

# 0106\_R19\_C Scheme\_Extc\_IV\_ECC401\_EMIV\_QP

University of Mumbai

Examination 2021 under cluster 05 (Lead College: APSIT)

Examinations Commencing from 1st June 2021 to 10th June 2021

Program: BE Electronics and Telecommunication Engineering

Curriculum Scheme: Rev 2019 'C' Scheme

Examination: SE Semester IV

Course Code: ECC401 and Course Name: Engineering Mathematics IV

Time: 2 hour

Max. Marks: 80

Your email will be recorded when you submit this form

Not [singhsparsh@kccemsr.edu.in](mailto:singhsparsh@kccemsr.edu.in)? [Switch account](#)

\* Required

If  $x$  is a discrete random variable with the following probability distribution

$x$	1	2	3
$P(x)$	$a$	$2a$	$a$

Find  $P(X \leq 2)$ .

- ☐ 1/4
- ☐ 1/2
- ☒ 3/4
- ☐ 1

Clear selection



---

The following results were obtained from records of age (x) and systolic blood pressure (y) of a group of 10 men:

	x	y
mean	53	142
variance	130	165

Correlation coefficient = 0.8

Estimate the blood pressure of a man whose age is 45?

---

☒ 134.78

☐ 130.56

☐ 129.56

☐ 137.56

Clear selection

---

If X and Y are independent random variables with means 2,3 and variance 1,2 respectively, find the mean and variance of the random variable  $Z = 2X - 5Y$

☒ -11 , 54

☐ 19 , 54

☐ 19 , -8

☐ -11, -8

Clear selection

Name \*

Sparsh Singh

SEAT NO \*

20211EX4071



Evaluate  $\int_C \frac{e^z}{z-1} dz$  where  $C$  where  $c$  is the circle  $|z| = 2$ .

- ☐  $2\pi i$
- ☐  $2\pi e^2$
- ☒  $2\pi e$
- ☐  $\pi e^2$

Clear selection

Branch \*

- ☒ EXTC

CONTACT NO \*

9082213431

If the tangent of the angle made by the line of regression of  $y$  on  $x$  is  $0.6$  and  $\sigma_x = \frac{1}{2}\sigma_y$  Find the correlation coefficient between  $x$  and  $y$ .

- ☐  $-2.5$
- ☐  $0.25$
- ☐  $-0.3$
- ☒  $0.3$

Clear selection



A coefficient of correlation is computed to be -0.95 means that

- ☒ The relationship between the two variables is weak
- ☐ The relationship between the two variables is strong and positive.
- ☐ The relationship between the two variables is strong but negative.
- ☐ The correlation coefficient cannot have this value.

Clear selection

A necessary condition for  $I = \int_{x_1}^{x_2} f(x, y, y', y'') dx$  to be an extremal is that

$$\frac{\partial f}{\partial y} - \frac{d}{dx} \left( \frac{\partial f}{\partial y'} \right) + \frac{d^2}{dx^2} \left( \frac{\partial f}{\partial y''} \right) = 0$$

☒ Option 1

$$\frac{\partial f}{\partial y} - \frac{d}{dx} \left( \frac{\partial f}{\partial y'} \right) = 0$$

☐ Option 2

$$\frac{\partial f}{\partial y} + \frac{d}{dx} \left( \frac{\partial f}{\partial y'} \right) = 0$$

☐ Option 3

$$\frac{\partial f}{\partial y} + \frac{d}{dx} \left( \frac{\partial f}{\partial y'} \right) + \frac{d^2}{dx^2} \left( \frac{\partial f}{\partial y''} \right) = 0$$

☐ Option 4

Clear selection



Find the value of the integral  $\int_0^{1+i} (x^2 - iy) dz$  along the path  $y = x$

- ☒ (5-i)/6
- ☐ (5+i)/6
- ☐ (1+5i)/6
- ☐ (1-5i)/6

Clear selection

Find  $E(X)$  if  $X$  has the p.d.f  $f(x) = \begin{cases} \frac{3}{4}(2x - x^2), & 0 \leq x \leq 2 \\ 0, & \text{otherwise} \end{cases}$

