Problem Set 9 Solutions

Question 1. This problem will replicate some of the results in Lee (2008), one of the most influential studies using regression discontinuity. Each observation is a Congressional district election between 1948 and 1998. The running variable is difdemshare, the difference between the Democratic candidate's vote share and the largest vote share of the other parties. If the Democrat won, difdemshare is greater than zero.

Conduct a regression discontinuity analysis to estimate the effect of Democratic incumbency in year t on two outcomes: difdemsharenext, the difference between the Democratic vote share and the largest vote share of the other parties in the next election (year t+1), and demwinnext, a binary variable equal to 1 if a Democrat won the next election and 0 otherwise. Your analysis should include the following elements: (55 points)

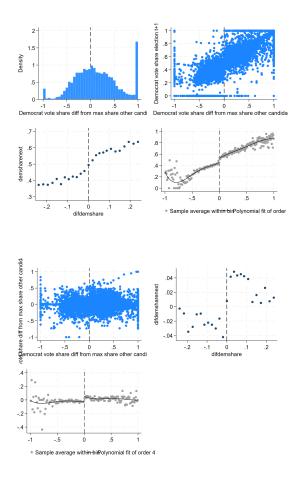
See the attached log file for all results.

(a) Write down the assumptions that should hold in order for your RD estimate to be considered the causal effect of incumbency. (5 points)

There are four key assumptions. First, there is a discontinuous jump in "treatment" at the cutpoint. Define "treatment" as a Democrat winning the election. The running variable in this case is the net Democratic vote share. When this value is below zero, the non-Democratic candidate won. When it exceeds zero, the Democrat won. The discontinuity is sharp. Second, the relationship between the outcome and the running variable is continuous in the neighborhood of the cutpoint, in the absence of treatment. Consider the outcome difdemsharenext, which is the net Democratic vote share in election t+1. In the absence of a treatment effect, there is no reason to believe that Democratic support in election t+1 would change discontinuously with the net vote share in election t. Third, the forcing variable has not been manipulated to affect who receives treatment. In the U.S., elections are generally conducted with integrity, so manipulation seems unlikely. More importantly, even if maleficent persons were working to influence the outcome of an election, it would be hard for them to do so precisely enough to have an impact right at the margin of victory (i.e., near the cutpoint). We can at least conduct a test to look for irregularities in the density of the running variable. Fourth, there are no other "treatments" with the same eligibility rule, and thus no confounders. In other words, there is not something else changing abruptly at the threshold, beyond the identity of the victor.

(b) A scatterplot and RD plot showing the relationship between demsharenext and the running variable across the full range of data. (If it helps visually, you can also show the scatter and RD plots for observations closer to the cutpoint, e.g., abs(difdemshare) < 0.25). Is there visual evidence of a discontinuity? (5 points)

Four plots are shown below, clockwise from upper left: (1) a histogram of the running variable difdemshare, (2) a scatterplot showing the relationship between demsharenext and difdemshare over the full range of data, (3) a binned scatter plot limited to the range +/- 0.25, and (4) an RD plot with a fitted 4th order polynomial. A discontinuity is not evident in the scatterplot, but is in the latter two plots. The second set of plots repeats this for the difdemsharenext variable, which is the outcome used in later regressions



(c) Parametric RD models using OLS for each outcome assuming a linear relationship with the running variable, then a quadratic (p = 2), and then a quartic (p = 4). In each case allow the slope coefficients to differ on each side of the cutoff. Repeat these models but include two covariates in the regression: demofficeexp and othofficeexp (measures

of the Democrat's and opposition's experience in office). You may want to collect your regression results into one or more tables for easy comparison. (There will be a total of 12 regressions). What do these regressions show? Do the differing polynomial orders lead to different conclusions? (10 points)

Estimates from parametric RD models are reported in Tables 1-2. In Table 1, columns (1)-(3) report results from linear, quadratic, and quartic models in which the outcome is the net Democratic share in election t+1. Columns (4)-(6) do the same, but for the binary outcome of a Democratic victory in election t+1. Table 2 repeats the analysis in Table 1, but includes controls for the Democrat's and opponent's experience in political office. The models without controls indicate that—at the margin of victory—a Democratic win in election t increases the likelihood of a Democratic win in election t+1 by 14.3 to 22.9 percentage points (columns 4-6). The impact on the net Democratic vote share is 5.2 to 8.1 percentage points (columns 1-3). The point estimates from the quartic model stand out as the largest of these (columns 3 and 6), and the inclusion of controls for prior experience in office generally produce larger point estimates (Table 2).

Table 1: Parametric RD models (no covariates)

	(1)	(2)	(3)	(4)	(5)	(6)
	difdemsharenext	difdemsharenext	difdemsharenext	demwinnext	demwinnext	demwinnext
1.demwin	0.052***	0.055***	0.081***	0.143***	0.107***	0.229***
	(0.007)	(0.010)	(0.016)	(0.020)	(0.029)	(0.048)
\overline{N}	6559	6559	6559	6559	6559	6559

Standard errors in parentheses

Table 2: Parametric RD models (w/covariates)

			\	/		
	(1)	(2)	(3)	(4)	(5)	(6)
	difdemsharenext	difdemsharenext	difdemsharenext	demwinnext	demwinnext	demwinnext
1.demwin	0.086***	0.067***	0.080***	0.242***	0.143***	0.226***
	(0.007)	(0.010)	(0.016)	(0.021)	(0.029)	(0.047)
demofficeexp	-0.008***	-0.008***	-0.008***	-0.021***	-0.023***	-0.022***
	(0.001)	(0.001)	(0.001)	(0.002)	(0.002)	(0.002)
othofficeexp	0.009***	0.010***	0.010***	0.029***	0.031***	0.029***
-	(0.001)	(0.001)	(0.001)	(0.003)	(0.003)	(0.003)
N	6559	6559	6559	6559	6559	6559

Standard errors in parentheses

(d) Non-parametric RD models for each outcome using a local linear regression, the MSE-optimal bandwidth, and triangular kernel. Repeat, including the two covariates listed

^{*} p < 0.05, ** p < 0.01, *** p < 0.001

^{*} p < 0.05, ** p < 0.01, *** p < 0.001

in part (c). (There should be 4 regressions for this part). What do these regressions show? Do the conclusions differ from part (c)? (10 points)

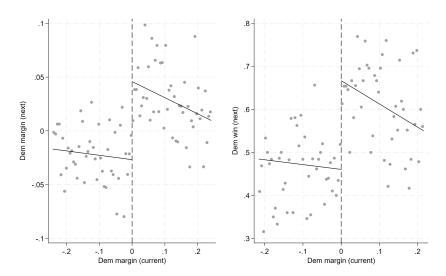
The non-parametric RD estimates using the optimal bandwidth are reported in the first row of Table 3. A Democratic win in election t increases the likelihood of a Democratic win in election t+1 by 20.6 to 21.5 percentage points (columns 2 and 4). These are close to the point estimates from the quartic model. The estimated impact on the net Democratic share in election t+1 is 7.3 to 7.6 percentage points (columns 1 and 3). These numbers are actually quite close to those in Table 2 of Lee (2008).

