What are Algebraic Variables?

In Algebra a variable, like x, is an unknown value

$$x+5 = 10 \Rightarrow x=5$$

0.0 - 1 - 4

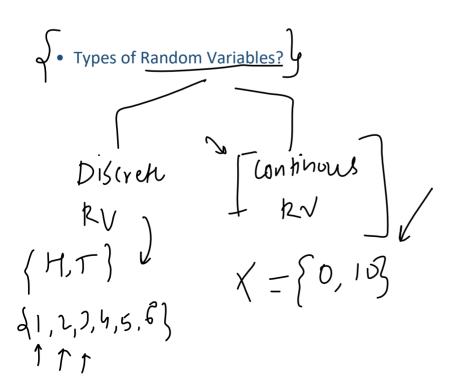
• What are Random Variables in Stats and Probability?

A Random Variable is a set of possible values from a random experiment.

$$X = \{1,0\}$$

$$XYZ$$
 x,y,z

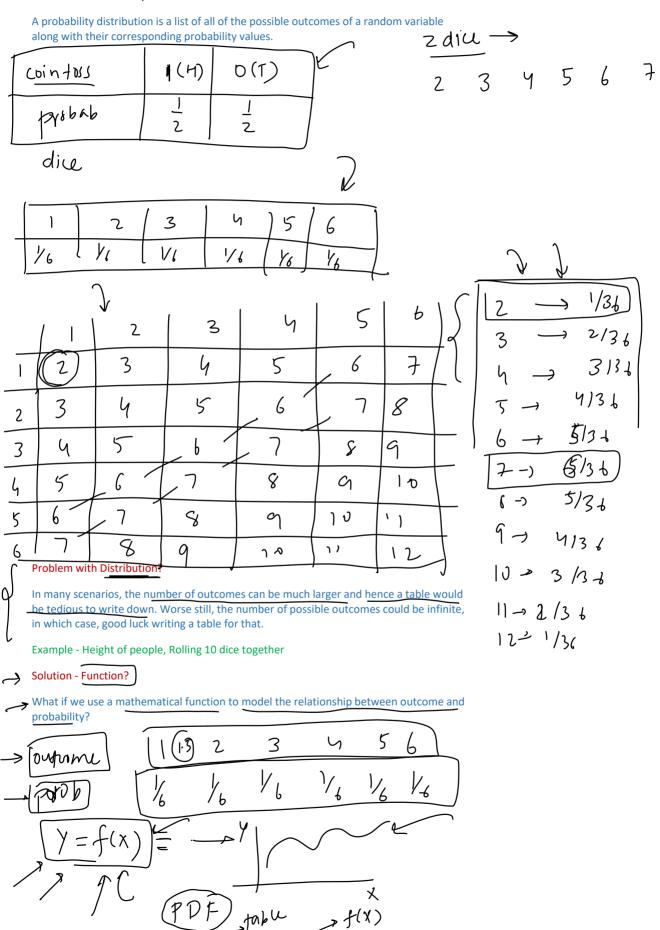
$$\frac{X}{X} = \frac{1}{2}, \frac{1}{2},$$



Probability Distributions

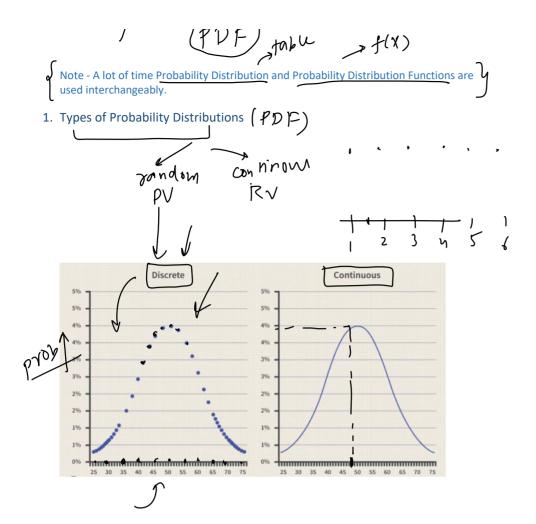
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1. What are Probability Distributions?

