## **Spatstat Quick Reference guide**

May 10, 2020

spatstat-package

The Spatstat Package

## **Description**

This is a summary of the features of **spatstat**, a package in R for the statistical analysis of spatial point patterns.

#### **Details**

**spatstat** is a package for the statistical analysis of spatial data. Its main focus is the analysis of spatial patterns of points in two-dimensional space. The points may carry auxiliary data ('marks'), and the spatial region in which the points were recorded may have arbitrary shape.

The package is designed to support a complete statistical analysis of spatial data. It supports

- creation, manipulation and plotting of point patterns;
- · exploratory data analysis;
- spatial random sampling;
- simulation of point process models;
- parametric model-fitting;
- non-parametric smoothing and regression;
- formal inference (hypothesis tests, confidence intervals);
- · model diagnostics.

Apart from two-dimensional point patterns and point processes, **spatstat** also supports point patterns in three dimensions, point patterns in multidimensional space-time, point patterns on a linear network, patterns of line segments in two dimensions, and spatial tessellations and random sets in two dimensions.

The package can fit several types of point process models to a point pattern dataset:

- Poisson point process models (by Berman-Turner approximate maximum likelihood or by spatial logistic regression)
- Gibbs/Markov point process models (by Baddeley-Turner approximate maximum pseudolikelihood, Coeurjolly-Rubak logistic likelihood, or Huang-Ogata approximate maximum likelihood)

Cox/cluster point process models (by Waagepetersen's two-step fitting procedure and minimum contrast, composite likelihood, or Palm likelihood)

• determinantal point process models (by Waagepetersen's two-step fitting procedure and minimum contrast, composite likelihood, or Palm likelihood)

The models may include spatial trend, dependence on covariates, and complicated interpoint interactions. Models are specified by a formula in the R language, and are fitted using a function analogous to 1m and g1m. Fitted models can be printed, plotted, predicted, simulated and so on.

## **Getting Started**

For a quick introduction to **spatstat**, read the package vignette *Getting started with spatstat* installed with **spatstat**. To read that document, you can either

- visit https://cran.r-project.org/package=spatstat and click on Getting Started with Spatstat
- start R, type library(spatstat) and vignette('getstart')
- start R, type help.start() to open the help browser, and navigate to Packages > spatstat > Vignettes.

Once you have installed **spatstat**, start R and type library(spatstat). Then type beginner for a beginner's introduction, or demo(spatstat) for a demonstration of the package's capabilities.

For a complete course on **spatstat**, and on statistical analysis of spatial point patterns, read the book by Baddeley, Rubak and Turner (2015). Other recommended books on spatial point process methods are Diggle (2014), Gelfand et al (2010) and Illian et al (2008).

The **spatstat** package includes over 50 datasets, which can be useful when learning the package. Type demo(data) to see plots of all datasets available in the package. Type vignette('datasets') for detailed background information on these datasets, and plots of each dataset.

For information on converting your data into **spatstat** format, read Chapter 3 of Baddeley, Rubak and Turner (2015). This chapter is available free online, as one of the sample chapters at the book companion website, <a href="https://spatstat.github.io/book">https://spatstat.github.io/book</a>.

For information about handling data in **shapefiles**, see Chapter 3, or the Vignette *Handling shape-files in the spatstat package*, installed with **spatstat**, accessible as vignette('shapefiles').

#### **Updates**

New versions of **spatstat** are released every 8 weeks. Users are advised to update their installation of **spatstat** regularly.

Type latest.news to read the news documentation about changes to the current installed version of **spatstat**.

See the Vignette *Summary of recent updates*, installed with **spatstat**, which describes the main changes to **spatstat** since the book (Baddeley, Rubak and Turner, 2015) was published. It is accessible as vignette('updates').

Type news(package="spatstat") to read news documentation about all previous versions of the package.

#### FUNCTIONS AND DATASETS

Following is a summary of the main functions and datasets in the **spatstat** package. Alternatively an alphabetical list of all functions and datasets is available by typing library(help=spatstat).

For further information on any of these, type help(name) or ?name where name is the name of the function or dataset.

#### **CONTENTS:**

I. Creating and manipulating dataII. Exploratory Data Analysis

III. Model fitting (Cox and cluster models)
IV. Model fitting (Poisson and Gibbs models)
V. Model fitting (determinantal point processes)
VI. Model fitting (spatial logistic regression)

VII. Simulation

VIII. Tests and diagnostics IX. Documentation

#### I. CREATING AND MANIPULATING DATA

## Types of spatial data:

The main types of spatial data supported by **spatstat** are:

ppp point pattern
owin window (spatial region)
im pixel image
psp line segment pattern
tess tessellation
pp3 three-dimensional point pattern
ppx point pattern in any number of dimensions
1pp point pattern on a linear network

1pp point pa

## To create a point pattern:

ppp create a point pattern from (x,y) and window information ppp(x, y, xlim, ylim) for rectangular window ppp(x, y, poly) for polygonal window ppp(x, y, mask) for binary image window convert other types of data to a ppp object clickppp interactively add points to a plot attach/reassign marks to a point pattern