Table 3: Non-parametric RD models (no covariates)

	· · · ·	/-×	(-)	· · · · · ·
	(1)	(2)	(3)	(4)
	difdemsharenext	demwinnext	difdemsharenext	demwinnext
RD_Estimate	0.073***	0.206***	0.076***	0.215***
	(0.012)	(0.044)	(0.012)	(0.042)
N	6559	6559	6559	6559

Standard errors in parentheses

(e) An RD plot for each outcome based on the optimal bandwidths used in part (d) for the models without covariates. (5 points)

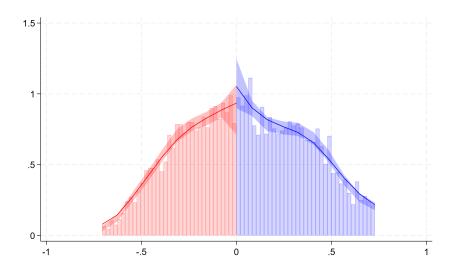


(f) A density test for manipulation around the cutoff. Provide the density plot and report the *p*-value of the test (and conclusion). Is manipulation theoretically plausible in this case? Why or why not? (5 points)

The density plot is shown below and shows no evidence of manipulation at the cutpoint. Manipulation seems unlikely in U.S. elections; it would imply

^{*} p < 0.05, ** p < 0.01, *** p < 0.001

that an unexpectedly high proportion of elections result in the Democratic Party earning just over 50% of the vote (and unexpectedly fewer with the Democratic Party earning just under 50% of the vote). The test statistic for the density test is 1.42 with a p-value of 0.1545. We do not find significant evidence of manipulation at the cutpoint.



(g) As a validity check, repeat part (d)—without covariates—in which you use demshareprev and demwinprev as the outcome variables. (These represent the Democratic vote share and a Democratic win in the previous election, t-1). What does this accomplish and what do you find? (5 points)

Table 4 shows the non-parametric RD estimates in which the outcomes are the Democratic vote share in the *previous* election and a binary Democratic win in the previous election. While a small change in the vote share in the current election can produce a large change in the identity of the victor (and, as we have shown, the probability of winning in the following year) there is no reason to think a small change in this year's election would have an effect on the *prior* outcome. Indeed that is what we see here, at least using the optimal bandwidth, where there are no statistically significant effects.

Table 4: Validity test: outcome is previous election

	(1)	(2)
	demshareprev	demwinprev
RD_Estimate	0.001	0.041
	(0.012)	(0.050)
N	6559	6559

Standard errors in parentheses

^{*} p < 0.05, ** p < 0.01, *** p < 0.001

(h) One would not expect there to be a discontinuity in the covariates used in parts (c)-(d) at the cutpoint. Repeat part (d)—without covariates—in which you use *demofficeexp* and *othofficeexp* as the outcome variables. What do you find? (5 points)

Table 5 finds no discontinuities at the cutpoint in the two covariates: the Democratic candidate's political experience and the opposing candidate's political experience.

Table 5: Validity test: continuity in pre-determined covariates

	(1)	(2)
	demofficeexp	othoffice exp
RD_Estimate	0.221	0.135
	(0.237)	(0.201)
N	6559	6559

Standard errors in parentheses

(i) Finally, conduct some tests for discontinuities elsewhere the distribution of difdemshare. I suggest looking at "fake" cutpoints equal to the 1st, 2nd, 3rd, 4th, etc., deciles of the difdemshare distribution. Since there is a known "real" cutpoint at 0, limit these analyses to either values below 0 (Republican win) or above 0 (Democratic win), depending on where your "fake" cutpoint sits. Summarize what you find. (5 points)

See the log file for how this was done. The first four columns of Table 6 limit the sample to those with *difdemshare* less than 0 and test for discontinuities at the 1st, 2nd, 3rd, and 4th deciles. The latter four columns limit the sample to those with *difdemshare* above 0 and test for discontinuities at the 6th, 7th, 8th, and 9th deciles. There is a marginally significant jump at the 8th decile but no significant effects elsewhere, which is reassuring.

Table 6: Validity test: discontinuities elsewhere

	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
	difdemsharenext							
RD_Estimate	-0.026	0.010	-0.008	0.002	-0.023	-0.020	0.053*	0.116
	(0.027)	(0.017)	(0.029)	(0.032)	(0.026)	(0.019)	(0.021)	(0.140)
N	2740	2740	2740	2740	3818	3818	3818	3818

Standard errors in parentheses

^{*} p < 0.05, ** p < 0.01, *** p < 0.001

^{*} $p < 0.05, \, ^{**}$ $p < 0.01, \, ^{***}$ p < 0.001

Question 2. Consider the sharp RD model in which the running variable (x_i) is allowed to have a linear relationship with the outcome (Y_i) that varies on either side of the cutoff (c). Let the treatment status variable $D_i = 1$ whenever $x_i > c$.

$$Y_i = \pi_0 + \pi_1 x_i + \pi_2 D_i + \pi_3 (D_i \times x_i) + v_i$$

Suppose that the running variable x_i is not centered at c. (That is, we do not first subtract off c from x_i). Show that π_2 in this case is not the impact of the treatment at the threshold c. You can show this however you like: algebraically, using the simulated data, as in the in-class exercise, or any other valid method. (5 points)

Let the cutoff point be c. Intuitively, if $c \neq 0$ the expected value of Y_i as we approach c from the left is $\pi_0 + \pi_1 c$. The expected value of Y_i as we approach c from the right is $\pi_0 + \pi_1 c + \pi_2 + \pi_3 c$. The difference between these two is: $\pi_2 + \pi_3 c$, not π_2 . Put another way, π_2 is the intercept shift when x = 0; $\pi_3 c$ is the difference in the intercept shift when x = c. If the cutpoint were 0, the expected value of Y_i as we approach c from the left would be π_0 , while the expected value of Y_i as we approach c from the right would be $\pi_0 + \pi_2$.

