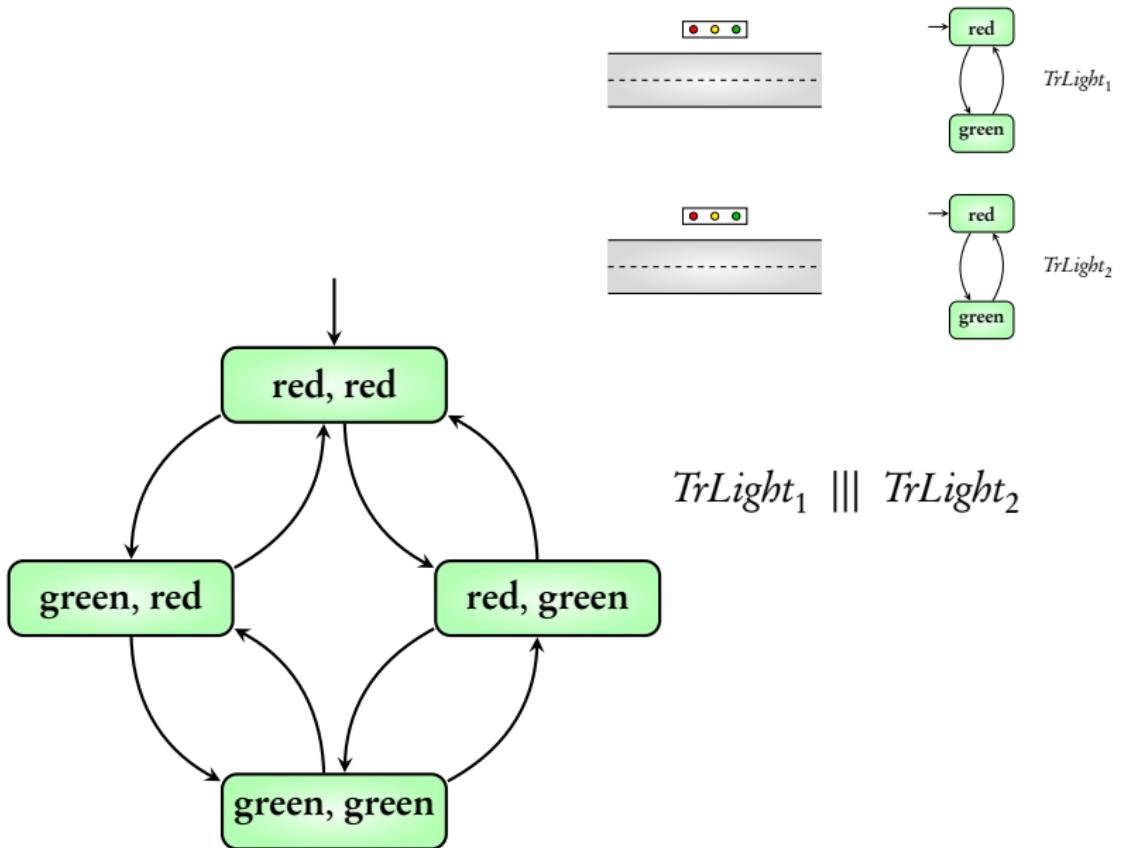


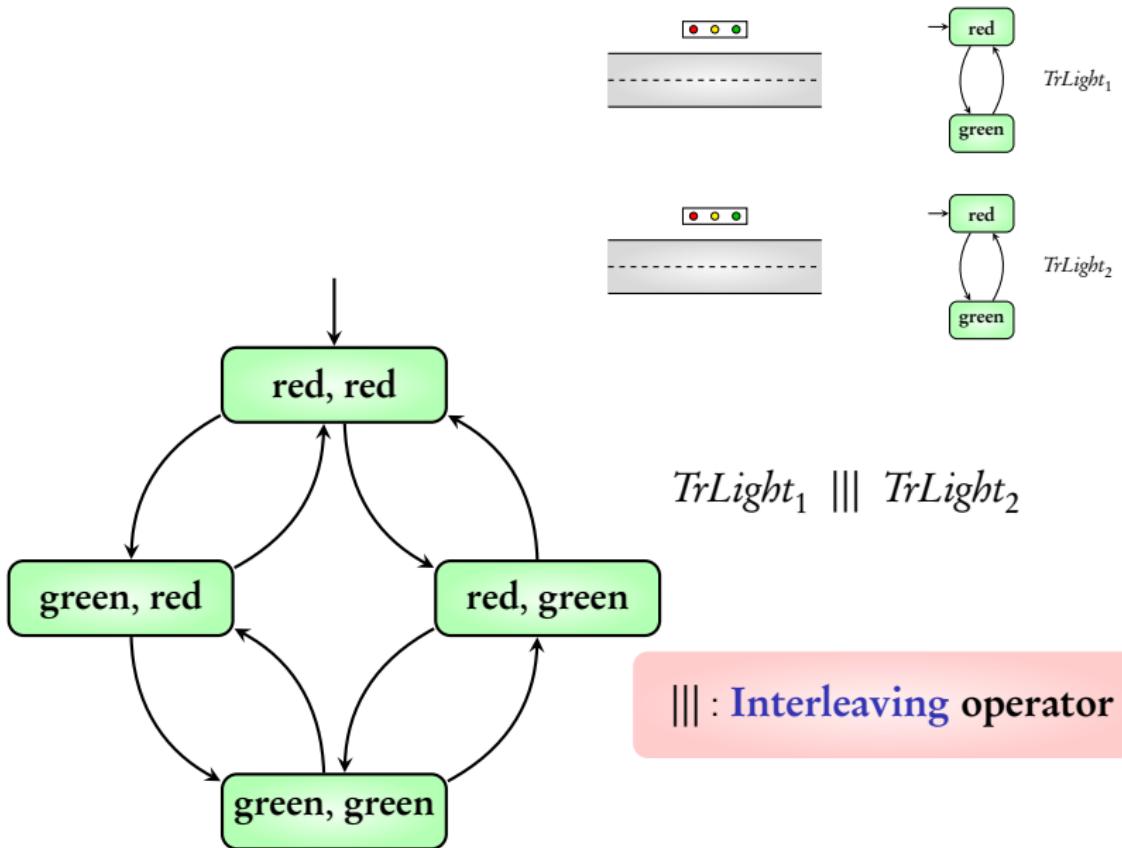


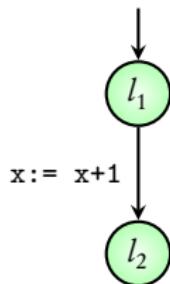




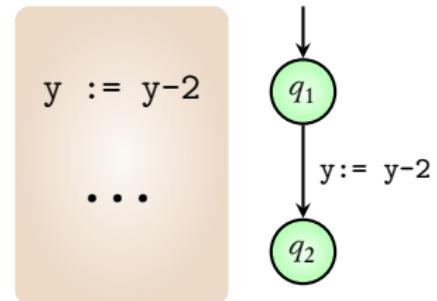
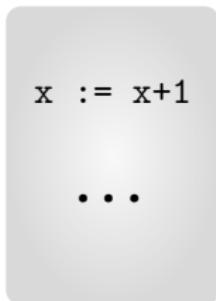




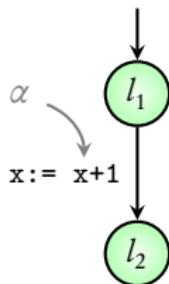




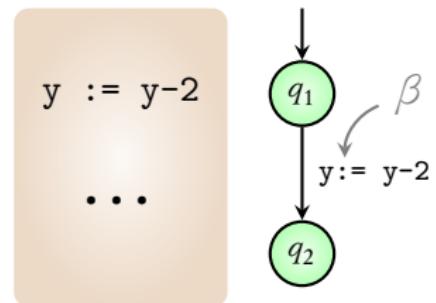
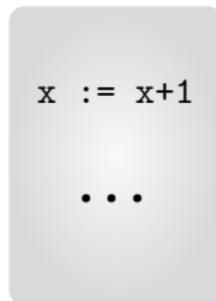
$PG_1$



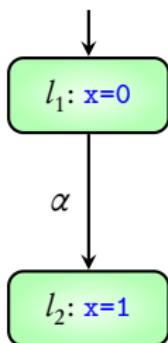
$PG_2$



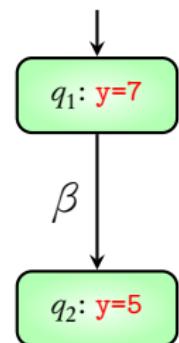
$PG_1$



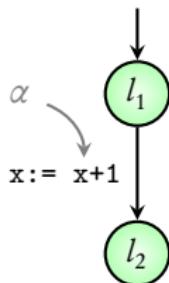
$PG_2$



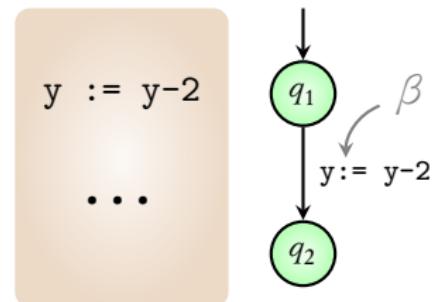
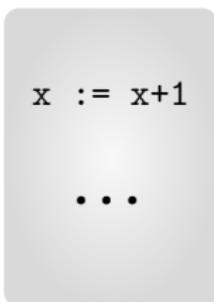
$TS_1$   
(initially  $x=0$ )



