

Academic Finance for the Practical Investor

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2022 Fall

BACKGROUND

Although the word “quant” today conjures up images of lightning-fast computers and huge datasets with server racks pressed up as close to the wall as possible so that electrical signals don’t have to travel a single millimeter farther along the Ethernet cable than necessary, those things are much more useful in high-frequency proprietary trading than medium-term systematic investing.

On the other hand, people tend to associate academic finance with stodgy research into banking systems and curmudgeonly debates over fiscal policy. But the literature is rich with applications of statistics and optimization that actually matter to a practitioner. This is my attempt at a survey of some outstanding examples of papers that are:

- Rigorous.
- Easy (or at least, reasonable) to digest.
- Interesting.
- Useful.

ASSET PRICES AS STOCHASTIC PROCESSES

- Blyth, Stephen. 2013. Harvard Management Company, Harvard Dept of Statistics. “An Introduction to Quantitative Finance” . Oxford Press.
 - Key takeaway: The Fundamental Theorem of Asset Pricing.
 - Topics: Arbitrage, Equivalent martingale measures.
 - What this will help teach you: Understand and price derivatives like forwards, futures, swaps, and options.
 - Investment strategies that apply this: Futures-curve arbitrage, Options arbitrage.
 - Questions you should be able to answer after reading this:
 - * When Bloomberg runs the headline “September 2023 S&P 500 futures point higher”, why does that have nothing to do with where people expect stocks are going to be next year, and everything to do with where they expect stocks to be 45 minutes from now at 930am when the market opens? (A: Spot-futures no-arb relationship.)
 - * Why do we tend to see a “smirk” in the implied-volatility surface? (A: Black-Scholes does not have parameters for skew or kurtosis, nor does it have a parameter for put premia being bid up by risk-averse investors looking to insure their large stock portfolios.)
 - * Why, in light of the above two questions, can I not effectively go long the VIX by going long VIX futures, waiting for a blowup, and then retiring with my profits? After all, the VIX has never dropped to zero, but it often doubles within weeks. (A: There is no tradable spot VIX security, so there is no way to construct the replicating portfolio that would usually enforce the spot-futures no-arb relationship. Therefore, there is immense downward pressure on prices for long-dated contracts (which will be active for a long time), which tends to relax as maturity approaches and no immediate danger seems imminent. The futures-spot carry is hence bleedingly negative on average. Unfortunately, the XIV meltdown shows that the opposite approach—opening a passive short position and rolling every quarter—isn’t a sure bet either.)

- Followup questions:
 - * Arbitraging a security requires it to be very liquid, as you’ve got to be able to buy it at the low venue and sell it at the high venue very quickly, else you run the risk that prices will move against you, closing or even inverting the gap. But liquid securities are exactly the ones least likely to see mispricings, since there are so many people paying attention to them. How often do arbitrage opportunities arise in the real world, and what are the limits of arbitrage that can keep them open?

PORTFOLIO-CONSTRUCTION BASICS

- Markowitz, Harry. 1952. RAND Corp. “Portfolio Selection” . Journal of Finance, Vol 7, Iss 1.

- Key takeaway: A mean-variance investor is a Sharpe-maximizing investor:

$$\arg \max_w \left(w' \mu - \frac{\gamma}{2} w' \Sigma w \right) = \gamma^{-1} w^* \quad \text{where} \quad w^* = \Sigma^{-1} \mu.$$

This is the $E = mc^2$ of quant finance.

