

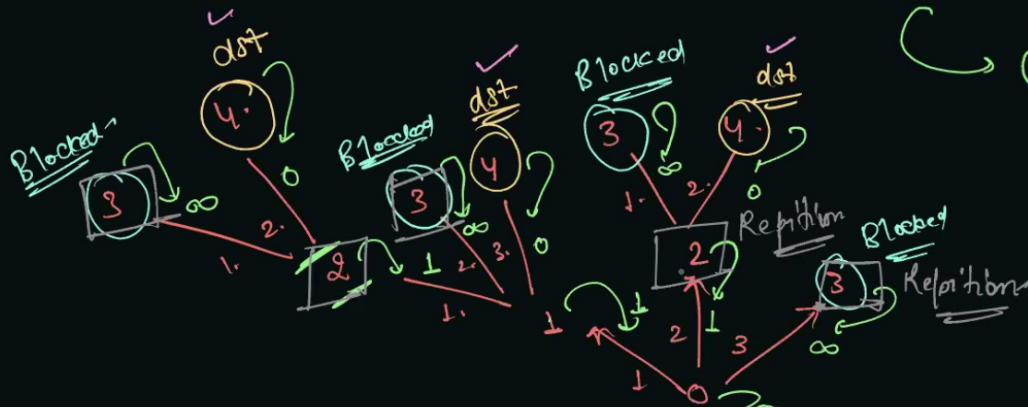
stair	0	1	2	3	4
jumps →	3	3	2	0	1

C 0 jump-

path from src + dst →

③ → 1 1 2  
 ⑤ → 1 3  
 ⑥ → 2 2

} main jumps  
in these  
path,  
② is main  
jumps



```

public static int cbmm_mem(int[] arr, int n, int i, int[] qb) {

    if (i == n) {
        // System.out.println(i);
        return 0;
    }
    if (qb[i] != 0) {
        return qb[i];
    }
    int mini = Integer.MAX_VALUE;
    for (int j = 1; j <= arr[i] && i + j <= n; j++) {

        // System.out.println(i + j);
        int rr = cbmm_mem(arr, n, i + j, qb);
        mini = Math.min(rr, mini);
        // System.out.println(mini);
    }

    mini = mini != Integer.MAX_VALUE ? 1 + mini : Integer.MAX_VALUE;

    // store in qb
    qb[i] = mini;
    return mini;
}

```

```

public static int cbmm_rec(int[] arr, int n, int i) {

    if (i == n) {
        // System.out.println(i);
        return 0;
    }
    int mini = Integer.MAX_VALUE;
    for (int j = 1; j <= arr[i] && i + j <= n; j++) {

        // System.out.println(i + j);
        int rr = cbmm_rec(arr, n, i + j);
        mini = Math.min(rr, mini);
        // System.out.println(mini);
    }
    return mini != Integer.MAX_VALUE ? 1 + mini : Integer.MAX_VALUE;
}

```

```

public static int cbmm_tab1(int[] arr, int n, int i, int[] qb) {

    for (i = n; i >= 0; i--) { // small to big problem
        if (i == n) {
            qb[i] = 0;
            continue;
        }

        int mini = Integer.MAX_VALUE;
        for (int j = 1; j <= arr[i] && i + j <= n; j++) {

            int rr = qb[i + j]; // instead of calling cbmm_mem(arr, n, i + j, qb); and removing the part where
            // we try to fetch from qb
            mini = Math.min(rr, mini);
        }

        mini = mini != Integer.MAX_VALUE ? 1 + mini : Integer.MAX_VALUE;

        qb[i] = mini;
    }
    return qb[0];
}