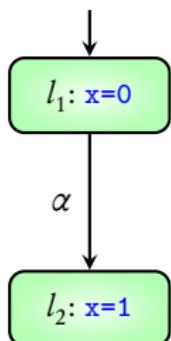
$TS_2$   
(initially  $y=7$ )



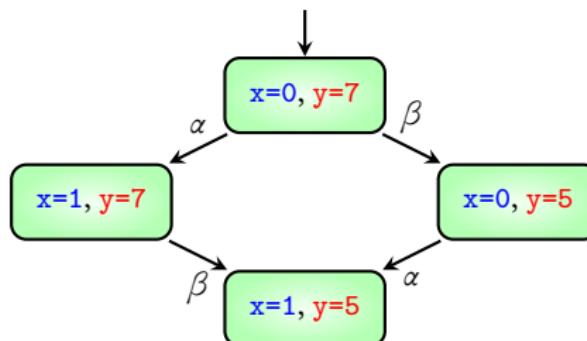
PG<sub>1</sub>



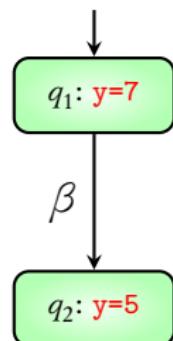
PG<sub>2</sub>



TS<sub>1</sub>  
(initially x=0)

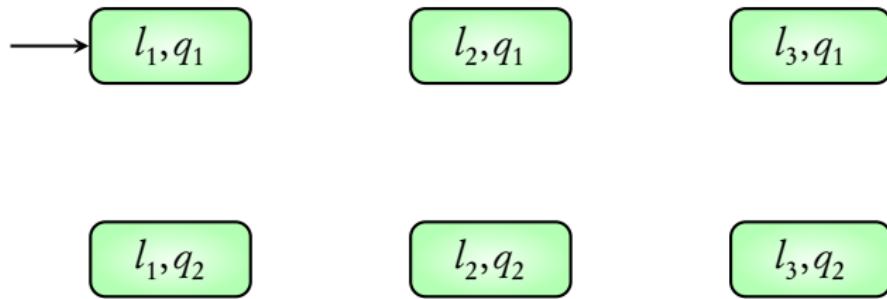


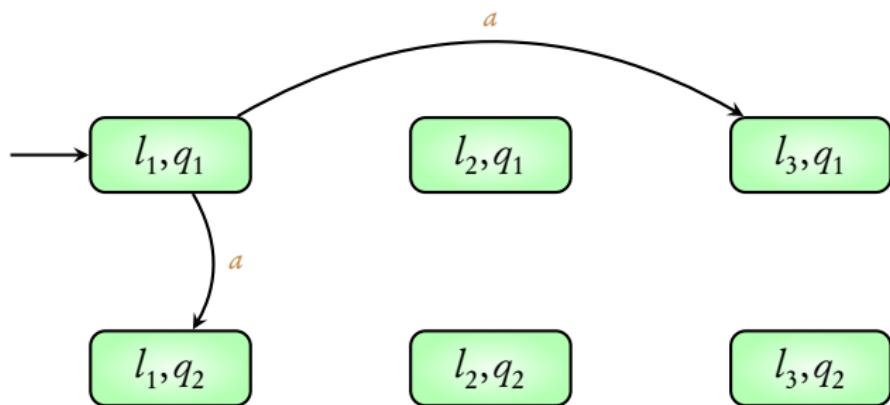
TS<sub>1</sub> ||| TS<sub>2</sub>

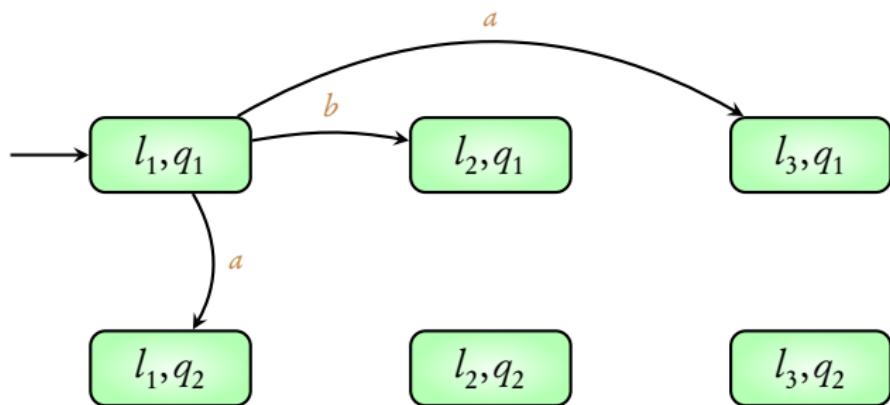


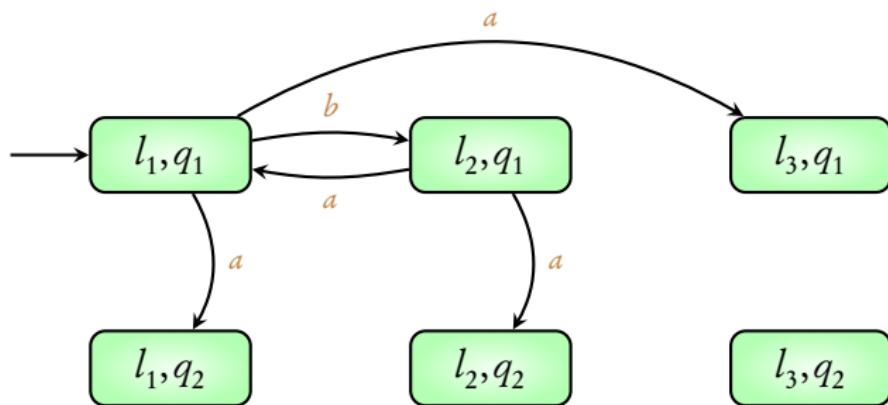
TS<sub>2</sub>  
(initially y=7)

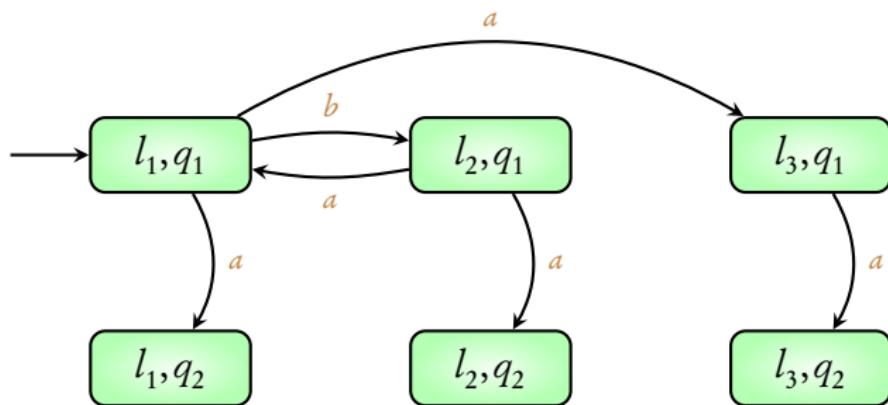


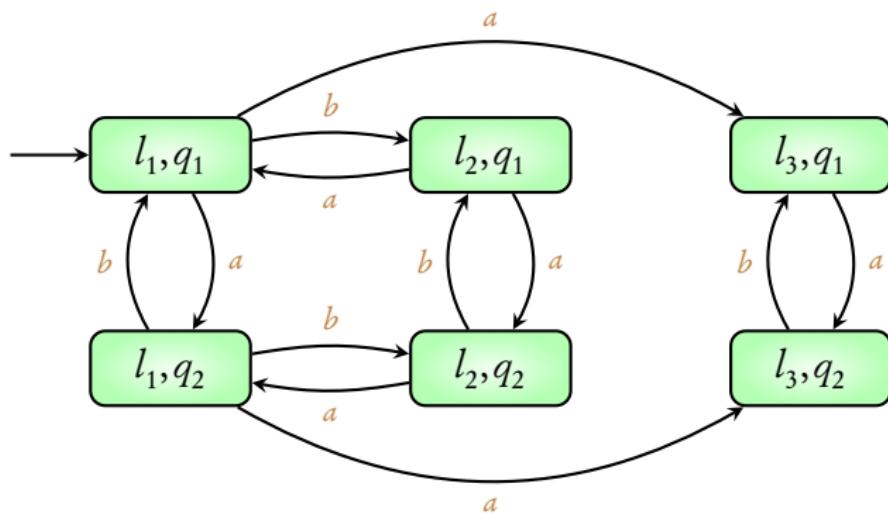












# Multiple systems

TS<sub>1</sub> ||| TS<sub>2</sub> ||| ... ||| TS<sub>n</sub>

# Multiple systems

TS<sub>1</sub> ||| TS<sub>2</sub> ||| ... ||| TS<sub>n</sub>

Exercise: Try out an example of interleaving **three** systems

# Concurrent systems

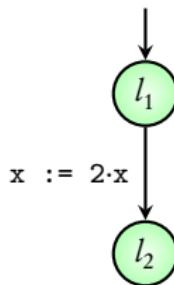
Independent

Interleaving

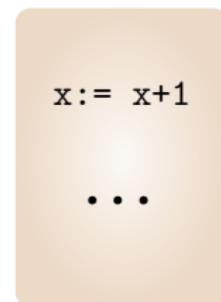
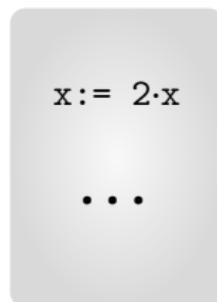
$\text{TS}_1 \parallel \text{TS}_2 \parallel \dots \parallel \text{TS}_n$