We can also see this using simulated data from the in-class exercise in which we generated 10,000 student observations with underlying "ability," a grade 3 test score, and a grade 4 test score. Students above the eligibility threshold for the gifted program (56) were assigned to the gifted treatment. When we fit an RD model in which the running variable (grade 3 score) is centered at 0, the coefficient on inGT (being at or above the treatment threshold) was 3.02. If we fit the model (using the same data) with a running variable not centered at 0, the coefficient on inGT is 2.76. To get the actual jump at the cutoff we would need to calculate $\hat{\pi}_2 + \hat{\pi}_3 * 56 = 2.76 + 0.0046 * 56 = 3.02$. The Stata output is attached.

```
. // ********************
. // LPO-8852 Problem set 9 solutions . // Last updated: December 5, 2024
. // *****
. // (1)
. // ******
. // ********************************
. // Re-analysis of Lee (2008) on the effect of incumbency
. // ********************************
. // Read source data
         clear
         use https://github.com/spcorcor18/LPO-8852/raw/main/data/Lee 2008 for
> RD.dta
. // Scatterplot and RD plot showing relationship between demsharenext (or
. // difdemshare) and running variable difdemshare
         histogram difdemshare, xline(0) name(xhist, replace)
(bin=38, start=-1, width=.05263158)
         scatter demsharenext difdemshare, xline(0) name(gr1, replace)
         binscatter demsharenext difdemshare if abs(difdemshare)<0.25, ///
                 xline(0) linetype(none) nq(25) name(gr2, replace)
         rdplot demsharenext difdemshare, c(0) binmethod(qsmv) ///
                 graph options(legend(position(6)) name(gr3, replace))
Mass points detected in the running variable.
RD Plot with evenly spaced mimicking variance number of bins using polynomial re
> gression.
       Cutoff c = 0 | Left of c Right of c
                                                 Number of obs =
                                                                   ردن
Uniform
                                                                         6559
                                                   Kernel =
       Number of obs | 2740 3819
  Eff. Number of obs
                           2740
                                      3819
Order poly. fit (p) | 4 4 4 8W poly. fit (h) | 1.000 1.000 Number of bins scale | 1.000 1.000
Outcome: demsharenext. Running variable: difdemshare.
                   | Left of c Right of c
_____
  Bins selected | 87 146
Average bin length | 0.011 0.007
Median bin length | 0.011 0.007
 IMSE-optimal bins | 20
Mimicking Var. bins | 87
         -----
Rel. to IMSE-optimal: |
   | Implied scale | 4.350 | 8.588 | WIMSE var. weight | 0.012 | 0.002 | WIMSE bias weight | 0.988 | 0.998 |
```

```
graph combine xhist gr1 gr2 gr3, rows(2) xsize(8) ysize(6)
          graph export rdplots1a.png, as(png) replace
file rdplots1a.png saved as PNG format
          // now difdemsharenext (used in later regressions)
          scatter difdemsharenext difdemshare, xline(0) name(gr1, replace)
          binscatter difdemsharenext difdemshare if abs(difdemshare) < 0.25, ///
                   xline(0) linetype(none) nq(25) name(gr2, replace)
          rdplot difdemsharenext difdemshare, c(0) binmethod(qsmv) ///
                   graph options(legend(position(6)) name(gr3, replace))
Mass points detected in the running variable.
RD Plot with evenly spaced mimicking variance number of bins using polynomial re
> gression.
                                                         Number of obs = 6559
Kernel = Uniform
        Cutoff c = 0 | Left of c Right of c
       Number of obs | 2740 3819
Eff. Number of obs | 2740
Order poly. fit (p) | 4
BW poly. fit (h) | 1.000
Number of bins scale | 1.000
                                           3819
                                             4
                                         1.000
                                           1.000
Outcome: difdemsharenext. Running variable: difdemshare.
               | Left of c Right of c
  Bins selected | 62 85
Average bin length | 0.016 0.012
Median bin length | 0.016 0.012
-----
 IMSE-optimal bins | 6
Mimicking Var. bins | 62
Rel. to IMSE-optimal: |
   Implied scale | 10.333 12.143
WIMSE var. weight | 0.001 0.001
WIMSE bias weight | 0.999 0.999
          graph combine gr1 gr2 gr3, rows(2) xsize(8) ysize(6)
          graph export rdplots1b.png, as(png) replace
file rdplots1b.png saved as PNG format
. // Parametric RD models - no controls
          gen demwin = difdemshare>0
          estimates drop all
          // Outcome: Democratic advantage in the next election (t+1)
```

```
// Linear, then quadratic, then quartic. Note: should probably cluster
       // by statedisdec, but I do not here.
       eststo: reg difdemsharenext c.difdemshare##i.demwin
Total | 180.806529 6,558 .027570376 Root MSE
______
difdemshare~t | Coefficient Std. err. t P>|t| [95% conf. interval]
 difdemshare | .0018766 .0137495 0.14 0.891 -.025077 .0288301 1.demwin | .0518415 .0067638 7.66 0.000 .0385823 .0651008
    demwin#|
c.difdemshare |
           -.0347857 .0160789 -2.16 0.031
                                        -.0663057 -.0032658
      cons | -.0205111 .0050908 -4.03 0.000 -.0304907 -.0105316
(est1 stored)
       _eststo: reg difdemsharenext c.difdemshare##c.difdemshare##i.demwin
difdemshare~t | Coefficient Std. err. t P>|t| [95% conf. interval]
difdemshare | -.0012222 .0393918 -0.03 0.975 -.0784431 .0759986
       c.
difdemshare#|
           -.0035163 .0418868 -0.08 0.933 -.0856282
c.difdemshare |
                                                  .0785956
                             5.61 0.000
   1.demwin |
            .054634 .0097345
                                        .0355513
                                                  .0737167
    demwin#|
c.difdemshare |
     1 |
           -.0468318 .050983 -0.92 0.358 -.146775 .0531114
    demwin#1
       c. I
 difdemshare#|
c.difdemshare |
           .0179042 .0513539
                            0.35 0.727 -.0827663 .1185747
_cons | -.0209308 .0071354 -2.93 0.003 -.0349185 -.0069431
(est2 stored)
       _eststo: reg difdemsharenext ///
c.difdemshare##c.difdemshare##c.difdemshare##i.
  _____
    Total | 180.806529 6,558 .027570376 Root MSE
```

