

Closed Loop Control

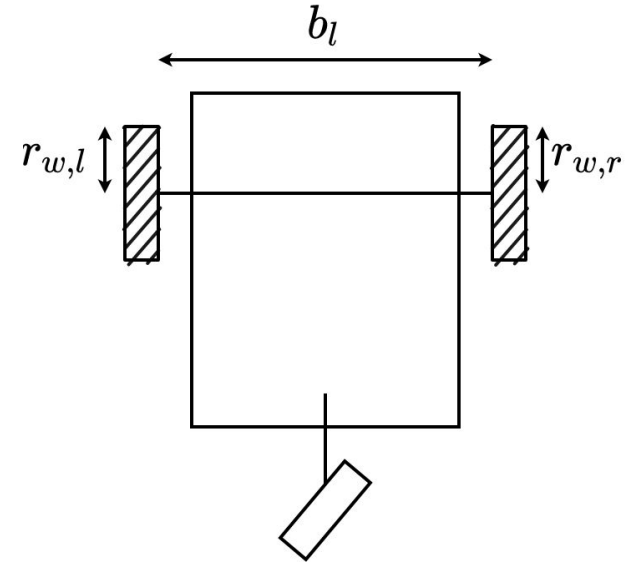
Exercise



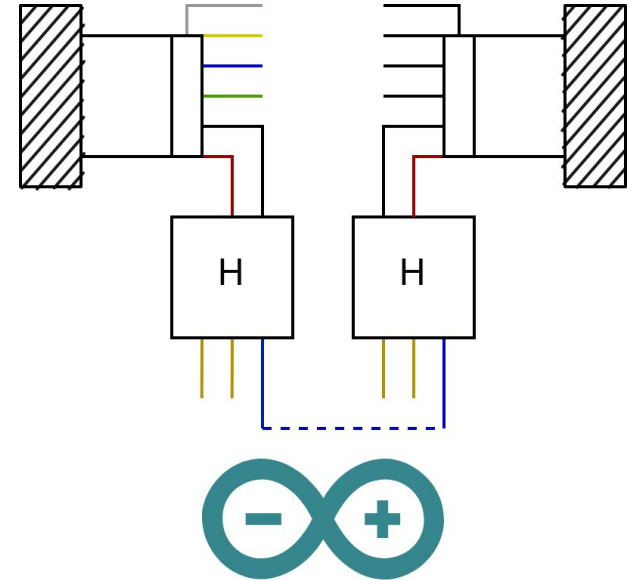
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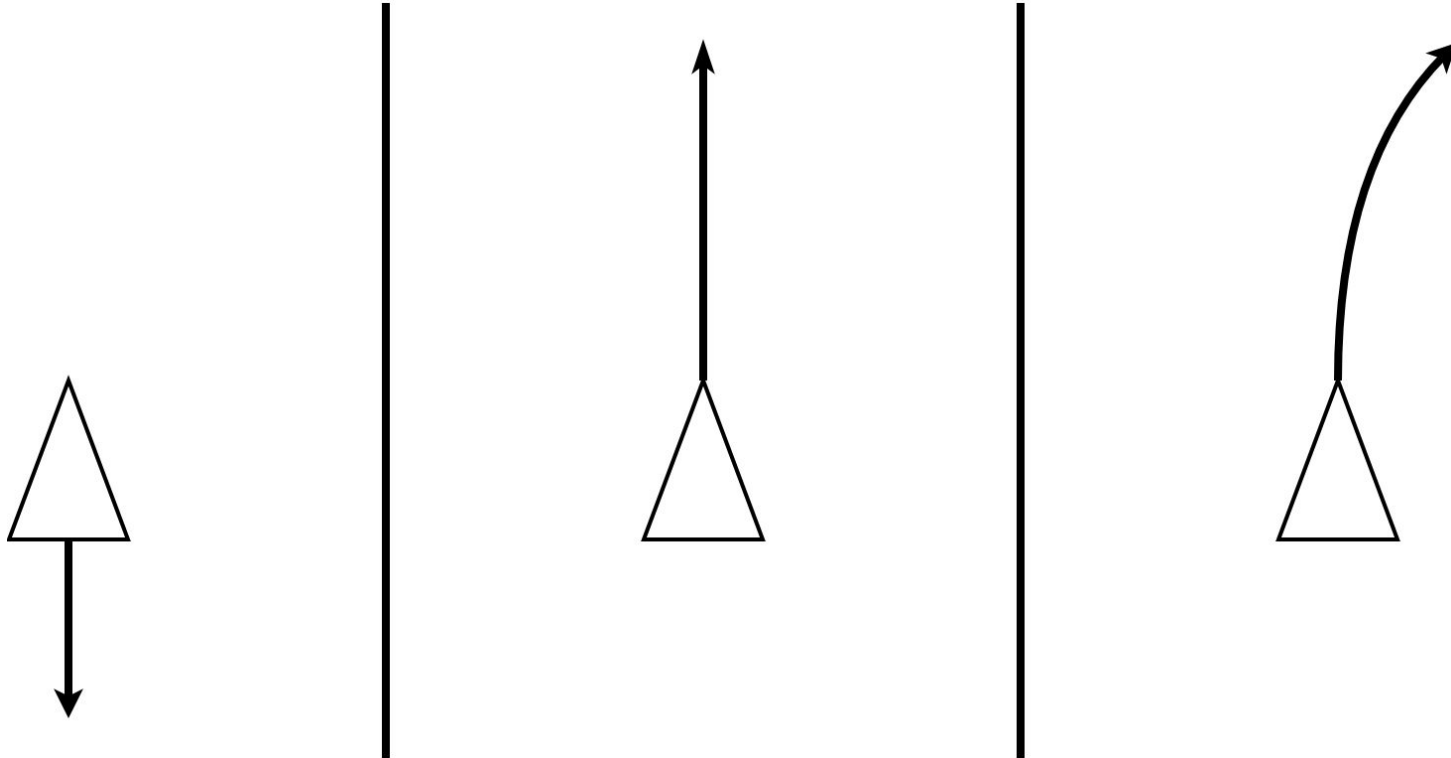
- ❖ Imagine to realize a Differential Drive M.R.
- ❖ We need:
 - Platform
 - 2 Motorized wheels [Brushed DC + H Bridge]
 - 1 Caster