Shared variables

Shared actions



PG<sub>1</sub>



PG<sub>2</sub>

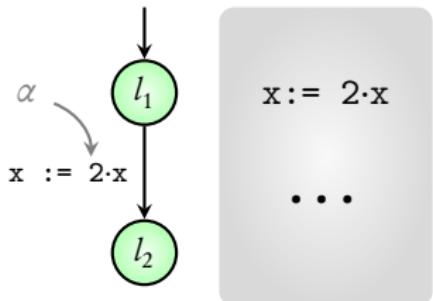
$x := x+1$

• • •

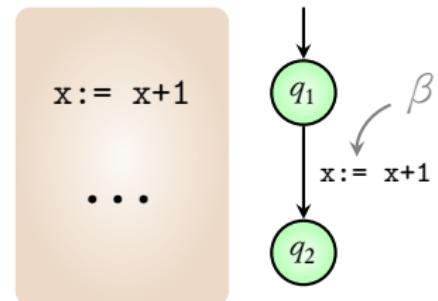
$q_1$

$x := x+1$

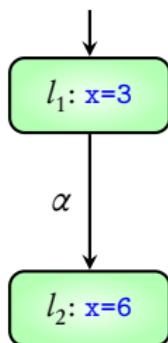
$q_2$



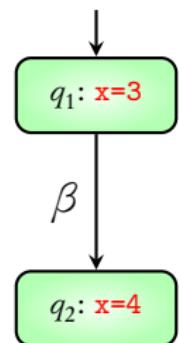
$PG_1$



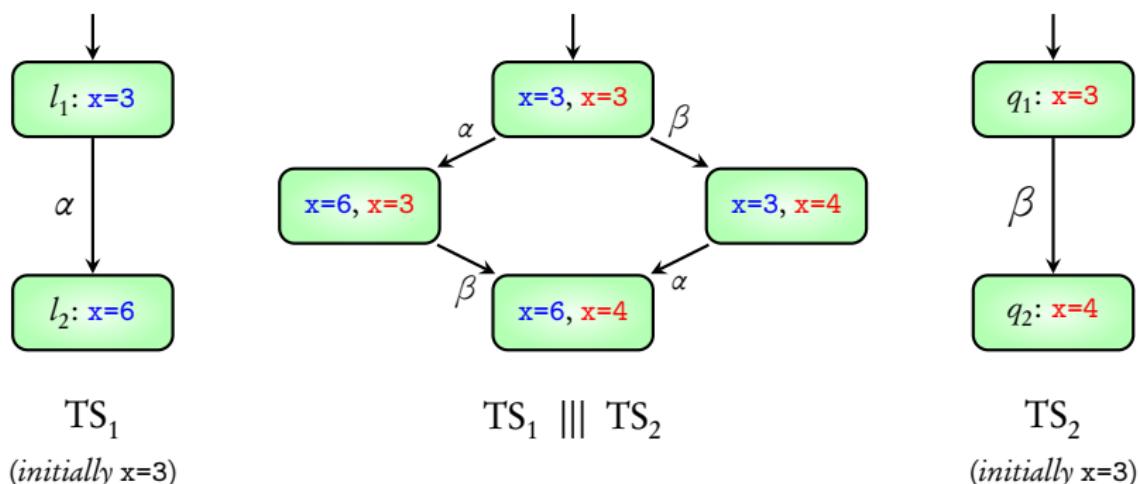
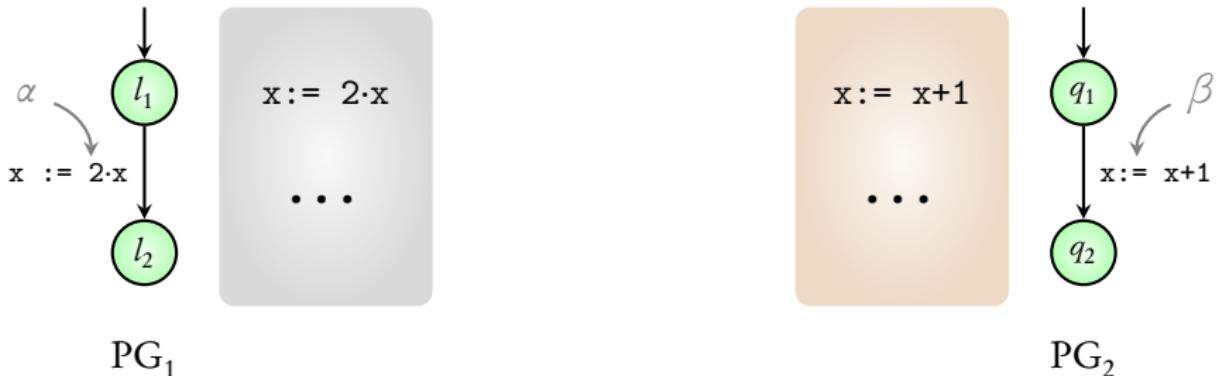
$PG_2$

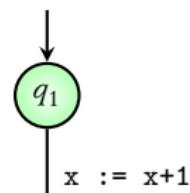
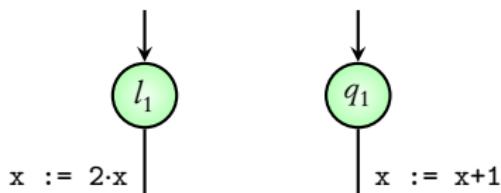


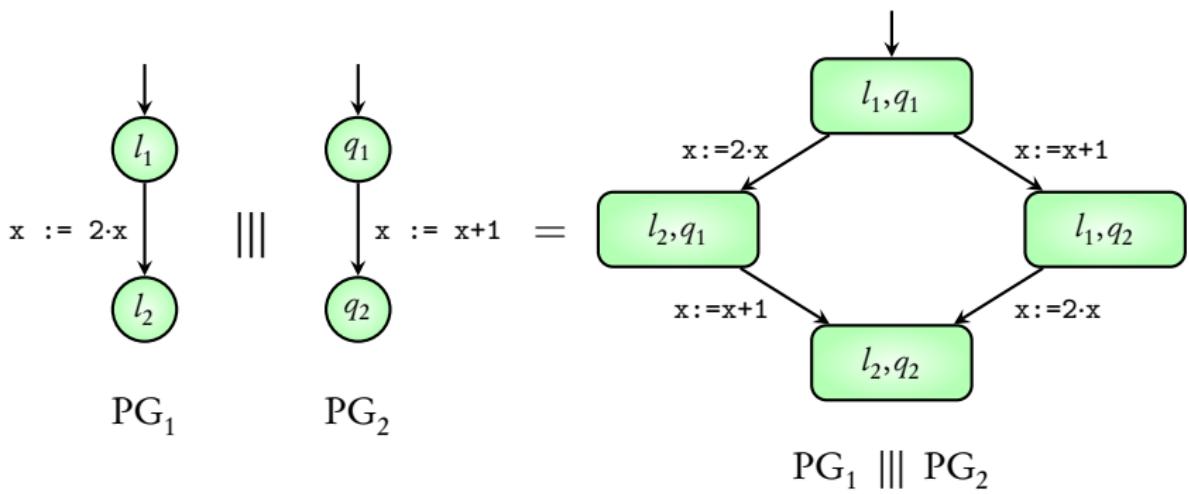
$TS_1$   
(initially  $x=3$ )

