PLANETESIMAL ACCRETION AT SHORT ORBITAL PERIODS

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ABSTRACT

Formation models in which terrestrial bodies grow via the pairwise accretion of planetesimals have been reasonably successful at reproducing the general properties of the solar system, including small body populations. However, planetesimal accretion has not yet been fully explored in the context of more exotic terrestrial systems, particularly those that host short-period planets. In this work, we use direct N-body simulations to explore and understand the growth of planetary embryos from planetesimals in disks extending down to $\simeq 1$ day orbital periods. We show that planetesimal accretion becomes nearly 100 percent efficient at short orbital periods, leading to embryo masses that are roughly twice as large as the classical isolation mass. For rocky bodies, the physical size of the object begins to occupy a significant fraction of its Hill sphere at orbital periods less than about 50 days. In this regime, most close encounters result in collisions, rather than scattering, and the system cannot bifurcate into a collection of dynamically hot planetesimals and dynamically cold oligarchs, like is seen in previous work. The highly efficient accretion seen at short orbital periods implies that systems of tightly-packed inner planets should be almost completely devoid of any residual small bodies. We demonstrate the robustness of our results to assumptions about the initial disk model, and also investigate how far material can radially mix across the accretion boundary.

1. INTRODUCTION

Planetesimal accretion is one of a number of stages in which micron-sized solids from the protostellar nebula coalesce to eventually build terrestrial planets. In the earliest stages, aerodynamic forces dominate the growth and evolution of the solids. Millimeter-sized bodies grow through adhesive pairwise collisions and stay wellcoupled to the surrounding gas. Beyond this size, however, a number of growth barriers present themselves. Most notably, larger solids orbit the central star at Keplerian speeds as they decouple from the gas, which orbits at a sub-keplerian speed due to radial pressure support. This leads the solids to feel a headwind, which is maximally effective at sapping away angular momentum for objects around 1 meter in size. At this size, the timescale for the growing solids to fall onto the star is catastrophically short and leads to what is known as the drift barrier. In addition, two-body collisions between mm- to cm-sized bodies tend to result in bouncing or destruction, rather than continued growth. For these reasons, a number of mechanisms have been proposed which facilitate fast growth from mm to km sizes by locally concentrating solids. Dust traps, streaming instability, pebble piles...etc.

Beyond kilometer scales, gravity begins to dominate and aerodynamic gas drag plays a smaller and smaller role. During this phase, collision cross sections are enhanced as gravitational focusing (safronov citation) acts to bend the trajectories of bodies undergoing close encounters. Large bodies are most effective at focusing the trajectories of nearby planetesimals, leading to a period of runaway growth (citations to wetherill, kokubo+ida, barnes). Eventually, the largest bodies (known as oligarchs) dynamically heat the surrounding planetesimals, severely limiting further growth (cite kokubo+ida). The end result of this phase is a bimodal population of dynamically cold oligarchs, surrounded by dynamically hot, difficult to accrete residual planetesimals. Lines of evidence suggest that the asteroid belt, kuiper belt and the oort cloud are largely composed of the leftovers of this stage of planet formation. (Mention more specific evidence, morbidelli 09 paper, CAIs?)

Although gas drag has a minimal influence on the Moon to Mars-sized oligarchs, it is enough to prevent these largest bodies from perturbing each other onto crossing orbits. Simulations show that evaporation of the gas disk is required to allow instability to trigger a phase of giant impacts (Mention that disk fraction decay timescale roughly matches timing of giant impacts in SS). It is during this phase that oligarchs collide to form Earth-sized planets (chambers wetherill 1998, raymond 2006).

Over the last few decades, terrestrial planet formation models have largely advanced by matching properties of the solar system. Compared to exoplanetary systems,

the solar system provides a rich set of constraints (isotopic ratios, cratering records, small body populations) that are mostly unmeasurable for even the closest neighboring planet forming systems. However, the system architectures discovered by spaced-based missions in the last decade reveal that the solar system could very well be an outlier in terms of what a typical planet-forming disk produces. In addition, the sizes and compositions of the terrestrial planets likely rely on a series of finelytuned events to play out that involve truncation of the primordial planetesimal disk (Raymond & Izidoro 2017), inward, followed by outward migration of an outer giant planet (Walsh et al. 2011), or a large-scale instability triggered by a pair of convergently migrating giant planets (Tsiganis et al. 2005; Levison et al. 2011; Nesvorný 2011). Given qualitatively similar initial conditions, solar system formation models can even occasionally reproduce the correct masses and orbital periods of the terrestrial planets without invoking any of the aforementioned scenarios, given the right random number seed (Fischer & Ciesla 2014).