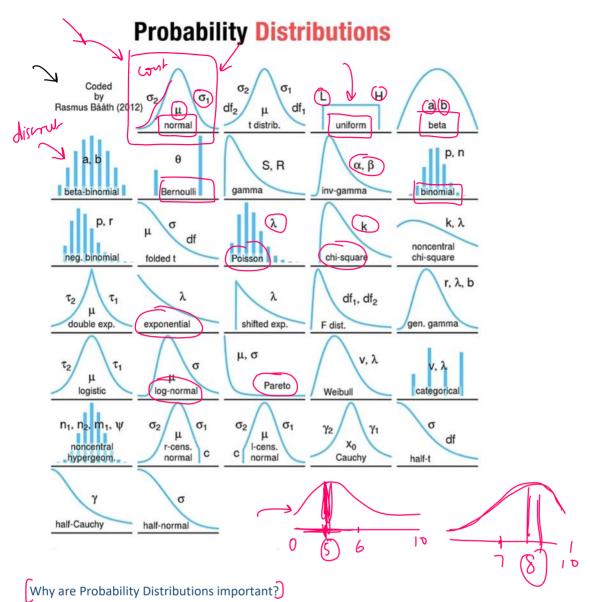


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Note - A lot of time Probability Distribution and Probability Distribution Functions are



Famous Probability Distributions



- Gives an idea about the shape/distribution of the data.

And if our data follows a famous distribution then we automatically know a lot about the data.

A note or Parameters (PDF)

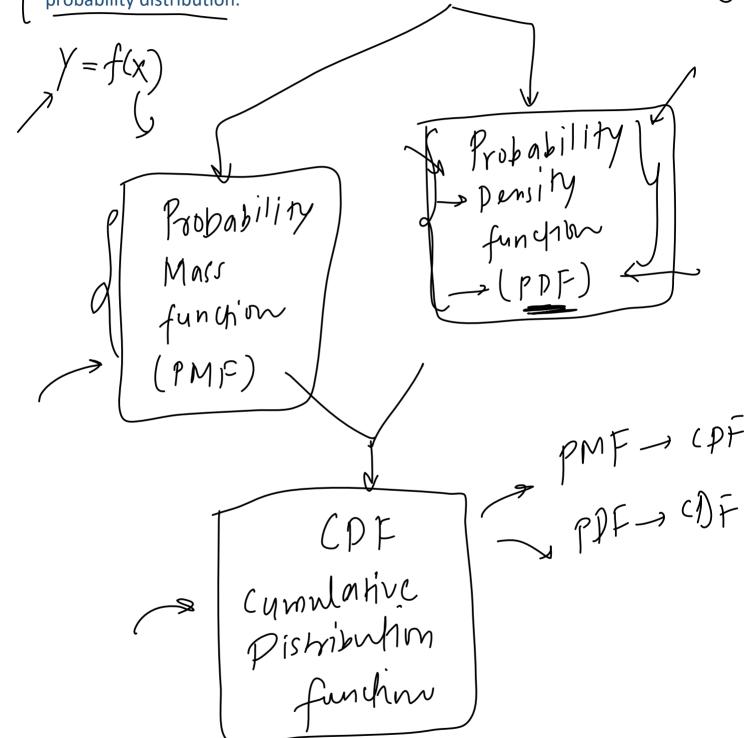
Parameters in probability distributions are numerical values that determine the shape, location, and scale of the distribution.

<u>Different probability distributions</u> have different sets of parameters that <u>determine their</u> shape and characteristics, and <u>understanding these parameters</u> is <u>essential</u> in statistical analysis and <u>inference</u>.

Probability Distribution Functions $\rightarrow PDF$ 20:08

15 March 2023

A probability distribution function (PDF) is a mathematical function that describes the probability of obtaining different values of a random variable in a particular probability distribution.



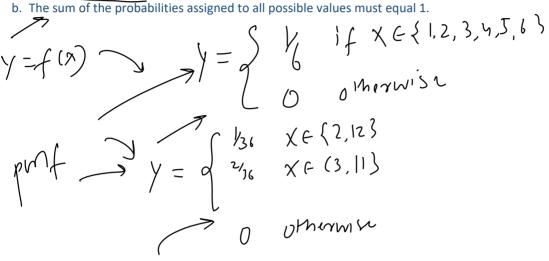
Probability Mass Function (PMF)

PMF stands for Probability Mass Function. It is a mathematical function that describes the probability distribution of a discrete random variable.

The PMF of a discrete random variable assigns a probability to each possible value of the random variable. The probabilities assigned by the PMF must satisfy two conditions:

a. The probability assigned to each value must be non-negative (i.e., greater than or equal to zero).

b. The sum of the probabilities assigned to all possible values must equal 1.



