

VU Computational Aspects of Digital Fabrication

3D Printable Microstructures from Polyhedral Voronoi Diagrams

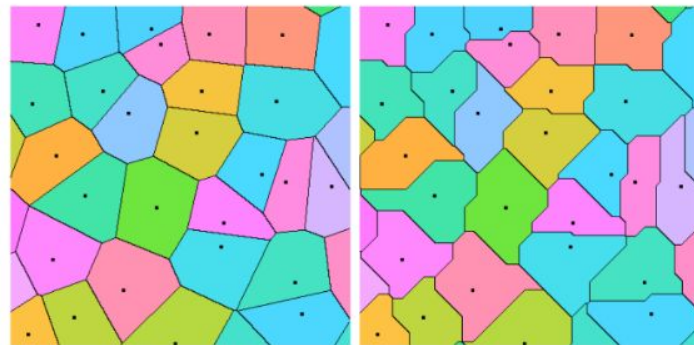
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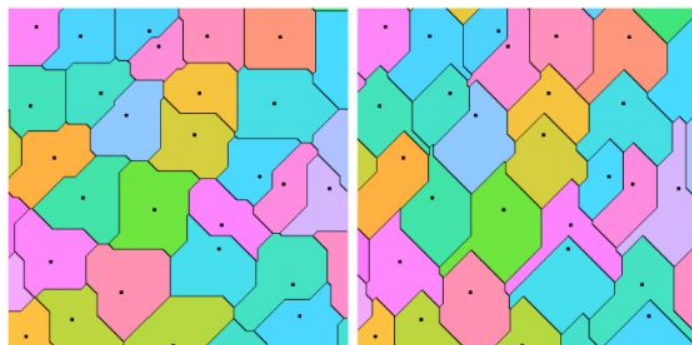
Idea (2D)