- Topics: MPT (modern portfolio theory), MVO (mean-variance optimization), Efficient frontier, Tangency portfolio, Capital market line.
- What this will help teach you: Formalize the tradeoffs faced by a risk-averse investor, and construct an optimal portfolio in response.
- Investment strategies that apply this: All of them.
- Questions you should be able to answer after reading this:
 - * How can I construct a Sharpe-maximizing portfolio?
 - * How can I use hedging to turn a non-optimal portfolio into an optimal one?
 - * What role does leverage play in helping me hit my ER targets (or respect my risk caps)?
- Followup questions:
 - * In the real world, correlation matrices are estimated. Why is shrinkage so important? (A: The same reason that collinearity blows out standard errors in an OLS regression. In that setting we call it $(X^T X)^{-1}$, here we call it $\hat{\Sigma}^{-1}$, but it’s the same thing and has the same sensitivities.)
 - * What are the implications for rational capital markets? (A: See CAPM, Black-Litterman.)
 - * What if I want to define risk as something other than portfolio variance? (A: Any reasonable definition of risk should scale monotonically with position size so that e.g. zero position entails zero risk. And keep in mind that “low ER” isn’t risk in this framework – you dislike money-losing positions not because they inflate the second term, but because they deflate the first term. But if you embrace this framework you will find that it is quite flexible, and amenable to adjustments to account for different definitions of risk, presence of transaction costs, and constraints.)
- Asness, Cliff. 1996. Goldman Sachs Asset Mgmt. “Why Not 100% Equities” . Journal of Portfolio Management, Vol 22, No 2.
 - Key takeaway: A levered safe portfolio can be a better deal than an unlevered risky one.
 - Topics: Risk-adjusted return, Diversification, Concentration, Asset allocation.
 - What this will help teach you: Leverage is not a single-edged sword.
 - Investment strategies that apply this: Risk parity.
 - Questions you should be able to answer after reading this:
 - * How can I quantify the riskiness of a levered but diversified portfolio, versus an unlevered but concentrated one?
 - Followup questions:

- * Are there cases where the above analysis breaks down? (A: Yes, in high-volatility climates, geometric returns are no longer approximately-Normal. An unlevered portfolio can fall to zero, but a levered portfolio in this climate can actually go underwater. This effect will be exacerbated by the fact that you will be getting margin-called on the way down. The good news is that, in a high-volatility climate, you will not need leverage. In fact, in such a climate, a 60/40 portfolio will actually be *more* exposed to risk than a corresponding risk parity portfolio, as the risk parity portfolio will actually *delever* in response to the elevated risk.)
- Sharpe, William F. 1991. Stanford Dept of Economics. “The Arithmetic of Active Management” . Financial Analysts’ Journal, Vol 47, No 1.
 - Key takeaway: It is mathematically impossible for the active-management industry as a whole to beat the market. Before costs, the average alpha will be zero, and after costs, it will be negative.
 - Topics: Alpha, Beta, Active management, Passive management, Index funds.
 - What this will help teach you: Humility.
 - Investment strategies that apply this: All of them.
 - Questions you should be able to answer after reading this:
 - * Why is alpha a zero-sum game?
 - * Why does a passive market-tracking fund never have to trade?
 - Followup questions:
 - * What are common ways an investor can be tricked into thinking their manager has alpha, given that the average manager has none? (A: One is leverage. A manager who invests in a double-levered SPX tracker will earn about twice the excess return of an S&P 500 tracker, which is expected to be positive over the long term. That’s not alpha, that’s just... more beta. This way is especially bad if the manager isn’t transparent with you about the amount of risk they’re taking on your behalf. Another way is “investing outside the universe”. For example, some investment-grade-focused corporate bond funds will legally allow some small allocation to attractive junk bonds. They will tend to outperform the IG corporates market, since they have an allocation to higher-yielding junk that isn’t included when calculating the market return. But the real question—which the manager will rarely answer—is whether their junk allocation outperformed the *junk bond* market. Otherwise, they’re still not giving you alpha, they’re just giving you different (and riskier) beta.)

FACTOR INVESTING

- Fama, Eugene F; French, Kenneth R. 1992. Univ of Chicago Graduate School of Business. “The Cross-Section of Expected Stock Returns” . Journal of Finance, Vol 47, No 2.
 - Key takeaway:

$$R_{i,t} = \alpha_{i,t} + \beta_{i,t}^M (R_{M,t} - R_{f,t}) + \beta_{i,t}^{SMB} SMB_t + \beta_{i,t}^{HML} HML_t + \varepsilon_{i,t}.$$

The formalization of the idea that stocks can be exposed to common risk factors beyond just market beta was a breakthrough innovation.
 - Topics: Factor models, CAPM (capital-asset pricing model), APT (arbitrage pricing theory), Factor zoo, Alpha, Beta, Compensated risk factors, Uncompensated risk factors, Risk premia, Market returns, Excess returns, Pricing anomalies.
 - What this will help teach you: Model and inference-test hypothetical drivers of out- or under- performance of securities *within* a single time period. Understand how common risk exposures can drive covariances between security returns.
 - Investment strategies that apply this: EMN (equity market-neutral), FIRV (fixed-income relative-value).
 - Questions you should be able to answer after reading this:
 - * How can long-short portfolios help me profit off ER models without requiring a view on whether a security’s price will rise or fall in absolute terms?
 - * Why does the discovery of a long-short factor with significant alpha over its exposures to the named factors provide evidence that the 3-factor model is incomplete?

