

## Approach.

- ① Recursion
- ② Memorization
- ③ Tabulation



to get better understanding and grasp of problem

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## Partition into subset.

$n = \text{no. of element}$

$k = \text{no. of subset}$

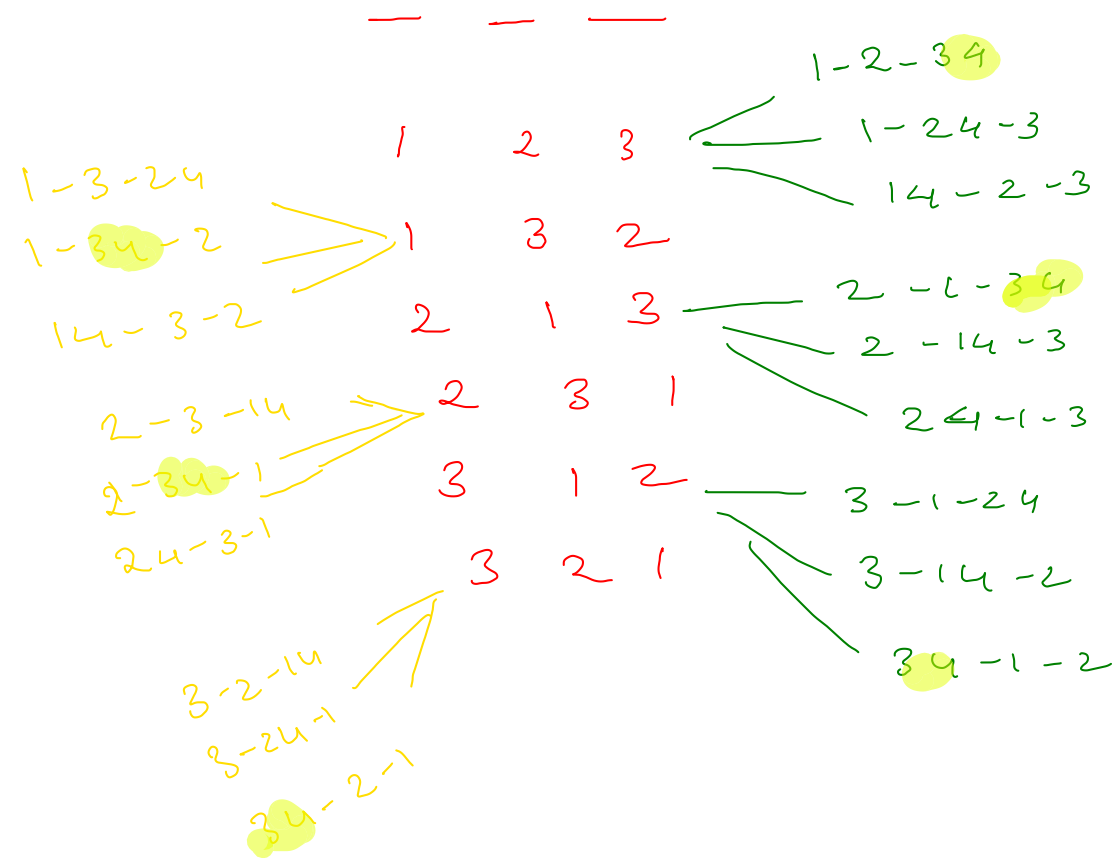
Print - no. of ways in which elements can be partitioned in  $k$  non empty subset

$n = 4$  elements

$(1, 2, 3, 4)$

$k = 3$

— — —                      1 2



Total permutation

1 2 3 = 6 permutation.

with each 2 can put  
left element in 4 sets.

∴  $6 \times 3 = 18$  permutation.

we need combinations



n k

4 - 3

3 - 3

3 - 4

n < k

n = k

n > k

1 way

0 way

1 2 3 (empty)

1 - 2 3 - 4

1 3 - 2 - 4

1 2 - 3 - 4

$n \neq k = 7, 4, 7, 3$  or  $5, 7, 3$

1 2 3 4 5

How to come up with solution

1 2 3 4 5

                                  
↑  
space.

only 3 elements you can  
give space.