- Jonàs Martínez et al.: Polyhedral Voronoi diagrams for additive manufacturing



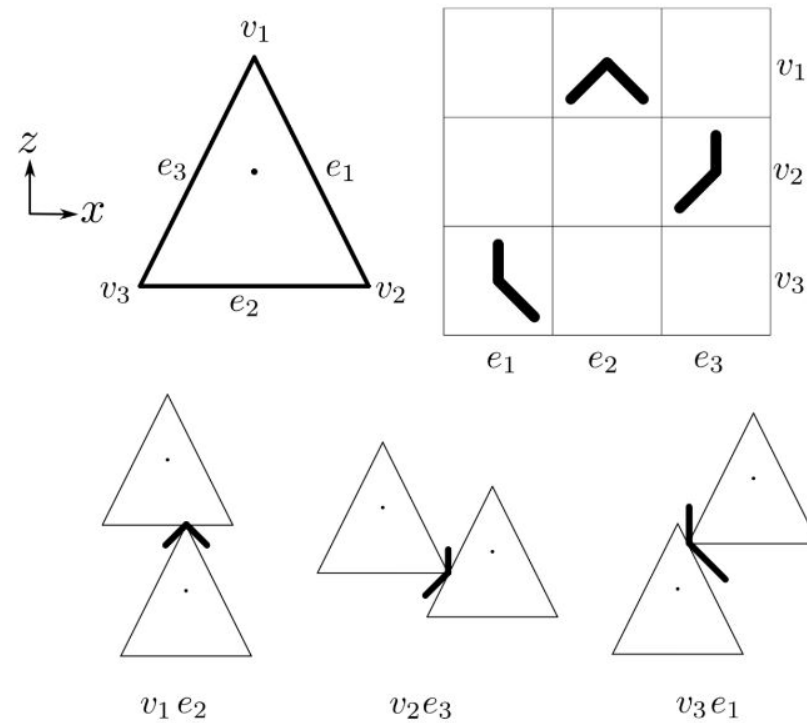
Euclidean \bigcirc

L_1 \diamond

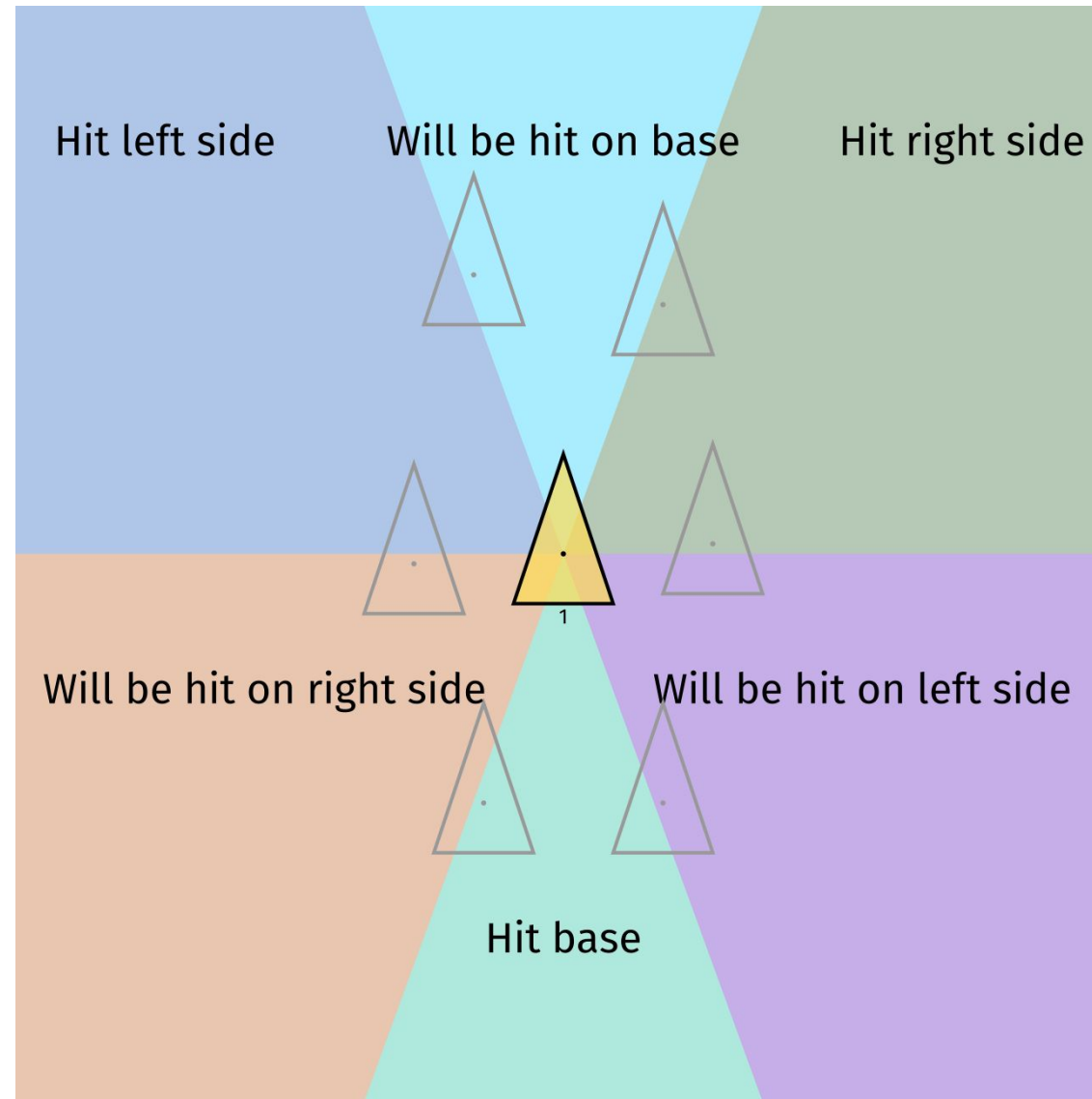


L_∞ \square

Cone \triangle



Collision Planning: HOW will the Triangles collide?