## To simulate a random point pattern:

runifpoint generate n independent uniform random points rpoint generate n independent random points rmpoint generate n independent multitype random points simulate the (in)homogeneous Poisson point process rpoispp simulate the (in)homogeneous multitype Poisson point process rmpoispp runifdisc generate n independent uniform random points in disc rstrat stratified random sample of points systematic random sample of points rsyst apply random displacements to points in a pattern rjitter simulate the Matérn Model I inhibition process rMaternI rMaternII simulate the Matérn Model II inhibition process rSSI simulate Simple Sequential Inhibition process

rStrauss simulate Strauss process (perfect simulation)
rHardcore simulate Hard Core process (perfect simulation)
rStraussHard simulate Strauss-hard core process (perfect simulation)
rDiggleGratton simulate Diggle-Gratton process (perfect simulation)
rDGS simulate Diggle-Gates-Stibbard process (perfect simulation)

rPenttinen simulate Penttinen process (perfect simulation)
rNeymanScott simulate a general Neyman-Scott process
rPoissonCluster simulate a general Poisson cluster process
rMatClust simulate the Matérn Cluster process

rThomas simulate the Thomas process

rGaussPoisson simulate the Gauss-Poisson cluster process rCauchy simulate Neyman-Scott Cauchy cluster process

rVarGamma simulate Neyman-Scott Variance Gamma cluster process

rthin random thinning

rcell simulate the Baddeley-Silverman cell process

rmhsimulate Gibbs point process using Metropolis-Hastingssimulate.ppmsimulate Gibbs point process using Metropolis-HastingsrunifpointOnLinesgenerate n random points along specified line segmentsrpoisppOnLinesgenerate Poisson random points along specified line segments

#### To randomly change an existing point pattern:

rshift random shifting of points

rjitter apply random displacements to points in a pattern

rthin random thinning

rlabel random (re)labelling of a multitype point pattern

quadratresample block resampling

#### **Standard point pattern datasets:**

Datasets in **spatstat** are lazy-loaded, so you can simply type the name of the dataset to use it; there is no need to type data(amacrine) etc.

Type demo(data) to see a display of all the datasets installed with the package.

Type vignette('datasets') for a document giving an overview of all datasets, including background information, and plots.

amacrine Austin Hughes' rabbit amacrine cells
anemones Upton-Fingleton sea anemones data
ants Harkness-Isham ant nests data
bdspots Breakdown spots in microelectrodes

bei Tropical rainforest trees

betacells Waessle et al. cat retinal ganglia data

bramblecanes Bramble Canes data
bronzefilter Bronze Filter Section data
cells Crick-Ripley biological cells data

chicago Chicago crimes

chorley Chorley-Ribble cancer data
clmfires Castilla-La Mancha forest fires

copper Berman-Huntington copper deposits data

dendriteDendritic spinesdemohyperSynthetic point patternsdemopatSynthetic point pattern

finpines Finnish Pines data flu Influenza virus proteins

gordon People in Gordon Square, London

gorillas Gorilla nest sites

hamster Aherne's hamster tumour data

humberside North Humberside childhood leukaemia data

hyytiala Mixed forest in Hyytiälä, Finland

japanesepines Japanese Pines data Lansing Woods data lansing longleaf Longleaf Pines data Cells in gastric mucosa mucosa Murchison gold deposits murchison New Brunswick fires data nbfires Mark-Esler-Ripley trees data nztrees Osteocyte lacunae (3D, replicated) osteo Kimboto trees in Paracou, French Guiana paracou Getis-Franklin ponderosa pine trees data ponderosa Pyramidal neurons from 31 brains pyramidal Strauss-Ripley redwood saplings data redwood redwoodfull Strauss redwood saplings data (full set) Data from Baddeley et al (2005) residualspaper Galaxies in an astronomical survey shaplev

simulated point pattern (inhomogeneous, with interaction)

spiders Spider webs on mortar lines of brick wall

sporophores Mycorrhizal fungi around a tree

spruces Spruce trees in Saxonia

swedishpines Strand-Ripley Swedish pines data

urkiola Urkiola Woods data

waka Trees in Waka national park waterstriders Insects on water surface

## To manipulate a point pattern:

plot.ppp plot a point pattern (e.g. plot(X)) spatstat.gui::iplot plot a point pattern interactively

edit.ppp interactive text editor

[.ppp extract or replace a subset of a point pattern

pp[subset] or pp[subwindow]

subset.ppp extract subset of point pattern satisfying a condition

superimpose combine several point patterns

by . ppp apply a function to sub-patterns of a point pattern

cut.ppp classify the points in a point pattern split.ppp divide pattern into sub-patterns

unmark remove marks

npoints count the number of points

coords extract coordinates, change coordinates
marks extract marks, change marks or attach marks

rotate rotate pattern shift translate pattern

flipxy swap x and y coordinates reflect reflect in the origin

periodify make several translated copies affine apply affine transformation

scalardilate apply scalar dilation kernel estimation of point pattern intensity density.ppp kernel smoothing of marks of point pattern Smooth.ppp mark value of nearest data point nnmark data sharpening sharpen.ppp interactively identify points identify.ppp remove duplicate points unique.ppp duplicated.ppp determine which points are duplicates map duplicated points to unique points uniquemap.ppp connected.ppp find clumps of points compute Dirichlet-Voronoi tessellation dirichlet compute Delaunay triangulation delaunay graph distance in Delaunay triangulation delaunayDistance convexhull compute convex hull discretise discretise coordinates approximate point pattern by pixel image pixellate.ppp as.im.ppp approximate point pattern by pixel image

See spatstat.options to control plotting behaviour.

#### To create a window:

An object of class "owin" describes a spatial region (a window of observation).

owin Create a window object owin(xlim, ylim) for rectangular window owin(poly) for polygonal window owin(mask) for binary image window Extract window of another object Window Extract the containing rectangle ('frame') of another object Frame Convert other data to a window object as.owin make a square window square disc make a circular window ellipse make an elliptical window Ripley-Rasson estimator of window, given only the points ripras compute convex hull of something convexhull letterR polygonal window in the shape of the R logo interactively draw a polygonal window clickpoly interactively draw a rectangle clickbox

## To manipulate a window:

plot.owin	plot a window.
	plot(W)
boundingbox	Find a tight bounding box for the window
erosion	erode window by a distance r
dilation	dilate window by a distance r
closing	close window by a distance r
opening	open window by a distance r
border	difference between window and its erosion/dilation
complement.owin	invert (swap inside and outside)
simplify.owin	approximate a window by a simple polygon

rotate rotate window

 $\begin{array}{ll} \mbox{flipxy} & \mbox{swap } x \mbox{ and } y \mbox{ coordinates} \\ \mbox{shift} & \mbox{translate window} \\ \mbox{periodify} & \mbox{make several translated copies} \\ \mbox{affine} & \mbox{apply affine transformation} \\ \mbox{as.data.frame.owin} & \mbox{convert window to data frame} \end{array}$ 