- ❖ Mount everything and test the platform
- ❖ H Bridge configuration:
 - Dual Dir + PWM [3 control pins]
- ❖ Apply same PWM signal to both motors



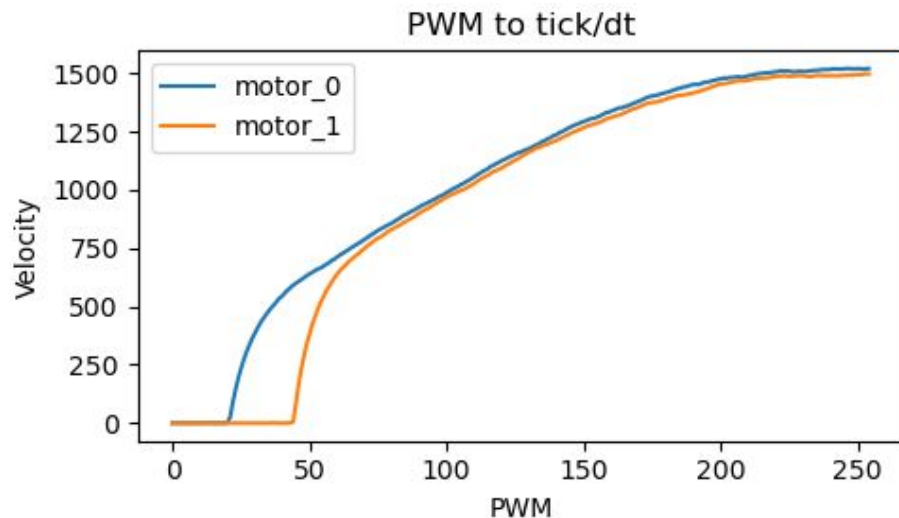
❖ What happens ?



