

# Final Undergraduate Psuedo-Sudoku Submission

Spencer Hirsch, Thomas Johnson

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## Summary of Project

Following our original submission we have implemented another algorithm. With our original submission we implemented a backtracking algorithm, which worked very well for our first milestone. For this final milestone we have implemented a forwarding checking with a heuristic algorithm. Both algorithms solve the given test cases, however after doing an analysis of the two comparing the input size and the number of removed cells there is a clear difference in the complexity of the two different algorithms.

In order to generate reasonable test cases to demonstrate the time complexity of our our two algorithms. We have implemented a generator to generate test cases to give to our algorithms. Each algorithm tests a total of 2700 different test cases with varying difficulty. The goal of implementing a generator was to make the tests as random as possible and to easily generate a larger sum of test cases. For each  $n$  (the size of the matrix,  $n \times n$ ) there are 15 additional test cases that have varying  $m$  (number of missing cells). Each of these  $n \times m$  combinations is tested a total of 30 times. This is how we have determined that there are a total of 2700 different test cases run on each of the algorithms.

All aspects of the board aside from the size of the board is randomly determined. The values for each squares are randomly assigned for the size of the board. Once all of the values are determined the number of removed cells is randomly selected and unique to each row. The purpose of creating this random algorithm was to ensure that bias was reduced.

In order to demonstrate the time complexity of each of the algorithms the cpu time is recorded for each test and plotted against the number of removed squares from the sudoku board. To ensure the accuracy of our results the same test cases are run on both of the algorithms. Two scatter plots are constructed for the two algorithms, one displaying every point gathered from the test sets and the other plot demonstrating the averages of the 15 points for each  $n \times m$  pair.

## Backtracking Algorithm

```
# Function next empty cell in the matrix

def find_cell(board, size):
    iterate through the board to find the next instance of a 0 value in
    a cell

    If no value is found, return -1, -1

    otherwise return the coordinate of the cell that contains a 0 value

# Function checks for a valid move given the value of the current
# Cell

def valid_move(coordinate_1, coordinate_2, board, size, number):

    Iterate through the size of the board
        Check to see if there is a cell in the column has the current val
        if so, return false

    Iterate through the size of the board
        Check to see if there is a cell in the row that has the current val
        If so, return false

    return true # It is a valid move for the algorithm to make

def solve(board, size):
    Create a list of all possible numbers based on size of the board
    Find the coordinate to the next empty cell
```

Check to see if cell is valid

iterate through all possible numbers to fill a cell

Check to see if the move is a valid move

Continue until all cells are filled or no solution is found

*How the backtracking algorithm works:*

## Forwarding-checking with Heuristic

*How the forwarding-tracking with heuristic algorithm works:*

## **Analysis of Algorithms**

*Backtracking*

*Forward-checking with Heuristic*