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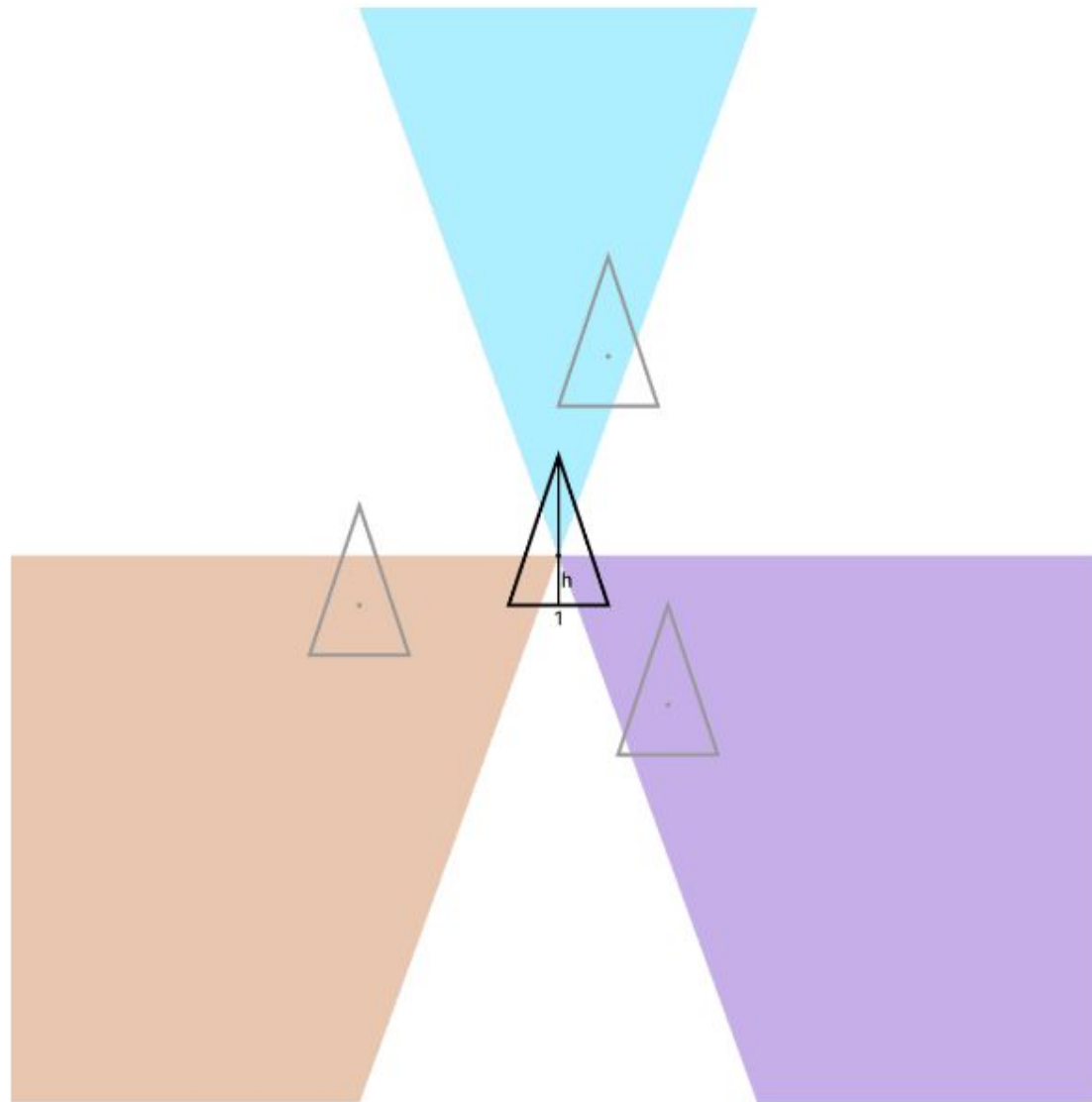
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