difdemshare~t	Coefficient	Std. err	. t	P> t	[95% conf.	interval]
difdemshare					4112493	.3397191
c. difdemshare# c.difdemshare		.8985005	0.27	0.789	-1.520369	2.002339
c. difdemshare# c. difdemshare#						
c.difdemshare		1.514671	0.64	0.520	-1.993673	3.944828
c. difdemshare# c. difdemshare#						
c. difdemshare						
c.difdemshare		.8057804	0.89	0.373	8624379	2.296747
1.demwin	.0811036	.0160571	5.05	0.000	.0496264	.1125809
demwin# c.difdemshare 1		.2536922	-1.40	0.162	8517007	.1429383
demwin# C.						
<pre>difdemshare# c.difdemshare 1 </pre>		1.150691	0.93	0.353	-1.186506	3.324952
demwin# c. difdemshare#						
c. difdemshare# c.difdemshare 1		1.883308	-1.42	0.157	-6.358031	1.025766
demwin# c.						
difdemshare# c.						
difdemshare# c. difdemshare#						
c.difdemshare 1		.9817663	-0.00	0.998	-1.927472	1.921693
_cons	0272428	.011781	-2.31	0.021	0503375	0041481
(est3 stored)						
. // Li	y statedisdec,	adratic, t but I do	then quartion not here.	c. Note	: should proba	bly cluster
_	sto: reg demwi					
Source				F(3,	er of obs = 6555) =	6,559 65.65
Residual	47.8281881 1591.92177	6 , 555	.242856106	R-sq Adi	> F = quared = R-squared =	65.65 0.0000 0.0292 0.0287
Total	1639.74996	6,558	.250038116	Root	MSE =	.4928

demwinnext	Coefficient	Std. err.	t	P> t	[95% conf.	interval]
difdemshare 1.demwin	.2254137 .1428544	.0411138	5.48 7.06	0.000	.1448171 .1032066	.3060102 .1825021
demwin# c.difdemshare 1	4690135	.0480792	-9.76	0.000	5632644	3747625
_cons	.5048468	.0152224	33.16	0.000	.4750058	.5346877
(est4 stored)						
ests	sto: reg demwi	nnext c.di	fdemshare#	#c.difde	emshare##i.dem	win
Source	SS	df	MS		er of obs = 6553) =	6,559 40.91
Model Residual	49.6306746 1590.11929	5 6 , 553	9.92613491 .242655164	Prob R-squ		0.0000
Total	1639.74996	6,558	.250038116	Root		.4926
demwinnext	Coefficient	Std. err.	t	P> t	[95% conf.	interval]
difdemshare	.1954246	.1177251	1.66	0.097	0353549	.4262041
c. difdemshare# c.difdemshare	0340293	.1251815	-0.27	0.786	2794259	.2113672
 1.demwin	.1072047	.0290921	3.69	0.000	.0501747	.1642346
demwin# c.difdemshare 1	1855631	.1523658	-1.22	0.223	4842498	.1131236
demwin# c. difdemshare# c.difdemshare 1		.1534745	-1.35	0.178	5076239	.0940963
_cons	.5007855 	.0213245	23.48	0.000	.4589824 	.5425885
<pre>(est5 stored)ests > > demwin Source </pre>	SS	are##c.dif	MS	Numbe	mshare##c.difde	6,559
Model Residual	59.4264016 1580.32356	9 6 , 549	6.60293351 .241307613	Prob R-squ	6549) = > F = aared = Requared =	0.0000
Total	1639.74996	6 , 558	.250038116	Adj F Root	R-squared = MSE =	.49123
demwinnext	Coefficient	Std. err.	t	P> t	[95% conf.	interval]
difdemshare						.7187418
c. difdemshare# c.difdemshare	3190757	2.679125	-0.12	0.905	-5.571035	4.932884
difdemshare# c. difdemshare# c.difdemshare c.difdemshare	3.151483	4.516408	0.70	0.485	-5.70215	12.00512

```
difdemshare#|
    C .
 difdemshare#|
        c.
 difdemshare#|
             2.984974 2.402655 1.24 0.214 -1.725014 7.694961
c.difdemshare |
                                 4.78 0.000
             .2290831 .0478788
                                               .1352251 .3229411
    1.demwin |
     demwin#1
c.difdemshare |
              -.365491 .7564528 -0.48 0.629 -1.848385 1.117403
      1 |
     demwin#|
        c.
 difdemshare#|
c.difdemshare |
             1.664212 3.431099 0.49 0.628 -5.061862 8.390285
       1 |
     demwin#|
        c.
 difdemshare#|
        c.
 difdemshare#|
c.difdemshare |
             -3.216946 5.615599 -0.57 0.567 -14.22535 7.791461
       1 |
     demwin#|
        C .
 difdemshare#|
        c.
 difdemshare#|
        c.
 difdemshare#
c.difdemshare |
             -3.821473 2.927405
                                 -1.31 0.192 -9.560142 1.917196
    _cons | .4431664 .0351284 12.62 0.000
                                               .3743032 .5120295
(est6 stored)
       qui esttab all using "Table1.tex", keep(1.demwin) b(3) se(3) tex repl
> ace
. // Parametric RD models - with controls
        global cov "demofficeexp othofficeexp"
        estimates drop all
        // Outcome: Democratic advantage in the next election (t+1)
       // Linear, then quadratic, then quartic. Note: should probably cluster
        // by statedisdec, but I do not here.
        eststo: reg difdemsharenext c.difdemshare##i.demwin $cov
Source | SS df MS
```

difdemshare~t	Coefficient	Std. err.	t	P> t	[95% conf.	interval]
difdemshare 1.demwin	.0303334 .0864789	.0137117	2.21 12.30	0.027	.003454	.0572128
demwin#c.difdemshare	 0420087	.015894	-2.64	0.008	0731662	0108513
1	0420067	.013694	-2.04	0.000	0731662	0106313
demofficeexp	0077403	.00068	-11.38	0.000	0090733	0064073
othofficeexp	.0093216	.0010271	9.08	0.000	.0073081	.011335
cons	0370097	.0055293	-6.69	0.000	0478489	0261705
(est1 stored)						