Examples

https://en.wikipedia.org/wiki/Bernoulli distribution

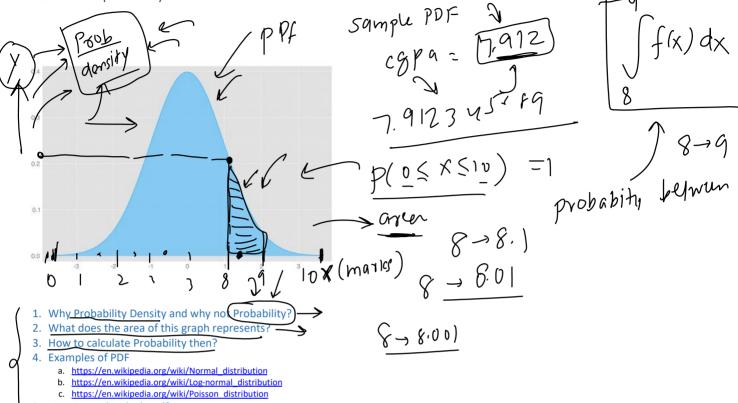
https://en.wikipedia.org/wiki/Binomial distribution

The cumulative distribution function (CDF) F(x) describes the probability that a random variable X with a given probability distribution will be found at a value less than or equal to x $F(x) = P(X \le x)$ $f(x=5) = \frac{1}{6}$ = f(x=4) + f(x=3) + f(x=3)Examples: 3 https://en.wikipedia.org/wiki/Bernoulli distribution https://en.wikipedia.org/wiki/Binomial distribution 3/6 4/6

Probability Density Function (PDF)

5. How is graph calculated?

PDF stands for Probability Density Function. It is a mathematical function that describes the probability distribution of a **continuous random variable.**



Density Estimation

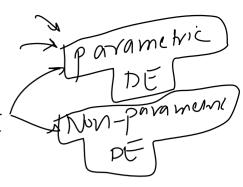
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Density estimation is a <u>statistical technique</u> used to estimate the <u>probability</u> density function (PDF) of a random variable based on a <u>set of observations</u> or data. In <u>simpler terms</u>, it involves estimating the <u>underlying distribution of a set of data points</u>.

Density estimation can be used for a variety of purposes, such as **hypothesis testing**, **data analysis**, **and data visualization**. It is particularly useful in areas such as **machine learning**, where it is often used to estimate the probability distribution of input data or to model the likelihood of certain events or outcomes.

There are various methods for density estimation, including **parametric** and **non-parametric approaches**. Parametric methods <u>assume that the data follows a specific probability distribution</u> (such as a normal distribution), <u>while non-parametric methods</u> do not make any assumptions about the distribution and instead estimate it directly from <u>the data</u>.

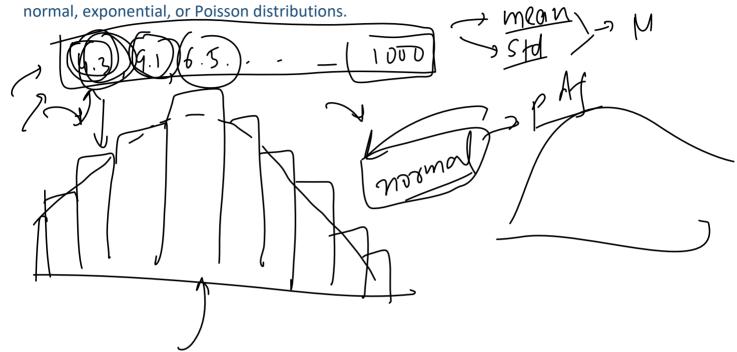
Commonly used techniques for density estimation include kernel density estimation (KDE), histogram estimation, and Gaussian mixture models (GMMs). The choice of method depends on the specific characteristics of the data and the intended use of the density estimate.



Parametric Density Estimation

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Parametric density estimation is a method of estimating the probability density function (PDF) of a random variable by assuming that the underlying distribution belongs to a specific parametric family of probability distributions, such as the



Non-Parametric Density Estimation (KDE)

