

## LU SIMPLE

```
[[ 4 1 1 0 1]
 [-1 -3 1 1 0]
 [ 2 1 5 -1 -1]
 [-1 -1 -1 4 0]
 [ 0 2 -1 1 4]]
```

---

```
[[ 4 1 1 0 1]
 [ 0 -2 1 1 0]
 [ 0 0 4 -1 -1]
 [ 0 0 0 4 0]
 [ 0 2 -1 1 4]]
```

```
[[ 1.  0.  0.  0.  0. ]
 [-0.25 1.  0.  0.  0. ]
 [ 0.5  0.  1.  0.  0. ]
 [-0.25 0.  0.  1.  0. ]
 [ 0.  0.  0.  0.  1. ]]
```

---

```
[[ 4 1 1 0 1]
 [ 0 -2 1 1 0]
 [ 0 0 4 -1 -1]
 [ 0 0 0 4 0]
 [ 0 0 0 2 4]]
```

```
[[ 1.  0.  0.  0.  0. ]
 [-0.25 1.  0.  0.  0. ]
 [ 0.5 -0.  1.  0.  0. ]
 [-0.25 -0.  0.  1.  0. ]
 [ 0. -1.  0.  0.  1. ]]
```

---

```
[[ 4 1 1 0 1]
 [ 0 -2 1 1 0]
 [ 0 0 4 -1 -1]
 [ 0 0 0 4 0]
 [ 0 0 0 2 4]]
```

```
[[ 1.  0.  0.  0.  0. ]
 [-0.25 1.  0.  0.  0. ]
 [ 0.5 -0.  1.  0.  0. ]
 [-0.25 -0.  0.  1.  0. ]
 [ 0. -1.  0.  0.  1. ]]
```

---

```
[[ 4 1 1 0 1]
 [ 0 -2 1 1 0]
 [ 0 0 4 -1 -1]
 [ 0 0 0 4 0]
 [ 0 0 0 0 4]]
```

```
[[ 1.  0.  0.  0.  0. ]
 [-0.25 1.  0.  0.  0. ]
 [ 0.5 -0.  1.  0.  0. ]
 [-0.25 -0.  0.  1.  0. ]
 [ 0. -1.  0.  0.5  1. ]]
```

---

Out[9]:  
array([[ 0.90820312],  
 [-1.8984375 ],  
 [ 1.828125 ],  
 [ 1.875 ],  
 [ 2.4375 ]])

### LU PARTIAL

[[ 4 1 1 0 1]  
 [-1 -3 1 1 0]  
 [ 2 1 5 -1 -1]  
 [-1 -1 -1 4 0]  
 [ 0 2 -1 1 4]]

---

[[ 4 1 1 0 1]  
 [ 0 -2 1 1 0]  
 [ 0 0 4 -1 -1]  
 [ 0 0 0 4 0]  
 [ 0 2 -1 1 4]]  
[[ 1. 0. 0. 0. 0. ]  
 [-0.25 1. 0. 0. 0. ]  
 [ 0.5 0. 1. 0. 0. ]  
 [-0.25 0. 0. 1. 0. ]  
 [ 0. 0. 0. 0. 1. ]]

---

[[ 4 1 1 0 1]  
 [ 0 -2 1 1 0]  
 [ 0 0 4 -1 -1]  
 [ 0 0 0 4 0]  
 [ 0 0 0 2 4]]  
[[ 1. 0. 0. 0. 0. ]  
 [-0.25 1. 0. 0. 0. ]  
 [ 0.5 -0. 1. 0. 0. ]  
 [-0.25 -0. 0. 1. 0. ]  
 [ 0. -1. 0. 0. 1. ]]

---

[[ 4 1 1 0 1]  
 [ 0 -2 1 1 0]  
 [ 0 0 4 -1 -1]  
 [ 0 0 0 4 0]  
 [ 0 0 0 2 4]]  
[[ 1. 0. 0. 0. 0. ]  
 [-0.25 1. 0. 0. 0. ]  
 [ 0.5 -0. 1. 0. 0. ]  
 [-0.25 -0. 0. 1. 0. ]  
 [ 0. -1. 0. 0. 1. ]]

