3 Panel data

LPO 8852: Regression II

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LPO 8852 (Corcoran)

Lecture :

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Matching and weighting recap

Matching and weighting approaches seek to construct a comparison group where the conditional independence assumption is satisfied:

$$Y(0), Y(1) \perp \!\!\!\perp D|X$$

That is, conditional on X (or a one-number summary like the propensity score), potential outcomes are independent of treatment status D. If this holds, we can use mean outcomes of the matched or weighted comparison group as a stand-in for the treated group counterfactual.

$$\underbrace{E[Y(0)|D=1,X]}_{\text{unobserved}} = \underbrace{E[Y(0)|D=0,X]}_{\text{matched comparison group}}$$

Matching and weighting recap

Challenges:

- The conditional independence assumption (selection on observables) is strong! In most settings we have to be concerned about selection on unobservables
- Constructing matched samples is somewhat of an art, and results may be sensitive to specification of the matching model.
- We are typically comparing outcomes at one point in time (e.g., post treatment).

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Panel data

Panel, longitudinal, or "cross-sectional time series" data consist of observations on cross-sectional units (e.g., students, schools, hospitals, neighborhoods, counties, states) at multiple points in time.

- N cross-sectional (panel) units and T time periods ($T \ge 2$)
- A balanced panel has exactly N × T observations (T time observations for all N panel units)
- An unbalanced panel has T_i observations for panel unit i, where T_i is not the same for all i

Differs from a *pooled cross-section*, although panel methods can be used with this type of data.

Panel data - long

Panel data in *long* format, N students in T=4 years:

studentID	year	readscore	mathscore	incomecat	
1	1999	75	82	3	
1	2000	78	84	4	
1	2001	80	90	4	
1	2002	<i>7</i> 8	91	3	
2	1999	91	92	2	
2	2000	94	92	2	
2	2001	80	85	2	
2	2002	87	83	2	
3	1999	62	50	5	
3	2000	70	47	5	
3	2001	75	55	4	
3	2002	73	60	5	

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Panel data - wide

Panel data in wide format, N students in T=4 years:

studentID	read99	math99	inc99	read00	math00	inc00	read01	
1	75	82	3	78	84	4	80	
2	91	92	2	94	92	2	80	
3	62	50	5	70	47	5	75	
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Panel data - reshape long

Moving between *long* and *wide* format in Stata with reshape, beginning with *wide* data:

- i() contains the time invariant variables (e.g., ID, gender)
- j() specifies the time variable to be created (e.g., year)
- The list of time varying variables are "stubs" that end in the j suffix

reshape long stubnames, i(varlist) j(varname)

- If j() consists of string rather than numeric values, use the string option
- Example time-varying variable names: score98, score99, score00 (Stata will have problems with 00 as a j() value if string option is not used).

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Panel data - reshape wide

Moving between *long* and *wide* format in Stata with reshape, beginning with *long* data:

- i() contains the time invariant variables (e.g., ID, gender)
- j() specifies the time variable (e.g., year)
- The list of time varying variables are "stubs" that will end in the j suffix, once converted to wide

reshape wide stubnames, i(varlist) j(varname)

- After reshaping, Stata allows you to revert back easily without losing information. E.g., after the above command just type reshape long
- Most panel regression commands expect the data to be in long format.

In-class example 1

Illustration of reshape commands using Census_states_1970_2000 data:

- Cross sectional unit: state
- Time variable: year (decennial Census years)
- Time-varying variables: median household income, unemployment rate

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Stata panel commands

Stata has many useful xt commands for working with panel data. Typically these require that you first declare the data to be a panel using xtset:

- xtset panelvar timevar
- The panelvar must be numeric. If it is not, you can use encode: encode panelvar, gen(panelvar2)
- It is possible to tell Stata in the xtset options what units of time the data represent—e.g., years, quarters, minutes (useful for some purposes–I don't usually do this)
- xtset alone will report back the panel settings

Stata panel commands

Other useful Stata panel data commands for description:

- xtdescribe—to see patterns of participation/data availability
- xtsum—for descriptive statistics that show between- and within-unit variation
- xttab—for one-way tabulations with separate counts within and between units
- xttrans—for transition probabilities (movement between categories of a categorical variable)
- xtline and xtline, overlay—for separate line graphs by panel unit (see in-class example)

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Stata panel commands

Other useful Stata commands when working with panels:

- duplicates report varnames—to affirm that there is one only observation per unit per time period
- isid varnames—same: affirms that combinations of varnames uniquely identify the observations

xtsum

Decomposition of variation in xtsum:

$$s_w^2 = \frac{1}{NT - 1} \sum_{i} \sum_{t} (X_{it} - \bar{X}_i)^2$$
$$s_b^2 = \frac{1}{N - 1} \sum_{i} (\bar{X}_i - \bar{X})^2$$
$$s_o^2 = \frac{1}{NT - 1} \sum_{i} \sum_{t} (X_{it} - \bar{X})^2$$

Note \bar{X} is the grand mean of X. Can also write:

$$s_w^2 = \frac{1}{NT - 1} \sum_{i} \sum_{t} (X_{it} - \bar{X}_i + \bar{X})^2$$

because adding a constant (\bar{X}) will not affect s_w^2 .

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xtsum

xtsum also shows the min and max of:

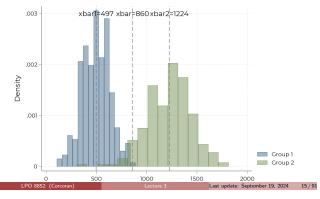
- X_{it}: overall
- \bar{X}_i : between
- $(X_{it} \bar{X}_i + \bar{X})$: within

Note: on xtsum, see also https://www.stata.com/support/faqs/ statistics/decomposed-variances-in-xtsum/

- Between and within variation do not sum to overall
- \bullet With unbalanced panels, s_b is calculated using mean of panel means, not \bar{X} (may not be the same)

xtsum

Simulated data, two groups (N=250 each): within vs. between variation



In-class example 2

Illustration of xt commands using State_school_finance_panel data:

- Cross sectional unit: state
- Time variable: year (annual 1990-2010)
- Time-varying variables: various school finance measures

Panel data - advantages

Why use panel data?