Given the difficult question of whether to treat the solar system as an outlier, the best way forward is to use statistical samples of exoplanetary architectures to develop and inform formation models. This is generally done through the use of population synthesis models (ida + lin, alibert), but many of the mechanisms in these models are informed and tuned by solar system constraints. One pervasive and exotic result revealed by the Kepler space telescope has the discovery of hundreds of compact multi-planet terrestrial systems, dubbed systems of tightly-packed inner planets (STIPs). Although there is no formal definition of a STIP, they typically contain 3 or more Earth-sized planets with orbital periods extending between 1 and 100 days. Reconciling the structural differences between the solar system (devoid of large bodies interior to 88 days) and STIPs is going to be an important step in building a general, widelyapplicable planet formation model.

To date, a large body of work exists that has attempted to reproduce the architectures of STIPs, starting from planetary embryos (cite some examples). However, the runaway and oligarchic growth phases, which precede the assembly of the embryos, are assumed to be ubiquitous. Given that the timescales for accretion and gravitational scattering scale differently with encounter velocity, which itself scales with orbital period, it is not entirely clear that planetary embryos should form in the same way close to the star as they do at much longer, more thoroughly studied orbital periods. In this paper, we use direct N-body simulations to explore the outcome of the planetesimal accretion stage at orbital

periods shorter than 100 days. In particular, we seek to understand what the orbital and mass distributions of the embryos and residual planetesimals look like, and to assess whether the initial conditions used by late-stage simulations of STIP assembly are reasonable.

In section 2 we provide an overview of the theory behind planetesimal accretion and show that assumptions used to derive the well-known modes of growth are only valid at sufficiently long orbital periods. We then motivate the need for N-body simulations to study this problem and describe the code used, along with how our initial conditions were constructed in section 3. In section ??, we present parameter study of planetesimal accretion using a series of simulations of narrow annuli at various orbital periods. We also present a set of simulations starting with a much wider planetesimal disk and demonstrate that a transition between accretion modes occurs at moderately small ($\simeq 50d$) orbital periods. Next, we assess the impact of simplifications made to our collision model on this result in section 7. In section 8, we discuss the implications of this multimodal accretion behavior throughout the disk for planet formation models and conclude.

2. OVERVIEW OF PLANETESIMAL ACCRETION

2.1. Oligarchic and Runaway Growth

We begin our analysis by considering a disk of equal planetesimals with radius r_{pl} , mass m_{pl} and surface density Σ_{pl} . The collision rate in the vicinity of an orbit defined by Keplerian frequency Ω can be written as $n\Gamma v$, where $n=\Sigma_{pl}\Omega/2m_{pl}v$, Γ is the effective collision cross section and v is the typical encounter velocity between planetesimals. Assuming that every collision results in a perfect merger, the growth rate of a planetesimal is given by

$$\frac{dM}{dt} = \frac{\Sigma\Omega}{2m_{pl}}\Gamma.$$
 (1)

In the case where the collision cross section Γ depends only on the physical size of the planetesimals, the growth scales linearly with mass and the mass distribution is expected to evolve in an 'orderly' fashion. However, bodies larger than ~ 100 km in size are expected to exert a significant gravitational force on each other during encounters and the collision cross section depends on both the size of the bodies and their encounter velocities. In this case, $\Gamma = \Gamma_{geo} \left(1 + v_{esc}^2/v^2\right)$, where v_{esc} is the escape velocity from the two bodies at the point of contact.

In the limit that $v_{esc}\gg v$, it can be shown that $M\propto M^{4/3}$, which implies a runaway scenario, in which growth accelerates with mass. This mode of growth was confirmed with N-body simulations by Kokubo & Ida

(1996) and appears necessary to construct protoplanets within the lifetime of a protoplanetary disk. Due to the velocity dependence of the gravitational focusing effect, it isn't clear how ubiquitous this mode of growth is. In particular, encounter velocities at short orbital periods will be rather large (because $v \sim v_k$) and the $v_{esc} \gg v$ condition may not always be satisfied. The effect that a dynamically hot disk has on runway growth will be examined in detail in section ??.