---

[[ 4 1 1 0 1]  
 [ 0 -2 1 1 0]

```
[ 0 0 4 -1 -1]
[ 0 0 0 4 0]
[ 0 0 0 0 4]]
[[ 1.  0.  0.  0.  0. ]
[-0.25 1.  0.  0.  0. ]
[ 0.5 -0.  1.  0.  0. ]
[-0.25 -0.  0.  1.  0. ]
[ 0. -1.  0.  0.5  1. ]]
```

-----

Out[10]:

```
array([[ 0.90820312],
       [-1.8984375 ],
       [ 1.828125  ],
       [ 1.875    ],
       [ 2.4375   ]])
```

### CROUT

```
[[ 4.      0.      0.      0.      ]
 [ 1.     15.75     0.      0.      ]
 [ 0.     -1.3    -3.75238095  0.      ]
 [14.      8.5    -3.61904762 13.94923858]]
[[ 1.     -0.25     0.      0.75     ]
 [ 0.      1.      0.19047619 0.46031746]
 [ 0.      0.      1.     -0.45262267]
 [ 0.      0.      0.      1.      ]]
```

Out[17]:

```
array([[ 0.52510917],
       [ 0.25545852],
       [-0.41048035],
       [-0.28165939]])
```

### DOOLITTLE

```
[[ 1.      0.      0.      0.      ]
 [ 0.25     1.      0.      0.      ]
 [ 0.     -0.08253968  1.      0.      ]
 [ 3.5      0.53968254 0.96446701  1.      ]]
[[ 4.     -1.      0.      3.      ]
 [ 0.     15.75     3.      7.25     ]
 [ 0.      0.     -3.75238095 1.6984127 ]
 [ 0.      0.      0.     13.94923858]]
```

Out[18]:

```
array([[ 0.52510917],
       [ 0.25545852],
       [-0.41048035],
       [-0.28165939]])
```

### CHOLESKY

```
(array([[ 2.      ,  0.      ,  0.      ,  0.      ],
```

```

[ 0.5      , 3.96862697, 0.      , 0.      ],
[ 0.      , -0.32756921,      nan, 0.      ],
[ 7.      , 2.14179868,      nan,      nan]],
array([[ 2.      , -0.5      , 0.      , 1.5      ],
[ 0.      , 3.96862697, 0.75592895, 1.82682829],
[ 0.      , 0.      ,      nan,      nan],
[ 0.      , 0.      , 0.      ,      nan]]))

```

**JACOBI**

```

[[0.]
[0.]
[0.]
[0.]]
[[ 0.25 ]
[ 0.06451613]
[-0.25 ]
[ 0.03333333]]
[[ 0.24112903]
[ 0.07956989]
[-0.26180108]
[-0.11075269]]
[[ 0.35295699]
[ 0.15679327]
[-0.3063172 ]
[-0.1099086 ]]
[[ 0.37162977]
[ 0.15775893]
[-0.33118268]
[-0.17793329]]
[[ 0.4228897 ]
[ 0.19647642]
[-0.35020331]
[-0.18846589]]
[[ 0.44046853]
[ 0.20228693]
[-0.36568296]
[-0.22010815]]
[[ 0.46565284]
[ 0.22048036]
[-0.37627299]
[-0.230312  ]]
[[ 0.47785409]
[ 0.22617175]
[-0.38499192]
[-0.24580292]]
[[ 0.49089513]
[ 0.23506742]
[-0.39110162]
[-0.25302666]]