```

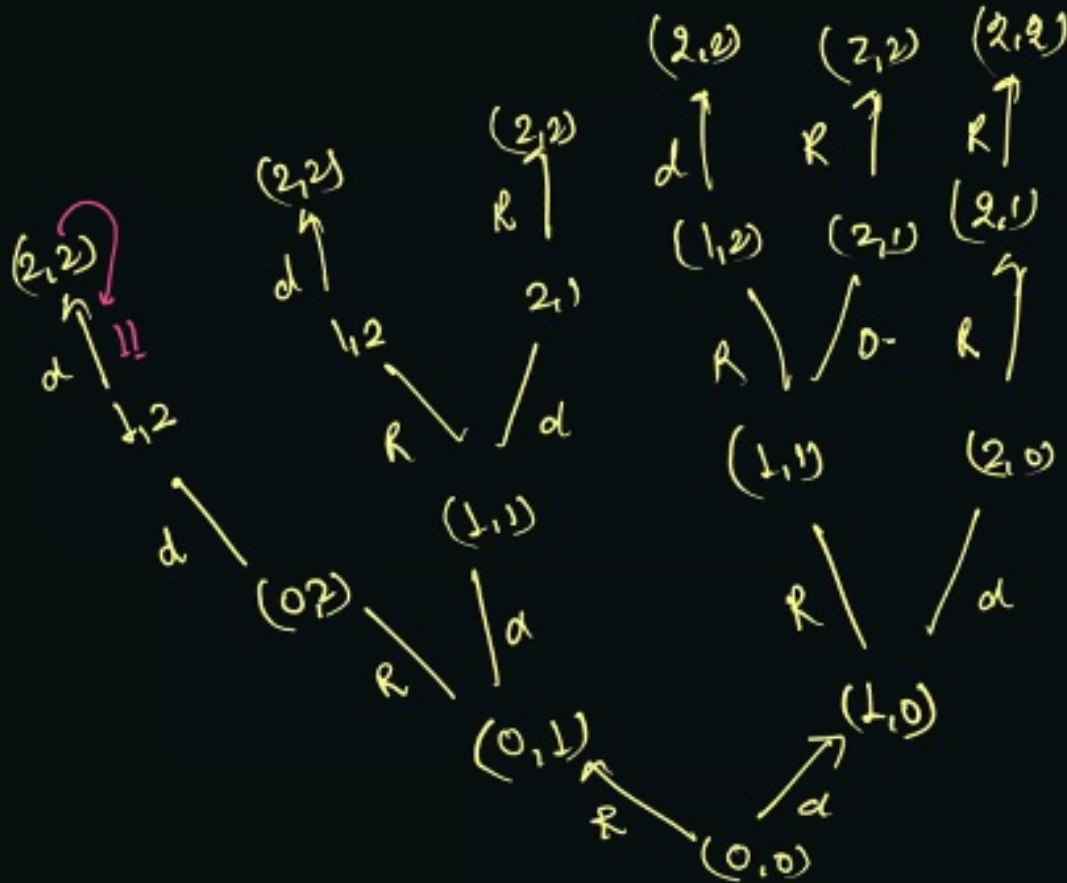
# Min Cost In Maze Traversal

Thursday, 24 June 2021 6:12 PM

jumps allowed  $\rightarrow$  right

$(x, y) \rightarrow (x, y+1)$  down  
 $\downarrow$   
 $(x, y)$

dst  
intermediate  
src



Maze with cost  $\rightarrow$

src  $\rightarrow$  (0,0)

dst  $\rightarrow$  (3,3)

Condition is  $\rightarrow$  Minimize the cost

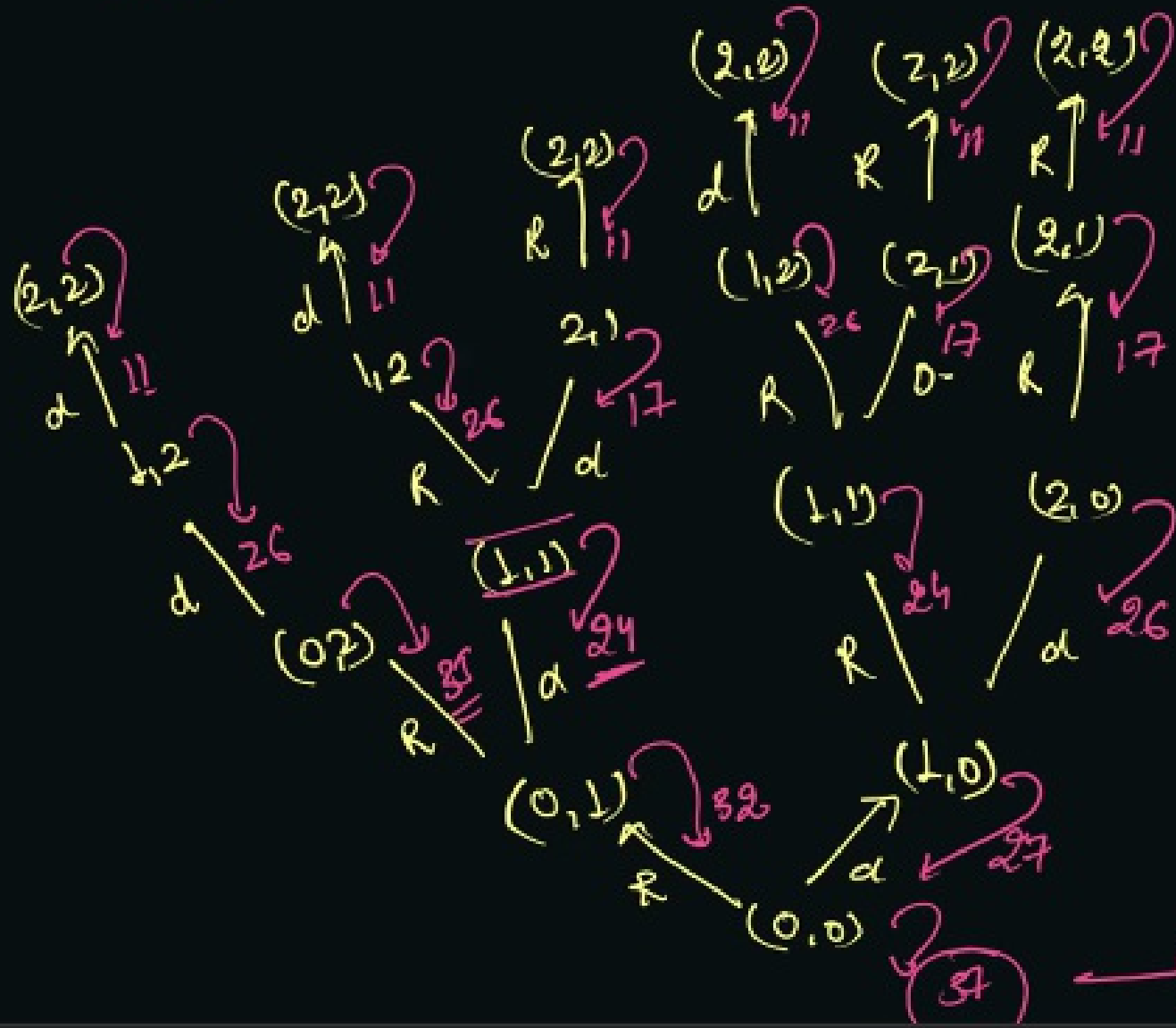
	0	1	2	3
0	10	8	9	8
1	3	7	15	6
2	9	6	11	10
3	7	12	6	1

path  $\rightarrow$

	Cost
RRDD	53
RDRD	51
RDDR	42
DRRD	46
DRDR	37
DDRR	33

Min cost path  $\rightarrow$  DDRR

$(x, y)$



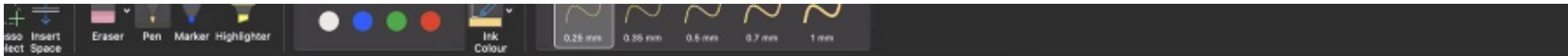
dot  $\Rightarrow (2,2)$

Condition is  
 $\rightarrow$  Minimize the cost

path

$\leftarrow$  min cost result





Cost  
(2,2) →  
0/11

(1,2) →  
0/26

(0,2) →  
R/35 D/24

(0,1) →  
R/32 D/27

(0,0) →  
37 final Result.