An important feature is missing from the model described above, which limits its applicability at late times. Encounters between planetesimals that do not result in a collision play a crucial role over long timescales. These close encounters act to convert energy from Keplerian shear into random motion. Over time, this gravitational stirring effect will raise the typical encounter velocities between bodies and diminish the effectiveness of gravitational focusing. With a spectrum of masses, these velocity differences become even more pronounced because as system drifts towards a state of quasi-equilibrium where $v \sim m^{1/2}$. For a system of equal mass bodies in which encounters are driven by random motions rather than Keplerian shear (dispersion dominated), the timescale for gravitational stirring is described by the two-body relaxation time (Ida & Makino 1993)

$$t_{relax} = \frac{v^3}{n\pi G^2 m_{nl} ln\Lambda},\tag{2}$$

where $ln\Lambda$ is the Coulomb logarithm. As mentioned above, the system will tend toward a state of energy equipartition for a non-uniform mass distribution. Kokubo & Ida (1998) showed that runaway growth is actually self-limiting. As the runaway bodies grow larger, they become more effective at heating the remaining planetesimals, which diminishes the effectiveness of gravitational focusing and throttles the growth rate. Around the time that the massive runaway bodies make up about 50 percent of the solid surface density (citation), a period of less vigorous 'oligarchic' growth commences, in which the few largest bodies continue to accrete planetesimals at similar rates.

The picture described above relies upon an important factor, which is that the mass distribution evolves slow enough for gravitational stirring to maintain energy equipartition. In other words, the relaxation timescale must remain short relative to the growth timescale. For typical conditions near the terrestrial planet forming region of the solar system, this timescale condition is satisfied. Due to the steep dependence of the relaxation time on encounter velocity, this condition can easily be violated at shorter orbital periods.

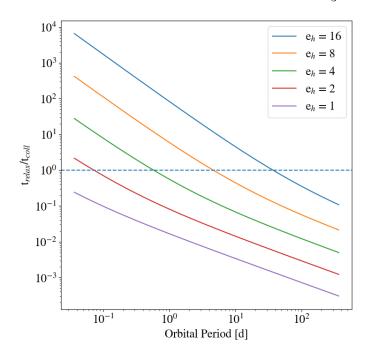


Figure 1. The ratio between the two-body relaxation and collision timescale for a population of equal-mass planetesimals. Only in regions where $t_{relax} \ll t_{coll}$ can the velocity distribution respond to changes in the mass of the bodies such that oligarchic growth can operate. This condition is no longer satisfied for a dynamically hot disk at sufficiently short orbital periods.

In figure 1, we show ratio between the relaxation and collision timescale for a population of equalmass planetesimals as a function of orbital period. Here, the encounter velocity is described by $v = \left(5/8 \left\langle e^2 \right\rangle^{1/2} + \left\langle i^2 \right\rangle^{1/2}\right)^{1/2} v_k$, where $\left\langle e^2 \right\rangle^{1/2}$ and $\left\langle i^2 \right\rangle^{1/2}$ are the eccentricity and inclination dispersions of the planetesimal disk and v_k is the Keplerian velocity. For simplicity, we assume that $\left\langle e^2\right\rangle^{1/2}=2\left\langle i^2\right\rangle 1/2$ (Ida et al. 1993) and that the eccentricity dispersion is constant with orbital period. The eccentricity dispersion is described in units scaled by the Hill factor $(m_{pl}/3M_{star})^{1/3}$ such that $e_h = 1$ corresponds to the boundary between shear and dispersion dominated encounters. The horizontal dashed line indicates where $t_{relax} = t_{coll}$. The timescale criterion for oligarchic growth is only satisfied in regions where the disk is sufficiently dynamically cold and the orbital period is sufficiently long. In section ?? we will explore the behavior and outcome of planetesimal accretion in regions where this criterion is *not* satisfied.

2.2. Planetesimal Size and Extent of Hill Sphere

In the formalism described above, the mass and velocity distribution of the bodies are both a function of time. Due to the interdependence of these quantities, it is not clear whether the timescales for gravitational scattering and growth will remain proportional as the oligarchs develop. In the case of many studies of planetesimal accretion in the solar system (cite examples), the $t_{relax} \ll t_{coll}$ condition must remain true, otherwise runaway growth would have continued until all of the planetesimals were consumed. However, it isn't immediately clear what will happen if the system begins in a state where $t_{coll} \ll t_{relax}$.