```

[[ 0.49853685]  
[ 0.23913697]  
[-0.39597924]  
[-0.2610024 ]]  
[[ 0.50553605]  
[ 0.24370452]  
[-0.39949518]  
[-0.26557197]]  
[[ 0.51010511]  
[ 0.24629195]  
[-0.40223626]  
[-0.26983392]]  
[[ 0.51394843]  
[ 0.24872742]  
[-0.40424921]  
[-0.27258013]]  
[[ 0.51661695]  
[ 0.25028647]  
[-0.40579595]  
[-0.27491378]]  
[[ 0.51875696]  
[ 0.25161814]  
[-0.40694439]  
[-0.27652205]]  
[[ 0.52029607]  
[ 0.25253243]  
[-0.40781946]  
[-0.27781923]]  
[[ 0.52149753]  
[ 0.25327201]  
[-0.40847333]  
[-0.2787482 ]]  
[[ 0.52237915]  
[ 0.25380052]  
[-0.40896916]  
[-0.27947574]]  
[[ 0.52305693]  
[ 0.25421511]  
[-0.409341 ]  
[-0.2800083 ]]  
[[ 0.52356 ]  
[ 0.25451822]  
[-0.40962219]  
[-0.28041849]]  
[[ 0.52394342]  
[ 0.2547519 ]  
[-0.40983351]  
[-0.28072252]]  
[[ 0.52422986]  
[ 0.25492498]

[-0.40999306]  
[-0.28095448]]  
[[ 0.52444711]  
[ 0.25505711]  
[-0.4101131 ]  
[-0.28112764]]  
[[ 0.52461001]  
[ 0.2551557 ]  
[-0.41020366]  
[-0.28125904]]  
[[ 0.52473321]  
[ 0.25523054]  
[-0.41027184]  
[-0.28135753]]  
[[ 0.52482578]  
[ 0.25528662]  
[-0.41032324]  
[-0.28143204]]  
[[ 0.52489568]  
[ 0.25532905]  
[-0.41036196]  
[-0.28148802]]  
[[ 0.52494828]  
[ 0.25536092]  
[-0.41039115]  
[-0.28153029]]  
[[ 0.52498795]  
[ 0.255385 ]  
[-0.41041313]  
[-0.28156209]]  
[[ 0.52501782]  
[ 0.25540311]  
[-0.4104297 ]  
[-0.28158609]]  
[[ 0.52504034]  
[ 0.25541677]  
[-0.41044218]  
[-0.28160415]]  
[[ 0.5250573 ]  
[ 0.25542706]  
[-0.41045159]  
[-0.28161777]]  
[[ 0.52507009]  
[ 0.25543481]  
[-0.41045868]  
[-0.28162802]]  
[[ 0.52507972]  
[ 0.25544065]  
[-0.41046402]  
[-0.28163576]]

[[ 0.52508698]  
[ 0.25544506]  
[-0.41046805]  
[-0.28164158]]  
[[ 0.52509245]  
[ 0.25544837]  
[-0.41047108]  
[-0.28164597]]  
[[ 0.52509657]  
[ 0.25545087]  
[-0.41047336]  
[-0.28164928]]  
[[ 0.52509968]  
[ 0.25545276]  
[-0.41047509]  
[-0.28165177]]  
[[ 0.52510202]  
[ 0.25545418]  
[-0.41047638]  
[-0.28165365]]  
[[ 0.52510378]  
[ 0.25545525]  
[-0.41047736]  
[-0.28165506]]  
[[ 0.52510511]  
[ 0.25545605]  
[-0.4104781 ]  
[-0.28165613]]  
[[ 0.52510611]  
[ 0.25545666]  
[-0.41047865]  
[-0.28165693]]  
[[ 0.52510686]  
[ 0.25545712]  
[-0.41047907]  
[-0.28165754]]  
[[ 0.52510743]  
[ 0.25545746]  
[-0.41047939]  
[-0.28165799]]  
[[ 0.52510786]  
[ 0.25545772]  
[-0.41047962]  
[-0.28165834]]  
[[ 0.52510818]  
[ 0.25545792]  
[-0.4104798 ]  
[-0.2816586 ]]  
[[ 0.52510843]  
[ 0.25545806]

```

[-0.41047994]
[-0.28165879]]
[[ 0.52510861]
 [ 0.25545818]
 [-0.41048004]
 [-0.28165894]]
[[ 0.52510875]
 [ 0.25545826]
 [-0.41048012]
 [-0.28165905]]
[[ 0.52510885]
 [ 0.25545832]
 [-0.41048017]
 [-0.28165913]]
[[ 0.52510893]
 [ 0.25545837]
 [-0.41048022]
 [-0.2816592 ]]
iterations 52
error 8.997367404010961e-08
Out[20]:
array([[ 0.52510899],
       [ 0.25545841],
       [-0.41048025],
       [-0.28165924]])