_eststo: reg difdemsharenext c.difdemshare##c.difdemshare##i.demwin \$c . > ov

Source	SS	df	MS		er of obs = 6551) =	6,559 49.70
Model Residual	9.11788579 171.688643	7 6 , 551	1.30255511 .026208005	Prob R-sq	> F = uared = R-squared =	0.0000 0.0504 0.0494
Total	180.806529	6 , 558	.027570376	Root		.16189
difdemshare~t	Coefficient	Std. err	. t	P> t	[95% conf.	interval]
difdemshare	.1030666	.0395998	2.60	0.009	.025438	.1806951
c. difdemshare# c.difdemshare	 .0809306	.0417136	1 04	0.052	0008417	.1627028
c.dildemshare	.0809306	.041/136	1.94	0.052	000841/	.102/028
1.demwin	.0665156	.0095914	6.93	0.000	.0477133	.0853179
demwin# c.difdemshare 1	 037541	.0505926	-0.74	0.458	1367191	.061637
demwin# C. difdemshare# c.difdemshare	İ					
1	1533416	.0516865	-2.97	0.003	254664	0520192
demofficeexp othofficeexp _cons	0080769 .0098052 0282428	.000691 .0010421 .0072026	-11.69 9.41 -3.92	0.000 0.000 0.000	0094316 .0077624 0423621	0067223 .0118481 0141234
(est2 stored)	·					-

_eststo: reg difdemsharenext ///
c.difdemshare##c.difdemshare##c.difdemshare##i. . _est
>
> demwin \$cov

Source		SS	di	MS	Number of obs	=	6 , 559
	-+-				F(11, 6547)	=	31.95
Model		9.21148008	11	.83740728	Prob > F	=	0.0000
Residual		171.595049	6 , 547	.026209722	R-squared	=	0.0509
	-+-				Adj R-squared	=	0.0494
Total		180.806529	6,558	.027570376	Root MSE	=	.16189

difdemshare~t	Coefficient	Std. err.	t	P> t	[95% conf.	interval]
difdemshare					2560026	
c. difdemshare# c.difdemshare	!	.8831359	0.42	0.671	-1.356446	2.106023
c. difdemshare# c. difdemshare# c.difdemshare	 	1.489182	0.55	0.584	-2.103352	3.735211
c. difdemshare# c. difdemshare# c.	 	1.103102	3.33	0.001	21103302	3.733211
<pre>difdemshare# c.difdemshare</pre>	'	.792405	0.69	0.493	-1.009904	2.096841
1.demwin	.0801106	.01578	5.08	0.000	.0491766	.1110447
demwin#c.difdemshare1	 2700642 	.2493648	-1.08	0.279	7589007	.2187723
demwin# C. difdemshare# C.difdemshare 1 demwin#	 - .4981574 	1.131399	0.44	0.660	-1.719754	2.716069
difdemshare# c. difdemshare# c.difdemshare 1	 	1.852545	-1.19	0.234	-5.838089	1.425096
demwin# c. difdemshare# c. difdemshare#	 					
c. difdemshare# c.difdemshare 1		.9648837	0.12	0.907	-1.779249	2.003725
demofficeexp othofficeexp _cons	008045 .0096291 0301559	.000693 .0010471 .0116901	-11.61 9.20 -2.58	0.000 0.000 0.010	0094034 .0075764 0530723	0066865 .0116818 0072396

^{//} Outcome: Democratic win in the next election (t+1)
// Linear, then quadratic, then quartic. Note: should probably cluster
// by statedisdec, but I do not here.

_eststo: reg demwinnext c.difdemshare##i.demwin \$cov Adj R-squared = 0.0588 _____ Total | 1639.74996 6,558 .250038116 Root MSE demwinnext | Coefficient Std. err. t P>|t| [95% conf. interval] ______ difdemshare | .3100538 .0410649 7.55 0.000 .2295532 .3905545 1.demwin | .2422674 .0210546 11.51 0.000 .2009934 .2835414 demwin#1 c.difdemshare | 1 -.4937646 .0476007 -10.37 0.000 -.5870775 -.4004518

 demofficeexp
 -.0209044
 .0020365
 -10.26
 0.000
 -.0248967
 -.0169121

 othofficeexp
 .0286803
 .003076
 9.32
 0.000
 .0226503
 .0347104

 _cons
 .452476
 .0165596
 27.32
 0.000
 .4200139
 .4849382

 _cons | (est4 stored) eststo: reg demwinnext c.difdemshare##c.difdemshare##i.demwin \$cov = 0.0643 = 0.0633 . 48394 demwinnext | Coefficient Std. err. t P>|t| [95% conf. interval] difdemshare | .5145865 .1183778 4.35 0.000 .2825274 .7466455 c. difdemshare#| 1.80 0.072 -.0198518 c.difdemshare | .2245942 .1246966 .4690401 4.97 0.000 1.demwin | .1425147 .0286721 .0863081 .1987212 demwin#| c.difdemshare | -.1720347 .1512391 -1.14 0.255 -.4685126 .1244432 1 | demwin#1 c. I difdemshare#| c.difdemshare | -.7193499 .154509 -4.66 0.000 -1.022238 -.4164618 1 1 (est5 stored) _eststo: reg_demwinnext /// c.difdemshare##c.difdemshare##c.difdemshare##i. > demwin \$cov

demwinnext	Coefficient	Std. err.	t	P> t	[95% conf.	interval]
difdemshare	.036322	.5626409	0.06	0.949	-1.066638	1.139282
c. difdemshare# c.difdemshare		2.635979	0.02	0.988	-5.126822	5.207935
difdemshare# c.difdemshare# c.difdemshare		4.4449	0.59	0.557	-6.103616	11.32329
c. difdemshare# C. difdemshare#						
<pre>difdemshare# c.difdemshare </pre>	 2.433287	2.365166	1.03	0.304	-2.20321	7.069784
1.demwin	.2259717	.0471002	4.80	0.000	.13364	.3183034
demwin# c.difdemshare 1	1227831	.7443027	-0.16	0.869	-1.581859	1.336293
demwin# c. difdemshare# c.difdemshare 1		3.376994	0.00	0.998	-6.612772	6.627247
demwin#		E	0.22	0.751	12 50102	0.000077
demwin# c. difdemshare# c. difdemshare#		5.529465	-0.32	0.751	-12.59103	9.088077
difdemshare# c.difdemshare 1	-3.467152	2.879979	-1.20	0.229	-9.112851	2.178547
demofficeexp othofficeexp _cons	.0293487	.0020683 .0031255 .0348924	-10.87 9.39 12.38	0.000 0.000 0.000	0265357 .0232218 .3634862	0184265 .0354756 .5002873

(est6 stored)

[.] qui esttab _all using "Table2.tex", keep(1.demwin \$cov) b(3) se(3) tex
> replace

```
. // Nonparametric RD models using rdrobust
```

estimates drop _all

. _eststo: rdrobust difdemsharenext difdemshare, c(0) kernel(triangular) Mass points detected in the running variable.