An insight into the expected behavior in this regime can be gained by defining the dimensionless parameter α , which is the ratio between the physical size of a body and it's Hill radius

$$\alpha = \frac{r_{pl}}{r_h} = \frac{1}{a} \left(\frac{9M_*}{4\pi\rho_{pl}} \right)^{1/3},$$
 (3)

where a is the semimajor axis of the body and ρ_{pl} is its bulk density. Assuming a fixed bulk density as bodies collide and grow, and that no large-scale migration occurs, the scaling of both r_{pl} and r_h with $m_{pl}^{1/3}$ means that α will be constant with time. For a composition of ice and rock, α is small for any populated region of the solar system ($\alpha \sim 10^{-2}$ for Earth and $\alpha \sim 10^{-4}$ in the Kuiper belt). As one moves close to the star α becomes larger than 1, which implies that the physical extent of a body exceeds its Hill sphere. (also mention that hill sphere size independent of velocity for small eccentricity)

The size of α controls the relative importance of gravitational scattering and collisions in driving the evolution of the planetesimal disk. In the case that α is small, most close encounters will result in a gravitational interaction only, moving the system toward a state of relaxation. If, however, the Hill sphere is largely filled by the body itself, these same encounters will instead drive evolution of the masses. Because α is independent of time, the innermost region of the planetesimal disk, where collisions dominate over scattering events, should remain that way.

We also introduce a second dimensionless quantity, which relates the physical size of the bodies to the velocity state of the system

$$\beta = \frac{r_{pl}}{r_q}. (4)$$

where $r_g = Gm_{pl}/v^2$ is the gravitational radius of a body. Encounters between bodies inside of a distance of r_g result in significant deflections of their trajectories. It should be noted that the gravitational focusing enhancement factor v^2/v_{esc}^2 is equal to 1 for $\beta=1$. In the case where r_g is smaller than the size of a planetesi-

mal, the gravitational focusing enhancement factor will be between 0 and 1.

Need a transition to next section here.

3. NUMERICAL METHODS

We use the tree-based N-body code CHANGA 1 to model the gravitational and collisional evolution of planetesimals at short orbital periods (where α is large). CHANGA is written using the CHARM++ parallel programming language and has been shown to perform well on up to half a million processors (Menon et al. 2015) and can follow the evolution of gravitationally interacting swarms of up to billions of particles. Using a modified Barnes-Hut tree with hexadecapole expansions of the moments to approximate forces, CHANGA integrates the equations of motion using a kick-drift-kick leapfrog scheme. For all of the simulations presented in this paper, we use a node opening criteria of $\theta_{BH} = 0.7$. Additional information about the code is available in (Jetley et al. 2008).

Using the neighbor-finding algorithm in Changa, originally designed for SPH calculations, we have recently implemented a solid body collision module in the code. This work is largely based on the solid-body collision implementation in PKDGRAV, which is described in Richardson (1994) and Richardson et al. (2000). To summarize, imminent collisions are detected during the 'drift' phase by extrapolating positions of bodies forward in time, using the velocity calculated at the opening 'kick'. For each body, any neighboring particles which fall within a search ball of radius fillinlater are tested for an imminent collision. In the case that a collision is detected, the particles are merged into a single larger body, which is given the center of mass position and velocity of the two children. Resolving a collision can produce another imminent collision, so collisions are handled one-by-one and another full collision check is run after the previous event is resolved. For a more detailed description of the collision module in Changa, see (Wallace & Quinn 2019). (mention grav stepping here as well, since its used for all simulations)

4. NARROW ANNULUS SIMULATIONS

We begin by presenting a parameter study of planetesimal accretion, motivated by two questions raised in section 2. 1. Does runaway growth still operate when the condition that $v \ll v_{esc}$ is not satisfied? 2. How does planetesimal accretion proceed when the planetes-

¹ A public version of Changa can be downloaded from http://www-hpcc.astro.washington.edu/tools/Changa.html

imals themselves occupy a significant fraction of their Hill spheres?

To answer these questions, we run a series of simulations in which a narrow annulus of planetesimals orbits a star. The values of α and β are varied individually. 4000 planetesimals with individual masses of 5×10^{23} g are placed with semimajor axes randomly drawn between 0.95 and 1.05 AU about a 1 M_{\odot} star. The argument of perihelion ω , longitude of ascending node Ω , and mean anomaly M for each body is drawn from a uniform distribution $\in [0, 2\pi)$. The inclination dispersion $\langle i^2 \rangle^{1/2}$ is chosen to be half the eccentricity dispersion $\langle e^2 \rangle^{1/2}$ (Ida et al. 1993).