- ☐ 3/2
- ☒ 1
- ☐ 2
- ☐ 1/2

Clear selection

Find the residue of  $f(z) = \frac{z^2}{(z+2)(z-1)^2}$  at  $z = -2$

- ☐ 1/9
- ☐ 5/9
- ☐ 1/3
- ☒ 4/9

Clear selection



The extremal of the functional  $I = \int_a^b (16y^2 - y'^2 + x^2) dx$  is

$$y = c_1 \cos 2x + c_2 \sin 2x$$

☐ Option 1

$$y = c_1 e^{2x} + c_2 e^{-2x}$$

☐ Option 2

$$y = c_1 e^{2x} + c_2 e^{-2x} + c_3 \cos 2x + c_4 \sin 2x$$

☒ Option 3

$$y = c_1 e^x + c_2 e^{-x} + c_3 \cos x + c_4 \sin x$$

☐ Option 4

Clear selection

If  $u = (3, 1, 4, -2)$   $v = (2, 2, 0, 1)$  then find  $\langle u, v \rangle$  and  $\|u\|, \|v\|$

☐ -6,  $\sqrt{30}$ ,  $\sqrt{10}$

☐ 5,  $\sqrt{2}$ ,  $\sqrt{6}$

☐ 5,  $\sqrt{30}$ , 3

☒ 6,  $\sqrt{30}$ , 3

Clear selection



Write down the matrix of the quadratic form

$$x_1^2 + 2x_2^2 - 7x_3^2 - 4x_1x_2 + 6x_2x_3 + 8x_3x_1$$

$$\begin{bmatrix} 1 & -2 & 4 \\ -2 & 2 & 3 \\ 4 & 3 & -7 \end{bmatrix}$$

☐ Option 1

$$\begin{bmatrix} 1 & -4 & 8 \\ -4 & 2 & 6 \\ 8 & 6 & -7 \end{bmatrix}$$

☒ Option 2

$$\begin{bmatrix} 1 & 2 & 4 \\ 2 & 2 & 3 \\ 4 & 3 & -7 \end{bmatrix}$$

☐ Option 3

$$\begin{bmatrix} 1 & 4 & 8 \\ 4 & 2 & 6 \\ 8 & 6 & 7 \end{bmatrix}$$

☐ Option 4

Clear selection

Identify the type of singularity of the function  $f(z) = \frac{\sinh z}{z^7}$

- ☐  $z = 0$  is a pole of order 7 for the given function
- ☒  $z = 0$  is a pole of order 6 for the given function
- ☐  $z = 0$  is an essential singularity
- ☐  $z = 0$  is a pole of order 3 for the given function

Clear selection



Suppose the number of accidents occurring weekly on a particular stretch of a highway follow a Poisson distribution with mean 3 .Calculate the probability that there is at least one accident this week.

- ☐ 0.6 347
- ☒ 0.9502
- ☐ 0.7275
- ☐ 0.8002

Clear selection

Find the rank, signature, index of the transformed quadratic form

$$3y_1^2 + \frac{2}{3}y_2^2 - \frac{39}{2}y_3^2.$$

- ☐ rank = 3, signature =2, index =1
- ☒ rank = 3, signature =1, index =2.
- ☐ rank = 2, signature =3, index =1.
- ☐ rank = 2, signatur e=1, index =3.

Clear selection





The functional  $I = \int_a^b (y'^2 + 12xy) dx$  has the following extremal with  $c_1$  and  $c_2$  as arbitrary constants.

$$c_1 x^3 + c_2 x$$

☒ Option 1

$$x^2 + c_1 x + c_2$$

☐ Option 2

$$c_1 x + c_2$$

☐ Option 3

$$x^3 + c_1 x + c_2$$

☐ Option 4

Clear selection



Determine which of the following are subspaces of  $R^3$

$$W_1 = \{(a, 0, b), a, b \in R\}$$

$$W_2 = \{(a, b, 1), a, b \in R\}$$

$W_1$  and  $W_2$  are the subspaces of  $R^3$

☐ Option 1

$W_1$  and  $W_2$  are not the subspaces of  $R^3$

☐ Option 2

$W_1$  is a subapace of  $R^3$  but  $W_2$  is not a subspace of  $R^3$

☐ Option 3

$W_1$  is not a subapace of  $R^3$  but  $W_2$  is a subspace of  $R^3$

☒ Option 4

Clear selection

SUBJECT \*

☒ EM IV



Evaluate  $\int_c \frac{7z-1}{(z-3)(z+5)} dz$ , where  $c$  is the circle  $|z|=1$ .

- ☐  $2\pi i$
- ☒  $0$
- ☐  $6\pi i$
- ☐  $\pi i$

Clear selection

Find the vector orthogonal to  $(2,1,-2)$  and  $(1,2,2)$

- ☐  $(1,-2,1)$
- ☒  $(2,-2,1)$
- ☐  $(1,-1,1)$
- ☐  $(2,2,-1)$

Clear selection

Submit

Never submit passwords through Google Forms.

This form was created inside of K.C.College of Engineering And Management Studies And Research. [Report Abuse](#)

Google Forms