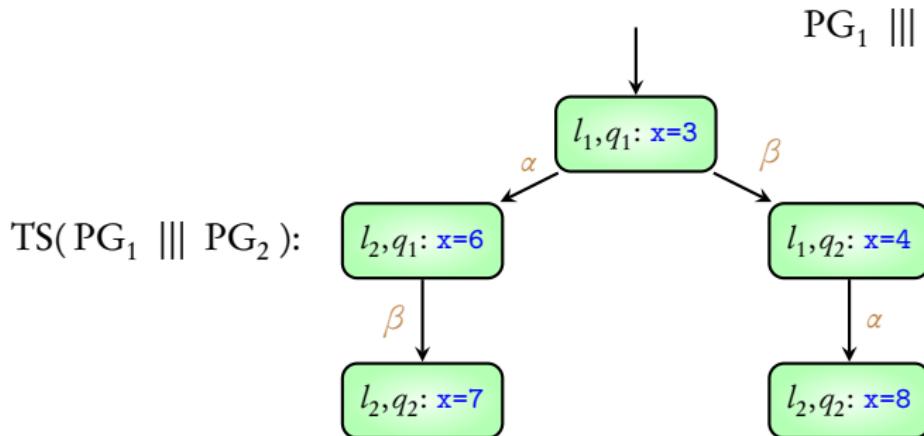
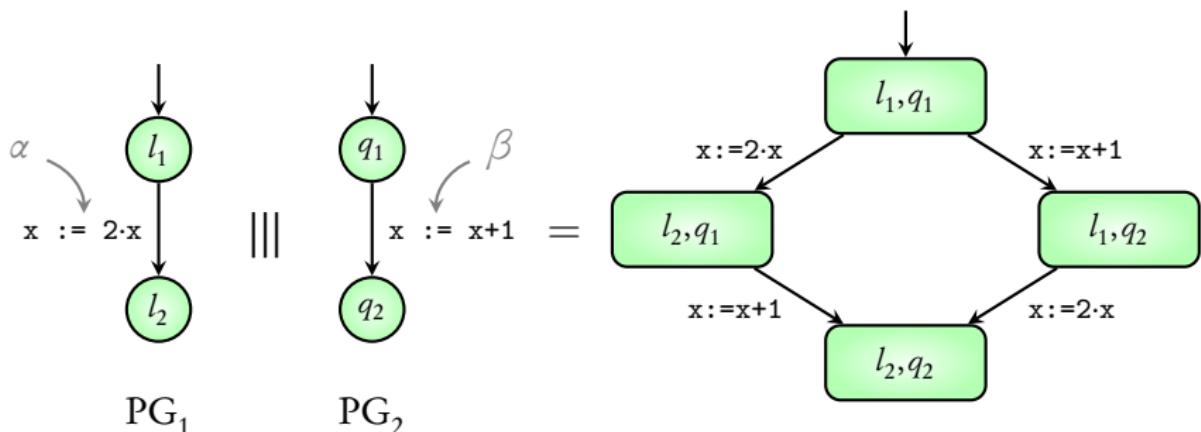


$TS_2$   
(initially  $x=3$ )









# Concurrent systems

## Independent

Interleaving

$TS_1 \parallel TS_2 \parallel \dots \parallel TS_n$

## Shared variables

$TS(PG_1 \parallel PG_2 \parallel \dots \parallel PG_n)$

## Shared actions

**Coming next:** Another example

**while**  $x < 200$

$x := x+1$

**while**  $x > 0$

$x := x-1$

**while**  $x = 200$

$x := 0$

```
while x < 200
```

```
    x := x+1
```

```
while x>0
```

```
    x := x-1
```

```
while x=200
```

```
    x := 0
```

Is the value of  $x$  always between 0 and 200?

**while**  $x < 200$

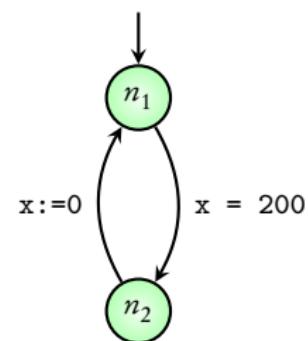
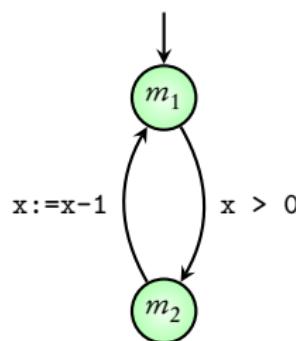
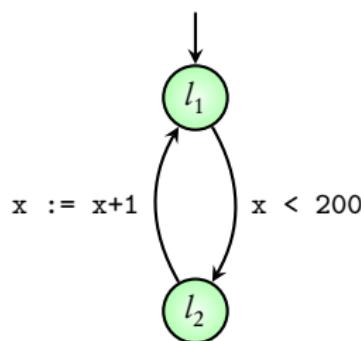
$x := x + 1$