*optimized*  
(2,2) →  
R/11

(1,2) →  
L/26 D/17

(1,1) →  
R/21 D/26

dp →

	0	1	2	3
0		32	35	/
1	27	24	26	/
2	26	17	11	/
3	/	/	/	/

*optimized*  
(2,1) →  
R/17

maze →

	0	1	2	3
0	10	8	9	8
1	3	7	15	5
2	9	6	11	10
3	7	12	6	1

$$dp[r][c] = \text{minCost} + \text{maze}[r][c]$$

```

public static int minCostPath_memo(int[][] maze, int x, int y, int[][] dp) {
    if(x == maze.length - 1 && y == maze[0].length - 1) {
        return dp[x][y] = maze[x][y];
    }

    if(dp[x][y] != 0) {
        return dp[x][y];
    }

    int minCost = (int)1e9;
    // right call
    if(y + 1 < maze[0].length) {
        minCost = Math.min(minCost, minCostPath_memo(maze, x, y + 1, dp));
    }
    // down call
    if(x + 1 < maze.length) {
        minCost = Math.min(minCost, minCostPath_memo(maze, x + 1, y, dp));
    }

    return dp[x][y] = minCost + maze[x][y];
}

```

```

public static int recursion(int[][] arr, int x, int y, int n, int m) {
    if (x == n - 1 && y == m - 1) {
        return arr[x][y];
    }
    int h = (int) 1e9;
    int v = (int) 1e9;
    if (x + 1 < n) {
        h = recursion(arr, x + 1, y, n, m);
    }
    if (y + 1 < m) {
        v = recursion(arr, x, y + 1, n, m);
    }

    return arr[x][y] + Math.min(h, v);
}

```

```

public static int memorization(int[][] arr, int x, int y, int n, int m, int[][] qb) {
    if (x == n - 1 && y == m - 1) {
        return arr[x][y];
    }

    if (qb[x][y] != 0) {
        return qb[x][y];
    }
    int min = (int) 1e9;
    if (x + 1 < n) {
        int h = recursion(arr, x + 1, y, n, m);
        min = Math.min(min, h);
    }
    if (y + 1 < m) {
        int v = recursion(arr, x, y + 1, n, m);
        min = Math.min(min, v);
    }

    int res = arr[x][y] + min;
    qb[x][y] = res;
    return res;
}

```

```

public static int tabulation(int[][] arr, int n, int m, int[][] qb) {
    for (int x = n - 1; x >= 0; x--) {
        for (int y = m - 1; y >= 0; y--) {
            if (x == n - 1 && y == m - 1) {
                qb[x][y] = arr[x][y];
                continue;
            }

            int min = (int) 1e9;
            if (x + 1 < n) {
                int h = qb[x + 1][y]; // recursion(arr, x + 1, y, n, m);
                min = Math.min(min, h);
            }
            if (y + 1 < m) {
                int v = qb[x][y + 1]; // recursion(arr, x, y + 1, n, m);
                min = Math.min(min, v);
            }

            int res = arr[x][y] + min;
            qb[x][y] = res;
        }
    }
    return qb[0][0];
}

```

```

public static int minCostPath_tab1(int[][] maze, int x, int y, int[][] dp) {
    for(x = maze.length - 1; x >= 0; x--) {
        for(y = maze[0].length - 1; y >= 0; y--) {
            if(x == maze.length - 1 && y == maze[0].length - 1) {
                //bottom-right corner
                dp[x][y] = maze[x][y];
            } else if(x == maze.length - 1) {
                //last row
                dp[x][y] = maze[x][y] + dp[x][y + 1];
            } else if(y == maze[0].length - 1) {
                //last col
                dp[x][y] = maze[x][y] + dp[x + 1][y];
            } else {
                //middle section
                dp[x][y] = maze[x][y] + Math.min(dp[x][y + 1], dp[x + 1][y]);
            }
        }
    }
    return dp[0][0];
}

```

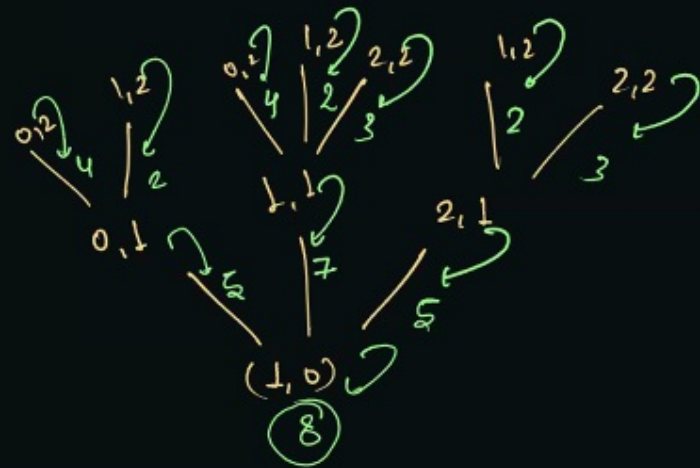
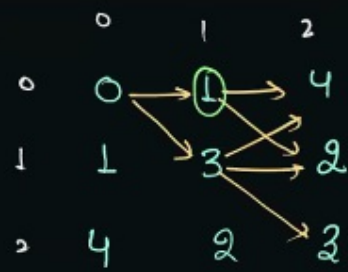
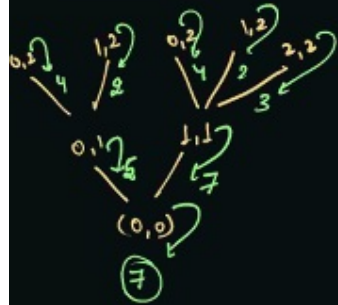
```

public static void minCostPath(int[][] dp, int x, int y, String psf) {
    if(x == dp.length - 1 && y == dp[0].length - 1) {
        System.out.println(psf);
    } else if(x == dp.length - 1) {
        minCostPath(dp, x, y + 1, psf + "R ");
    } else if(y == dp[0].length - 1) {
        minCostPath(dp, x + 1, y, psf + "D ");
    } else {
        if(dp[x][y + 1] == dp[x + 1][y]) {
            // both side
            minCostPath(dp, x + 1, y, psf + "D ");
            minCostPath(dp, x, y + 1, psf + "R ");
        } else if(dp[x][y + 1] < dp[x + 1][y]) {
            // right side
            minCostPath(dp, x, y + 1, psf + "R ");
        } else {
            // down side
            minCostPath(dp, x + 1, y, psf + "D ");
        }
    }
}
}

