Optimization Algorithms

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1 introduction

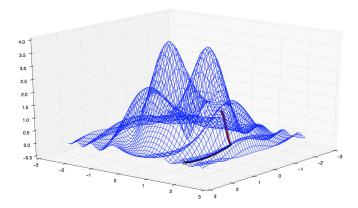
Three algorithms were used to varying degrees of effect to find the global minima of a given function:

$$z = \frac{\sin(x^2 + 3y^2)}{0.1 + r^2} + (x^2 + 5y^2) \times \frac{\exp(1 - r^2)}{2}, r = \sqrt{x^2 + y^2}$$
 (1)

The global minima, rounded to 10 decimals, was found to be -0.1502519641, which corresponds to the points x = -2.17 y = 0.0.

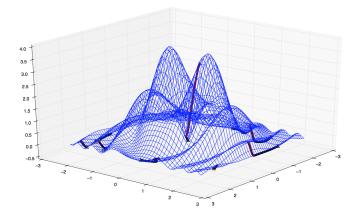
2 Hill Climbing

Hill climbing was the first and simplest method used. Hill climbing is a greedy algorithm that simply searches for the best adjecent step and moves there until no better moves remain. Over a thousand trials the mean minimum was -0.120838860537 with a standard deviation of 0.0408106788745. The average time it took to find the min was 0.0079797763826 seconds.



3 Hill Climbing With Random Restarts

Hill climbing with random restarts worked the best out of all the algorithms acheiving an average min of -0.150221658736 with a standard deviation of 0.000957860475357. Adjusting the step size to .01 allowed for the algorithm to only need 12 random restarts to find the global min about 99.9% of the time, And did so in a brisk 0.0915080306533 seconds on average.



4 Simulated Annealing

Simulated annealing on average found a slightly better mininimum than standard hill climbing at -0.123023846929 with a slightly lower standard deviation of 0.0236085881272, however the time it took was an order of magnitude higher at 0.0756657974717. Looking at the graph it seems simulated annealing often went over the area where the global minima lies and got stuck in other local minima as it began to cool. its effectiveness could probably be greatly increased if it remembered promosing positions. Another reason it seems such a simple algorithm like hill climbing in some sense outpreformed simulated annealing was the relatively large area of the graph that would lead to the global minima through hill climbing. If it was a funcion with more local minima for hill climbing to get stuck in perhaps simulated annealing would have prefromed much better in comparison.