- Followup questions:
 - * How much of this is just p -hacking? (A: A lot. It is well-documented that ER of a factor is highest in-sample, lower out-of-sample, lower still in the period between the end of the backtest and the article's publication date.)
 - * How much of this can be exploited if everyone knows about it? Won't quants "arb away" the profits i.e. buy up value stocks and sell short growth stocks until their prices become fair and there's no more anomalous profit? (A: Again, it is well-documented that ER of a factor gets discretely lower after publication of the article describing it. The consistency of this phenomenon suggests that quants do indeed read the article, implement the factor, and thereby diminish profit opportunities for second movers. Remember, by definition, a profitable factor is one whose positions can be sold at more favorable prices by first movers to second movers – and favorable to one party means unfavorable to the other!)
- Frazzini, Andrea (AQR Capital Mgmt); Kabiller, David G (AQR Capital Mgmt); Pedersen, Lasse Heje (Copenhagen Business School, NYU Stern, CEPR, AQR Capital Mgmt). 2013. "Buffett's Alpha". *Financial Analysts' Journal*, Vol 74, Iss 4.
 - Key takeaway: Much of Buffett's portfolio performance seems driven by a few liquid quant factors plus leverage.
 - Topics: Factor investing, RBSA (returns-based style analysis), Portfolio decomposition, Leverage.
 - What this will help teach you: Think about market-neutral equity strategies not as picking individual stocks, but rather as loading on or against systematically-constructed factors.
 - Investment strategies that apply this: Style premia, ARP (alternative risk premia), Smart beta.
 - Questions you should be able to answer after reading this:
 - * What has the legendary Warren Buffett's realized Sharpe been? 2? 5? 10? (Spoiler alert: No. It's about 0.79. That's very good at scale!)
 - * Does Buffett's private- or public-equity portfolio explain most of his outperformance?
 - * How much leverage has Buffett historically applied to his holdings?
 - Followup questions:
 - * What is the point of quants if they're just backfitting things that discretionary stock pickers already know about? (A: The quant edge isn't necessarily that computers can find brand-new signals – It's often simply that computers can systematize the implementation so that rather than applying the signal to 10 or 20 stocks, you can apply the signal to 1000 or 2000 stocks at once. It's also much easier to expand or port research between asset classes. Finally, it can help dampen the effects of human emotion on judgment – Computers don't get cranky when lunch is late.)
 - * Okay, then what is the point of humans if computers can systematize the signals and then run them for free on a couple dollars of electricity per day? (A: Somebody has got to do the fundamental research that decides which datasets and models go into production! There's also always an epsilon between the model ER and a more precise ground-truth ER, and intense scrutiny by humans can help bridge that gap. Many deep-value strategies use computer-screened asset universes from which flagged opportunities are sent to humans to validate that they are not "value traps".)
 - * So if everyone knows about these factors now, why should they persist? (A: Sometimes they don't. In fact, sometimes they're just artifacts of overfitting. But in other cases, they can persist for good reasons like risk aversion, behavioral bias, or liquidity dynamics.)
- Ritholtz, Barry. 2007. *Ritholtz Wealth Mgmt. "Dear Investor...: Quant Letters to Clients"*. The Big Picture.
 - Key takeaway: In August of 2007, losses of 10-20% struck quant equity portfolios across Wall Street within just a few days – then recovered almost just as quickly. The consensus by now is that some large whale was hit with a redemption request and had to unwind their book immediately to meet it (otherwise they themselves would not have accepted the fire-sale prices that showed up on Bloomberg screens after the fact!). The fact that everyone in the market-neutral quant equity game from Goldman to RenTech was following essentially the same factors meant that they all saw huge paper losses as a result, but those losses recovered as the fire sale subsided and the underlying stocks resumed trading at reasonable prices. What is remarkable is that this was purely a long-short phenomenon: The longs

plunged and the shorts skyrocketed, but because they balanced each other out, the S&P 500 hardly budged over this period. The crisis was harrowing as it unfolded, and investors were knocking down doors demanding to know what was going on. Every quant runs some version of a risk-targeter, and these books are run at about 10% vol. Accounting for the 261 trading days per year, a loss of even just 5% in one day is an 8σ event.