Sharp RD estimates using local polynomial regression.

Cutoff $c = 0$	Left of c	Right of c	Number of obs		6559
	+		BW type		mserd
Number of obs		3819	Kernel	=	Triangular
Eff. Number of obs	1338	1359	VCE method	=	NN
Order est. (p)	1	1			
Order bias (q)	2	2			
BW est. (h)	0.242	0.242			
BW bias (b)	0.380	0.380			
rho (h/b)	0.637	0.637			
Unique obs	2606	3210			

Outcome: difdemsharenext. Running variable: difdemshare.

Method	 	Coef.	S	td. Er	r.	Z	P	> z	 [95%	Conf.	Ir	nterval]
Conventional Robust				.01217		5.9636 5.1275	-		.048			.09642

Estimates adjusted for mass points in the running variable. (est1 stored)

. _eststo: rdrobust demwinnext difdemshare, c(0) kernel(triangular) Mass points detected in the running variable.

Sharp RD estimates using local polynomial regression.

Cutoff $c = 0$	Left of c	Right of c	Number of obs	=	6559
	+		BW type	=	mserd
Number of obs	2740	3819	Kernel	=	Triangular
Eff. Number of obs	1203	1221	VCE method	=	NN
Order est. (p)	1	1			
Order bias (q)	2	2			
BW est. (h)	0.216	0.216			
BW bias (b)	0.333	0.333			
rho (h/b)	0.648	0.648			
Unique obs	2606	3210			

Outcome: demwinnext. Running variable: difdemshare.

Method	Coef.	Std. Err.	z	P> z	[95% Conf.	Interval]
Conventional Robust		.04368	4.7211 4.0162	0.000	.120615 .108119	.291853 .314232

Estimates adjusted for mass points in the running variable. $({\tt est2}\ {\tt stored})$

. __eststo: rdrobust difdemsharenext difdemshare, c(0) kernel(triangular)
> covs(\$cov)

Mass points detected in the running variable.

Covariate-adjusted Sharp RD estimates using local polynomial regression.

Cutoff $c = 0$	Left of c	Right of c	Number of obs	=	6559
	+		BW type	=	mserd
Number of obs	2740	3819	Kernel	=	Triangular
Eff. Number of obs	1346	1361	VCE method	=	NN
Order est. (p)	1	1			
Order bias (q)	2	2			
BW est. (h)	0.243	0.243			
BW bias (b)	0.383	0.383			
rho (h/b)	0.634	0.634			
Unique obs	2606	3210			

Outcome: difdemsharenext. Running variable: difdemshare.

Method		Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
Conventional Robust					0.000	.053396	.098502

Covariate-adjusted estimates. Additional covariates included: 2 Estimates adjusted for mass points in the running variable. (est3 stored)

. _eststo: rdrobust demwinnext difdemshare, c(0) kernel(triangular) covs > (cov) Mass points detected in the running variable.

Covariate-adjusted Sharp RD estimates using local polynomial regression.

Cutoff c = 0	Left of c	Right of c	Number of obs BW type	= 6559 = mserd
Number of obs	1 2740	3819		= Triangular
				_
Eff. Number of obs	1195	1209	VCE method	= NN
Order est. (p)	1	1		
Order bias (q)	1 2	2		
BW est. (h)	0.213	0.213		
BW bias (b)	0.331	0.331		
rho (h/b)	0.643	0.643		
Unique obs	2606	3210		

Outcome: demwinnext. Running variable: difdemshare.

Method	 +-	Coef.	 Std. Err.	z	P> z	[95% Conf.	Interval]
Conventional Robust			.04179	5.1562 4.1926		.13356 .112239	.297359 .309302

Covariate-adjusted estimates. Additional covariates included: 2 Estimates adjusted for mass points in the running variable. (est4 stored)

RD Plot with evenly spaced mimicking variance number of bins using spacings esti > mators.

	Cutoff c = 0]	Left of c	Right of c	Number Kernel	obs		2697 Triangular
	Number of obs	i	1338	1359			_	IIIangulai
	Number of obs		1338	1359				
Order	poly. fit (p)	ĺ	1	1				
BW	poly. fit (h)		0.242	0.242				
Number	of bins scale		1.000	1.000				

Outcome: difdemsharenext. Running variable: difdemshare.

	Left of c	Right of c
Bins selected	44	46
Average bin length	0.005	0.005
Median bin length	0.005	0.005
IMSE-optimal bins	6	6
Mimicking Var. bins	44	46
Rel. to IMSE-optimal: Implied scale WIMSE var. weight WIMSE bias weight	7.333 0.003 0.997	7.667 0.002 0.998

```
dui rdrobust demwinnext difdemshare, c(0) kernel(triangular)

local bandwidth = e(h_l)

rdplot demwinnext difdemshare if abs(difdemshare) <= `bandwidth', ///
p(1) h(`bandwidth') kernel(triangular) graph_options(name(rdp2), replace) ///
legend(off) ytitle(Dem win (next)) xtitle(Dem margin (current))
))</pre>
```

RD Plot with evenly spaced mimicking variance number of bins using spacings esti > mators.

Cutoff c = 0	Left of c +	Right of c	Number of obs Kernel	= 2424 = Triangular
Number of obs Eff. Number of obs Order poly. fit (p) BW poly. fit (h) Number of bins scale	1203 1 1 0.216	1221 1221 1 0.216 1.000	ROTHOL	TTTUNGUTUT

Outcome: demwinnext. Running variable: difdemshare.

	Left of c	Right of c
Bins selected Average bin length Median bin length	42 0.005 0.005	43 0.005 0.005
IMSE-optimal bins Mimicking Var. bins	4 42	4 4 3
Rel. to IMSE-optimal:	10.500 0.001 0.999	10.750 0.001 0.999

```
graph combine rdp1 rdp2, rows(1) xsize(8) ysize(5)
```

. graph export rdplots2.png, as(png) replace file rdplots2.png saved as PNG format $\,$

. // Density test

. rddensity difdemshare, plot graph_opt(name(denstest, replace) legend(o
> ff))
Computing data-driven bandwidth selectors.

Point estimates and standard errors have been adjusted for repeated observations > . (Use option nomasspoints to suppress this adjustment.)