**while**  $x > 0$

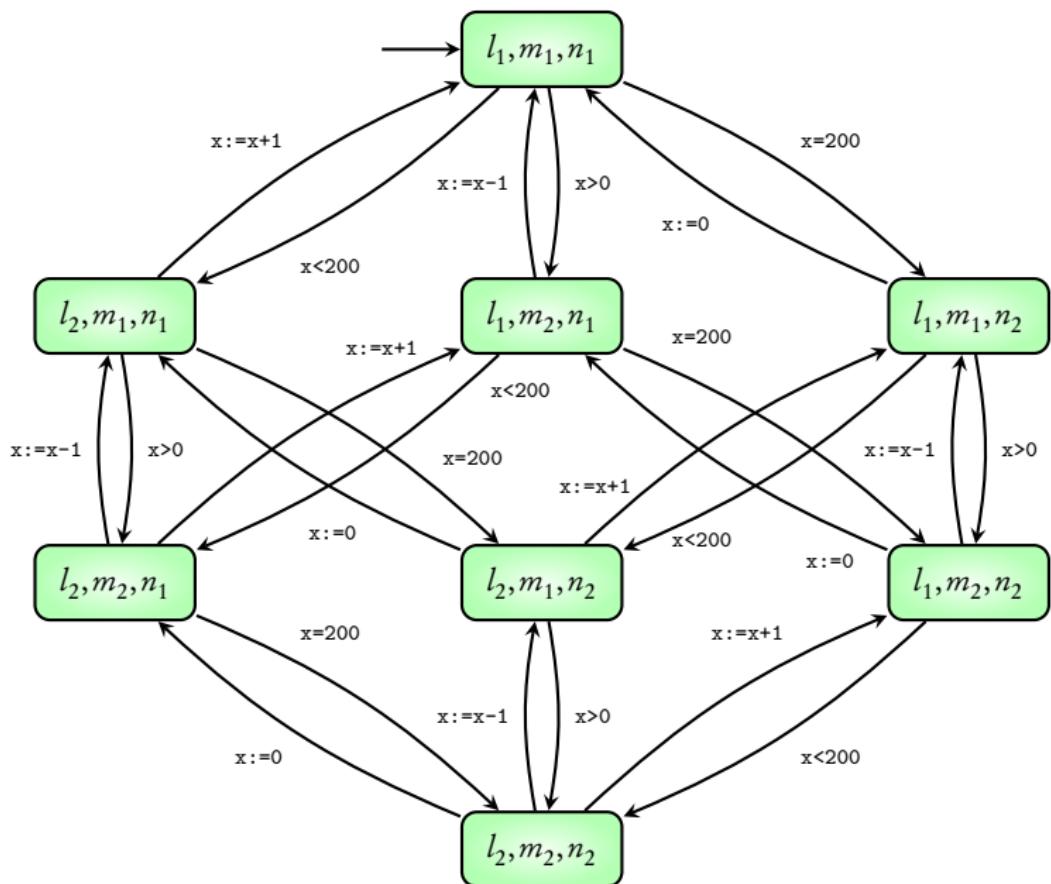
$x := x - 1$

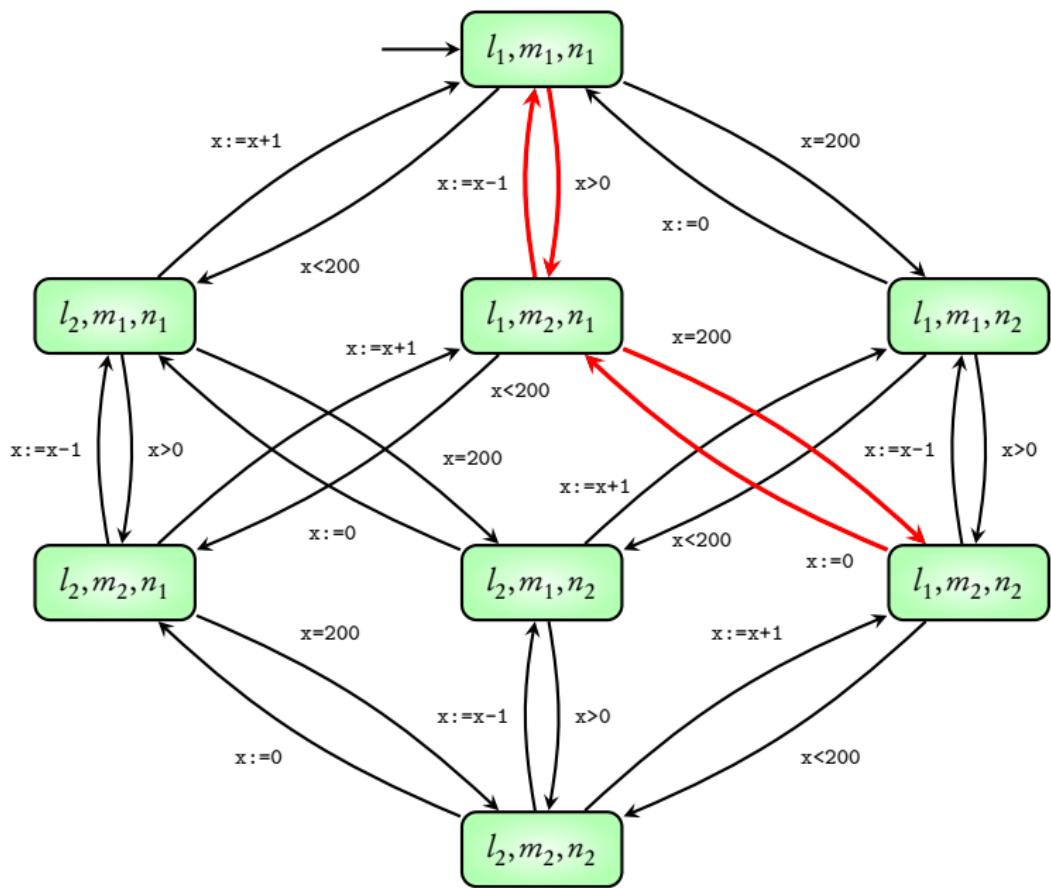
**while**  $x = 200$

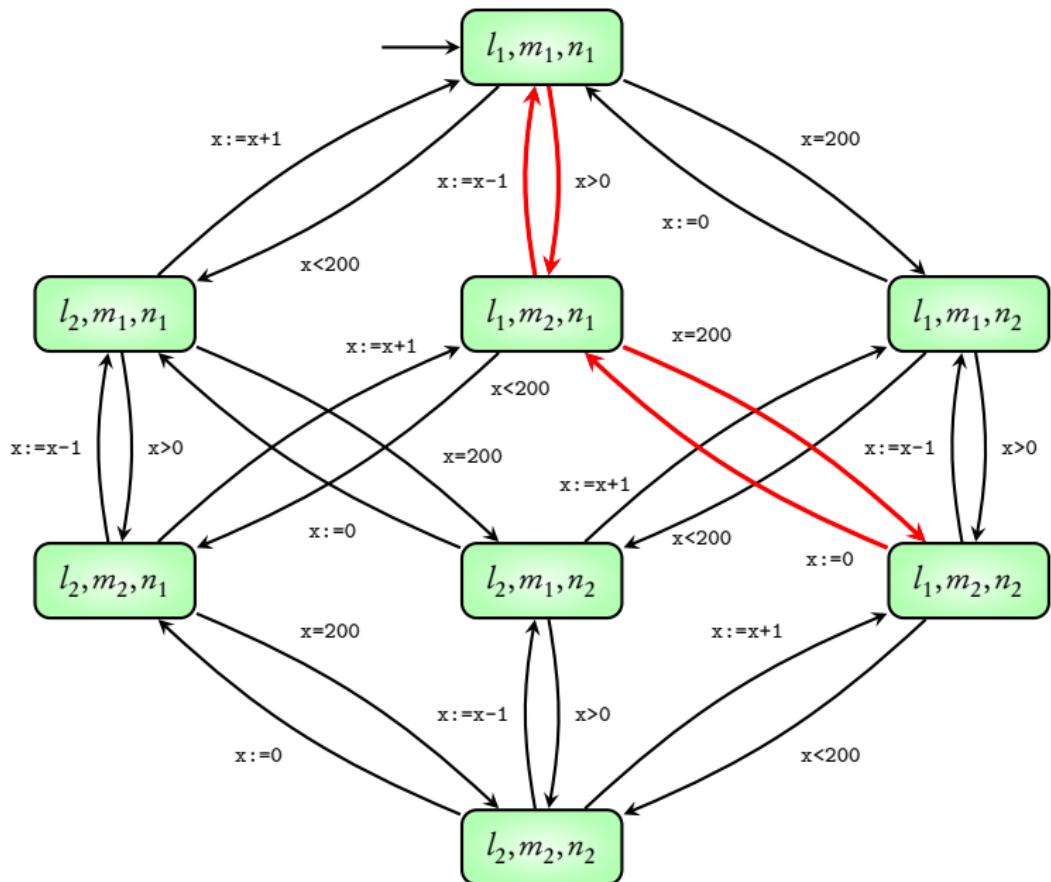
$x := 0$



Is the value of  $x$  always between 0 and 200?

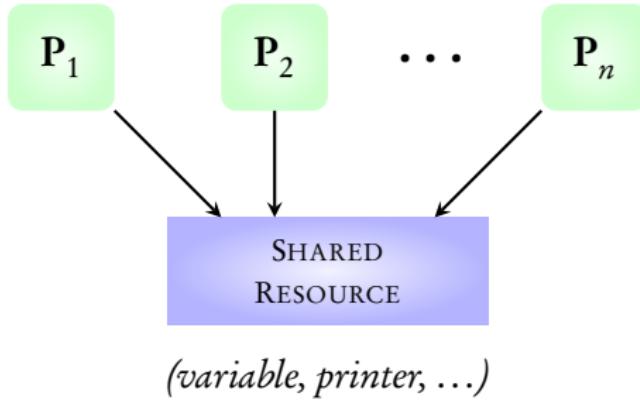






Is the value of  $x$  always between 0 and 200? **No**

**Coming next: Mutual exclusion**



**Mutual Exclusion:** No two processes can access the resource simultaneously

**Goal:** Modeling the **protocols** used for mutual exclusion

$P_1$

loop forever

: \*non-critical actions\*

*request*

critical section

*release*

: \*non-critical actions\*

end loop

$P_2$

loop forever

: \*non-critical actions\*

*request*

critical section

*release*

: \*non-critical actions\*

end loop

$P_1$

loop forever

: \*non-critical actions\*

*request*

critical section

*release*

: \*non-critical actions\*

end loop

$P_2$

loop forever

: \*non-critical actions\*

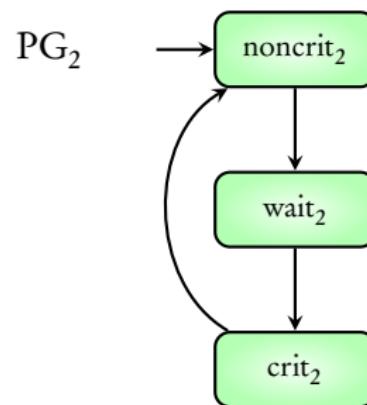
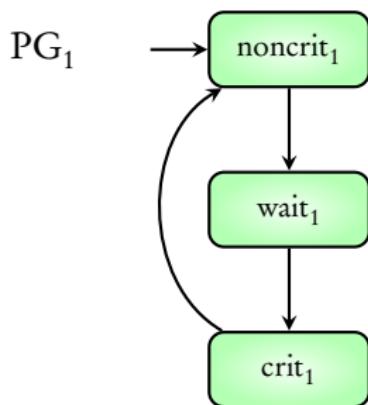
*request*

critical section

*release*

: \*non-critical actions\*

end loop



$P_1$

loop forever

⋮ \*non-critical actions\*

{ if  $y > 0$ :  $y := y - 1$  } \*request\*

critical section

$y := y + 1$  \*release\*

⋮ \*non-critical actions\*

end loop

$P_2$

loop forever

⋮ \*non-critical actions\*

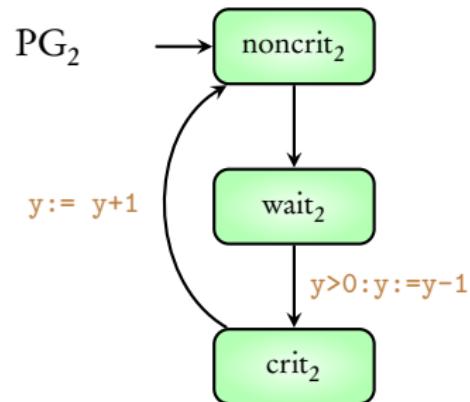
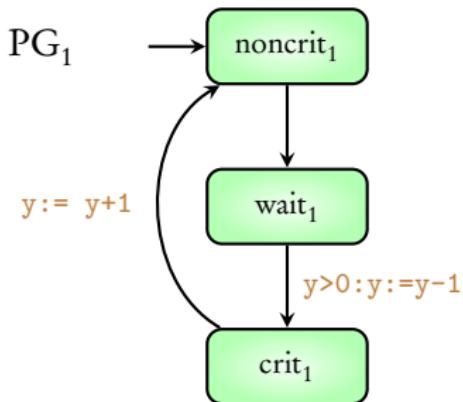
{ if  $y > 0$ :  $y := y - 1$  } \*request\*

critical section

$y := y + 1$  \*release\*

⋮ \*non-critical actions\*

end loop



$P_1$

loop forever

⋮ \*non-critical actions\*

{ if  $y > 0$ :  $y := y - 1$  } \*request\*

critical section

$y := y + 1$  \*release\*

⋮ \*non-critical actions\*

end loop

$P_2$

loop forever

⋮ \*non-critical actions\*

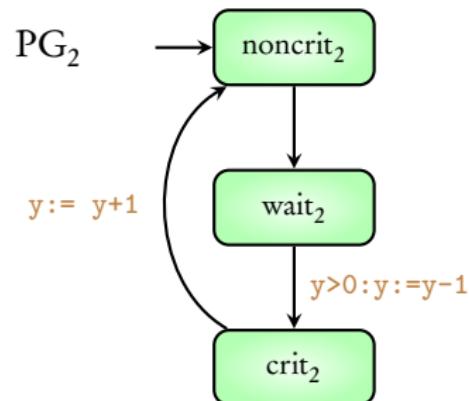
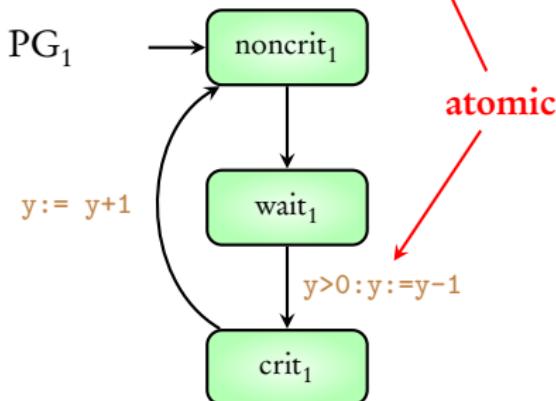
{ if  $y > 0$ :  $y := y - 1$  } \*request\*