```

## GAUSS SEIDEL

```

[[0.]
 [0.]
 [0.]
 [0.]]
[[ 0.25   ]
 [ 0.0483871 ]
 [-0.26572581]
 [-0.1091129 ]]
[[ 0.34393145]
 [ 0.15007414]
 [-0.32878014]
 [-0.17409904]]
[[ 0.41809282]
 [ 0.19103484]
 [-0.35996356]
 [-0.21761336]]
[[ 0.46096873]
 [ 0.21676315]
 [-0.3802917 ]
 [-0.24326538]]
[[ 0.48663982]
 [ 0.23228118]

```



[-0.39238936]  
[-0.25863807]]  
[[ 0.50204885]  
[ 0.24156283]  
[-0.39963339]  
[-0.26785883]]  
[[ 0.51128483]  
[ 0.24712813]  
[-0.40397782]  
[-0.27338613]]  
[[ 0.51682163]  
[ 0.25046457]  
[-0.40658217]  
[-0.27669967]]  
[[ 0.52014089]  
[ 0.25246471]  
[-0.40814344]  
[-0.2786861 ]]  
[[ 0.52213075]  
[ 0.25366376]  
[-0.4090794 ]  
[-0.27987694]]  
[[ 0.52332364]  
[ 0.25438258]  
[-0.4096405 ]  
[-0.28059083]]  
[[ 0.52403877]  
[ 0.25481351]  
[-0.40997687]  
[-0.2810188 ]]  
[[ 0.52446748]  
[ 0.25507184]  
[-0.41017852]  
[-0.28127536]]  
[[ 0.52472448]  
[ 0.25522671]  
[-0.41029941]  
[-0.28142917]]  
[[ 0.52487856]  
[ 0.25531955]  
[-0.41037188]  
[-0.28152138]]  
[[ 0.52497092]  
[ 0.25537521]  
[-0.41041532]  
[-0.28157665]]  
[[ 0.52502629]  
[ 0.25540857]  
[-0.41044137]  
[-0.28160979]]

[[ 0.52505948]  
[ 0.25542858]  
[-0.41045698]  
[-0.28162965]]  
[[ 0.52507938]  
[ 0.25544057]  
[-0.41046634]  
[-0.28164156]]  
[[ 0.52509131]  
[ 0.25544776]  
[-0.41047195]  
[-0.2816487 ]]  
[[ 0.52509847]  
[ 0.25545206]  
[-0.41047531]  
[-0.28165298]]  
[[ 0.52510275]  
[ 0.25545465]  
[-0.41047733]  
[-0.28165555]]  
[[ 0.52510532]  
[ 0.2554562 ]  
[-0.41047854]  
[-0.28165709]]  
[[ 0.52510686]  
[ 0.25545713]  
[-0.41047926]  
[-0.28165801]]  
[[ 0.52510779]  
[ 0.25545768]  
[-0.4104797 ]  
[-0.28165856]]  
[[ 0.52510834]  
[ 0.25545802]  
[-0.41047996]  
[-0.28165889]]  
[[ 0.52510867]  
[ 0.25545822]  
[-0.41048012]  
[-0.28165909]]  
[[ 0.52510887]  
[ 0.25545834]  
[-0.41048021]  
[-0.28165921]]  
[[ 0.52510899]  
[ 0.25545841]  
[-0.41048027]  
[-0.28165928]]

iterations 30

error 9.96798326917106e-08

```
Out[21]:
array([[ 0.52510906],
       [ 0.25545845],
       [-0.4104803 ],
       [-0.28165932]])
```