RD Manipulation test using local polynomial density estimation.

	c = (0.000	1	Left of c	Right of c	Number of o Model		6559 unrestricted
			- !	0.0	0010			
	Number of	t obs		2740	3819	BW method	=	comb
Eff.	Number of	f obs		1297	1361	Kernel	=	triangular
(Order est	. (p)		2	2	VCE method	=	jackknife
(Order bias	s (q)		3	3			
	BW est	. (h)		0.236	0.243			

Running variable: difdemshare.

Method	!	T	P> T
Robust		1.4240	0.1545

P-values of binomial tests. (HO: prob = .5)

Window Length / 2	<c< td=""><td>>=c </td><td>P> T </td></c<>	>=c	P> T
0.002 0.003 0.005 0.006 0.008 0.009 0.011 0.012 0.014 0.015	6 14 26 33 40 45 50 57 68 75	14 21 30 42 50 60 67 75 84	0.1153 0.3105 0.6889 0.3557 0.5203 0.6817 0.3909 0.4191 0.6160 0.5259

. graph export denstest.png, as(png) replace file denstest.png saved as PNG format $\,$

```
. // Validity check - using demshareprev and demwinprev as outcomes > . . . . estimates drop all
```

. _eststo: rdrobust demshareprev difdemshare, c(0) kernel(triangular) Mass points detected in the running variable.

Cutoff c = 0	Left of c	Right of c	Number of obs BW type	6559 mserd
Number of obs	1 2740	3819	Kernel	Triangular
Eff. Number of obs	1061	1082	VCE method	NN
Order est. (p)	1	1		
Order bias (q)	1 2	2		
BW est. (h)	0.187	0.187		
BW bias (b)	0.291	0.291		
rho (h/b)	0.642	0.642		
Unique obs	2606	3210		

Outcome: demshareprev. Running variable: difdemshare.

Method	ļ	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
Conventional Robust						022765 029851	.024505

Estimates adjusted for mass points in the running variable. $({\tt est1}\ {\tt stored})$

. _eststo: rdrobust demwinprev difdemshare, c(0) kernel(triangular) Mass points detected in the running variable.

Sharp RD estimates using local polynomial regression.

Cutoff $c = 0$	Left of c	Right of c	Number of obs		
	+		BW type	=	mserd
Number of obs	2740	3819	Kernel	=	Triangular
Eff. Number of obs	865	896	VCE method	=	NN
Order est. (p)	1	1			
Order bias (q)	2	2			
BW est. (h)	0.150	0.150			
BW bias (b)	0.291	0.291			
rho (h/b)	0.513	0.513			
Unique obs	2606	3210			

Outcome: demwinprev. Running variable: difdemshare.

Method		Coef.	 Std. Err.	Z	P> z	[95% Conf.	Interval]
Conventional Robust			.01301	0.0211	0.111	056486 090115	.13798

Estimates adjusted for mass points in the running variable. (est2 stored)

```
. qui esttab _all using "Table4.tex", se(3) b(3) tex replace
```

. // Validity check - continuity in covariates

. estimates drop _all

. _eststo: rdrobust demoffice exp difdemshare, c(0) kernel(triangular) Mass points detected in the running variable.

Sharp RD estimates using local polynomial regression.

Cutoff c = 0	Left of c	Right of c	Number of obs BW type	6559 mserd
Number of obs		3819 1075	Kernel	Triangular
Order est. (p) Order bias (q)	1	1 2	ven meenoa	1414
BW est. (h) BW bias (b)	0.185	0.185		
rho (h/b) Unique obs	0.539	0.539 3210		

Outcome: demofficeexp. Running variable: difdemshare.

Method		Coef.	Sto	d. Err	. z	P> z	[95% Conf.	Interval]
Conventional Robust			. 2				1243325 7399783	.684664 .653661

Estimates adjusted for mass points in the running variable. (est1 stored)

. _eststo: rdrobust othofficeexp difdemshare, c(0) kernel(triangular) Mass points detected in the running variable.

Sharp RD estimates using local polynomial regression.

Cutoff $c = 0$	Left of c	Right of c	Number of obs	
	+		z. ojpo	= mserd
Number of obs	2740	3819	Kernel	= Triangular
Eff. Number of obs	995	999	VCE method	= NN
Order est. (p)	1	1		
Order bias (q)	1 2	2		
BW est. (h)	0.172	0.172		
BW bias (b)	0.307	0.307		
rho (h/b)	0.561	0.561		
Unique obs	2606	3210		

Outcome: othofficeexp. Running variable: difdemshare.

Method	 Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
Conventional Robust					259402 242887	.529602

Estimates adjusted for mass points in the running variable. (est2 stored)

```
qui esttab all using "Table5.tex", se(3) b(3) tex replace
. // Test for continuities at other ``fake'' cutpoints
          // Here is one way to determine the deciles and save as local macros
          forvalues j=10(10)90 {
 2.
                qui centile difdemshare, centile(`j')
 3.
                local d'j' = r(c_1)
 4.
          // Fake cutpoints below 0
         estimates drop all
          forvalues j=10(10)40 {
                _eststo: rdrobust difdemsharenext difdemshare if difdemshare<0,
> ///
                c(`d`j'') kernel(triangular)
 3.
Mass points detected in the running variable.
```

Sharp RD estimates using local polynomial regression.

Cutoff $c =41254$	173	79732132	Left of cRight	of c	Number of obs		
	-+-				BW type	=	mserd
Number of obs		655	2085		Kernel	=	Triangular
Eff. Number of obs		326	481		VCE method	=	NN
Order est. (p)		1	1				
Order bias (q)		2	2				
BW est. (h)		0.116	0.116				
BW bias (b)		0.185	0.185				
rho (h/b)		0.628	0.628				
Unique obs		557	2049				

Outcome: difdemsharenext. Running variable: difdemshare.