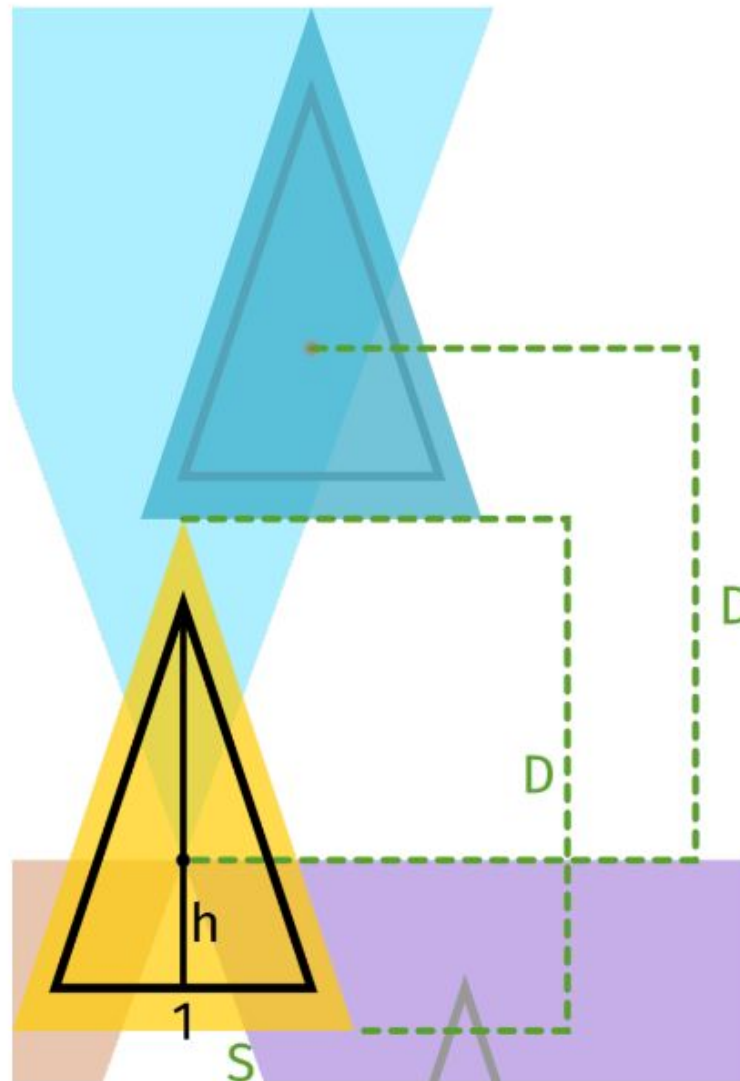
Collision Planning: WHERE will the Triangles collide?