– Topics: Quant crisis.

– Followup questions:

- * As a factor gains AUM, pricing pressures will naturally “richen” it: Managers will buy up the longs, inflating their value, and sell down the shorts, deflating their value. This is good on the way up, but does it arb away the factor’s short- to medium-term profits?
- * The scenario above ends up with a crowded position. That is, in an extreme case, the people who are long the factor’s shorts and short its longs are a mix of individuals, institutions, and managers. But the people who are long the factor’s longs and short its shorts are purely quant-equity managers. They have together cornered the market on a risky asset, but because they are not literally a single entity, they will trip over each other in case there’s a run for the exit. How do you fortify your defenses against this?
- * Even worse, those longs and shorts are the only things on their books. The fact that they don’t have any diversifying positions to cushion an out-of-the-blue single-factor crisis means that they are very vulnerable to such a single-factor run being triggered. How do you fortify your defenses against *this*? Magically build up a business in an unrelated asset class as a diversification tactic?

GLOBAL MACRO

- Brooks, Jordan. 2017. NYU Stern, AQR Capital Mgmt. “A Half Century of Macro Momentum” . Alternative Investment Analyst Review.
 - Key takeaway: There are simple, intuitive global-macro signals useful for both directional and market-neutral investment strategies (depending on how you implement a given signal).
 - Topics: Global macro, Momentum, Trend.
 - What this will help teach you: Hard-code economically-motivated signals in an appealingly lightweight and self-consistent framework.
 - Investment strategies that apply this: Systematic macro.
 - Questions you should be able to answer after reading this:
 - * Is rising domestic inflation bullish or bearish for the home currency?
- Taylor, John B. 1993. Stanford Dept of Economics. “Discretion vs Policy Rules in Practice” . Carnegie-Rochester Conference Series on Public Policy, No 39.
 - Key takeaway: $r := p + 0.5y + 0.5(p - 2) + 2$.
 - Topics: Monetary policy, Federal Reserve, FFR (fed funds rate).
 - What this will help teach you: Reason about policy-driven changes in security prices.
 - Investment strategies that apply this: FIRC (fixed income, rates, and credit).
 - Questions you should be able to answer after reading this:
 - * How aggressively should you raise the FFR if GDP growth comes in 2% too hot?
 - Followup questions:
 - * Obviously, the Taylor Rule could be a self-fulfilling prophecy: Fed economists *think* it is the right response, and they decide the ultimate policy, so it becomes the actual response. But what about market participants? Suppose they expect the Fed to think the Taylor Rule is the right response. And suppose the Rule recommends raising rates. Will they rush to dump bonds, driving down prices and thereby accomplishing the rate hike with no Fed intervention at all?
- Diebold, Francis X (Univ of Penn Dept of Economics); Li, Canlin (UC Riverside Anderson). 2006. “Forecasting the Term Structure of Government Bond Yields” .

- Key takeaway: Yield-curve forecasting can be reduced to three key parameters: level, slope, and curvature.
- Topics: Yield-curve analysis.
- What this will help teach you: Even the most compelling contemporaneous regression teaches you nothing about how to make money in the real world where you need to decide your position before you can trade into it.
- Investment strategies that apply this: FIRC (fixed income, rates, and credit).
- Questions you should be able to answer after reading this:
 - * What (intuitively) is captured by the level, slope, and curvature features of the yield curve?
 - * How can you construct level, slope, and curvature securities? (A: $5 \cdot 2Y + 10Y$, $10Y - 5 \cdot 2Y$, $10Y - 2 \cdot 5Y + 5 \cdot 2Y$.)
- Followup questions:
 - * Are there ways to extend this analysis to other securities whose prices are sensitive to or evolve similarly to changes in the yield curve?