## SOR

```
[[0.]
 [0.]
 [0.]
 [0.]]
[[ 0.375   ]
 [ 0.06048387]
 [-0.40448589]
 [-0.26806956]]
[[ 0.5117597 ]
 [ 0.34197623]
 [-0.45004916]
 [-0.30469599]]
[[ 0.59014422]
 [ 0.23522845]
 [-0.39033638]
 [-0.30859371]]
[[ 0.51530648]
 [ 0.28152633]
 [-0.4443708 ]
 [-0.27123634]]
[[ 0.52806002]
 [ 0.24390875]
 [-0.38360511]
 [-0.28336154]]
[[ 0.52121751]
 [ 0.25512531]
 [-0.42445767]
 [-0.27939858]]
[[ 0.52438664]
 [ 0.25800267]
 [-0.40379938]
 [-0.28225196]]
[[ 0.52709114]
 [ 0.25251377]
 [-0.41262971]
 [-0.28222923]]
[[ 0.52365497]
 [ 0.25813679]
 [-0.41094639]
 [-0.2810727 ]]
[[ 0.5261806 ]
 [ 0.25369679]
 [-0.40914648]
```

[-0.28212891]]  
[[ 0.52444102]  
[ 0.25638029]  
[-0.41179033]  
[-0.28131836]]  
[[ 0.52540526]  
[ 0.25508527]  
[-0.40950273]  
[-0.28184609]]  
[[ 0.5250312 ]  
[ 0.2555134 ]  
[-0.41107293]  
[-0.28158444]]  
[[ 0.52508442]  
[ 0.25554748]  
[-0.41019651]  
[-0.2816734 ]]  
[[ 0.52517067]  
[ 0.25533652]  
[-0.41056857]  
[-0.28167376]]  
[[ 0.52504884]  
[ 0.25556209]  
[-0.41049266]  
[-0.2816371 ]]  
[[ 0.5251531 ]  
[ 0.25538879]  
[-0.41043101]  
[-0.28167892]]  
[[ 0.52508303]  
[ 0.2554967 ]  
[-0.41053169]  
[-0.28164601]]  
[[ 0.52512151]  
[ 0.25544277]  
[-0.41044149]  
[-0.28166689]]  
[[ 0.52510554]  
[ 0.25546126]  
[-0.41050422]  
[-0.28165617]]  
[[ 0.52510839]  
[ 0.25546165]  
[-0.41046862]  
[-0.28166007]]  
[[ 0.5251115 ]  
[ 0.25545384]  
[-0.41048422]  
[-0.2816599 ]]  
[[ 0.52510682]

[ 0.2554626 ]  
[-0.41048062]  
[-0.28165854]]  
[[ 0.52511092]  
[ 0.25545573]  
[-0.41047851]  
[-0.28166015]]  
[[ 0.52510811]  
[ 0.25546007]  
[-0.41048235]  
[-0.28165885]]  
[[ 0.52510968]  
[ 0.25545785]  
[-0.41047881]  
[-0.28165969]]  
[[ 0.52510901]  
[ 0.25545865]  
[-0.41048131]  
[-0.28165925]]  
[[ 0.52510915]  
[ 0.25545862]  
[-0.41047987]  
[-0.28165942]]  
[[ 0.52510926]  
[ 0.25545834]  
[-0.41048052]  
[-0.28165941]]  
[[ 0.52510908]  
[ 0.25545868]  
[-0.41048035]  
[-0.28165936]]  
[[ 0.52510924]  
[ 0.2554584 ]  
[-0.41048028]  
[-0.28165942]]  
[[ 0.52510913]  
[ 0.25545858]  
[-0.41048043]  
[-0.28165937]]  
[[ 0.52510919]  
[ 0.25545849]  
[-0.41048029]  
[-0.2816594 ]]  
[[ 0.52510916]  
[ 0.25545852]  
[-0.41048039]  
[-0.28165938]]

iterations 35

error 5.945865342973044e-08

Out[24]:

```
array([[ 0.52510917],
       [ 0.25545852],
       [-0.41048033],
       [-0.28165939]])
```