## **Digital approximations:**

as.mask Make a discrete pixel approximation of a given window as.im.owin convert window to pixel image convert window to pixel image pixellate.owin find common pixel grid for windows commonGrid map continuous coordinates to raster locations nearest.raster.point raster x coordinates raster.x raster y coordinates raster.y raster x and y coordinates raster.xy convert pixel mask to polygonal window as.polygonal

See spatstat.options to control the approximation

#### Geometrical computations with windows:

clickdist

extract boundary edges edges intersection of two windows intersect.owin union.owin union of two windows set subtraction of two windows setminus.owin determine whether a point is inside a window inside.owin area.owin compute area compute perimeter length perimeter compute diameter diameter.owin incircle find largest circle inside a window inradius radius of incircle find connected components of window connected.owin compute areas of eroded windows eroded.areas dilated.areas compute areas of dilated windows bdist.points compute distances from data points to window boundary compute distances from all pixels to window boundary bdist.pixels boundary distance for each tile in tessellation bdist.tiles distance transform image distmap.owin distfun.owin distance transform compute centroid (centre of mass) of window centroid.owin is.subset.owin determine whether one window contains another determine whether a window is convex is.convex compute convex hull convexhull triangulate.owin decompose into triangles as.mask pixel approximation of window as.polygonal polygonal approximation of window test whether window is a rectangle is.rectangle test whether window is polygonal is.polygonal test whether window is a mask is.mask setcov spatial covariance function of window pixelcentres extract centres of pixels in mask

measure distance between two points clicked by user

**Pixel images:** An object of class "im" represents a pixel image. Such objects are returned by some of the functions in **spatstat** including Kmeasure, setcov and density.ppp.

create a pixel image im convert other data to a pixel image as.im pixellate convert other data to a pixel image as.matrix.im convert pixel image to matrix convert pixel image to data frame as.data.frame.im convert pixel image to function as.function.im plot a pixel image on screen as a digital image plot.im contour.im draw contours of a pixel image persp.im draw perspective plot of a pixel image create colour-valued pixel image rgbim create colour-valued pixel image hsvim [.im extract a subset of a pixel image replace a subset of a pixel image Γ<-.im rotate.im rotate pixel image apply vector shift to pixel image shift.im affine.im apply affine transformation to image print very basic information about image X summary of image X summary(X) hist.im histogram of image mean pixel value of image mean.im integral of pixel values integral.im quantiles of image quantile.im convert numeric image to factor image cut.im is.im test whether an object is a pixel image interpolate a pixel image interp.im apply Gaussian blur to image blur Smooth.im apply Gaussian blur to image connected.im find connected components test whether two images have compatible dimensions compatible.im harmonise.im make images compatible find a common pixel grid for images commonGrid evaluate any expression involving images eval.im evaluate a function of several images im.apply scaletointerval rescale pixel values zapsmall.im set very small pixel values to zero levelset level set of an image region where an expression is true solutionset imcov spatial covariance function of image convolve.im spatial convolution of images transect.im line transect of image extract centres of pixels pixelcentres convert matrix of pixel values transmat to a different indexing convention rnoise random pixel noise

#### Line segment patterns

An object of class "psp" represents a pattern of straight line segments.

psp create a line segment pattern

as.psp	convert other data into a line segment pattern
edges	extract edges of a window
is.psp	determine whether a dataset has class "psp"
plot.psp	plot a line segment pattern
print.psp	print basic information
summary.psp	print summary information
[.psp	extract a subset of a line segment pattern
subset.psp	extract subset of line segment pattern
as.data.frame.psp	convert line segment pattern to data frame
marks.psp	extract marks of line segments
marks <psp< td=""><td>assign new marks to line segments</td></psp<>	assign new marks to line segments
unmark.psp	delete marks from line segments
midpoints.psp	compute the midpoints of line segments
endpoints.psp	extract the endpoints of line segments
lengths_psp	compute the lengths of line segments
angles.psp	compute the orientation angles of line segments
superimpose	combine several line segment patterns
flipxy	swap $x$ and $y$ coordinates
rotate.psp	rotate a line segment pattern
shift.psp	shift a line segment pattern
periodify	make several shifted copies
affine.psp	apply an affine transformation
pixellate.psp	approximate line segment pattern by pixel image
as.mask.psp	approximate line segment pattern by binary mask
distmap.psp	compute the distance map of a line segment pattern
distfun.psp	compute the distance map of a line segment pattern
density.psp	kernel smoothing of line segments
selfcrossing.psp	find crossing points between line segments
selfcut.psp	cut segments where they cross
crossing.psp	find crossing points between two line segment patterns
extrapolate.psp	extrapolate line segments to infinite lines
nncross	find distance to nearest line segment from a given point
nearestsegment	find line segment closest to a given point
project2segment	find location along a line segment closest to a given point
pointsOnLines	generate points evenly spaced along line segment
rpoisline	generate a realisation of the Poisson line process inside a window
rlinegrid	generate a random array of parallel lines through a window

## **Tessellations**

An object of class "tess" represents a tessellation.

tess	create a tessellation
quadrats	create a tessellation of rectangles
hextess	create a tessellation of hexagons
polartess	tessellation using polar coordinates
quantess	quantile tessellation
venn.tess	Venn diagram tessellation
dirichlet	compute Dirichlet-Voronoi tessellation of points
delaunay	compute Delaunay triangulation of points
as.tess	convert other data to a tessellation
plot.tess	plot a tessellation
tiles	extract all the tiles of a tessellation

