Total Ennon =  $E = d_1 + d_2 + d_3 + ... + d_n$ =  $d_2^2 + d_2^2 + d_3^2 + ... + d_n^2$ =>  $E = \frac{Q}{i=1} d_i^2 \qquad | d = y_i - \hat{y}_i$ =>  $E = \frac{Q}{i=1} (y_i - \hat{y}_i)^2$ i=n

A regression line in created to calculating the when input and output columns value of m (slope) and b intercepts. Now we have to calculate create a line i.e. a m and b for what the total error i.e. E of that line will be minimized. It is the value for x; which is created by that line but we have to predict Ji for that x;.

E can only be minimized SELECTING UPON THE PIGHT m and b.

:. ŷ; = mx; tb

EES

: E(m,b) = \(\frac{1}{2}(\frac{1}{2}i - mn; -b)^{\frac{1}{2}}\)

[Read right side's explanation].

Led's find man b now.

E high

E high

E high

E high high high high high

It we ppin the line to on center (since b=0), our E in terms of m changes somewhat like parabala.

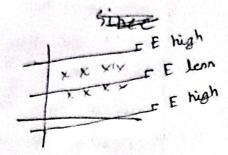
there both hi and Ji ane constant, which in given an the dataset. We can only change the value of m and b to create what even line we want because that line may pass through the points on not for our enperiment purpose.

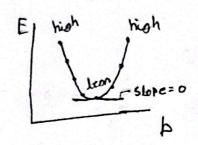
E(m,b) is now a bunction which depends on the value of manb as they are not constant.

for mand b will be completed abten calculating them but belone that we can draw it ANYWHERE we want it but we need to bind such m and 6 bore what total ennow will be minimized.

ion b

Annume m=1 i.e. constant i.e. the constant





So bon the changer of b, my E is changing lite parabola.

So box in terms of both mand b. E changes like Parabola. Our & target in to have the 'lens' paint to minimize the Error bunction. The Slope at 'lens' in O. I stope=0 which in obvious. And to calculate hope need to do derivative and equal the it to O since or slope=0 derivative == slope

And how do we calculate plope? The changes of y box the changes of x | a penticular - point - ot - x e.g. dy dx.

For our case, we want the error bunction be minimized for both m and b. so our slopes,  $\frac{\partial E}{\partial m}$  and  $\frac{\partial E}{\partial h}$ . But since the  $\Rightarrow$ ennon bunction is minimized on 'lear' paint Cohene Blope ( JE bon E, m graph, JE bon E, b graph)

$$\frac{3\mu}{9E} = 0$$

$$\frac{3\rho}{9E} = 0$$

 $\frac{\partial E}{\partial m} = 0. \quad \frac{\partial E}{\partial b} = 0$ This is what we need to do now to minimize the E box in terms ob both mand be which in our main target in Lincour Regression

$$\frac{1}{2}y_i - \sum_{i=1}^{n} m x_i - \sum_{i=1}^{n} b = 0$$

$$\frac{\sum_{i=1}^{n}y_{i}}{n} - \frac{\sum_{i=1}^{n}y_{i}}{n} - \frac{\sum_{i=1}^{n}y_{i}}{n} = 0$$

$$-3$$
  $\sqrt{y}$  -  $m\bar{n}$  -  $mb$  in constant here.

Let by the state of t

$$:E = \sum (y_i - mn_i - y + m\bar{n})^2 \left| \sum_{i=1}^{\infty} \frac{n_i}{i} \right|$$

$$\frac{3m}{3E} = 0$$

$$=) \sum_{i=1}^{n} (y_i - mx_i - \hat{y} + mx_i)^2 = 0$$

=> 
$$\sum -2 [(y_1 - \bar{y}) - m(n_1 - \bar{n})] (n_1 - \bar{n}) = 0$$

=> 
$$\sum [(y_i-\hat{y})(x_i-\hat{x}) - m(x_i-\hat{x})^2] = 0$$

So Simple Linear Regression is all about: Draw that regression line(the Predicted values for input column) in a way with such m and b, so the Total Error gets minimized.