- Can help us answer questions not possible with a cross-section or time-series approach
- Can generate measures not possible with cross-sectional or time series data (e.g., growth, work spells, turnover)
 - ► If 50% of women are working in year t, does this reflect 50% of women working at any given point, or 50% of women who work all the time?
- Allows us to address selection bias due to unobserved heterogeneity that is fixed over time ("fixed effects")

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Selection bias revisited

Lecture 1: interpretation of regression coefficients as causal is often complicated by selection bias. Example:

$$Y_i = \beta_0 + \beta_1 X_i + u_i$$

with $E(u_i|X_i) \neq 0$ because we believe potential outcomes are not independent of X. We can attempt to mitigate selection bias through the inclusion of additional covariates or matching/weighting, but this only solves the problem if adjusting for these observables eliminates OVB.

In practice we are often more concerned about selection on unobservables.

Unobserved heterogeneity

Suppose there are **unobserved**, **fixed differences** across units (C_i) that affect the outcome and are (potentially) correlated with the explanatory variable of interest (X_i) :

$$Y_i = \beta_0 + \beta_1 X_i + C_i + u_i$$

 C_i could represent the effects of ability, health, motivation, intelligence, county of birth, parental resources, managerial quality, organizational culture, state/local policies or regulations, etc.

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First difference model

Suppose we have two time periods (T=2) for each cross-sectional unit i, and assume the linear model above applies in both periods:

$$Y_{i2} = \beta_0 + \beta_1 X_{i2} + C_i + u_{i2}$$
$$Y_{i1} = \beta_0 + \beta_1 X_{i1} + C_i + u_{i1}$$

Now subtract period 1 from period 2 for the "first difference":

$$\Delta Y_i = \beta_1 \Delta X_i + \Delta u_i$$
$$Y_i^* = \beta_1 X_i^* + u_i^*$$

Because C_i is time-invariant, it differences out of the model. Notice the constant β_0 also differences out.

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First difference model

 β_1 can be identified from the first difference model using OLS as long as the usual OLS assumptions apply to it:

- The new error term $u_i^* = \Delta u_i$ (change in the unobserved residual over time) is uncorrelated with the new explanatory variable, $X_i^* = \Delta X_i$ (change in the observed X over time).
- This requires that we have no cross-period correlations between u and X: this is called strict exogeneity.
- The X_i must vary over time for at least some i, else they difference out.

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In-class example 3

Example using panel of Texas elementary schools:

- use Texas_elementary_panel_2004_2007.dta
- xtset campus year
- xtdescribe
- rename ca311tar avgpassing
- egen avgclass = rowmean(cpctg01a-cpctgmea)
- reg avgpassing avgclass if year == 2007 (cross-sectional regression for 2007)

Note: avgclass is the mean class size across grades, and avgpassing is the school average passing rate across grades and subjects.

In-class example 3

Having declared the dataset as a panel, Stata recognizes the d. prefix as a "difference operator":

- reg d.avqpassing d.avqclass if year == 2007, noconstant
- This is the first difference regression, using 2007 only (and its <u>lag</u> in the calculation of *d.avgpassing* and *d.avgclass*)
- d. can be used after xtset or tsset (time series set)
- Note suppression of the constant. In theory the constant term differences out. In practice can still estimate with a constant, which allows for a year-to-year time trend.

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In-class example 3

A few things to note in example 3:

- Change in coefficient on class size: does it make sense?
- Change in sample size (re: unbalanced panel due to missing values)

A few things to think about:

- Is strict exogeneity likely to hold in this circumstance?
- Where is the identifying variation coming from?
- How much variation is there in the *change* in passing rates (ΔY) and class size (ΔX) ?
- Do outliers dominate the variation in changes?

gen davgpassing = d.avgpassing

/* create variable containing FD that can be described */

In-class example 3

The first difference model is easily generalizable to multiple years (T > 2).

- Each year of data is differenced with the prior year
- 1st period is sacrificed
- · Must continue to think about OLS assumptions, e.g. strict exogeneity

reg d.avgpassing d.avgclass, noconstant table year if e(sample)

* note 1st year of data is not used

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Fixed effects model

Alternatively, in the (one-way) fixed effects model, we could treat the C_i as parameters to be estimated (the "fixed effects"):

$$Y_{it} = \beta_0 + \beta_1 X_{it} + C_i + u_{it}$$

Effectively we are allowing for a *unique intercept* for every cross-sectional unit i. This is feasible to estimate since each i is observed multiple times.

Note on notation: in practice we cannot estimate β_0 and intercepts for the N cross-sectional units (re: collinearity). Often you will see fixed effects models (more precisely) written without the β_0 .

Fixed effects model: notation

You may see the fixed effects model written something like this:

$$Y_{it} = \beta_1 X_{it} + \sum_{i=1}^n \mathbf{1}(i=j)\gamma_i + u_{it}$$

Where $\mathbf{1}(i=j)$ is an indicator function that equals 1 when i=j. The n γ_i s are the fixed effects to be estimated. More often, it is written more concisely as:

$$Y_{it} = \beta_1 X_{it} + \gamma_i + u_{it}$$

where it is understood that the γ_i represent the n fixed effects to be estimated

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"Least squares dummy variables" approach

Now we are estimating β_0 , β_1 , and (N-1) fixed effects. This can be done by including N-1 dummy variables in the regression, one for each cross sectional unit (omitting one). This is sometimes called the "least squares dummy variable" (LSDV) model:

- reg avgpassing avgclass i.campus
- For this example limit to year>=2006 and houston==1 so that the number of schools is manageable.

Note omission of first cross-sectional unit with i.campus. Interpretation of the ${\it N}-1$ fixed effects are relative to this (arbitrary) omitted unit. You can control which unit is omitted if desired. See in-class example.

