

Topic: Linear combinations and span

Question: How many linearly independent vectors are needed to span \mathbb{R}^4 ?

Answer choices:

A 1

B 2

C 3

D 4



Solution: D

Any n n -dimensional linearly independent vectors will span \mathbb{R}^n . So in order to span \mathbb{R}^4 , we'll need 4 linearly independent vectors.



Topic: Linear combinations and span**Question:** Will the vectors span \mathbb{R}^2 ?

$$\vec{u} = (3,1)$$

$$\vec{v} = (6,2)$$

Answer choices:

- A Yes, because the vectors aren't parallel
- B Yes, because the vectors are parallel
- C No, because the vectors aren't parallel
- D No, because the vectors are parallel



Solution: D

The vectors $\vec{u} = (3,1)$ and $\vec{v} = (6,2)$ are parallel. We can tell this by sketching them, or by looking at the slope of each vector, where the slope of \vec{u} is $1/3$, and the slope of \vec{v} is $2/6 = 1/3$.

Parallel vectors can never span their space. So $\vec{u} = (3,1)$ and $\vec{v} = (6,2)$ can't span \mathbb{R}^2 because of the fact that they're parallel.



Topic: Linear combinations and span

Question: Can the standard basis vectors $\mathbf{i} = (1,0,0)$, $\mathbf{j} = (0,1,0)$ and $\mathbf{k} = (0,0,1)$ span \mathbb{R}^3 ?

Answer choices:

- A Yes, because three linearly independent vectors in \mathbb{R}^3 will span \mathbb{R}^3
- B Yes, because three linearly dependent vectors in \mathbb{R}^3 will span \mathbb{R}^3
- C No, because three linearly independent vectors in \mathbb{R}^3 won't span \mathbb{R}^3
- D No, because three linearly dependent vectors in \mathbb{R}^3 won't span \mathbb{R}^3



Solution: A

Any 3 three-dimensional linearly independent vectors will span \mathbb{R}^3 . The three-dimensional basis vectors \hat{i} , \hat{j} , and \hat{k} are linearly independent, which is why they span \mathbb{R}^3 .