```

# Goldmine

Thursday, 24 June 2021 6:13 PM

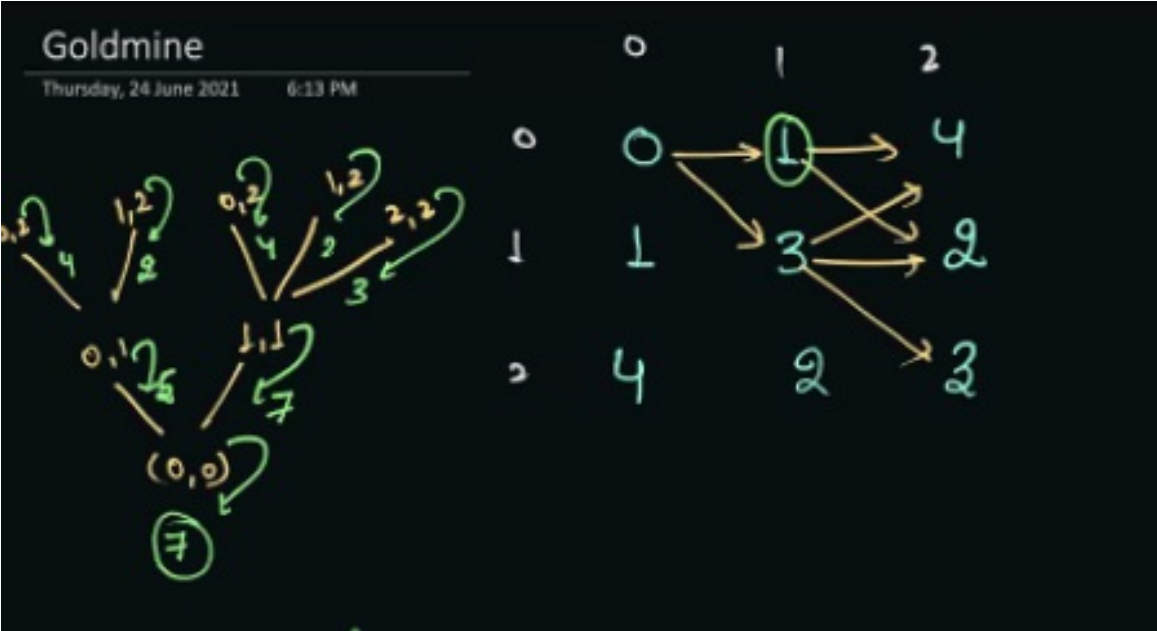


	0	1	2	3	4	5
0	0	1	4	2	8	2
1	4	3	6	5	0	4
2	1	2	4	1	4	6
3	2	0	7	3	2	2
4	3	1	5	9	2	4
5	2	7	0	8	5	1