Every triangle hits 3 other triangles
(or a bounding wall)



Collision Planning: WHERE will the Triangles collide?

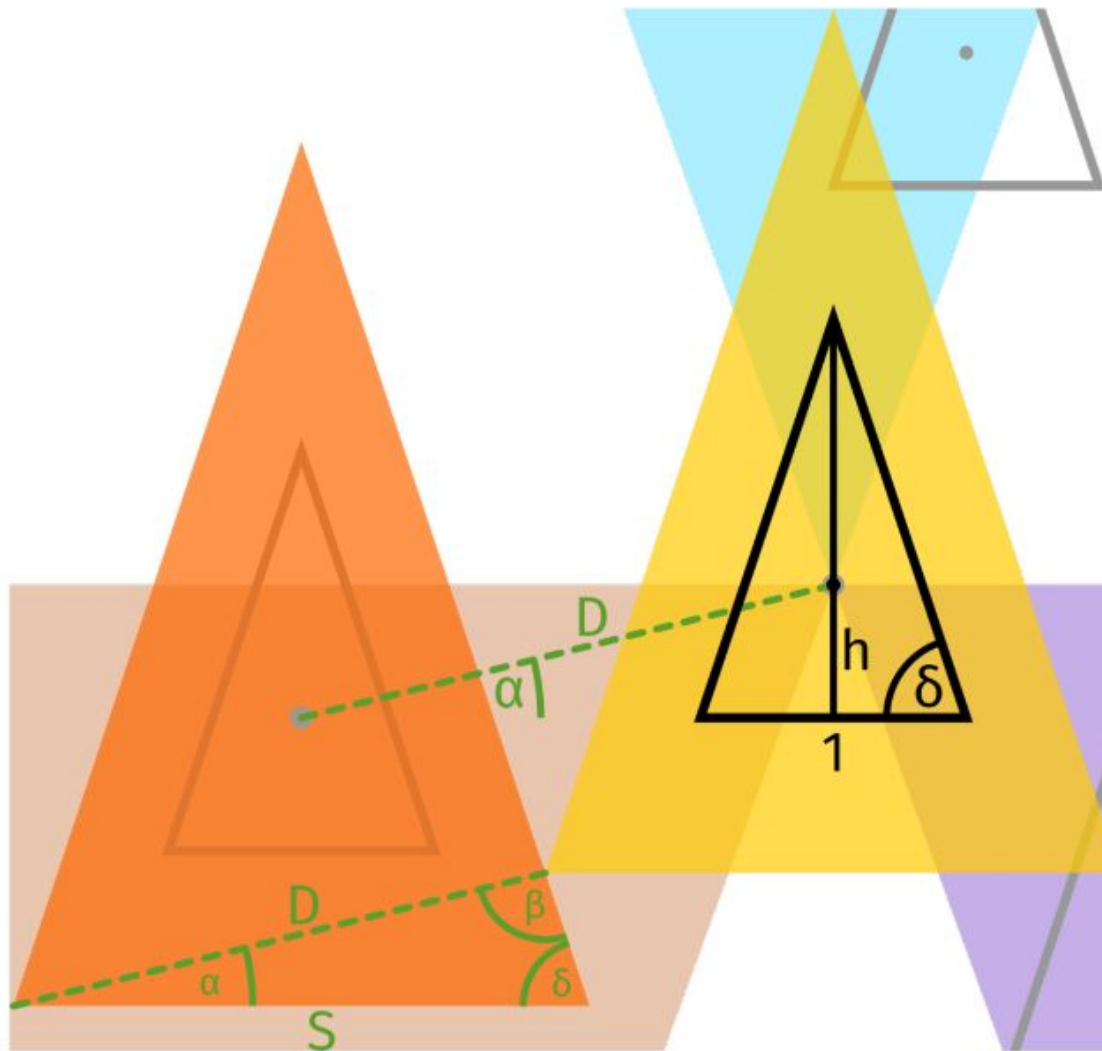


Base Hit Scale

$$\frac{D}{h} = \frac{S}{1}$$
$$S = \frac{D}{h}$$



Collision Planning: WHERE will the Triangles collide?



Side Hit Scale

$$\beta = 180 - (\alpha + \delta)$$

Law of Sines

$$\begin{aligned}\frac{D}{\sin \delta} &= \frac{S}{\sin \beta} \\ S &= \frac{D}{\sin \delta} \cdot \sin \beta \\ S &= \frac{D}{\sin \delta} \cdot \sin [180 - (\alpha + \delta)]\end{aligned}$$



- Create random points stored in a list points
- Create two lists of points
- For base = 1, find h and δ
 - pointsx = points sorted by x
 - pointsy = points sorted by y



- 4) Set currentScale = 1
- 5) In a loop, do the following
 - 1) Find minimal scale $>$ currentScale for two triangles to collide, respecting
 - 1) Hitted triangle center is in hitting zone of hitting triangle center
 - 2) Hitting point has analyzed hitting zone = true
 - 3) For base hit, use use Base Hit Scale (Euclidean Distance)
 - 4) For side hit, use Side Hit Scale
 - 2) Store the following information in a list
 - Hitting point, Hitted point, Hitting side, Coordinates, (Scale factor)
 - 3) For the hitting point set respective hitting zone (top, left or right) to false
 - 4) Set currentScale = scale factor



- Tried with FreeCAD
 - Idea: Use FreeCAD sketcher tools to do the math for us
 - Pros: Works pretty good in theory, helps try out geometric ideas
 - Cons: Begins to struggle really fast, syntax is rather difficult
- Visual Debugging using a simple renderer in C++
 - Pros: Faster code, simpler math operations, custom GUI debugging
 - Cons: Building a custom renderer using C++/OpenGL
- Python using Plotly 3D graphs
 - Pros: Features 3D camera movements and tooltips out of the box, renders many thousand points flawlessly once loaded
 - Cons: Designed for plots, objects are per default distorted if too far between