[.tess extract some tiles of a tessellation Γ<-.tess change some tiles of a tessellation intersect two tessellations intersect.tess or restrict a tessellation to a window subdivide a tessellation by a line chop.tess generate tessellation using Poisson line process rpoislinetess tile.areas area of each tile in tessellation bdist.tiles boundary distance for each tile in tessellation find connected components of tiles connected.tess shift.tess shift a tessellation rotate a tessellation rotate.tess reflect about the origin reflect.tess flipxy.tess reflect about the diagonal affine.tess apply affine transformation

## Three-dimensional point patterns

An object of class "pp3" represents a three-dimensional point pattern in a rectangular box. The box is represented by an object of class "box3".

create a 3-D point pattern pp3 plot a 3-D point pattern plot.pp3 coords extract coordinates as.hyperframe extract coordinates subset.pp3 extract subset of 3-D point pattern unitname.pp3 name of unit of length count the number of points npoints runifpoint3 generate uniform random points in 3-D generate Poisson random points in 3-D rpoispp3 generate simulation envelopes for 3-D pattern envelope.pp3 box3 create a 3-D rectangular box convert data to 3-D rectangular box as.box3 unitname.box3 name of unit of length diameter.box3 diameter of box volume of box volume.box3 shortest side of box shortside.box3 eroded.volumes volumes of erosions of box

## Multi-dimensional space-time point patterns

An object of class "ppx" represents a point pattern in multi-dimensional space and/or time.

create a multidimensional space-time point pattern ррх extract coordinates coords extract coordinates as.hyperframe subset.ppx extract subset unitname.ppx name of unit of length count the number of points npoints generate uniform random points runifpointx generate Poisson random points rpoisppx define multidimensional box boxx diameter of box diameter.boxx volume.boxx volume of box

```
shortside.boxx shortest side of box eroded.volumes.boxx volumes of erosions of box
```

## Point patterns on a linear network

An object of class "linnet" represents a linear network (for example, a road network).

create a linear network linnet interactively join vertices in network clickjoin spatstat.gui::iplot.linnet interactively plot network simplenet simple example of network lineardisc disc in a linear network network of Delaunay triangulation delaunayNetwork network of Dirichlet edges dirichletNetwork methods.linnet methods for linnet objects vertices.linnet nodes of network join existing vertices in a network joinVertices insert new vertices at positions along a network insertVertices add new vertices, extending a network addVertices thinNetwork remove vertices or lines from a network repair internal format repairNetwork pixellate.linnet approximate by pixel image

An object of class "lpp" represents a point pattern on a linear network (for example, road accidents on a road network).

create a point pattern on a linear network 1pp methods for 1pp objects methods.lpp subset.lpp method for subset simulate Poisson points on linear network rpoislpp simulate random points on a linear network runiflpp Chicago crime data chicago dendrite Dendritic spines data spiders Spider webs on mortar lines of brick wall

## **Hyperframes**

A hyperframe is like a data frame, except that the entries may be objects of any kind.

create a hyperframe hyperframe as.hyperframe convert data to hyperframe plot.hyperframe plot hyperframe with.hyperframe evaluate expression using each row of hyperframe cbind.hyperframe combine hyperframes by columns combine hyperframes by rows rbind.hyperframe as.data.frame.hyperframe convert hyperframe to data frame subset.hyperframe method for subset first few rows of hyperframe head.hyperframe tail.hyperframe last few rows of hyperframe

## Layered objects

A layered object represents data that should be plotted in successive layers, for example, a back-

ground and a foreground.

layered create layered object
plot.layered plot layered object
[.layered extract subset of layered object

#### Colour maps

A colour map is a mechanism for associating colours with data. It can be regarded as a function, mapping data to colours. Using a colourmap object in a plot command ensures that the mapping from numbers to colours is the same in different plots.

colourmap create a colour map
plot.colourmap plot the colour map only
tweak.colourmap alter individual colour values
interp.colourmap make a smooth transition between colours
beachcolourmap one special colour map

#### II. EXPLORATORY DATA ANALYSIS

#### **Inspection of data:**

summary(X) print useful summary of point pattern X
X print basic description of point pattern X
any(duplicated(X)) check for duplicated points in pattern X
spatstat.gui::istat(X) Interactive exploratory analysis
View(X) spreadsheet-style viewer

## Classical exploratory tools:

clarkevans Clark and Evans aggregation index
fryplot Fry plot
miplot Morisita Index plot

## **Smoothing:**

density.ppp kernel smoothed density/intensity kernel estimate of relative risk relrisk Smooth.ppp spatial interpolation of marks bw.diggle cross-validated bandwidth selection for density.ppp likelihood cross-validated bandwidth selection for density.ppp bw.ppl bw.CvL Cronie-Van Lieshout bandwidth selection for density estimation bw.scott Scott's rule of thumb for density estimation bw.abram Abramson's rule for adaptive bandwidths bw.relrisk cross-validated bandwidth selection for relrisk bw.smoothppp cross-validated bandwidth selection for Smooth.ppp bw.frac bandwidth selection using window geometry Stoyan's rule of thumb for bandwidth for pcf bw.stoyan

#### Modern exploratory tools:

clusterset Allard-Fraley feature detection

nnclean
sharpen.ppp
Choi-Hall data sharpening
rhohat
Kernel estimate of covariate effect
rho2hat
Spatialcdf
roc
Receiver operating characteristic curve