"Least squares dummy variables" approach

There are a number of reasons why you might not want to do it this way:

- Could be time-consuming and harder on memory with very large datasets (re: you are creating dummy variables for each unique i)
- Soaks up degrees of freedom; may result in the number of regressors exceeding the number of observations
- Often we are not interested in the estimates of the fixed effects themselves, so there is no need to see/report them.
- Exception: recent "school effects" and "teacher effects" studies work
 explicitly with fixed effects estimates (Ĉ_i)—but more on this later

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Within transformation

Suppose that panel data are available with multiple observations per i and the model is:

$$Y_{it} = \beta_1 X_{it} + C_i + u_{it}$$
 $t = 1, ..., T$ $\forall i$

Within each panel unit i, take the average over t on both sides and subtract the unit average from each it observation:

$$\begin{split} \bar{Y}_i &= \beta_1 \bar{X}_i + C_i + \bar{u}_i \\ Y_{it} - \bar{Y}_i &= \beta_1 (X_{it} - \bar{X}_i) + (u_{it} - \bar{u}_i) \end{split}$$

This is called "de-meaning" or the "within" transformation (sometimes denoted \dot{Y}_i) or "absorbing" the fixed effect. Notice that the intercepts C_i "difference out." This can only happen if the C_i are truly time invariant.

Within transformation

Under certain assumptions, an OLS regression of the de-meaned Y on the de-meaned X will yield unbiased and consistent estimates of β_1 .

$$Y_{it} - \bar{Y}_i = \beta_1(X_{it} - \bar{X}_i) + (u_{it} - \bar{u}_i)$$

$$Y_{it}^* = \beta_1 X_{it}^* + u_{it}^*$$

This is also known as the fixed effects or "within" regression, and extends to more than one explanatory variable $(X_1, ..., X_k)$.

Explanatory variables X_j that are time *invariant* fall out of the model. (They all equal their within-group mean, so the within-transformation equals zero). Common examples: gender, race or ethnicity, birthplace...

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Within transformation (FWL)

Another way to see the equivalency between LSDV and the within transformation is by applying the Frisch-Waugh-Lovell (FWL) theorem. FWL says the estimated coefficient on X_1 in a regression of Y on X_1 and X_2 will be the same as the coefficient resulting from the following:

- \bigcirc Regress X_1 on X_2 and get the residuals
- \bigcirc Regress Y on X_2 and get the residuals
- Regress the residuals in (2) on the residuals in (1)

Intuition: the residuals in (1) represent the part of X_1 that is unexplained by X_2 . The residuals in (2) represent the part of Y that is unexplained by X_2 . Part (3) is the bivariate relationship between "what's leftover".

Within transformation (FWL)

Suppose we have the following one-way fixed effects model with one covariate *X*:

$$Y_{it} = \beta_1 X_{it} + \gamma_i + u_{it}$$

Regressing X_{it} on a set of dummy variables (D_i) for the i units:

$$X_{it} = \sum_{i=1}^{n} D_i \alpha_i + v_{it}$$

The $\hat{\alpha}_i$ are just the unit means \bar{X}_i . So the residuals \hat{v}_{it} are:

$$\hat{v}_{it} = X_{it} - \bar{X}_i$$

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Within transformation (FWL)

Regressing Y_{it} on a set of dummy variables (D_i) for the i units:

$$Y_{it} = \sum_{i=1}^{n} D_i \delta_i + w_{it}$$

The $\hat{\delta}_i$ are just the unit means \bar{Y}_i . So the residuals \hat{w}_{it} are:

$$\hat{w}_{it} = Y_{it} - \bar{Y}_i$$

So, regressing \hat{w}_{it} on \hat{v}_{it} means you are regressing:

$$Y_{it} - \bar{Y}_i = \beta_1 (X_{it} - \bar{X}_i) + u_{it}$$

You will get the same estimate for β_1 !

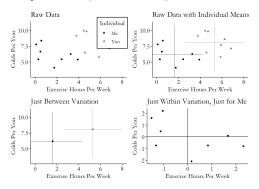
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Within transformation: illustrated

From Huntington-Klein chapter 16: relationship between exercise and colds



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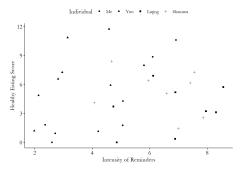
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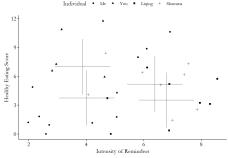
Within transformation: illustrated

Huntington-Klein Figure 16.4: intensity of reminders and healthy eating score, raw data (r=0.111)



Within transformation: illustrated

Huntington-Klein Figure 16.5: four individuals differ in their mean y and x. If we use only the *between* variation, there is a clear negative relationship (r = -0.440)



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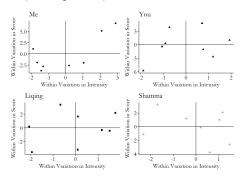
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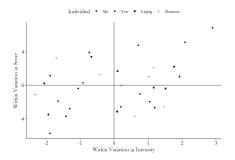
Within transformation: illustrated

Huntington-Klein Figure 16.6: remove between variation and focus on within. Data plotted again with person means centered at zero.



Within transformation: illustrated

Huntington-Klein Figure 16.7: overlay the "within" plots to see all of the within variation. The correlation is more positive (r = 0.363).



See also the animated gif FEanimation on Github

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Within transformation: xtreg

The fixed effects or "within" regression model can be estimated using OLS using xtreg:

- xtreg avgpassing avgclass, fe
- Note xtset must have been declared, or specify the cross-sectional unit in the options, e.g. i(campus)
- While the fixed effects are not estimated directly, can "back out" a prediction: $\hat{C}_i = \bar{Y}_i - \bar{X}_i \hat{\beta}_1$
- predict schlfe, u

Note the estimated fixed effects from xtreg are not the same as the dummy coefficients from the LSDV model. See the do file Simulated panel data for an illustration.