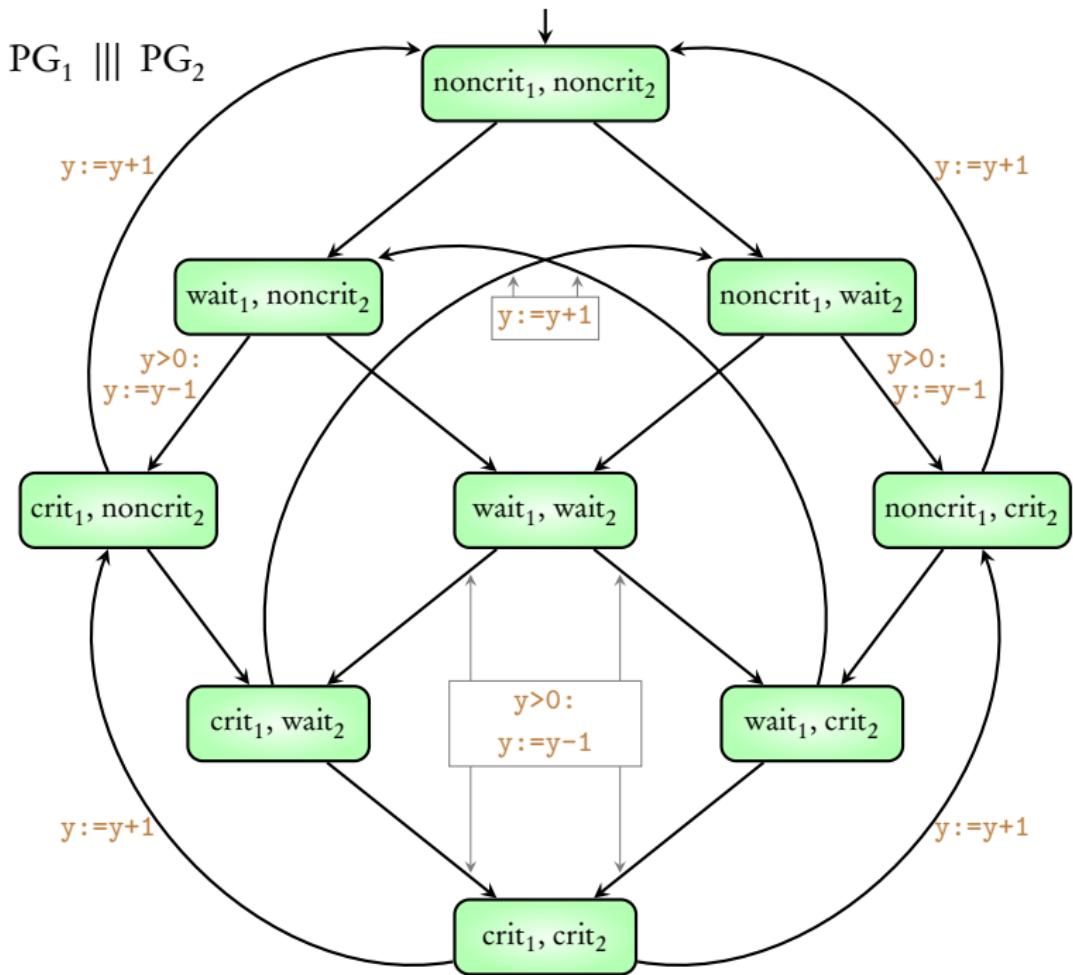
critical section

$y := y + 1$  \*release\*

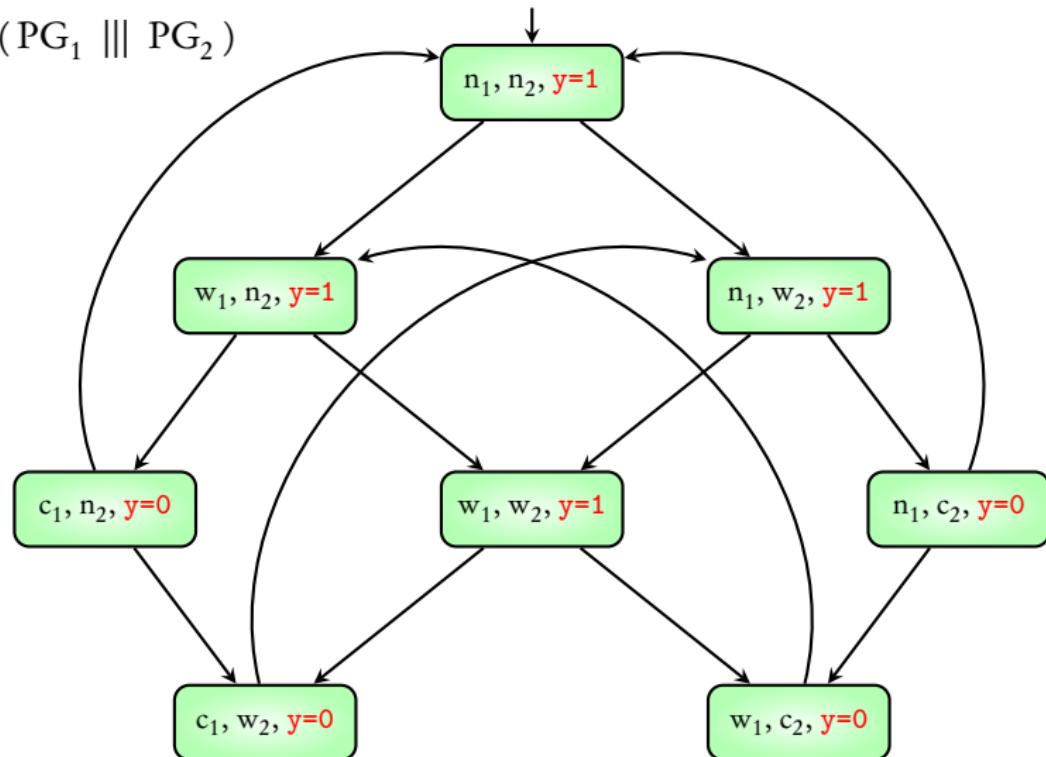
⋮ \*non-critical actions\*

end loop

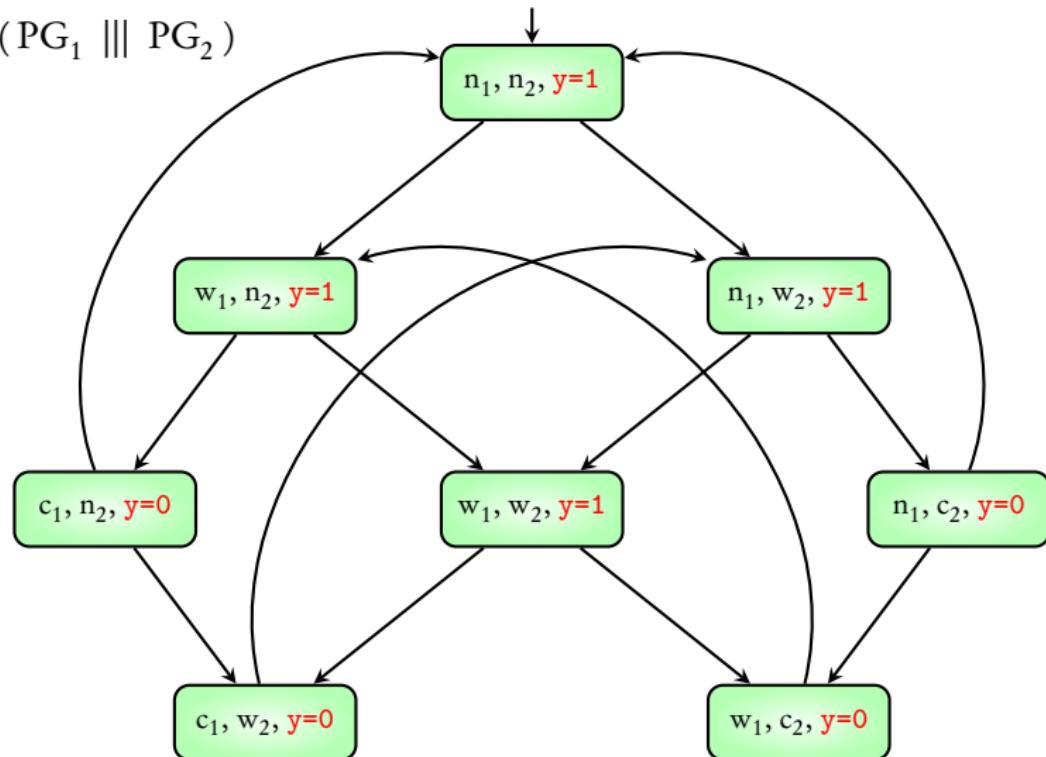




$\text{TS}(\text{PG}_1 \parallel\!\!\!|| \text{ PG}_2)$



$TS(PG_1 \parallel\| PG_2)$



Both processes **cannot be** in critical section **simultaneously**

# Concurrent systems

## Independent

Interleaving

$TS_1 \parallel TS_2 \parallel \dots \parallel TS_n$

## Shared variables

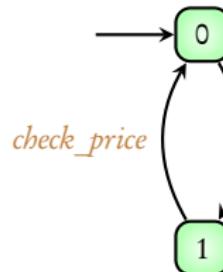
$TS(PG_1 \parallel PG_2 \parallel \dots \parallel PG_n)$