In the 'nominal' case, we give the bodies a bulk density of 3 g cm⁻³, and $\langle e^2 \rangle^{1/2} = 4e_h$, where $e_h = ea/r_h$ (define this in the previous section instead) which corresponds to $\alpha = 3.6 \times 10^{-2}$ and $\beta = 3.4 \times 10^{-3}$. These parameters are chosen to match the initial conditions of Kokubo & Ida (1998), which gave rise to oligarchic growth. To vary the value of α , we alter the bulk density of the particles. In the high- α case, the bulk density is reduced by a factor of ~ 7100 , which produces $\alpha = 1$. To vary β , the eccentricity dispersion is increased. For the high- β case, $\langle e^2 \rangle^{1/2}$ is increased to $1500e_h$, which corresponds to $\beta = 15,000$.

In all cases, the simulations are evolved with a base timestep of 1.7 days, which corresponds to 3\% of an orbital dynamical time $\sqrt{a^3/GM_*}$. Due to the vastly differing growth timescales in each case, a simulation is stopped when the growth of the most massive body flattens out. In figure 2, we show the a-e distribution of bodies in the initial (blue) and final (orange) snapshots from each of the 4 simulations. The size of the points indicates the relative masses of the bodies. Only in the case of small α does a residual population of dynamically hot planetesimals develop. The lack of high eccentricity planetesimals in the large α case suggests that most encounters instead result in accretion. In the case of large β , the protoplanets and remaining planetesimals end up in a dynamically cool state, compared to the initial conditions. (Are the inelastic collisions playing a significant role here?)

In figure 3, we show the mass distribution of bodies from the final snapshot in each of the four cases. In addition to leaving fewer residual planetesimals, the large α simulations produce significantly larger embryos. Despite the vastly different encounter velocities of each population of bodies, the initial size of β appears to have no significant effect on the final distribution of masses.

To investigate whether any of these planetesimal disks underwent runaway growth, we examine the time evo-

Table 1. Summary of Full Disk Simulations Run

Name	A	α
fdHi	100	1.5
${\it fdHiShallow}$	100	0.5
fdHiSteep	100	2.5
fdLo	1	1.5

lution of the maximum and mean masses in each case. The ratio $m_{max}/\langle m \rangle$ is plotted in figure 4. On this plot, a positive slope indicates that the growth rate is accelerating with mass, which is evident in all four cases. Even with a large value of β , which means that the effective collision cross section is very near the geometric value, runaway growth still appears to operate. This seems to imply that, as bodies collide and grow, the relative increase in their gravitational focusing factors, rather than its absolute size, is what drives the system towards runaway growth. Although larger encounter velocities will lengthen the growth timescales, this mode of growth appears to be inevitable, so long as gravity is the dominant force in the system.

Additionally, these results suggest that the value of α , which is a function of only the initial conditions, controls the qualitative outcome of accretion. Across most of a planet-forming disk, α is small, and frequent gravitational encounters between the growing bodies will allow oligarchic growth to operate. At shorter orbital periods, however, the Hill sphere of a body is no longer mostly empty space, and it appears as if collisions play a more significant role. In this regime, we observe that runaway growth still commences, but nearly all of the planetesimals are swept up by the forming protoplanets, rather than being scattered onto higher eccentricity orbits, where they would otherwise remain as a remnant of the early stages of planet formation (Kokubo & Ida 1998, 2000).

5. FULL DISK SIMULATION

Motivated by the apparent dependence of accretion modes on α , we next investigate whether this highly efficient, non-oligarchic growth mode should be expected to operate in a typical planet-forming disk. Given the dearth of short period terrestrial planets observed around M stars (citation), we model a series of wide planetesimal disks, which span from 1 to 100 days in orbital period orbiting a late-type M star of mass 0.08 M_{\odot} . For a population of planetesimals with a bulk density of 3 g cm⁻³, this orbital period range corresponds to $\alpha \in (0.7, 0.05)$. By simultaneously modeling a broad range of orbital periods, we can determine the critical

value of α that divides these two modes of accretion, and also explore how the oligarchic/non-oligarchic accretion boundary affects the resulting distribution of protoplanets.