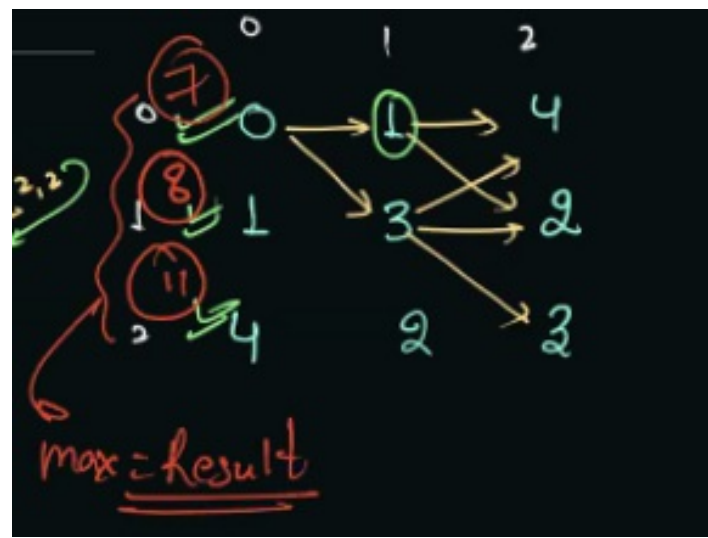
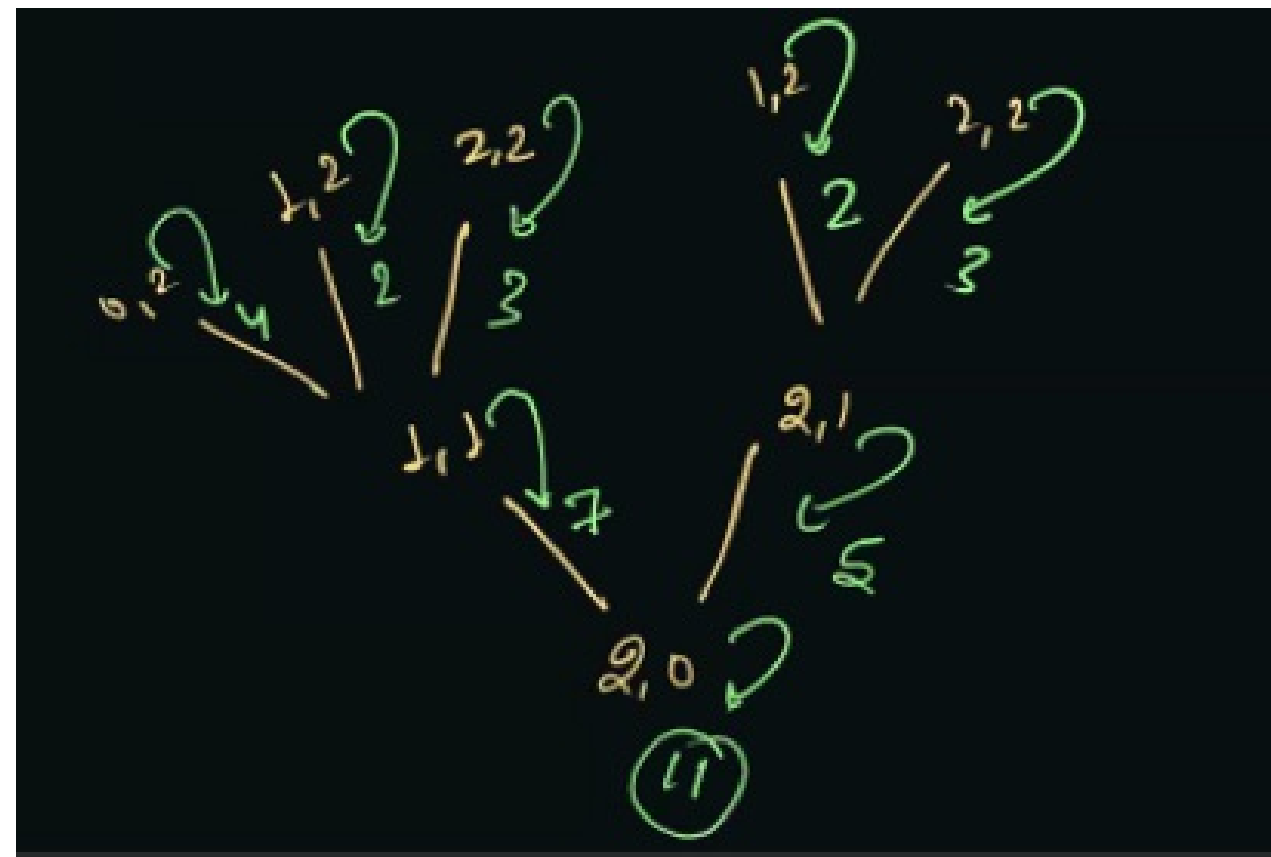
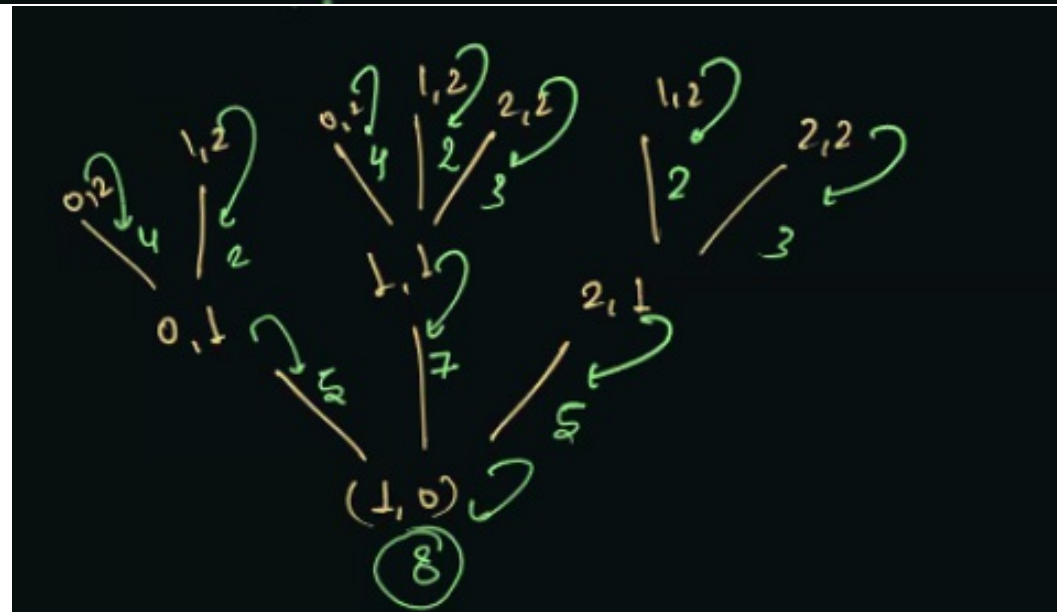


# Goldmine

Thursday, 24 June 2021 6:13 PM



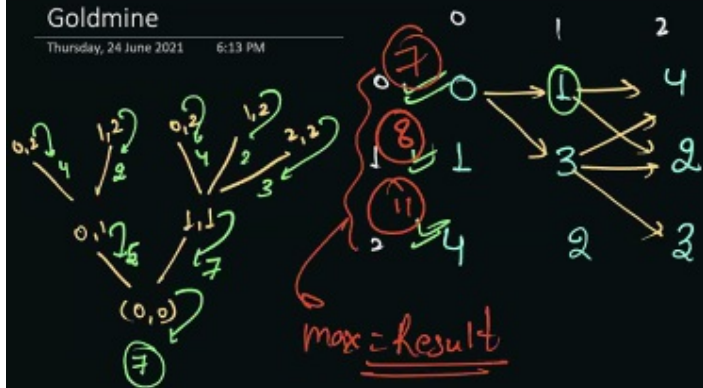
	0	1	2	3	4	5
0	0	1	4	2	8	2
1	4	3	6	5	0	4
2	1	2	4	1	4	6
3	2	0	7	3	2	2
4	3	1	5	9	2	4
5	2	7	0	8	5	1