Method		Coef.	 Std. Err.	Z	P> z	 [95% Conf.	Interval]
Conventional Robust			.02656	-0.9822 -0.9441			.025975

Estimates adjusted for mass points in the running variable. $(est1\ stored)$

Cutoff c =257012 Number of obs Eff. Number of obs Order est. (p) Order bias (q) BW est. (h) BW bias (b) rho (h/b)	2 0.108 0.175	0.108 0.175	1 2 3	c Numl BW Kern VCE	per of obs type nel method	= 2740 = mserd = Triangular = NN
Outcome: difdemshare						
	Coef.	Std. Err.	Z	P> z	[95% Con	f. Interval]
Conventional Robust	.00986	.01682	0.5862 0.5666	0.558 0.571	023109 027794	.042833
(est2 stored)						
Sharp RD estimates u	using local	polynomial	regressi	on.		
Number of obs Eff. Number of obs Order est. (p) Order bias (q) BW est. (h) BW bias (b) rho (h/b)			_	BW Keri	type nel	= 2740 = mserd = Triangular = NN
Outcome: difdemshare						
	Coef.	Std. Err.	Z	P> z	[95% Con	f. Interval]
Conventional Robust	00783 -	.02886	-0.2713	0.786	06439	.048734
(est3 stored)						
Sharp RD estimates u	using local	polynomial	regressi	on.		
Cutoff c =020856	51420440674	Left of o	cRight of	c Numl	per of obs	= 2740 = mserd
Cutoff c =020856 Number of obs Eff. Number of obs Order est. (p) Order bias (q) BW est. (h) BW bias (b) rho (h/b)	2 0.060 0.070	0.060	L 2))	Keri VCE	method	= Triangular = NN
Outcome: difdemshare	enext. Runni	ng variable	e: difdem	share.		
Method		Std. Err.	Z 	P> z	[95% Con	f. Interval]
Conventional Robust			0.0565 0.4316	0.955 0.666	060586 066468	.06418
. forvalues 2est >///	utpoints abo j=60(10)90 tsto: rdrobu d`j'') kerne	<pre>{ st difdems} cl(triangula)</pre>	ar)	difdemsl	hare if dif	demshare>0,

Cutoff c = .210406	8398475647	Left of cRight	of c	Number of obs BW type		3818 mserd
37 1 6 1	1 1104	0.604		4 1		
Number of obs	1194	2624		Kernel	=	Triangular
Eff. Number of obs	461	448		VCE method	=	NN
Order est. (p)	1	1				
Order bias (q)	2	2				
BW est. (h)	0.089	0.089				
BW bias (b)	0.137	0.137				
rho (h/b)	0.650	0.650				
Unique obs	1120	2089				

Outcome: difdemsharenext. Running variable: difdemshare.

Estimates adjusted for mass points in the running variable. $({\tt est5}\ {\tt stored})$

Mass points detected in the running variable.

Sharp RD estimates using local polynomial regression.

Cutoff $c = .339489251$	3751984	Left of cRight of c	Number of obs	=	
+			BW type	=	mserd
Number of obs	1851	1967	Kernel	=	Triangular
Eff. Number of obs	694	595	VCE method	=	NN
Order est. (p)	1	1			
Order bias (q)	2	2			
BW est. (h)	0.137	0.137			
BW bias (b)	0.217	0.217			
rho (h/b)	0.629	0.629			
Unique obs	1774	1435			

Outcome: difdemsharenext. Running variable: difdemshare.

Method	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
Conventional Robust	01984				057076 06783	.017398

Estimates adjusted for mass points in the running variable. (est6 stored)

Mass points detected in the running variable.

Sharp RD estimates using local polynomial regression.

Cutoff c = .490144	4613933563	Left of cRic	ght of c Number of BW type	obs = 3818 = mserd
Number of obs	I 2506	1312	Kernel	= Triangular
Eff. Number of obs		369	VCE method	_
Order est. (p)	1	1		
Order bias (q)	2	2		
BW est. (h)	0.146	0.146		
BW bias (b)	0.235	0.235		
rho (h/b)	0.622	0.622		
Unique obs	2421	788		

Outcome: difdemsharenext. Running variable: difdemshare.

Method		Coef.	Std. Err.	z	P> z	[95% Conf.	Interval]
Conventional Robust						.011377 .010871	.09402

Estimates adjusted for mass points in the running variable. (est7 stored)

Mass points detected in the running variable.

```
3818
Cutoff c = .8602508306503296 | Left of cRight of c Number of obs =
                                                    mserd
                                       BW type = mserd
Kernel = Triangular
Number of obs | 3162 656 Eff. Number of obs | 28 28
                  28
                                       VCE method =
                             28
                   1
2
                             1 2
  Order est. (p) |
    Dw est. (h) | 0.031
BW bias (b) | 0.062
rho (h/b) | 0.507
Unique obs | 3061
   Order bias (q) |
                         0.031
0.062
                          0.507
                             148
Outcome: difdemsharenext. Running variable: difdemshare.
______
       Method | Coef. Std. Err. z P>|z| [95% Conf. Interval]
Estimates adjusted for mass points in the running variable.
(est8 stored)
       qui esttab all using "Table6.tex", se(3) b(3) tex replace
       graph close all
. // *****
· // (2)
· // *****
. // *******************************
. // Illustration of not-centering running variable - using in-class exercise
. // 3 (Carruthers example)
clear
       set seed 195423
       set obs 10000
Number of observations (_N) was 0, now 10,000.
       gen id= n
       gen trueability = 50 + 4*rnormal()
       gen grade3test = trueability + rnormal()
       replace grade3test = round(grade3test, 0.25)
(10,000 real changes made)
. //
       students at or above 56 are eligible for G&T. Create a "gap" variable
. //
         centered at 56
       gen above56 = (grade3test>=56)
       gen gap = grade3test-56
```

assuming perfect compliance, everyone above 56 is treated (inGT) and

everyone below is not

. //

```
gen inGT = above56
. //
     create a grade 4 outcome variable
     gen grade4test = round(trueability + 5 + rnormal() + (3*inGT), 0.25)
. // RD model where grade3test centered at 0 (gap)
     reg grade4test c.gap##i.inGT
______
grade4test | Coefficient Std. err. t P>|t| [95% conf. interval]
   gap | .939221 .0040802 230.19 0.000 .9312229 .9472191
1.inGT | 3.02236 .0798731 37.84 0.000 2.865792 3.178927
 inGT#c.gap |
         .0046223 .0313781 0.15 0.883 -.0568851
                                         .0661296
         60.61455 .0306168 1979.78 0.000
 _cons |
                                  60.55453 60.67456
. // RD model using non-centered grade 3 test
     reg grade4test c.grade3test##i.inGT
                       MS Number of obs = 10,000
           SS
   Source |
  ______
 grade4test | Coefficient Std. err. t P>|t| [95% conf. interval]
-----
 inGT#|
c.grade3test |
   1 | .0046223 .0313781 0.15 0.883 -.0568851 .0661296
_cons | 8.018173 .2020343 39.69 0.000 7.622145 8.414201
```

capture log close