**Summary statistics for a point pattern:** Type demo(sumfun) for a demonstration of many of the summary statistics.

Mean intensity intensity Quadrat counts quadratcount intensity.quadratcount Mean intensity in quadrats empty space function FFest Gest nearest neighbour distribution function G *J*-function J = (1 - G)/(1 - F)Jest Ripley's K-function Kest Besag L-function Lest Third order T-function Tstat allstats all four functions F, G, J, Kpair correlation function pcf K for inhomogeneous point patterns Kinhom Linhom L for inhomogeneous point patterns pair correlation for inhomogeneous patterns pcfinhom Finhom F for inhomogeneous point patterns G for inhomogeneous point patterns Ginhom Jinhom J for inhomogeneous point patterns localL Getis-Franklin neighbourhood density function localK neighbourhood K-function localpcf local pair correlation function localKinhom local K for inhomogeneous point patterns localLinhom local L for inhomogeneous point patterns local pair correlation for inhomogeneous patterns localpcfinhom Directional K-function Ksector Kscaled locally scaled K-function Kest.fft fast K-function using FFT for large datasets reduced second moment measure **Kmeasure** envelope simulation envelopes for a summary function variances and confidence intervals varblock for a summary function

## Related facilities:

lohboot

plot.fv	plot a summary function
eval.fv	evaluate any expression involving summary functions
harmonise.fv	make functions compatible
eval.fasp	evaluate any expression involving an array of functions
with.fv	evaluate an expression for a summary function
Smooth.fv	apply smoothing to a summary function
deriv.fv	calculate derivative of a summary function
pool.fv	pool several estimates of a summary function

bootstrap for a summary function

nndist nearest neighbour distances find nearest neighbours nnwhich pairdist distances between all pairs of points distances between points in two patterns crossdist nearest neighbours between two point patterns nncross distance from any location to nearest data point exactdt distance map image distmap distance map function distfun nnmap nearest point image

nnfun nearest point function
density.ppp kernel smoothed density
Smooth.ppp spatial interpolation of marks
relrisk kernel estimate of relative risk

sharpen.ppp data sharpening

rknn theoretical distribution of nearest neighbour distance

**Summary statistics for a multitype point pattern:** A multitype point pattern is represented by an object X of class "ppp" such that marks (X) is a factor.

relrisk kernel estimation of relative risk scan.test spatial scan test of elevated risk Gcross, Gdot, Gmulti multitype nearest neighbour distributions  $G_{ij}$ ,  $G_{i\bullet}$ Kcross, Kdot, Kmulti multitype K-functions  $K_{ij}, K_{i\bullet}$ Lcross, Ldot multitype L-functions  $L_{ij}, L_{i\bullet}$ Jcross, Jdot, Jmulti multitype J-functions  $J_{ij}, J_{i\bullet}$ multitype pair correlation function  $g_{ij}$ pcfcross pcfdot multitype pair correlation function  $q_{i\bullet}$ general pair correlation function pcfmulti marked connection function  $p_{ij}$ markconnect estimates of the above for all i, j pairs alltypes **Iest** multitype *I*-function Kcross.inhom,Kdot.inhom inhomogeneous counterparts of Kcross, Kdot Lcross.inhom,Ldot.inhom inhomogeneous counterparts of Lcross, Ldot pcfcross.inhom,pcfdot.inhom inhomogeneous counterparts of pcfcross, pcfdot localKcross,localKdot local counterparts of Kcross, Kdot

localLcross, localLdot local counterparts of Lcross, Ldot localKcross.inhom, localLcross.inhom local counterparts of Kcross.inhom, Lcross.inhom

**Summary statistics for a marked point pattern:** A marked point pattern is represented by an object X of class "ppp" with a component X\$marks. The entries in the vector X\$marks may be numeric, complex, string or any other atomic type. For numeric marks, there are the following functions:

markmean smoothed local average of marks
markvar smoothed local variance of marks
markcorr mark correlation function

markcrosscorr mark cross-correlation function

 $\begin{array}{ll} {\rm mark\, vario} & {\rm mark\, variogram} \\ {\rm markmark scatter} & {\rm mark-mark\, scatterplot} \\ {\rm Kmark} & {\rm mark-weighted} \ K \ {\rm function} \end{array}$ 

nnmean	nearest neighbour mean index
nnvario	nearest neighbour mark variance index

For marks of any type, there are the following:

```
 \begin{array}{ll} \textbf{Gmulti} & \textbf{multitype nearest neighbour distribution} \\ \textbf{Kmulti} & \textbf{multitype } K\text{-function} \\ \textbf{Jmulti} & \textbf{multitype } J\text{-function} \\ \end{array}
```

Alternatively use cut.ppp to convert a marked point pattern to a multitype point pattern.

## **Programming tools:**

applynbd	apply function to every neighbourhood in a point pattern
markstat	apply function to the marks of neighbours in a point pattern
marktable	tabulate the marks of neighbours in a point pattern
pppdist	find the optimal match between two point patterns

## Summary statistics for a point pattern on a linear network:

These are for point patterns on a linear network (class 1pp). For unmarked patterns:

linearK	K function on linear network
linearKinhom	inhomogeneous $K$ function on linear network
linearpcf	pair correlation function on linear network
linearpcfinhom	inhomogeneous pair correlation on linear network

## For multitype patterns:

linearKcross	K function between two types of points
linearKdot	K function from one type to any type
linearKcross.inhom	Inhomogeneous version of linearKcross
linearKdot.inhom	Inhomogeneous version of linearKdot
linearmarkconnect	Mark connection function on linear network
linearmarkequal	Mark equality function on linear network
linearpcfcross	Pair correlation between two types of points
linearpcfdot	Pair correlation from one type to any type
linearpcfcross.inhom	Inhomogeneous version of linearpcfcross
linearpcfdot.inhom	Inhomogeneous version of linearpcfdot

## Related facilities:

pairdist.lpp	distances between pairs
crossdist.lpp	distances between pairs
nndist.lpp	nearest neighbour distances
nncross.lpp	nearest neighbour distances
nnwhich.lpp	find nearest neighbours
nnfun.lpp	find nearest data point
density.lpp	kernel smoothing estimator of intensity
distfun.lpp	distance transform
envelope.lpp	simulation envelopes
rpoislpp	simulate Poisson points on linear network
runiflpp	simulate random points on a linear network

It is also possible to fit point process models to 1pp objects. See Section IV.