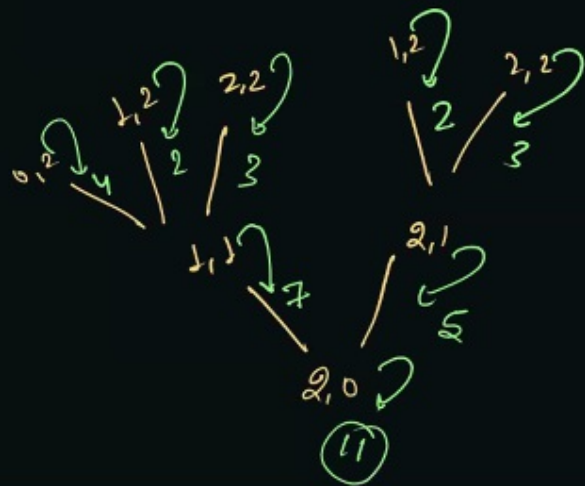
max = result

# Goldmine

Thursday, 24 June 2021 6:13 PM

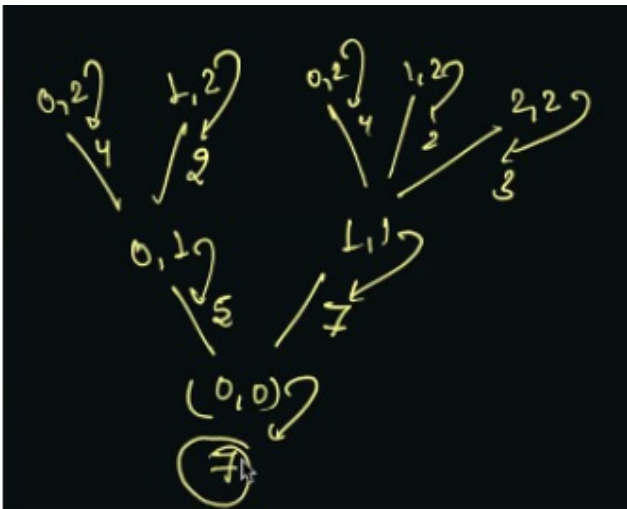


	0	1	2	3	4	5
0	0	1	4	2	8	2
1	4	3	6	5	0	4
2	1	2	4	1	4	6
3	2	0	7	3	2	2
4	3	1	5	9	2	4
5	2	7	0	8	5	1



```
public static int goldmineHelper_rec(int[][] mine, int x, int y) {  
    if(y == mine[0].length - 1) {  
        return mine[x][y];  
    }  
}
```

```
int cost = 0;  
// top-right  
if(x - 1 >= 0) {  
    cost = Math.max(cost, goldmineHelper_rec(mine, x - 1, y + 1));  
}  
// right -> no need for check of y  
cost = Math.max(cost, goldmineHelper_rec(mine, x, y + 1));  
// down-right  
if(x + 1 < mine.length) {  
    cost = Math.max(cost, goldmineHelper_rec(mine, x + 1, y + 1));  
}  
return cost + mine[x][y];
```



dp →

	0	1	2
0	7	5	4
1	0	7	2
2	0	0	3

	0	1	2
0	0	1	4
1	1	3	2
2	4	2	3

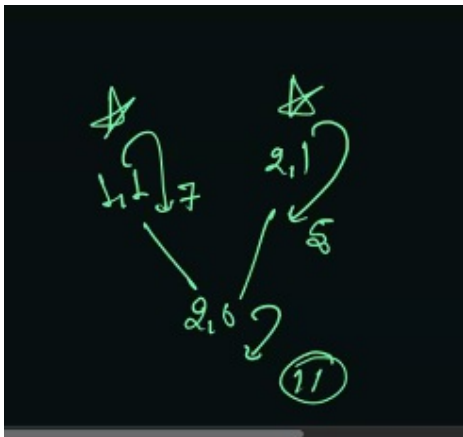


dp →

	0	1	2
0	7	5	4
1	8	7	2
2	0	5	3

Memoisation

Final Result =  $\max(7, 8, 11) = 11$  Ans



dp →

	0	1	2
0	7	5	4
1	8	7	2
2	11	5	3



# Goldmine-Tabulation →

outerloop → column  
innerloop → for row

max from 0th Row is final result

dp →	0	1	2	3	4	5
0	26	24	21	14	12	2
1	31	26	23	17	6	4
2	28	27	21	11	10	6
3	29	25	22	13	8	2
4	33	26	23	18	6	4
5	32	30	18	17	9	1

