

Kruskal (MST): Really Special Subtree



Problem	Submissions	Leaderboard	Discussions
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Given an undirected weighted connected graph, find the Really Special SubTree in it. The Really Special SubTree is defined as a subgraph consisting of all the nodes in the graph and:

- There is only one exclusive path from a node to every other node.
- The subgraph is of minimum overall weight (sum of all edges) among all such subgraphs.
- No cycles are formed

To create the Really Special SubTree, always pick the edge with smallest weight. Determine if including it will create a cycle. If so, ignore the edge. If there are edges of equal weight available:

- Choose the edge that minimizes the sum $u + v + wt$ where u and v are vertices and wt is the edge weight.
- If there is still a collision, choose any of them.

Print the overall weight of the tree formed using the rules.

For example, given the following edges:

u	v	wt
1	2	2
2	3	3
3	1	5

First choose $1 \rightarrow 2$ at weight **2**. Next choose $2 \rightarrow 3$ at weight **3**. All nodes are connected without cycles for a total weight of $3 + 2 = 5$.

Function Description

Complete the *kruskals* function in the editor below. It should return an integer that represents the total weight of the subtree formed.

kruskals has the following parameters:

- *g_nodes*: an integer that represents the number of nodes in the tree
- *g_from*: an array of integers that represent beginning edge node numbers
- *g_to*: an array of integers that represent ending edge node numbers
- *g_weight*: an array of integers that represent the weights of each edge

Input Format

The first line has two space-separated integers *g_nodes* and *g_edges*, the number of nodes and edges in the graph.

The next *g_edges* lines each consist of three space-separated integers *g_from*, *g_to* and *g_weight*, where *g_from* and *g_to* denote the two nodes between which the **undirected** edge exists and *g_weight* denotes the weight of that edge.

Constraints

- $2 \leq g_nodes \leq 3000$
- $1 \leq g_edges \leq \frac{N*(N-1)}{2}$
- $1 \leq g_from, g_to \leq N$
- $0 \leq g_weight \leq 10^5$

****Note: **** If there are edges between the same pair of nodes with different weights, they are to be considered as is, like multiple edges.

Output Format

Print a single integer denoting the total weight of the Really Special SubTree.

Current Buffer (saved locally, editable)

C++

```
1 #include <iostream>
2 #include <vector>
3 #include <list>
4 #include <algorithm>
5 using namespace std;
6
7 struct Pair{
8     int index;
9     int weight;
10 };
11 struct Node{
12     list<Pair> neighbours;
13     bool hasNeighbour(int index){
14         for(auto it:neighbours){
15             if(it.index==index){
16                 return true;
17             }
18         }
19         return false;
20     }
21     void addNeighbour(int index,int weight){
22         neighbours.push_back({index,weight});
23     }
24 };
25 struct Edge{
26     int from;
27     int to;
28     int weight;
29     bool operator <(const Edge& right) const{
30         return weight<right.weight;
31     }
32 };
33 struct Graph{
34     vector<Node> nodes;
35     Graph(int nodeCount=0){
36         nodes.resize(nodeCount);
37     }
38     void connect(int from, int to, int weight){
39
40         nodes[from].addNeighbour(to,weight);
41         nodes[to].addNeighbour(from,weight);
42     }
43
44     vector<Edge> getAllEdges(){
45         vector<Edge> allEdges;
46         for(int i=0;i<nodes.size();i++){
47             for(auto it:nodes[i].neighbours){
48                 if(i<it.index){
49                     allEdges.push_back({i,it.index,it.weight});
50                 }
51             }
52         }
53         return allEdges;
54     }
55
56     int kruskal(){
57         int result=0;
58         vector<Edge> allEdges=getAllEdges();
59         sort(allEdges.begin(),allEdges.end());
60         vector<int> components(nodes.size());
61         for(int i=0;i<nodes.size();i++){
62             components[i]=i;
63         }
64         for(auto Edge:allEdges){
65             if(components[Edge.from]!=components[Edge.to]){
66                 result+=Edge.weight;
67                 int oldComp=components[Edge.from];
68                 int newComp=components[Edge.to];
69                 for(int i=0;i<components.size();i++){
70                     if(components[i]==oldComp){
71                         components[i]=newComp;
72                     }
73                 }
74             }
75         }
76         return result;
77     }
78 };
79 int main(){
80     int nodeCount;
81     int edgeCount;
82     cin>>nodeCount;
83     cin>>edgeCount;
84     int from,to,weight;
85     Graph g(nodeCount);
86     for(int i=0;i<edgeCount;i++){
87         cin>>from>>to>>weight;
88         g.connect(from-1,to-1,weight);
89     }
90
91     cout<<g.kruskal();
92     return 0;
93 }
94 }
```

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