## Summary statistics for a three-dimensional point pattern:

These are for 3-dimensional point pattern objects (class pp3).

F3est empty space function F G3est nearest neighbour function G K3est K-function

pcf3est pair correlation function

#### Related facilities:

envelope.pp3 simulation envelopes
pairdist.pp3 distances between all pairs of points
crossdist.pp3 distances between points in two patterns
nndist.pp3 nearest neighbour distances
nnwhich.pp3 find nearest neighbours
nncross.pp3 find nearest neighbours in another pattern

#### Computations for multi-dimensional point pattern:

These are for multi-dimensional space-time point pattern objects (class ppx).

pairdist.ppx distances between all pairs of points distances between points in two patterns nearest neighbour distances find nearest neighbours

#### **Summary statistics for random sets:**

These work for point patterns (class ppp), line segment patterns (class psp) or windows (class owin).

Hest spherical contact distribution H Gfox Foxall G-function Jfox Foxall J-function

## III. MODEL FITTING (COX AND CLUSTER MODELS)

Cluster process models (with homogeneous or inhomogeneous intensity) and Cox processes can be fitted by the function kppm. Its result is an object of class "kppm". The fitted model can be printed, plotted, predicted, simulated and updated.

**kppm** Plot the fitted model plot.kppm Summarise the fitted model summary.kppm fitted.kppm Compute fitted intensity predict.kppm Compute fitted intensity Update the model update.kppm improve.kppm Refine the estimate of trend simulate.kppm Generate simulated realisations vcov.kppm Variance-covariance matrix of coefficients coef.kppm Extract trend coefficients Extract trend formula formula.kppm parameters Extract all model parameters

```
\begin{array}{ll} \textbf{clusterfield} & \textbf{Compute offspring density} \\ \textbf{clusterradius} & \textbf{Radius of support of offspring density} \\ \textbf{Kmodel.kppm} & K \text{ function of fitted model} \\ \textbf{pcfmodel.kppm} & \textbf{Pair correlation of fitted model} \end{array}
```

For model selection, you can also use the generic functions step, drop1 and AIC on fitted point process models. For variable selection, see sdr.

The theoretical models can also be simulated, for any choice of parameter values, using rThomas, rMatClust, rCauchy, rVarGamma, and rLGCP.

Lower-level fitting functions include:

```
lgcp.estK
                    fit a log-Gaussian Cox process model
                    fit a log-Gaussian Cox process model
lgcp.estpcf
thomas.estK
                    fit the Thomas process model
                    fit the Thomas process model
thomas.estpcf
matclust.estK
                    fit the Matérn Cluster process model
matclust.estpcf
                    fit the Matérn Cluster process model
                    fit a Neyman-Scott Cauchy cluster process
cauchy.estK
cauchy.estpcf
                    fit a Neyman-Scott Cauchy cluster process
                    fit a Neyman-Scott Variance Gamma process
vargamma.estK
vargamma.estpcf
                    fit a Neyman-Scott Variance Gamma process
                    low-level algorithm for fitting models
mincontrast
                    by the method of minimum contrast
```

## IV. MODEL FITTING (POISSON AND GIBBS MODELS)

## Types of models

Poisson point processes are the simplest models for point patterns. A Poisson model assumes that the points are stochastically independent. It may allow the points to have a non-uniform spatial density. The special case of a Poisson process with a uniform spatial density is often called Complete Spatial Randomness.

Poisson point processes are included in the more general class of Gibbs point process models. In a Gibbs model, there is *interaction* or dependence between points. Many different types of interaction can be specified.

For a detailed explanation of how to fit Poisson or Gibbs point process models to point pattern data using **spatstat**, see Baddeley and Turner (2005b) or Baddeley (2008).

## To fit a Poisson or Gibbs point process model:

Model fitting in **spatstat** is performed mainly by the function ppm. Its result is an object of class "ppm".

Here are some examples, where X is a point pattern (class "ppp"):

command	model
ppm(X)	Complete Spatial Randomness
ppm(X ~ 1)	Complete Spatial Randomness
ppm(X ~ x)	Poisson process with
	intensity loglinear in $x$ coordinate
ppm(X ~ 1, Strauss(0.1))	Stationary Strauss process
$ppm(X \sim x, Strauss(0.1))$	Strauss process with
	conditional intensity loglinear in $x$

It is also possible to fit models that depend on other covariates.

## Manipulating the fitted model:

_	
plot.ppm	Plot the fitted model
<pre>predict.ppm</pre>	Compute the spatial trend and conditional intensity
	of the fitted point process model
coef.ppm	Extract the fitted model coefficients
parameters	Extract all model parameters
formula.ppm	Extract the trend formula
intensity.ppm	Compute fitted intensity
Kmodel.ppm	K function of fitted model
pcfmodel.ppm	pair correlation of fitted model
fitted.ppm	Compute fitted conditional intensity at quadrature points
residuals.ppm	Compute point process residuals at quadrature points
update.ppm	Update the fit
vcov.ppm	Variance-covariance matrix of estimates
rmh.ppm	Simulate from fitted model
simulate.ppm	Simulate from fitted model
print.ppm	Print basic information about a fitted model
summary.ppm	Summarise a fitted model
effectfun	Compute the fitted effect of one covariate
logLik.ppm	log-likelihood or log-pseudolikelihood
anova.ppm	Analysis of deviance
model.frame.ppm	Extract data frame used to fit model
model.images	Extract spatial data used to fit model
model.depends	Identify variables in the model
as.interact	Interpoint interaction component of model
fitin	Extract fitted interpoint interaction
is.hybrid	Determine whether the model is a hybrid
valid.ppm	Check the model is a valid point process
project.ppm	Ensure the model is a valid point process

For model selection, you can also use the generic functions step, drop1 and AIC on fitted point process models. For variable selection, see sdr.