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Within transformation: areg

The areg command also absorbs fixed effects by de-meaning within group:

- areg avgpassing avgclass, absorb(campus)
- As with xtreg the fixed effect coefficients are not estimated/reported
- Here again can "back out" the fixed effects using predict. For example: predict schlfe, d
- ullet The intercept is not specific to any omitted group, but rather the intercept that makes the prediction calculated at the means of the X equal to \bar{Y}

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Within transformation: areg

- areg is intended for applications where the number of cross-sectional units or categories is fixed (e.g., states) and does not grow as the sample size gets larger. Many panel applications are the latter, so use of xtreg is advised. See later notes on standard error calculations.
- The R², RMSE, standard errors, etc., in areg are the same as the LSDV using reg. The model F statistic is different, however. It only tests the joint significance of the X (excluding the fixed effects).

Within transformation: transforming the dataset

The command xtdata, fe can be used to transform your dataset using the within-transformation. However, this is rarely done (in my experience) since it transforms *all* of the variables in your dataset. xtreg will do the transformation on the fly without altering your dataset.

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Fixed effects model

Compare xtreg, areg and first difference when T=2

- xtreg avgpassing avgclass3, fe
- areg avgpassing avgclass3, absorb(campus)
- reg d.avqpassing d.avqclass3, noconstant

Fixed effects model

A few notes about xtreg, fe

- FE is more efficient (smaller standard errors) than first differencing if the error terms are serially uncorrelated and T > 2
- Assumes no correlation in u across units of panel i (some tests for this using user-written xtscd, xttest3)
- The estimates of the fixed effects themselves (C_i) are unbiased but inconsistent in large samples. (Why? As the number of panel units grows (N → ∞) the number of parameters to estimate also grows).
- xtreg has not historically allowed svy specification (for complex sampling designs) but can use pweights and cluster() option. See also the mixed (or xtmixed) command for an alternative.

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Fixed effects model

Stata actually fits the following model with xtreg:

$$(Y_{it} - \bar{Y}_i + \bar{Y}) = \beta_0 + \beta_1 (X_{it} - \bar{X}_i + \bar{X}) + (u_{it} - \bar{u}_i + \bar{u})$$

Where the values with a bar but no subscript are the grand means. This includes an intercept which is the average of the fixed effects (C_i) .

Fixed effects model

Other useful output from xtreg:

	ssing avgclas					
ixed-effects roup variabl	(within) reg e: campus	ression		Number of Number of		
betwee	= 0.0039 n = 0.0087 l = 0.0032			Obs per g	group: min = avg = max =	1.9
orr(u_i, Xb)	= -0.1079			F(1,169) Prob > F	=	
avgpassing	coef.	Std. Err.	t	P> t	[95% Conf.	Interval]
avgclass3 _cons	2390704 76. 80355	. 294385 6. 032673	-0.81 12.73	0.418 0.000	820216 64. 89445	
		6. 032673	12.73		64.89445	. 3420752 88. 71265

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Fixed effects model

Other useful output from xtreg:

- F-test for joint significance of fixed effects (null hypothesis H₀ is that all fixed effects are zero). If rejected, fixed effects model is a reasonable assumption and regular OLS may provide inconsistent estimates. In practice, rarely rejected.
- R² within: variance "explained" by within-group deviations from group means
- R^2 between: variance in group means \bar{Y}_i "explained" by the group mean X's: \bar{X}_i
- $sigma_u$ estimate of the standard deviation in fixed effects (C_i)

Fixed effects model: assumptions for inference

- **FE.1:** linear model $Y_{it} = \beta_1 X_{it1} + ... + \beta_k X_{itk} + C_i + u_{it}$
- FE.2: cross-sectional units are a random sample
- FE.3: Xit varies over time for some i, no perfect collinearity
- FE.4: ∀t, E(u_{it}|X_i, C_i) = 0 or the expected value of u given X in all time periods is zero (strict exogeneity)
- **FE.5**: $Var(u_{it}|X_i, C_i) = Var(u_{it}) = \sigma_u^2$ homoskedasticity
- **FE.6:** for $t \neq s$ errors are uncorrelated: $Cov(u_{it}, u_{is}|X_i, C_i) = 0$. No serial correlation.

Under FE.1-FE.4, fixed effects model (and first difference model) is unbiased. Adding FE.5-FE.6, fixed effects model is BLUE. If FE.6 holds, fixed effects is more efficient than the first difference model. Can relax homoskedasticity assumption and calculate robust standard errors.

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Fixed effects model: assumptions for inference

Note: the econometric theory described here is for "short" panels, with N large relative to T. If the opposite is true in your context, use FE model with caution (see Wooldridge chapter 14, Cameron & Trivedi).

Fixed effects model: considerations

Fixed effects considerations:

- Where is the identification coming from?
- How much variation is there within panel units? When small, one risks imprecise estimates
- For stats on within- and between- school variation can use xtsum (described earlier), xttab and xttrans for categorical variables
- Example:

xtsum avgpassing avgclass

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Panel data models: on standard errors

With panel data it is hard to assume that errors are independent. You have multiple observations from the same cross-sectional unit and there is likely to be something omitted from the model that is correlated across observations.

- Should almost always use clustered standard errors with FE (at the same level as FE): vcecluster varname
- Note areg by default uses traditional OLS standard errors, although this can be adjusted
- With xtreg, using robust standard errors is equivalent to clustering on the cross-sectional unit, since Stata takes the panel structure into account.

Two-way fixed effects model

The two-way fixed effects model adds another dimension of fixed effects (often time periods). There is no explicit command for two-way models, rather can just include time dummies. Alternatively, reghdfe

```
xtreg avgpassing avgclass i.year, fe
* the i.year syntax introduces (T-1) time effects
test _Iyear_2006 _Iyear_2007
* joint test that time effects = 0
reghdfe avgpassing avgclass, absorb(campus year)
```

As with one-way fixed effects model, requires variation across units within time periods $\it t$.

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Two-way fixed effects model

The generalized difference-in-differences model is a two-way fixed effects model (covered in Lecture 4):

$$Y_{it} = \beta_0 + \beta_1(treat_i \times post_t) + \alpha_t + \gamma_i + \delta X_{it} + u_{it}$$

There are cross-sectional unit fixed effects (γ_i) which represent separate intercepts for each unit and time effects (α_t) which represent common variation over time within group.