Four wide disk simulations are run in total (see table 1). In each case, the solid surface density follows a power law profile

$$\Sigma(r) = \left(\frac{M_*}{M_{\odot}}\right) A \Sigma_{mmsn} \left(\frac{r}{1AU}\right)^{-\alpha}, \qquad (5)$$

where M_* is the mass of the central star, $\Sigma_{MMSN}=10~{\rm g}~{\rm cm}^{-2}$ is surface density of the minimum-mass solar nebula (Hayashi 1981) at 1 AU, and A is an enhancement factor. In the first case (fdHi), we model a disk that follows a MMSN power law slope, with the overall normalization enhanced by a factor of 100. This choice of parameters for the solid surface density profile appears necessary in order to reproduce many observed short period terrestrial worlds in-situ (Hansen & Murray 2012). Additionally, we vary the power law index (fdHiShallow, fdHiSteep) and overall normalization (fdLo) of the solids profile.

In all cases, the eccentricities and inclinations of the bodies are randomly drawn from a Rayleigh distribution, with $\langle e^2 \rangle^{1/2} = 2 \langle i^2 \rangle^{1/2} = e_{eq}$. The value of e_{eq} is chosen such that the timescales for viscous stirring and aerodynamic gas drag on the planetesimals are in equilibrium. The viscous stirring timescale is given by Ida & Makino (1993) as

$$\tau_{vs} = \frac{\langle e^2 \rangle}{d \langle e^2 \rangle / dt} \approx \frac{1}{40} \left(\frac{\Omega^2 a^3}{2Gm_{pl}} \right)^2 \frac{4m_{pl} \langle e^2 \rangle^2}{\Sigma a^2 \Omega}, \quad (6)$$

where Ω , a and e are the orbital frequencies, semimajor axes and eccentricities of the individual planetesimals. In the Stokes regime, the gas drag timescale is given by Adachi et al. (1976) as

$$t_s = \frac{2m_{pl}}{C_D \pi r_{pl}^2 \rho_q v_q},\tag{7}$$

where C_D is a drag coefficient of order unity, ρ_g is the local gas volume density and v_g is the headwind velocity of the gas experienced by the planetesimal. The local gas volume density is given by

$$\rho_g = \frac{\Sigma_g}{\sqrt{2\pi}h_g \exp\left[-z^2/\left(2h_g^2\right)\right]},\tag{8}$$

where Σ_g is the gas surface density (taken to be 240x the solid surface density), $h_g = c_s/\Omega$ is the local gas scale height and z is the height above the disk midplane. The sound speed profile is given by $c_s = \sqrt{k_B T(r)/(\mu m_H)}$, where k_B is Boltzmann's constant, $T(r) = T_0 r^{-Q}$, $\mu = 2.34$ and m_h is the mass of a hydrogen atom. For a protoplanetary disk around a typical M star, $T_0 = 148$ K and Q = 0.58 (Andrews & Williams 2005).

Finally, the headwind velocity of the gas, due to the fact that the gas disk is pressure supported, is given by

$$v_g = v_k \left[1 - \sqrt{Qc_s^2/v_k^2} \right], \tag{9}$$

where v_k is the local Keplerian velocity.

More stuff about initial conditions, timestepping issues, gas drag

6. ASSEMBLY HISTORY OF EMBRYOS

7. SIMPLIFYING ASSUMPTIONS

7.1. Collision Cross Section

7.2. Collision Model

How to reconcile our concerns with the results of Wallace et al. (2017)?

8. SUMMARY AND DISCUSSION

As was pointed out in Clement et al. (2020), late stage initial conditions with a uniform distribution of embryos is not accurate. Evolution happens in the inner part of the disk first, so bodies will be more massive there.