See spatstat.options to control plotting of fitted model.

## To specify a point process model:

The first order "trend" of the model is determined by an R language formula. The formula specifies the form of the logarithm of the trend.

```
\begin{array}{lll} {\rm X} \sim {\rm 1} & {\rm No\ trend\ (stationary)} \\ {\rm X} \sim {\rm x} & {\rm Loglinear\ trend\ } \lambda(x,y) = \exp(\alpha + \beta x) \\ {\rm where\ } x,y \ {\rm are\ Cartesian\ coordinates} \\ {\rm X} \sim {\rm polynom(x,y,3)} & {\rm Log\text{-}cubic\ polynomial\ trend} \\ {\rm X} \sim {\rm harmonic(x,y,2)} & {\rm Log\text{-}harmonic\ polynomial\ trend} \\ {\rm X} \sim {\rm Z} & {\rm Loglinear\ function\ of\ covariate\ Z} \\ {\rm X}(x,y) = \exp(\alpha + \beta Z(x,y)) \end{array}
```

The higher order ("interaction") components are described by an object of class "interact". Such objects are created by:

Poisson() the Poisson point process

AreaInter() Area-interaction process
BadGey() multiscale Geyer process
Concom() connected component interaction
DiggleGratton() Diggle-Gratton potential
DiggleGatesStibbard() Diggle-Gates-Stibbard potential

DiggleGatesStibbard()

Fiksel()

Diggle-Gates-Stibbard potential

Fiksel pairwise interaction process

Geyer() Geyer's saturation process

Hard core process

HierHard() Hierarchical multippe hard core process
HierStrauss() Hierarchical multippe Strauss process

HierStraussHard() Hierarchical multiype Strauss-hard core process

Hybrid() Hybrid of several interactions
LennardJones() Lennard-Jones potential
MultiHard() multitype hard core process
MultiStrauss() multitype Strauss process

MultiStraussHard()multitype Strauss/hard core processOrdThresh()Ord process, threshold potentialOrd()Ord model, user-supplied potentialPairPiece()pairwise interaction, piecewise constantPairwise()pairwise interaction, user-supplied potential

Penttinen() Penttinen pairwise interaction

SatPiece() Saturated pair model, piecewise constant potential Saturated() Saturated pair model, user-supplied potential Softcore() pairwise interaction, soft core potential

Strauss () Strauss process

StraussHard() Strauss/hard core point process

Triplets() Geyer triplets process

Note that it is also possible to combine several such interactions using Hybrid.

## Finer control over model fitting:

A quadrature scheme is represented by an object of class "quad". To create a quadrature scheme, typically use quadscheme.

quadscheme default quadrature scheme

using rectangular cells or Dirichlet cells quadrature scheme based on image pixels

quad create an object of class "quad"

To inspect a quadrature scheme:

pixelquad

plot(Q) plot quadrature scheme Q

print(Q) print basic information about quadrature scheme Q

summary (Q) summary of quadrature scheme Q

A quadrature scheme consists of data points, dummy points, and weights. To generate dummy points:

default.dummy default pattern of dummy points
gridcentres dummy points in a rectangular grid
stratified random dummy pattern
spokes radial pattern of dummy points

corners dummy points at corners of the window

To compute weights:

gridweights quadrature weights by the grid-counting rule dirichletWeights quadrature weights are Dirichlet tile areas

#### Simulation and goodness-of-fit for fitted models:

rmh.ppm simulate realisations of a fitted model simulate.ppm envelope simulate realisations of a fitted model compute simulation envelopes for a fitted model

#### Point process models on a linear network:

An object of class "1pp" represents a pattern of points on a linear network. Point process models can also be fitted to these objects. Currently only Poisson models can be fitted.

lppm point process model on linear network anova.lppm analysis of deviance for point process model on linear network simulation envelopes for envelope.lppm point process model on linear network fitted.lppm fitted intensity values predict.lppm model prediction on linear network linim pixel image on linear network plot.linim plot a pixel image on linear network eval.linim evaluate expression involving images function defined on linear network linfun methods.linfun conversion facilities

#### V. MODEL FITTING (DETERMINANTAL POINT PROCESS MODELS)

Code for fitting *determinantal point process models* has recently been added to **spatstat**.

For information, see the help file for dppm.

## VI. MODEL FITTING (SPATIAL LOGISTIC REGRESSION)

## Logistic regression

Pixel-based spatial logistic regression is an alternative technique for analysing spatial point patterns that is widely used in Geographical Information Systems. It is approximately equivalent to fitting a Poisson point process model.

In pixel-based logistic regression, the spatial domain is divided into small pixels, the presence or absence of a data point in each pixel is recorded, and logistic regression is used to model the presence/absence indicators as a function of any covariates.

Facilities for performing spatial logistic regression are provided in **spatstat** for comparison purposes.

## Fitting a spatial logistic regression

Spatial logistic regression is performed by the function slrm. Its result is an object of class "slrm". There are many methods for this class, including methods for print, fitted, predict, simulate, anova, coef, logLik, terms, update, formula and vcov.

For example, if X is a point pattern (class "ppp"):

command model

slrm(X ~ 1) Complete Spatial Randomness
slrm(X ~ x) Poisson process with
intensity loglinear in x coordinate
slrm(X ~ Z) Poisson process with
intensity loglinear in covariate Z

## Manipulating a fitted spatial logistic regression

anova.slrm Analysis of deviance coef.slrm Extract fitted coefficients vcov.slrm Variance-covariance matrix of fitted coefficients fitted.slrm Compute fitted probabilities or intensity Evaluate loglikelihood of fitted model logLik.slrm plot.slrm Plot fitted probabilities or intensity predict.slrm Compute predicted probabilities or intensity with new data Simulate model simulate.slrm

There are many other undocumented methods for this class, including methods for print, update, formula and terms. Stepwise model selection is possible using step or stepAIC. For variable selection, see sdr.