Comparison of models

It is important to be attentive to where the variation in each type of FE model is coming from:

- Fixed effects ("within") model: uses deviations from group (i) means, e.g., mean "pre" vs. mean "post"
- First differences model: uses variation in successive time periods, e.g., just prior to and just after a "treatment" (a change in x)
- Long differences is like first differences, but there is a long time span between observations. Here outcomes may be compared well before and well after a "treatment"

To evaluate these in your situation, need some idea of the speed in which X affects Y

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Comparison of models



Source: Nichols (2007). Figure shows one panel (i)'s contribution to the estimated effect of a treatment that =1 in post period (t>4). Notice the different treatment effects depending on FE, FD, or LD.

Fixed effects models in other applications

Fixed effects models are not exclusively used with panel data in which cross-sectional units i are observed in multiple time periods. They are also used with grouped or clustered data. For example:

- Family fixed effects, where the family is the cross-sectional unit and siblings are the group members (akin to the time dimension)
- School fixed effects with student-level data, where each school has its own intercept

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Fixed effects models in other applications

The researcher needs to provide a convincing rationale for why the unobserved variable should be considered fixed across multiple observations (e.g., siblings, years)

- Why did a mother's employment status change between siblings?
- Why did only 1 of 2 siblings participate in Head Start?
- Why did a student switch from a traditional school to a charter school?
- Why did an elementary school receive a new principal?

Fixed effects models: advantages and disadvantages

Advantages:

- \bullet Unobserved C_i can be correlated with the explanatory variables
- Slopes estimated using within-group (i) variation in X, Y

Disadvantages:

- Cannot estimate slope coefficients for time-invariant X
- Fixed effects "remove" a lot of the variation in Y
- The "within" model is less efficient (higher standard errors)
- There may be more measurement error (and attenuation bias, see Lecture 7) when relying on within-group changes vs. levels
- Group intercepts use up a lot of degrees of freedom

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Bonus slides: random effects models

Random effects

An alternative conception of C_i is as a random effect, uncorrelated with X_{it} .

$$Y_{it} = \beta_0 + \beta_1 X_{it} + \underbrace{C_i + e_{it}}_{V_{it}}$$

Think of v_{it} as a *composite* error consisting of a between-group component (C_i) common to all observations within the group, and a within-group component (e_{it}) . It is assumed C_i and e_{it} are independent of one another and:

$$C_i \sim N(0, \sigma_c^2)$$

 $e_{it} \sim N(0, \sigma_c^2)$

This is the random effects or random intercepts model.

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Random effects

If C_i is uncorrelated with X_{it} , then the composite error term v_{it} is uncorrelated with X_{it} . (We already assume e_{it} is uncorrelated with X_{it} .) This means the OLS estimator for β_1 will be unbiased and consistent.

Note: estimation of this model does *not* involve estimating the C_i 's as parameters as was done in the LSDV model.

Random effects

The composite error term v_{it} is not, however, i.i.d.:

$$Corr(v_{it}, v_{is}) = \rho = \frac{\sigma_c^2}{\sigma_c^2 + \sigma_e^2} \text{ for } s \neq t$$

The common error for observations in group $i(c_i)$ results in correlation between the composite error in period $t(v_{it})$ and in period $s(v_{is})$.

This means OLS is consistent but not efficient, and that traditional standard error formulas assuming i.i.d. errors are incorrect. The ratio above (ρ) is called the **intra-class correlation**.

Estimation using GLS (details later): xtreg, re.

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Success for All example

- Success for All is a whole-school literacy intervention.
- Borman et al. (2005) conducted a randomized evaluation of SFA in 2001-02 and 2002-03 (21 treatment schools and 20 control).
- This was a cluster-randomized design with randomization at the school level.
- The data used by Murnane & Willett (ch7_sfa.dta) include grade 1 only. The outcome of interest is wattack, the student's score on a "Word-Attack" test.

Next slide: an "unconditional" model with no X_{it} estimates variance components σ_c^2 and σ_e^2 and the intra-class correlation ρ . This provides a sense of the degree of between- vs. within-group variance in the outcome.

Random effects with xtreg

2,334	of obs =	Number of			Lon	s GLS regress:	Random-effects		
41	of groups =	Number of				: schid	Group variable		
	group;	Obs per q					R-sq:		
10	min =					0.0000	within =		
56.9	avg =			between = 0.0000					
134	max =					- 0.0000	overall =		
	2(0) =	Wald chi2							
					43	= 0 (assumed	corr(n i X)		
	chi2 =	Prob > ch			.,	- (0011(4_1) 11/		
	95% Conf.		z	Err.		Coef.	wattack		
Interval]			z 329.99	Err.	Std.				

This example: Success for All impact evaluation (from Murnane & Willett). $\sigma_c^2 = 8.87^2 = 78.7$ and $\sigma_e^2 = 17.73^2 = 314.35$. $\rho = 0.200$.

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loneway

loneway (one-way ANOVA) is another handy command for estimating variance components and ICC. (Note the difference in σ_c and ρ from xtreg, re. With unbalanced panels, these will differ slightly).