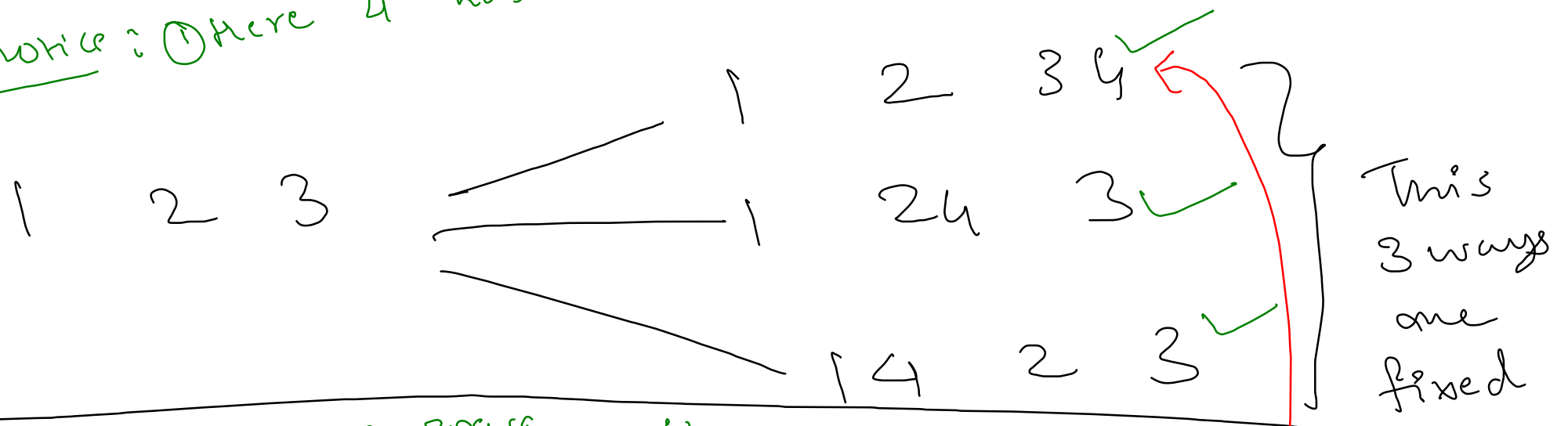
remaining  $(5-3) = 2$  element  
need to share space.

Let say if I put 1, 2, 3 occupies space

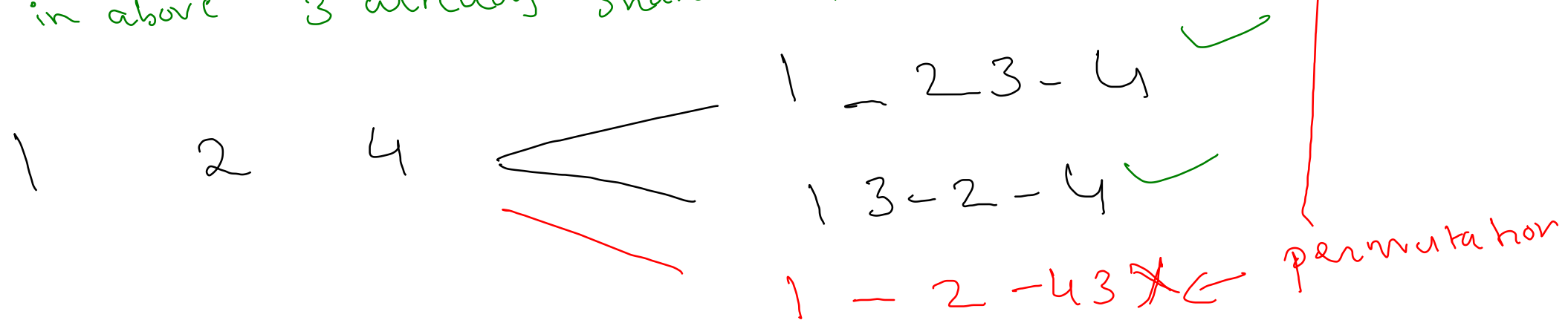
1    2    3

other 2 element <sup>(4,5)</sup> need  
to be shared with 1, 2, 3

$\underline{1} \quad \underline{2} \quad \underline{3}$   
points to notice: ① Here 4 has shared space with 1, 2, 3