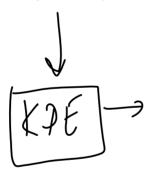
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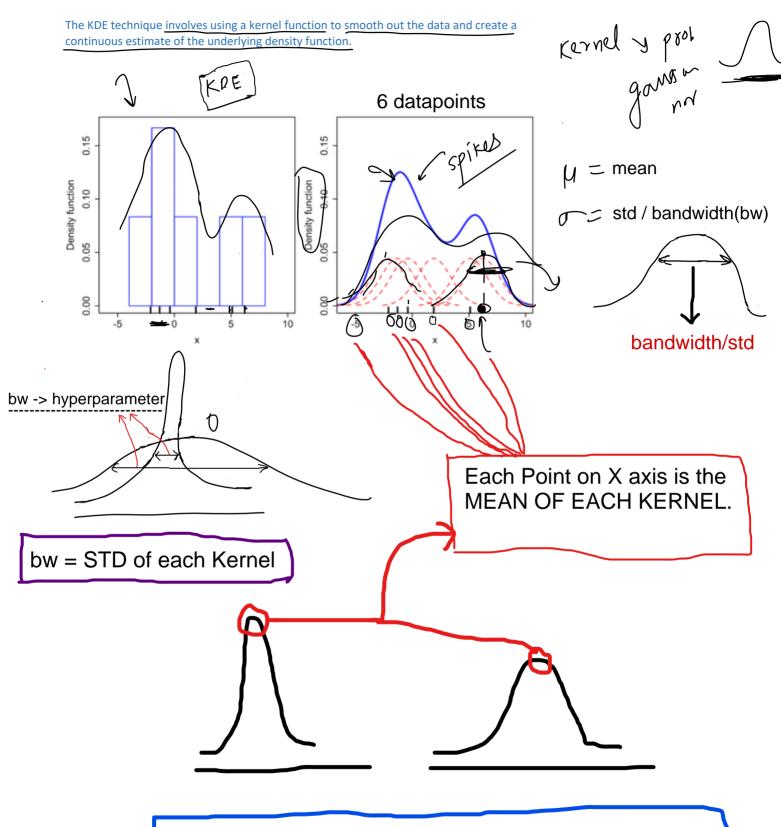
But sometimes the distribution is not clear or it's not one of the famous distributions.

Non-parametric density estimation is a <u>statistical technique</u> used to <u>estimate the probability</u> density function of a <u>random variable without making any assumptions about the underlying distribution. It is also <u>referred to as non-parametric density estimation</u> because it does not require the use of a predefined probability distribution function, as opposed to <u>parametric methods</u> such as the <u>Gaussian distribution</u>.</u>

The non-parametric density estimation technique involves constructing an estimate of the probability density function using the available data. This is typically done by creating a kernel density estimate

Non-parametric density estimation has several advantages over parametric density estimation. One of the main advantages is that it does not require the assumption of a specific distribution, which allows for more flexible and accurate estimation in situations where the underlying distribution is unknown or complex. However, non-parametric density estimation can be computationally intensive and may require more data to achieve accurate estimates compared to parametric methods.

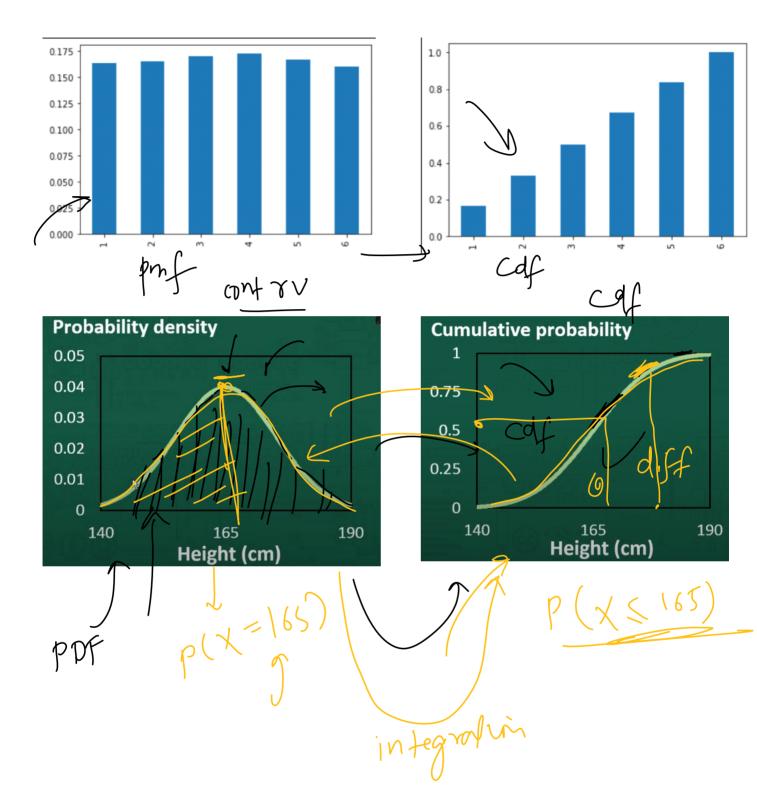




The mean is at the TOP which is each point on X axis but the std of both is not same. So, at first we need to decide what std will be for each kernel.

Cumulative Distribution Function(CDF) of PDF

15 March 2023 15:25



How to use PDF and CDF in Data Analysis

15 March 2023 20:10

2D Probability Density Plots

16 March 2023 06:50