	One-way Anal	ysis of Vari	ance for		ck: word a mber of ob R-square	os =	2,334 0.2185
Sou	rce	SS	df	MS		F	Prob > I
Between schid Within schid		201450.43 720466.21			. 2607 20244	16.03	0.0000
Total		921916.63	2,333	395.	16358		
	Intraclass correlation	Asy. S.E.	[95%	Conf.	Interval]		
	0.20993	0.04402	0.1	2366	0.2962	L	
	Estimated SD Estimated SD Est. reliabi (evalua	within schi	d chid mean		9.137203 17.72576 0.93763	5	

Random effects with xtreg

Random-effect:		ion		Number	of obs	-	
Group variable	: schid			Number	of grou	= aqu	41
R-sq:		Obs per group:					
within -		min =					
	between - 0.3960					avg =	56.9
overall -	- 0.1820					max -	134
				Wald ch			
corr(u_i, X)	= 0 (assume	i)		Wald ch Prob >			
corr(u_i, X)		d) Std. Err.	z	Prob >	chi2	=	0.0000
		Std. Err.		Prob >	chi2 [95%	= b Conf.	0.0000
wattack	Coef.	Std. Err.	1.50	Prob > P> z	chi2 [959	= b Conf.	0.0000 Interval]
wattack	Coef.	Std. Err.	1.50 17.45	Prob > P> z	Chi2 [959 -1.06	= b Conf.	0.0000 Interval] 7.943485 .5396771
wattack sfa ppvt	Coef. 3.440921 .4851754	Std. Err. 2.297268 .0278075	1.50 17.45	Prob > P> z 0.134 0.000	Chi2 [959 -1.06	= Conf. 51642 06737	0.0000 Interval] 7.943485 .5396771
wattack sfa ppvt _cons	Coef. 3.440921 .4851754 432.0475	Std. Err. 2.297268 .0278075	1.50 17.45	Prob > P> z 0.134 0.000	Chi2 [959 -1.06	= Conf. 51642 06737	0.0000 Interval]

This regression: includes the treatment indicator (sfa) and one covariate (ppvt). Note changes in σ_c and σ_e , ρ . The residual variability is reduced with the inclusion of X's.

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Random effects

Class size and passing rates in TX class size example:

. xtreg avgpassing avgclass, re i(campus) Number of obs = 16,062 Random-effects GLS regression Group variable: campus Number of groups -Obs per group: within = 0.0018 min = between = 0.0098 avg = 3.7 overall - 0.0060 max -Wald chi2(1) 2.74 corr(u i, X) = 0 (assumed)Prob > chi2 0.0978 avgpassing Coef. Std. Err. P>1z1 195% Conf. Intervall -.0442893 .0267548 -1.66 76.21828 .5503649 138.49 -.0967277 0081491 avgclass -1.66 0.098 cons 0.000 75.13959 77.29698 sigma u 12.391941 sigma_e 6.4870883 .78490199 (fraction of variance due to u i)

Random effects

Compare to fixed effects: very different slope coefficient estimate.



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Random vs. fixed effects

- The RE model is biased and inconsistent if the FE assumptions are more appropriate (correlation between X_{it} and C_i).
- If the RE assumptions hold (<u>no</u> correlation between X_{it} and C_i), both RE and FE are consistent. They should give "similar" answers in large samples, but the FE model will be inefficient (larger standard errors).
- A sufficiently large difference in point estimates suggests the FE assumption is probably correct and RE is inconsistent.
- The Hausman test is a formal test of this.

Hausman test

First use estimates store to save your fe and re estimates. Name them FE and RE, for example.

```
xtreg avgpassing avglcass, fe i(campus)
estimates store FE
xtreg avgpassing avgclass, re i(campus)
estimates store RE
hausman FE RE
```

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Hausman test

Null hypothesis: RE assumptions hold, both estimators consistent but RE is efficient. Alternative: RE assumptions do *not* hold and the RE estimator is inconsistent. In the TX example we can reject H_0 :



Review of GLS

In a linear regression with known heteroskedasticity, we can transform the original data and apply OLS to the transformed data. E.g.:

$$Y_i = \beta_0 + \beta_1 X_i + u_i$$

and assume ${\rm Var}(u_i)=k_i\sigma_u^2$. The GLS transformation divides the data by $\sqrt{k_i}$. Observations with greater variance get *less* weight. The transformed model satisfies homoskedasticity. Note:

$$Var\left(\frac{u_i}{\sqrt{k_i}}\right) = \frac{1}{k_i} Var(u_i)$$

$$= \frac{1}{k_i} k_i \sigma_u^2$$

$$= \sigma_u^2$$

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GLS estimation of random effects models

The random effects model with one covariate is:

$$Y_{it} = \beta_0 + \beta_1 X_{it} + \underbrace{C_i + e_{it}}_{V_{it}}$$

GLS estimation again involves a transformation. Let:

$$\theta = 1 - \sqrt{\frac{\sigma_e^2}{\sigma_e^2 + T\sigma_c^2}}$$

(and note the term under the square root looks like but is different from the ICC). ${\cal T}$ is the number of observations per group, assuming a balanced panel.

The transformations of Y_{it} and X_{it} are:

$$Y_{it} - \theta \bar{Y}_i$$

$$X_{it} - \theta \bar{X}_i$$

and OLS is estimated on the transformed model:

$$Y_{it} - \theta \bar{Y}_i = \beta_0 (1 - \theta) + \beta_1 (X_{it} - \theta \bar{X}_i) + (v_{it} - \theta \bar{v}_i)$$

The transformed Y_{it} and X_{it} are *quasi-demeaned*. If $\theta=1$, we have the demeaned (within) model.

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GLS estimation of random effects models

 θ is not known so it must first be estimated with consistent estimators for σ_e^2 and σ_e^2 . Then, $\hat{\theta}$ is used in OLS estimation ("feasible GLS").

$$\hat{\theta} = 1 - \sqrt{\frac{\hat{\sigma}_e^2}{\hat{\sigma}_e^2 + T\hat{\sigma}_c^2}}$$

Consistent estimators for σ_c^2 and σ_e^2 can be obtained using pooled OLS or fixed effects residuals.

One method for estimating σ_c^2 and σ_e^2 : note that

$$v_{it} = C_i + e_{it}$$

$$v_{it}v_{is} = (C_i + e_{it})(C_i + e_{is})$$

$$E(v_{it}v_{is}) = \underbrace{E(C_i^2)}_{\sigma_z^2} + \underbrace{E(C_ie_{is})}_{0} + \underbrace{E(C_ie_{it})}_{0} + \underbrace{E(e_{it}e_{is})}_{0}$$

Get the composite residuals \hat{v}_{it} using pooled OLS. The square of the RMSE in this regression estimates σ_v^2 . The within-group (i) covariance in \hat{v}_{it} (the sample analog of $E(v_{it}v_{is})$ above) provides a consistent estimate of σ_c^2 . Then, $\hat{\sigma}_e^2 = \hat{\sigma}_v^2 - \hat{\sigma}_c^2$.