Final Result →

mine

0	1	4	2	8	2
4	3	6	5	0	4
1	2	4	1	4	6
2	0	7	3	2	2
3	1	5	9	2	4
2	7	0	8	5	1

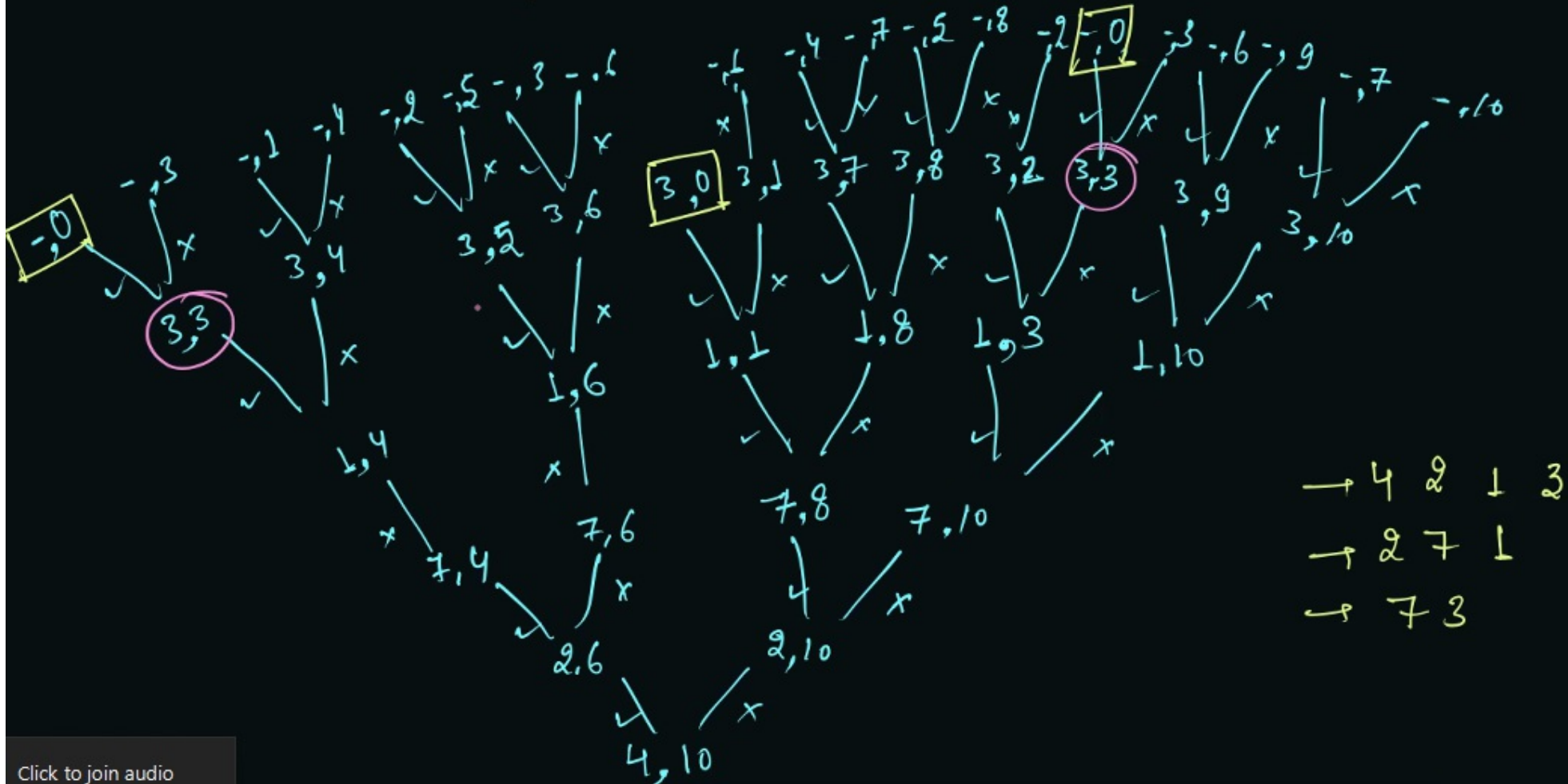
```
public static int goldmine_tab1(int[][] mine, int x, int y, int[][] dp) {
    int res = 0;
    for(y = mine[0].length - 1; y >= 0; y--) {
        for(x = 0; x < mine.length; x++) {
            if(y == mine[0].length - 1) {
                dp[x][y] = mine[x][y];
            } else if(x == 0) {
                dp[x][y] = Math.max(dp[x][y + 1], dp[x + 1][y + 1]) + mine[x][y];
            } else if(x == mine.length - 1) {
                dp[x][y] = Math.max(dp[x][y + 1], dp[x - 1][y + 1]) + mine[x][y];
            } else {
                dp[x][y] = Math.max(dp[x - 1][y + 1], Math.max(dp[x][y + 1], dp[x + 1][y + 1])) + mine[x][y];
            }
            res = Math.max(res, dp[x][y]);
        }
    }
    return res;
}
```

# Target Sum Subset - DP

Saturday, 26 June 2021 6:54 PM

Given  $\rightarrow \{4, 2, 7, 1, 3\}$   
 target = 10  
 True / False

$\square \rightarrow$  Base case  
 $\square \rightarrow$  Repetition



```
// ~~~~~Target Sum Subset~~~~~
public static boolean targetSumSubset_rec(int[] arr, int indx, int target) {
    if(target == 0) return true;
    if(indx == arr.length) {
        return false;
    }
    boolean res = false;
    // yes call
    if(target - arr[indx] >= 0) {
        res = targetSumSubset_rec(arr, indx + 1, target - arr[indx]);
    }
    // no call
    res = res || targetSumSubset_rec(arr, indx + 1, target);
    return res;
}
```

n=5  
4 2 7 1 3  
tar= 10

true 4213  
true 271  
true 73

```
// level option
public static void recursion1(int[] arr, int idx, int tar, String psf) {

    if (tar == 0) {
        System.out.println(true + " " + psf);
    }
    for (int i = idx; i < arr.length; i++) {
        recursion1(arr, i + 1, tar - arr[i], psf + arr[i]);
    }
}
```

```
public static boolean targetSumSubset_memo(int[] arr, int indx, int target, Boolean[][] dp) {
    if(target == 0) return dp[indx][target] = true;
    if(indx == arr.length) {
        return dp[indx][target] = false;
    }

    if(dp[indx][target] != null) {
        return dp[indx][target];
    }

    boolean res = false;
    // yes call
    if(target - arr[indx] >= 0) {
        res = targetSumSubset_rec(arr, indx + 1, target - arr[indx]);
    }
    // no call
    res = res || targetSumSubset_rec(arr, indx + 1, target);
    return dp[indx][target] = res;
}
```



target sum subset →

{ 4, 2, 7, 1, 3 } , target = 10

No call

yes call

$$dp[r][c] = dp[r-1][c] \parallel dp[r-1][c-val];$$

outer loop: target  
inner loop: array

Meaning of cell

$dp[i][j]$  can we make j target using elements from 0 to i

array → target

0 → -  
1 → 4  
2 → 2  
3 → 7  
4 → 1  
5 → 3

	0	1	2	3	4	5	6	7	8	9	10
0	T	F	F	F	F	F	F	F	F	F	F
1	T	F	F	F	T	F	F	F	F	F	F
2	T	F	T	F	T	F	T	F	F	F	F
3	T	F	T	F	T	F	T	T	F	T	F
4	T	T	T	T	T	T	T	T	T	T	T
5	T	T	T	T	T	T	T	T	T	T	T