② 3 need to share space with 1 & 2 & 3  
 in above 3 already shared space with 4



② 1 4 3  
 Here 2 has not slept with

③ Here, 2 need to share space with 1

total 6 ways

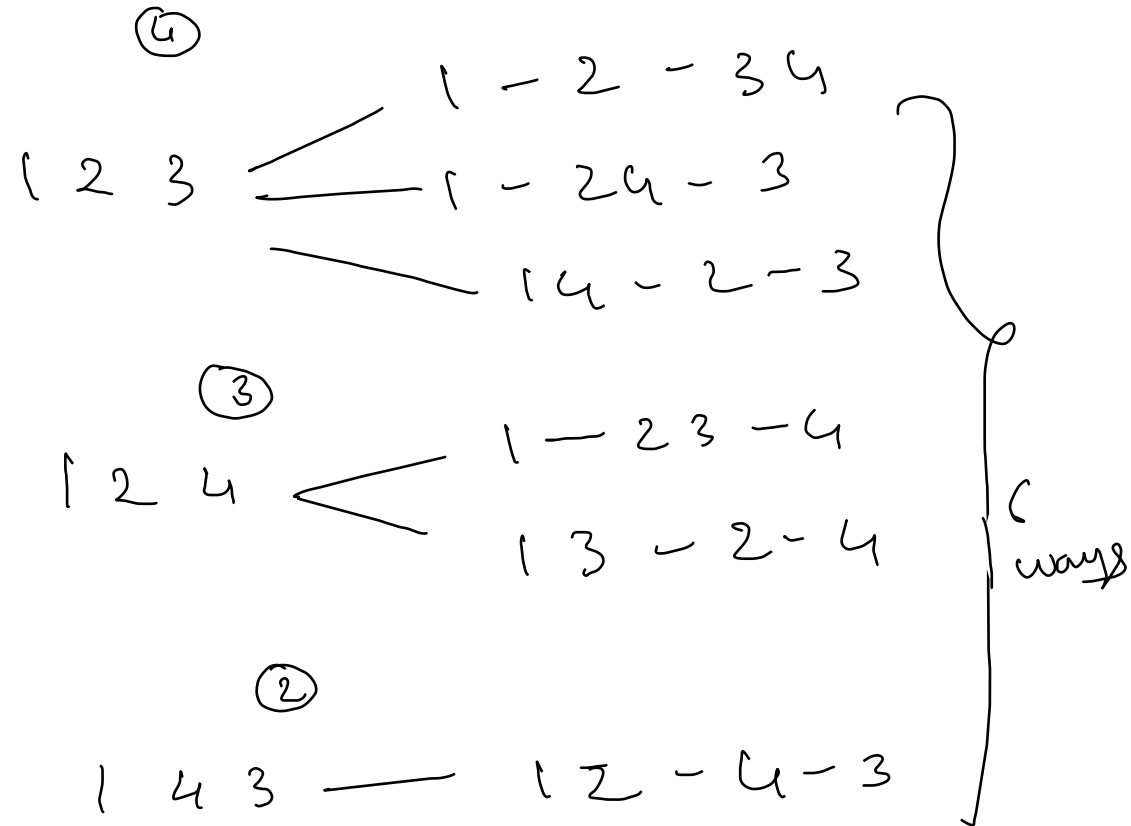
when

$n = 4$

$k = 3$

Try to divide problem in  
subproblem.

How?



Analogy → 4 log he & 3 ghar he.

Sub problem can be

- 3 log 3 ghar
- 3 log - 2 ghar
- 3 log - 1 ghar
- 3 log - 0 ghar

$$n = 4$$

$$k = 3$$

Looking at tree, assumptions.

(3,3) - mujhe 3 ka subset dega. from 3 element  
aur usme mujhe 1<sup>last</sup> element ko har ek  
k sath share karna padega.

(3,2) - mujhe 2 ka subset dega. from 3 elements  
aur jo last element rahega use  
append karke 3 ka subset bana dunga.

(3,1) - mujhe 1 ka subset dega from 3 elements  
means 1 2 3 in 1 set  
and last element ko 1 set  
me daale aur 1 empty set  
bachega

How?

$$\frac{123}{4}$$

So we will not consider 3,1 as  
option in Euler.

subproblems

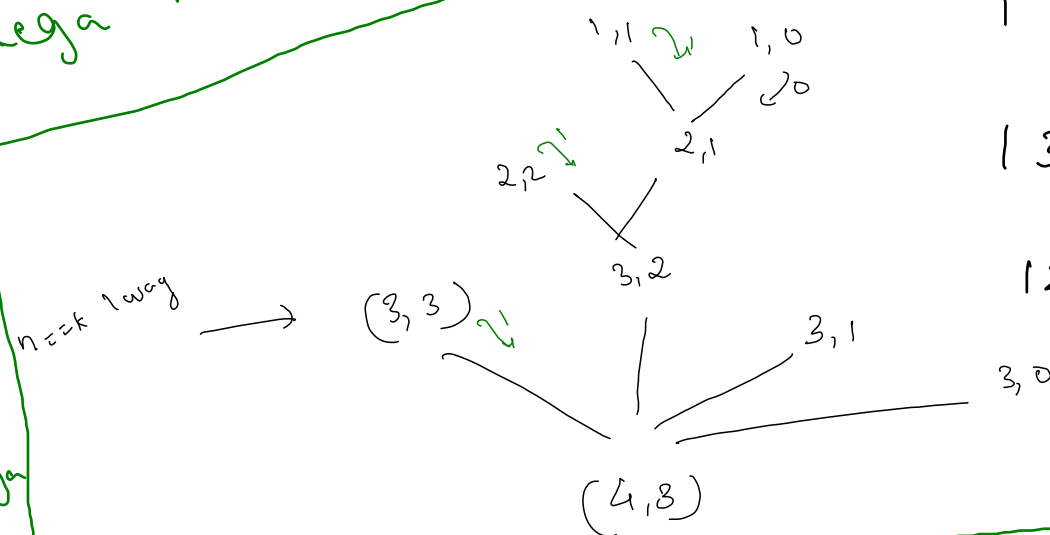
3 log 3 ghar  
3 log 2 ghar  
3 log 1 ghar  
2 log 0 ghar