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GLS estimation of random effects models

$$Y_{it} - \theta \bar{Y}_i = \beta_0 (1 - \theta) + \beta_1 (X_{it} - \theta \bar{X}_i) + (v_{it} - \theta \bar{v}_i)$$

$$\theta = 1 - \sqrt{\frac{\sigma_e^2}{\sigma_i^2 + T \sigma_i^2}}$$

Notice the transformation subtracts a *fraction* of the within-group mean, where the fraction depends on σ_e^2 , σ_c^2 , and T.

- When $\theta = 0$, the model reduces to pooled OLS
- When $\theta = 1$, the model reduces to fixed effects (within)
- \bullet So, the value of θ is indicative of which model RE is closer to

 θ gets closer to 1 as between-group variation σ_c^2 grows relative to within-group variation σ_e^2 , and as the number of time periods T grows.

Can request $\hat{\theta}$ in xtreg, re:



This uses the original unbalanced panel, so $\hat{\theta}$ varies with group size.

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GLS estimation of random effects models

Can request $\hat{\theta}$ in xtreg, re:



This uses the <u>balanced</u> panel, so $\hat{\theta}$ is constant.

It is useful to consider the error term in the quasi-demeaned model:

$$v_{it} - \theta \bar{v}_i = (1 - \theta)C_i + (e_{it} - \theta \bar{e}_i)$$

Suppose the RE assumption that C_i is uncorrelated with x_{it} does *not* hold. As $\theta \to 1$, the C_i component of the error term diminishes in importance, the RE estimator tends toward the FE estimator, and any bias associated with RE tends to zero.

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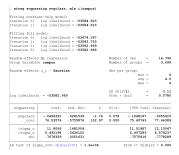
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MLE estimation of random effects models

Random effects models can also be estimated using **maximum likelihood** in which case all parameters of the model (β 's, σ 's) are estimated jointly:



Getting estimates of random effects C_i

As with xtreg, fe, one can obtain the \hat{C}_i estimates of the group random effects. Unlike fe, these are not coefficient estimates but rather estimated from residuals. The random effects \hat{C}_i can be calculated in two ways:

- Maximum likelihood (following xtreg, mle): predict
- Empirical Bayes / shrinkage approach: the Best Linear Unbiased Predictors (BLUPs)

Shrinkage approach: multiply \hat{C}_i by a shrinkage factor $\hat{R}_i = \frac{\hat{\sigma}_c^2}{\hat{\sigma}_c^2 + \frac{\hat{\sigma}_c^2}{\hat{t}_i^2}}$

where T_i is the number of observations in group i. Examples on next 3 slides.

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Getting estimates of random effects C_i : MLE



Getting estimates of random effects C_i : BLUP

Fitting comsta	ant-only model	li .					
teration 0:	log likeliho	od = -53584	.523				
teration 1:	log likeliho	ood = -53584	.523				
itting full m	nodel:						
teration 0:	log likeliho	ood = -53674	.187				
teration 1:	log likeliho	ood = -53583	.763				
teration 2:	log likeliho	ood = -53582	.969				
teration 3:	log likeliho	ood = -53582	.969				
landom-effects	ML regressio	on.		Number			14,796
roup variable	: campus			Number	of grow	ibs =	3,695
andom effects	u_i ~ Gaussi	ian		Obs per	group		
						min -	4
						avg =	4.0
						max =	
				LR chi2		-	3.11
og likelihood	53582.94	69		LR chi2 Prob >		-	3.11 0.0780
og likelihood		Std. Err.	z		chi2	-	
avgpassing			z -1.76	Prob >	chi2	- Conf.	0.0780
-	Coef.	Std. Err.		Prob >	(95)	- Conf.	0.0780 Interval]
avgpassing avgclass	Coef. 0496391 76.53576	Std. Err.	-1.76	Prob > P> z 0.078	(95) 104 75.4	- Conf.	0.0780 Interval)
avgpassing avgclass _cons /sigms_u /sigma_e	Coef. 0496391 76.53576 11.8066 6.492198	Std. Err. .0281539 .5755876	-1.76	Prob > P> z 0.078	chi2 [95] 104 75.4	- 1 Conf. 18197 10763	0.0780 Interval) .0055415 77.66385
avgpassing avgclass _coms /sigms_u	Coef. 0496391 76.53576 11.8066	Std. Err. .0281539 .5755876	-1.76	Prob > P> z 0.078	(95) 100 75.4	- Conf. 18197 10763	0.0780 Interval) .0055415 77.66389
avgpassing avgclass _cons /sigma_u /sigma_e rho	Coef0496391 76.53576 11.8066 6.492198 .7678329	Std. Err. .0281539 .5755876 .1481004 .0436102 .0051631	-1.76 132.97	Prob > P> z 0.078 0.000	(95) 100 75.4 11.5 6.40 .75	Conf. 18197 10763 51987 07283 75916	0.0780 Interval) .0055415 77.66389 12.10047 6.578237
avgpassing avgclass _cons /sigma_u /sigma_e rho & test of sig	Coef0496391 76.53576 11.8066 6.492198 .7678329	Std. Err. .0281539 .5755876 .1481004 .0436102 .0051631 ar2(01) = 1.	-1.76 132.97	Prob > P> z 0.078 0.000	(95) 104 75.4 11.5 6.44 .75	- Conf. 18197 10763 51987 07283 75916	0.0780 Interval] .0055415 77.66385 12.10047 6.578237 .7778285
avgpassing avgclass _coms _signs_u /signs_e /signs_e rho R test of sig	Coef0496391 76.53576 11.8066 6.492198 .7678329 pma_u=0: chibw	Std. Err0281539 .5755876 .1481004 .0436102 .0051631 ar2(01) = 1.:	-1.76 132.97	Prob > P> z 0.078 0.000	(95) 104 75.4 11.5 6.44 .75	- Conf. 18197 10763 51987 07283 75916	0.0780 Interval] .0055415 77.66385 12.10047 6.578237 .7778285
avgpassing avgclass _coms _signs_u /signs_e /signs_e rho R test of sig	Coef0496391 76.53576 11.8066 6.492198 .7678329 pma_u=0: chibw	Std. Err0281539 .5755876 .1481004 .0436102 .0051631 ar2(01) = 1.:	-1.76 132.97	Prob > P> z 0.078 0.000	(95) 104 75.4 11.5 6.44 .75	- Conf. 18197 10763 51987 07283 75916	0.0780 Interval] .0055415 77.66385 12.10047 6.578237 .7778285
avgpassing avgclass _coms /signs_u /signs_v rho R test of sig gen shrink = gen uhatls =	Coef. 0496391 76.53576 11.8066 6.492198 .7678329 pma_u=0: chibs b[/sigma_u] u+atl*shrink	Std. Err0281539 .5755876 .1481004 .0436102 .0051631 ar2(01) = 1.:	-1.76 132.97	Prob > P> z 0.078 0.000	(95) 104 75.4 11.5 6.44 .75	- Conf. 18197 10763 51987 07283 75916	0.0780 Interval] .0055415 77.66385 12.10047 6.578237 .7778285
avgpassing avgclass _coms /signs_u /signs_v rho R test of sig gen shrink = gen uhatls =	Coef. 0496391 76.53576 11.8066 6.492198 .7678329 pma_u=0: chibs b[/sigma_u] u+atl*shrink	Std. Err0281539 .5755876 .1481004 .0436102 .0051631 ar2(01) = 1.:	-1.76 132.97 2e+04 igma_u]^2	Prob > P> z 0.078 0.000 2 + (_b{/	(95) 104 75.4 11.5 6.44 .75	- Conf. 18197 10763 81987 77283 75916 - chiba	0.0780 Interval] .0055415 77.66385 12.10047 6.578237 .7778285
avgclass _coms /sigma_u /sigma_e rho R test of sig gen shrink = gen uhatis =	Coef. 0496391 76.53576 11.8066 6.492198 7.678329 pma_u=0: chibx =_b[/sigma_u] = uhatl*shrink	Std. Err0281539 .5755876 .1481004 .0436102 .0051631 ar2(01) = 1	-1.76 132.97 2e+04 iigma_u] ~2	Prob > P> z 0.078 0.000 2 + (_b{/	(95)104 -75.4 11.5 6.40 .75; Prob >= (sigma_6)	- Conf. 18197 10763 81987 77283 75916 - chiba	0.0780 Interval] .0055415 77.66385 12.10041 6.57823 .7778285 r2 = 0.000