Summary and discussion text goes here

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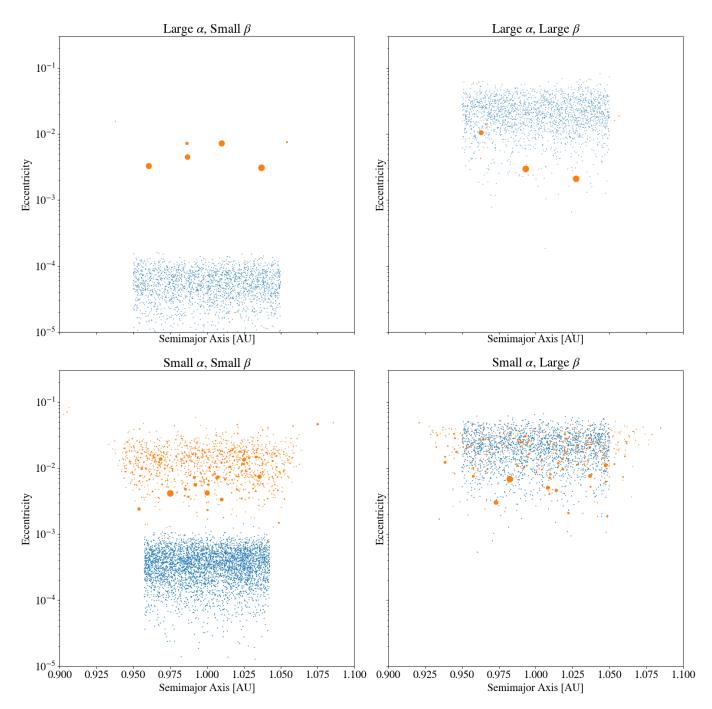


Figure 2. The initial (blue) and final (orange) states of the simulations described in section 4. Relative masses of the bodies are indicated by point size. In the case of large α , almost no residual planetesimal population remains. Regardless of the choice of β , the protoplanets that form attain similar eccentricities.

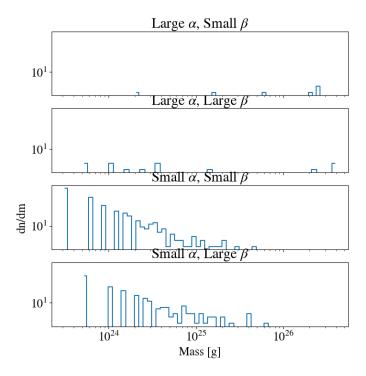


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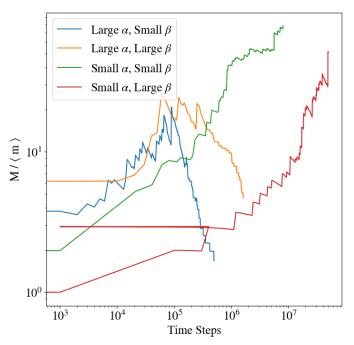


Figure 4. Caption goes here.

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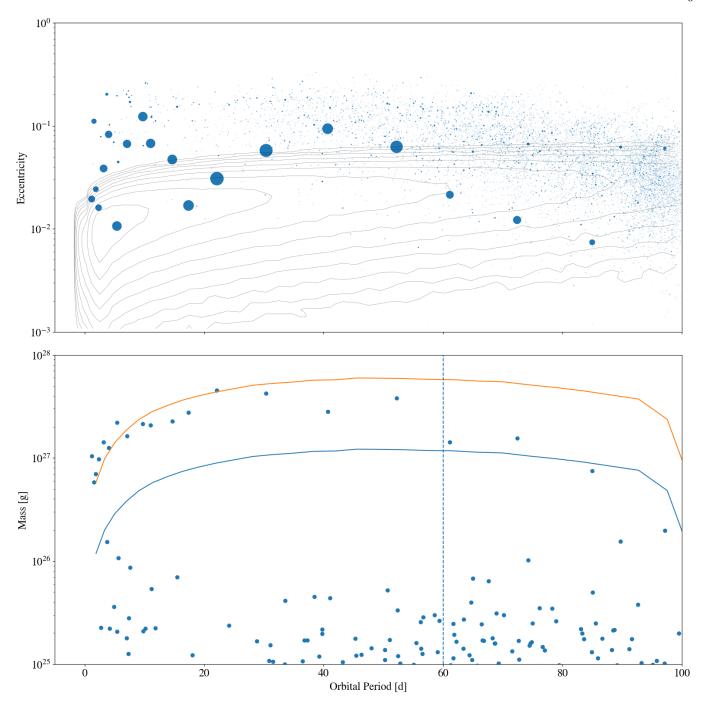


Figure 5. Caption goes here.

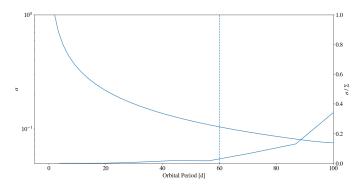


Figure 6. Caption goes here.