### Vandermonde

```
[-1.  1. -1.  1.]
[ 0.  0.  0.  1.]
[27.  9.  3.  1.]
[64. 16.  4.  1.]
```

### Newton

```
[ 15.5      0.      0.      0.      ]
[  3.     -12.5      0.      0.      ]
[  8.       1.66666667  3.54166667  0.      ]
[  1.       -7.      -2.16666667 -1.14166667]
```

### Trazadores lineales

M

```
[-1.  1.  0.  0.  0.  0.]
[ 0.  1.  0.  0.  0.  0.]
[ 0.  0.  3.  1.  0.  0.]
[ 0.  0.  0.  0.  4.  1.]
[ 0.  1.  0. -1.  0.  0.]
[ 0.  0.  3.  1. -3. -1.]
```

y

```
[15.5]
[ 3.]
[ 8.]
[ 1.]
[ 0.]
[ 0.]
```

sol

```
[-12.5   ]
[  3.     ]
[ 1.66666667]
[  3.     ]
[-7.      ]
[ 29.     ]
```

### Trazadores Cuadráticos

M

```
[ 1. -1.  1.  0.  0.  0.  0.  0.  0.]
[ 0.  0.  1.  0.  0.  0.  0.  0.  0.]
[ 0.  0.  0.  9.  3.  1.  0.  0.  0.]
```

[ 0. 0. 0. 0. 0. 0. 16. 4. 1.]  
[ 0. 0. 1. 0. 0. -1. 0. 0. 0.]  
[ 0. 0. 0. 9. 3. 1. -9. -3. -1.]  
[ 0. 1. 0. 0. -1. 0. 0. 0. 0.]  
[ 0. 0. 0. 6. 1. 0. -6. -1. 0.]  
[ 2. 0. 0. 0. 0. 0. 0. 0. 0.]

y  
[15.5]  
[ 3. ]  
[ 8. ]  
[ 1. ]  
[ 0. ]  
[ 0. ]  
[ 0. ]  
[ 0. ]  
[ 0. ]

sol  
[ 0.     ]  
[ -12.5     ]  
[ 3.     ]  
[ 4.72222222]  
[ -12.5     ]  
[ 3.     ]  
[ -22.83333333]  
[ 152.83333333]  
[ -245.     ]

Trazadores cúbicos  
M

[ -1. 1. -1. 1. 0. 0. 0. 0. 0. 0. 0. 0.]  
[ 0. 0. 0. 1. 0. 0. 0. 0. 0. 0. 0. 0.]  
[ 0. 0. 0. 0. 27. 9. 3. 1. 0. 0. 0. 0.]  
[ 0. 0. 0. 0. 0. 0. 0. 0. 64. 16. 4. 1.]  
[ 0. 0. 0. 1. 0. 0. 0. -1. 0. 0. 0. 0.]  
[ 0. 0. 0. 0. 27. 9. 3. 1. -27. -9. -3. -1.]  
[ 0. 0. 1. 0. 0. 0. -1. 0. 0. 0. 0. 0.]  
[ 0. 0. 0. 0. 27. 6. 1. 0. -27. -6. -1. 0.]  
[ 0. 2. 0. 0. 0. -2. 0. 0. 0. 0. 0. 0.]  
[ 0. 0. 0. 0. 18. 2. 0. 0. -18. -2. 0. 0.]  
[ 6. 2. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.]  
[ 0. 0. 0. 0. 0. 0. 0. 0. 6. 2. 0. 0.]

y  
[15.5]  
[ 3. ]  
[ 8. ]  
[ 1. ]  
[ 0. ]

[ 0. ]  
[ 0. ]  
[ 0. ]  
[ 0. ]  
[ 0. ]  
[ 0. ]  
[ 0. ]

sol

[-1.86724806]  
[ 5.60174419]  
[-5.03100775]  
[ 3.     ]  
[-1.12306202]  
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[ 3.     ]  
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[ 2.25290698]  
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[-7.04651163]