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Getting estimates of C_i : BLUP using xtmixed

. xtmixed avg	passing avgclass	campus	, mle			
Performing EM	optimization:					
Performing gra	adient-based opt	imization:				
Iteration 0: Iteration 1:	log likelihood log likelihood					
Computing star	idard errors:					
Mixed-effects Group variable	ML regression			Sumber of ob Sumber of gr		14,796 3,699
Log likelihoo	153582.969			Obs per grou Wald chi2(1) Prob > chi2	nin = avg = max =	4.0 4 3.13 0.0770
avgpassing	Coef. S	td. Err.	2	P>121 [9	5% Conf.	Interval]
avgclass _oons					046606 .41048	.0053823 77.66103
Random-effe	ots Parameters	Estima	te Std.	Err. [9	5% Conf.	Interval]
campus: Ident:	ity sd(_cons)	11.80	66 .148	1006 11	.51987	12.10047
	nd(Residual)	6.4921	97 .043	6102 6.	407283	6.578236
LR test vs. 1: . predict uhar . sum uhat2	inear model: chi	bar2(01) =	11666.05	Prob >	= chibar	2 = 0.0000
Variable	Oba	Mean	Std. De	r. Min		Max
uhat2	14,796 -	6.21e-10	11.3845	5 -44.10139	21.77	523

Getting estimates of random effects C_i

The shrinkage factor is smaller for groups with fewer observations (T_i) . Their \hat{C}_i is "shrunk" more toward the overall mean group effect of 0.

- · RE estimates generally smaller than FE estimates in absolute value
- True for both MLE and EB estimates of the RE, but especially the EB
- ullet The rank order of the \hat{C}_i is usually preserved whether one assumes RE or FF

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Random vs. fixed effects

When and where random effects are appropriate:

- As a rule, if the FE assumption holds the RE model is inappropriate.
 See the Texas class size example, where the Hausman test rejected RE.
- RE is appropriate with grouped or clustered data. See the Success for All example: assignment to treatment was random at the school level, so we need not be concerned about correlation between treatment and the error term. However, the errors are not i.i.d.

See Rabe-Hesketh and Skrondal MLM text for more guidance on RE vs. ${\sf FE}$ decision.

xttest0

The command xttest0 (following xtreg) provides a formal test for the presence of random effects. H_0 in this case is that the variance across panel units is zero, and thus RE is unnecessary.



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Standard errors in panel models

Whether using a FE or RE model, the assumption that errors u_{it} are i.i.d. is not often satisfied in panel data. With repeat observations on the same cross-sectional unit, it is likely that errors are correlated across observations for the same i.

 If Y is over-predicted in one period for a given i, it is likely to be over-predicted in the next period.

Standard errors in panel models

The RE model explicitly models the correlation across observations within group. There is an increasing preference, however, for <u>not</u> doing this and adjusting standard errors for within-panel clustering.

- For "short" panels (large N small T) use cluster-robust standard errors
- The "cluster" is typically the cross-sectional unit, although when the regressor of interest is aggregated at a higher level (e.g., state), can cluster at that level. Theory requires large N and that higher levels nest the cross-sectional units.
- vce(robust) or robust in xtreg assumes data are clustered
- Cluster-robust standard errors from areg are different from those using xtreg, fe. It is recommended that you use xtreg.

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