Mutual Exclusion

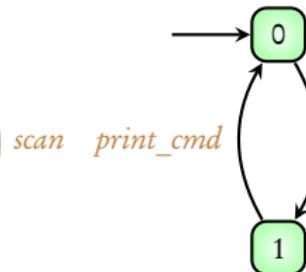
## Shared actions

**Coming next: Book-keeping system in a supermarket**

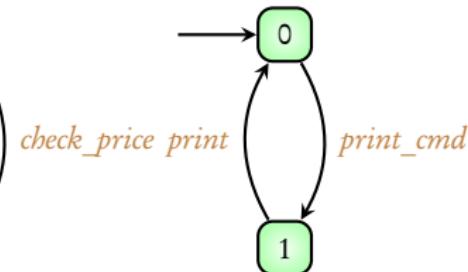
Bar-Code Reader (BCR)



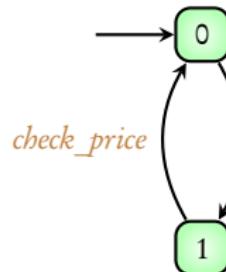
Booking Program (BP)



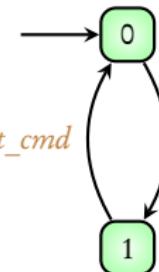
Printer (P)



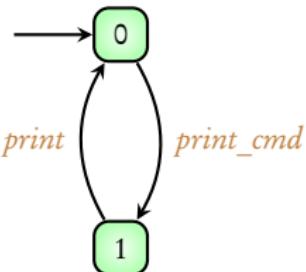
Bar-Code Reader (BCR)



Booking Program (BP)

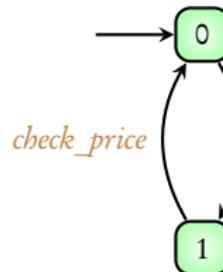


Printer (P)

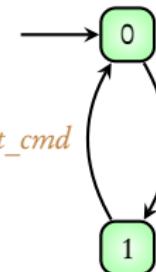


000

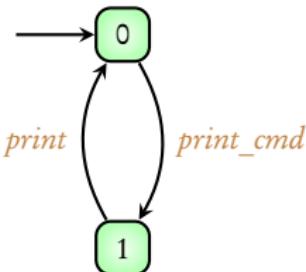
Bar-Code Reader (BCR)



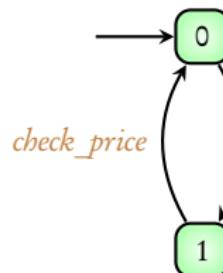
Booking Program (BP)



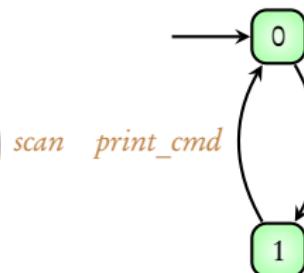
Printer (P)



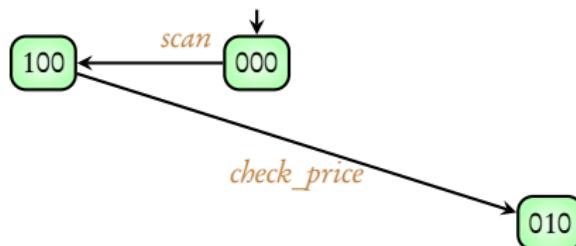
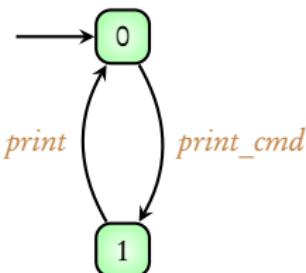
Bar-Code Reader (BCR)



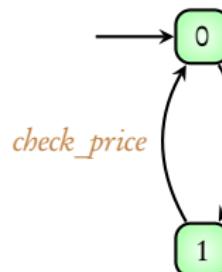
Booking Program (BP)



Printer (P)



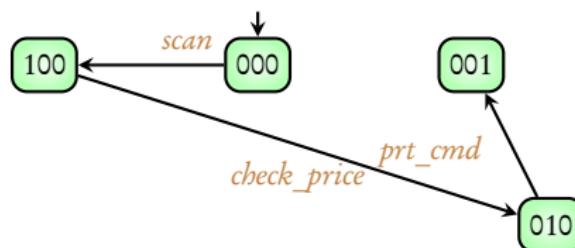
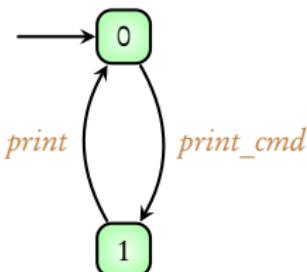
Bar-Code Reader (BCR)



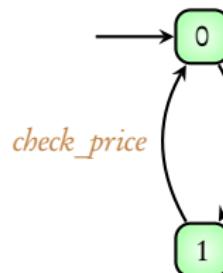
Booking Program (BP)



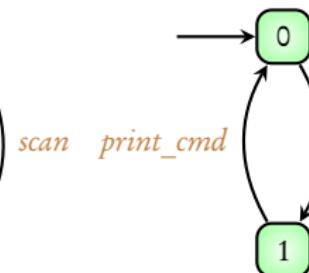
Printer (P)



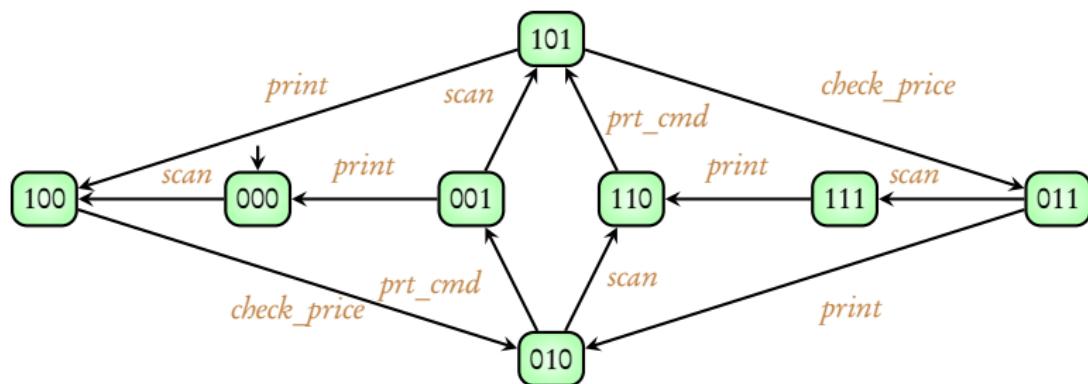
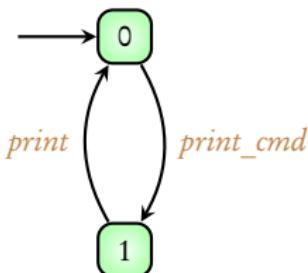
Bar-Code Reader (BCR)



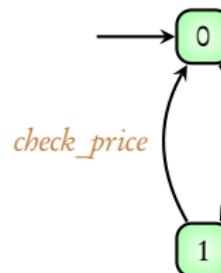
Booking Program (BP)



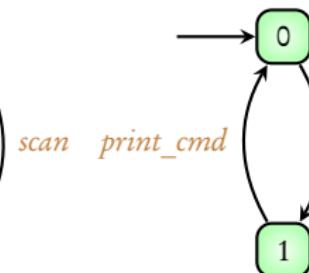
Printer (P)