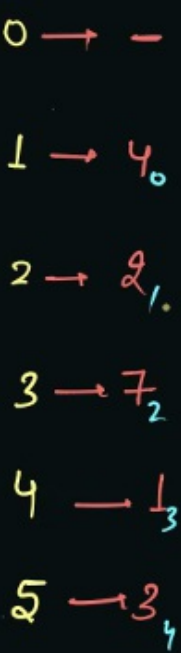
$$result = dp[5][10]$$



```
public static boolean targetSumSubset_memo(int[] arr, int indx, int target, Boolean[][] dp) {  
    if(target == 0) return dp[indx][target] == true;  
    if(indx == arr.length) {  
        return dp[indx][target] == false;  
    }  
  
    if(dp[indx][target] != null) {  
        return dp[indx][target];  
    }  
  
    boolean res = false;  
    // yes call  
    if(target - arr[indx] >= 0) {  
        res = targetSumSubset_rec(arr, indx + 1, target - arr[indx]);  
    }  
    // no call  
    res = res || targetSumSubset_rec(arr, indx + 1, target);  
    return dp[indx][target] = res;  
}
```

target = 16

0 1 2 3 4 5 6 7 8 9 10



```
public static boolean targetSumSubset_memo(int[] arr, int indx, int target) {
    if(target == 0) return dp[indx][target] == true;
    if(indx == arr.length) {
        return dp[indx][target] == false;
    }

    if(dp[indx][target] != null) {
        return dp[indx][target];
    }

    boolean res = false;
    // yes call
    if(target - arr[indx] >= 0) {
        res = targetSumSubset_rec(arr, indx - 1, target - arr[indx]);
    }
    // no call
    res = res || targetSumSubset_rec(arr, indx + 1, target);
    return dp[indx][target] = res;
}
```

arr, n-1, target

arr, 4, 6

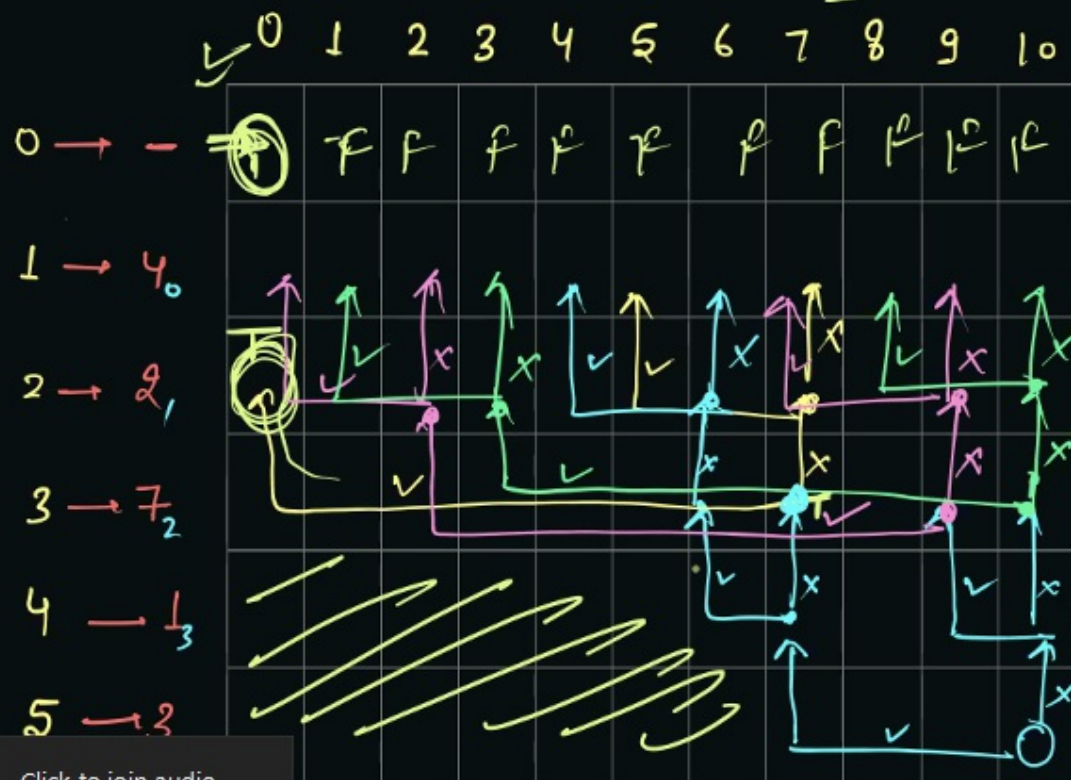
0 to i

result = dp [5][10] result

target = 10

target = 20

Memorisation



```
public static boolean targetSumSubset_memo(int[] arr, int indx, int target,
    if(target == 0) return dp[indx][target] = true;
    if(indx == arr.length) {
        return dp[indx][target] = false;
    }

    if(dp[indx][target] != null) {
        return dp[indx][target];
    }

    boolean res = false;
    // yes call
    if(target - arr[indx] >= 0) {
        res = targetSumSubset_rec(arr, indx + 1, target - arr[indx]);
    }
    // no call
    res = res || targetSumSubset_rec(arr, indx + 1, target);
    return dp[indx][target] = res;
}
```

Tabulation

Memorisation

Better

```

public static boolean targetSumSubset_tab1(int[] arr, int target) {
    boolean[][] dp = new boolean[arr.length + 1][target + 1];

    for(int indx = 0; indx < dp.length; indx++) {
        for(int targ = 0; targ < dp[0].length; targ++) {
            if(targ == 0) {
                dp[indx][targ] = true;
            } else if(indx == 0) {
                dp[indx][targ] = false;
            } else {
                int val = arr[indx - 1];
                if(targ < val) {
                    // only no call
                    dp[indx][targ] = dp[indx - 1][targ];
                } else {
                    // no call OR() yes call
                    dp[indx][targ] = dp[indx - 1][targ] || dp[indx - 1][targ - val];
                }
            }
        }
    }

    return dp[dp.length - 1][dp[0].length - 1];
}

```



## mem to tab

```
public static boolean targetSumSubset_tab2(int[] arr, int target) {
    boolean[][] dp = new boolean[arr.length + 1][target + 1];
    for(int indx = arr.length; indx >= 0; indx--) {
        for(int targ = 0; targ <= target; targ++) {
            if(targ == 0) {
                dp[indx][targ] = true;
                continue;
            }

            if(indx == arr.length) {
                dp[indx][targ] = false;
                continue;
            }

            boolean res = false;
            // yes call
            if(targ - arr[indx] >= 0) {
                res = dp[indx + 1][targ - arr[indx]]; // targetSumSubset_rec(arr, indx + 1, target - arr[indx])
            }
            // no call
            res = res || dp[indx + 1][targ]; //targetSumSubset_rec(arr, indx + 1, target);
            dp[indx][targ] = res;
        }
    }
    return dp[0][target];
}
```