## VII. SIMULATION

There are many ways to generate a random point pattern, line segment pattern, pixel image or tessellation in **spatstat**.

## **Random point patterns:**

runifpoint	generate $n$ independent uniform random points
rpoint	generate $n$ independent random points
rmpoint	generate $n$ independent multitype random points
rpoispp	simulate the (in)homogeneous Poisson point process
rmpoispp	simulate the (in)homogeneous multitype Poisson point process
runifdisc	generate $n$ independent uniform random points in disc
rstrat	stratified random sample of points
rsyst	systematic random sample (grid) of points
rMaternI	simulate the Matérn Model I inhibition process
rMaternII	simulate the Matérn Model II inhibition process
rSSI	simulate Simple Sequential Inhibition process
rHardcore	simulate hard core process (perfect simulation)
rStrauss	simulate Strauss process (perfect simulation)
rStraussHard	simulate Strauss-hard core process (perfect simulation)
rDiggleGratton	simulate Diggle-Gratton process (perfect simulation)
rDGS	simulate Diggle-Gates-Stibbard process (perfect simulation)
rPenttinen	simulate Penttinen process (perfect simulation)
rNeymanScott	simulate a general Neyman-Scott process
rMatClust	simulate the Matérn Cluster process
rThomas	simulate the Thomas process
rLGCP	simulate the log-Gaussian Cox process
rGaussPoisson	simulate the Gauss-Poisson cluster process

rCauchy simulate Neyman-Scott process with Cauchy clusters simulate Neyman-Scott process with Variance Gamma clusters

rcell simulate the Baddeley-Silverman cell process

#### Resampling a point pattern:

quadratresample block resampling

rjitter apply random displacements to points in a pattern

rshift random shifting of (subsets of) points

rthin random thinning

See also varblock for estimating the variance of a summary statistic by block resampling, and lohboot for another bootstrap technique.

#### **Fitted point process models:**

If you have fitted a point process model to a point pattern dataset, the fitted model can be simulated.

Cluster process models are fitted by the function kppm yielding an object of class "kppm". To generate one or more simulated realisations of this fitted model, use simulate.kppm.

Gibbs point process models are fitted by the function ppm yielding an object of class "ppm". To generate a simulated realisation of this fitted model, use rmh. To generate one or more simulated realisations of the fitted model, use simulate.ppm.

## Other random patterns:

rlinegrid generate a random array of parallel lines through a window simulate the Poisson line process within a window generate random tessellation using Poisson line process rMosaicSet generate random set by selecting some tiles of a tessellation generate random pixel image by assigning random values in each tile of a tessellation

#### **Simulation-based inference**

envelope critical envelope for Monte Carlo test of goodness-of-fit critical envelope for balanced two-stage Monte Carlo test diagnostic plot for interpoint interaction spatial scan statistic/test

studpermu.test studentised permutation test segregation.test test of segregation of types

#### VIII. TESTS AND DIAGNOSTICS

## **Hypothesis tests:**

quadrat.test  $\chi^2$  goodness-of-fit test on quadrat counts

cdf.test Spatial distribution goodness-of-fit test

berman.test Berman's goodness-of-fit tests

envelope critical envelope for Monte Carlo test of goodness-of-fit

scan.test spatial scan statistic/test

dclf.test Diggle-Cressie-Loosmore-Ford test

mad.test	Mean Absolute Deviation test
anova.ppm	Analysis of Deviance for point process models

More recently-developed tests:

dg.test	Dao-Genton test
bits.test	Balanced independent two-stage test
dclf.progress	Progress plot for DCLF test
mad.progress	Progress plot for MAD test

## Sensitivity diagnostics:

Classical measures of model sensitivity such as leverage and influence have been adapted to point process models.

```
leverage.ppm Leverage for point process model Influence.ppm dfbetas.ppm dffit.ppm Leverage for point process model Parameter influence diagnostic
```

## **Diagnostics for covariate effect:**

Classical diagnostics for covariate effects have been adapted to point process models.

```
parres Partial residual plot
addvar Added variable plot
rhohat Kernel estimate of covariate effect
rho2hat Kernel estimate of covariate effect (bivariate)
```

## **Residual diagnostics:**

Residuals for a fitted point process model, and diagnostic plots based on the residuals, were introduced in Baddeley et al (2005) and Baddeley, Rubak and Møller (2011).

Type demo(diagnose) for a demonstration of the diagnostics features.

diagnose.ppm	diagnostic plots for spatial trend
qqplot.ppm	diagnostic Q-Q plot for interpoint interaction
residualspaper	examples from Baddeley et al (2005)
Kcom	model compensator of $K$ function
Gcom	model compensator of $G$ function
Kres	score residual of $K$ function
Gres	score residual of $G$ function
psst	pseudoscore residual of summary function
psstA	pseudoscore residual of empty space function
psstG	pseudoscore residual of $G$ function
compareFit	compare compensators of several fitted models

## Resampling and randomisation procedures

You can build your own tests based on randomisation and resampling using the following capabilities:

```
quadratresample block resampling
```

rjitter apply random displacements to points in a pattern random shifting of (subsets of) points random thinning

#### IX. DOCUMENTATION

The online manual entries are quite detailed and should be consulted first for information about a particular function.

The book Baddeley, Rubak and Turner (2015) is a complete course on analysing spatial point patterns, with full details about **spatstat**.

Older material (which is now out-of-date but is freely available) includes Baddeley and Turner (2005a), a brief overview of the package in its early development; Baddeley and Turner (2005b), a more detailed explanation of how to fit point process models to data; and Baddeley (2010), a complete set of notes from a 2-day workshop on the use of **spatstat**.

Type citation("spatstat") to get a list of these references.

#### Licence

This library and its documentation are usable under the terms of the "GNU General Public License", a copy of which is distributed with the package.

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