3, 2

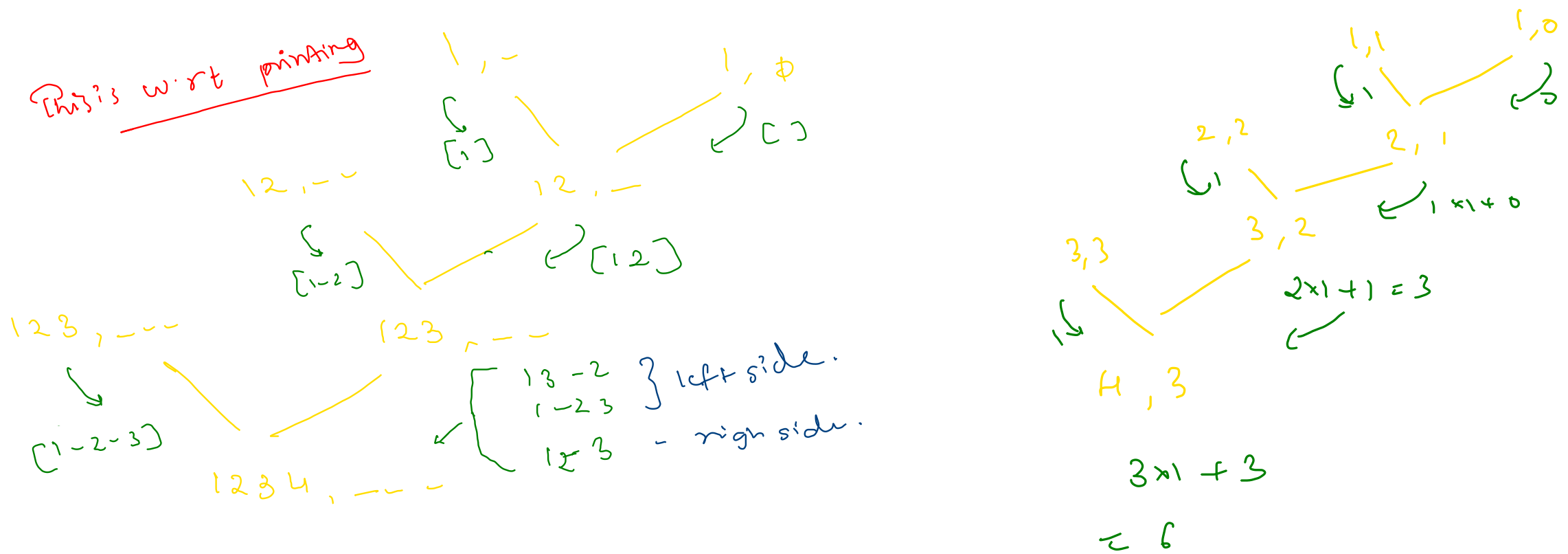
1 - 23

13 - 2

12 - 3



This is w.r.t printing



on left side, I will iterate  $k$  with each subset.

so 1-2-34, 1-24-3, 14-2-3

from right side, I get 2 ka subset, so I will append 4 on each ans

13-2-4, 1-23-4, 12-3-4

$$f(n, k) = k \times f(n-1, k) + f(n-1, k-1)$$

```
// ~~~~~Partition into K Subset~~~~~
public static long partitionKSubset(int n, int k) {
    long[][] dp = new long[n + 1][k + 1];

    for(int i = 0; i <= n; i++) {
        for(int j = 0; j <= i && j <= k; j++) {
            if(j == 0) {
                dp[i][j] = 0;
            } else if(i == j) {
                dp[i][j] = 1;
            } else {
                dp[i][j] = dp[i - 1][j - 1] + j * dp[i - 1][j];
            }
        }
    }

    return dp[n][k];
}
```

$n \geq k$  solve  
 $n \geq k$  return  
 $n < k$  return 0

$$n = 4$$
$$k = 3$$

→  $k$  space

$n \backslash k$	0	1	2	3
0	0	0	0	0
1	0	1	0	0
2	0	1	1	0
3	0	1	$1 \times 2 + 1$ 3	1
4	0	1	$3 \times 2 + 1$ 7	$1 \times 3 + 3$ 6

log