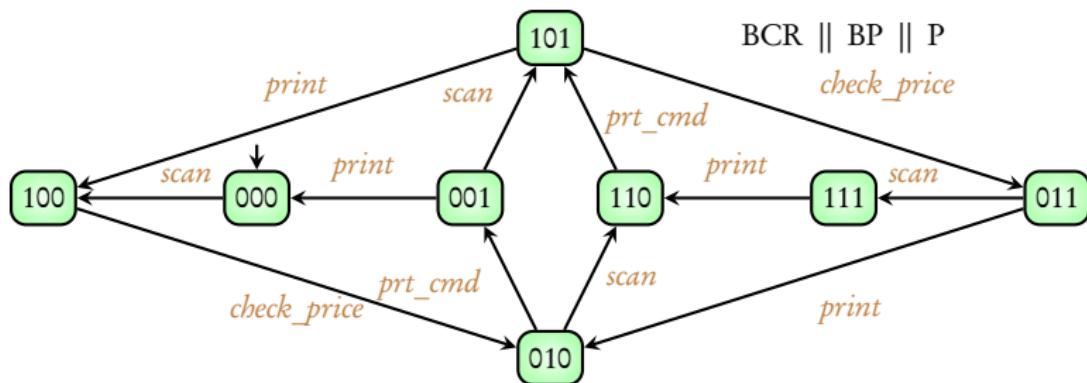
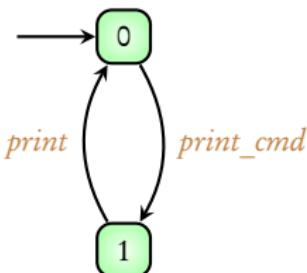
Bar-Code Reader (BCR)



Booking Program (BP)



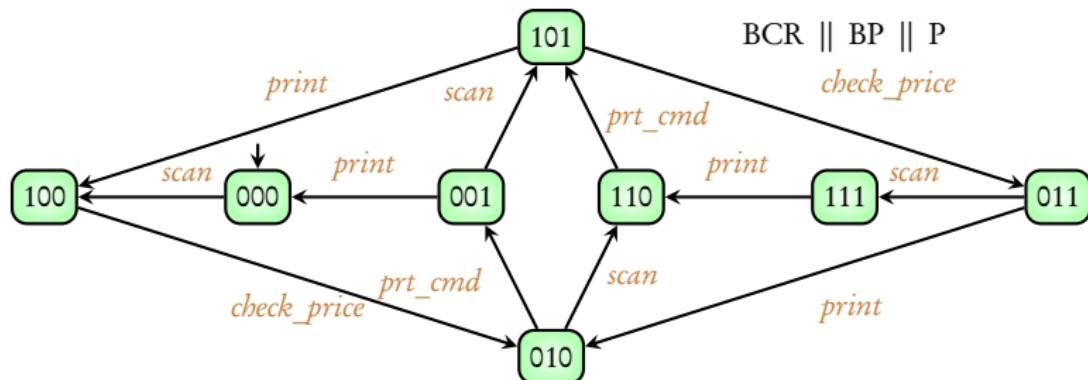
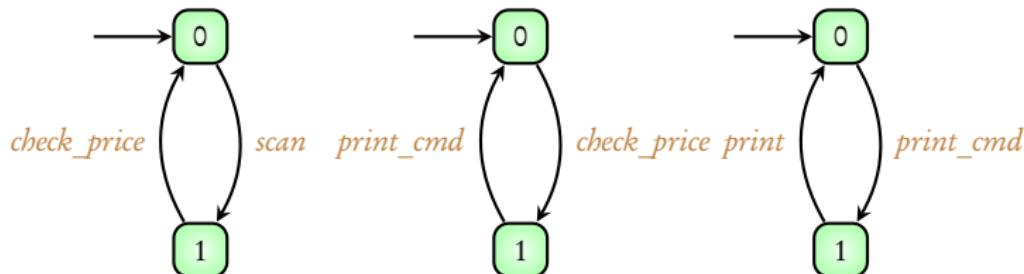
Printer (P)



Bar-Code Reader (BCR)

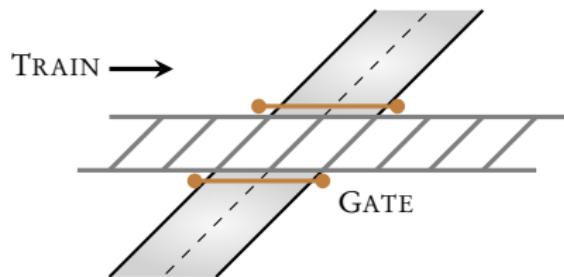
Booking Program (BP)

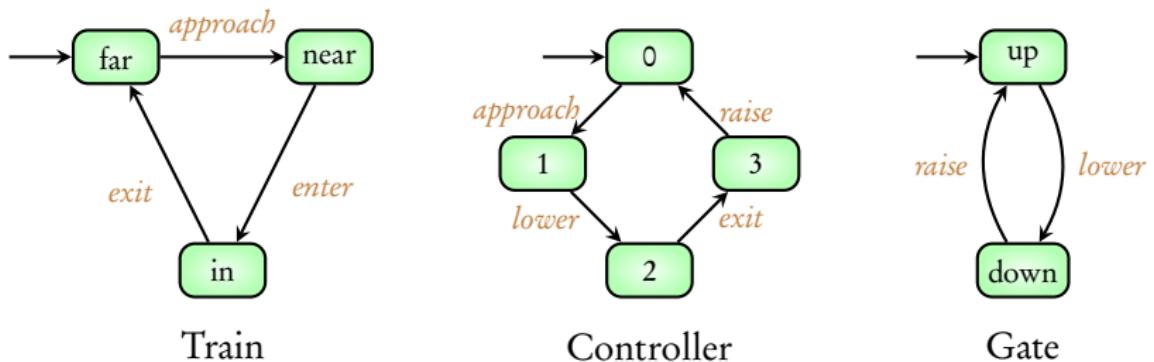
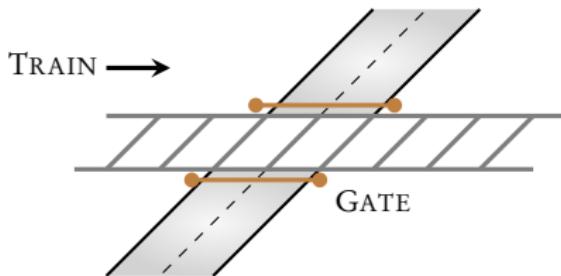
Printer (P)

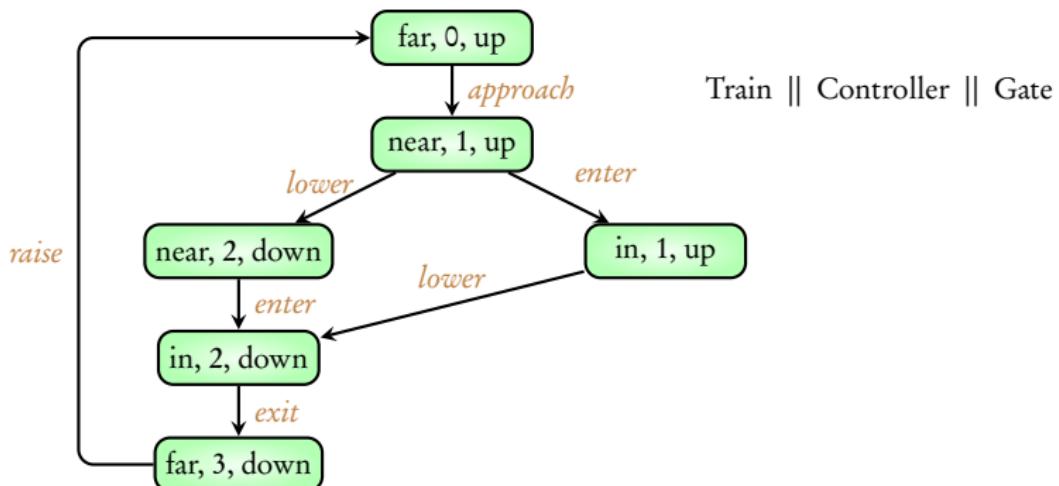
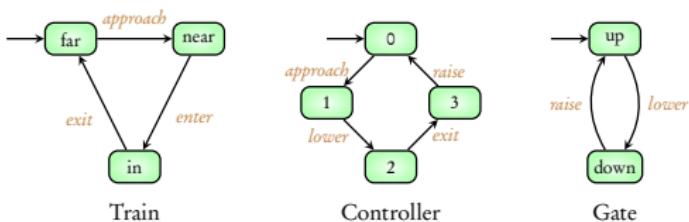


*check\_price, print\_cmd:* Shared actions (also called handshaking actions)

**Next example:** Train-Gate-Controller







Train  $\parallel$  Controller  $\parallel$  Gate

**||** : Handshake operator

## Independent

Interleaving

$TS_1 \parallel\!| TS_2 \parallel\!| \dots \parallel\!| TS_n$

## Shared variables

$TS(PG_1 \parallel\!| PG_2 \parallel\!| \dots \parallel\!| PG_n)$

Mutual Exclusion

## Shared actions

$TS_1 \parallel TS_2$

Reference: Principles of Model Checking, *Baier and Katoen*, MIT Press (2008)  
Pages 35 - 53

# Week-1: Introduction to model checking

B. Srivathsan

Chennai Mathematical Institute

*NPTEL-course*

July - November 2015

# Summary

- ▶ Course Overview
- ▶ **Module 1:** Transition systems, Modeling simple sequential programs
- ▶ **Module 2:** Modeling sequential hardware circuits
- ▶ **Module 3:** Modeling data-dependent programs
- ▶ **Module 4:** Modeling concurrent systems

**Important concepts:** Non-determinism, program graphs, interleaving and handshake operators