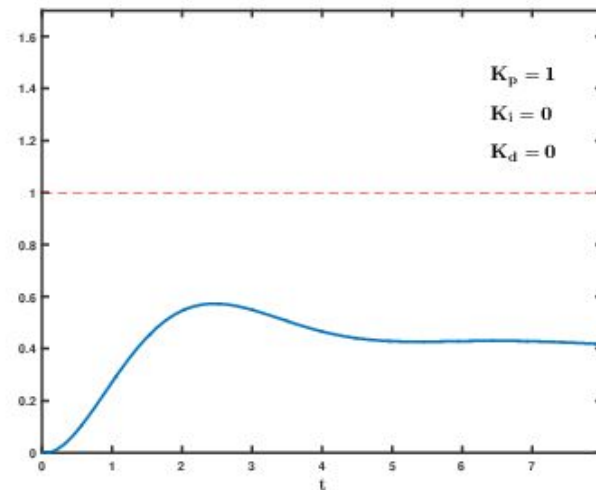
- ❖ Robot is unable to go straight
- ❖ The motors are similar but not identical
- ❖ How to correct this behavior ?
- ❖ Two solutions:
 - Calibrate PWM channels
 - Use Closed Loop Feedback correction



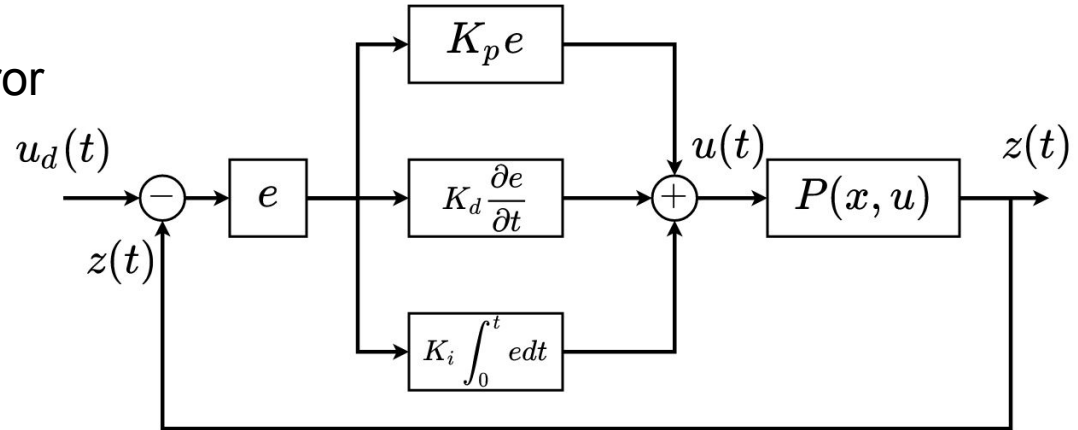
- ❖ Calibrating PWM channels is painful...
- ❖ Velocity differences are not constant
- ❖ Requires interpolation and parameter estimation
- ❖ Can be done... but why ?



- ❖ Is the shaft's angular velocity measurable ?
 - Yes! encoders
- ❖ Compares measurements with input commands
- ❖ Feedback design guarantees convergence
- ❖ Many Feedback controllers exists
 - We use *Proportional Integral Derivative* [PID]



- ❖ Compute error between desired and measured speed
- ❖ **P** acts like a spring
- ❖ **I** removes the steady-state error
- ❖ **D** acts like a damper



❖ We need to work with discrete time intervals

➤ Proportional

■ $u_P(t) = K_p e(t)$

➤ Integral

■ $u_I(t) = \sum_{t_i=0}^t K_i e(t_i) \Delta t$

➤ Derivative

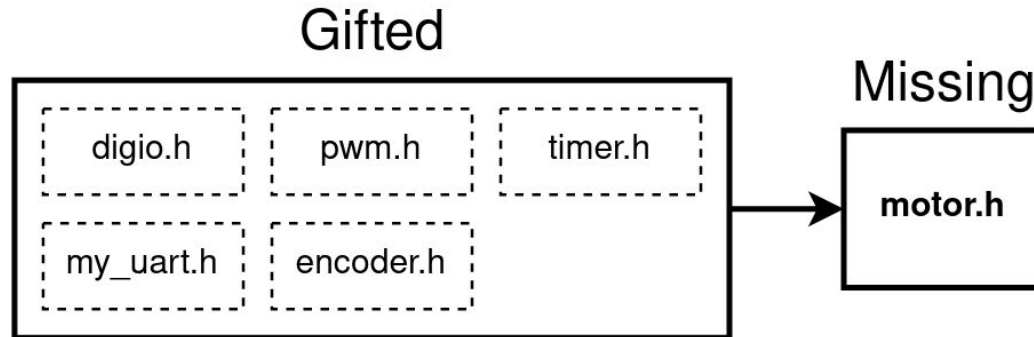
■ $u_D(t) = K_d \left(\frac{e(t) - e(t-1)}{\Delta t} \right)$

❖ Useful stability tips:

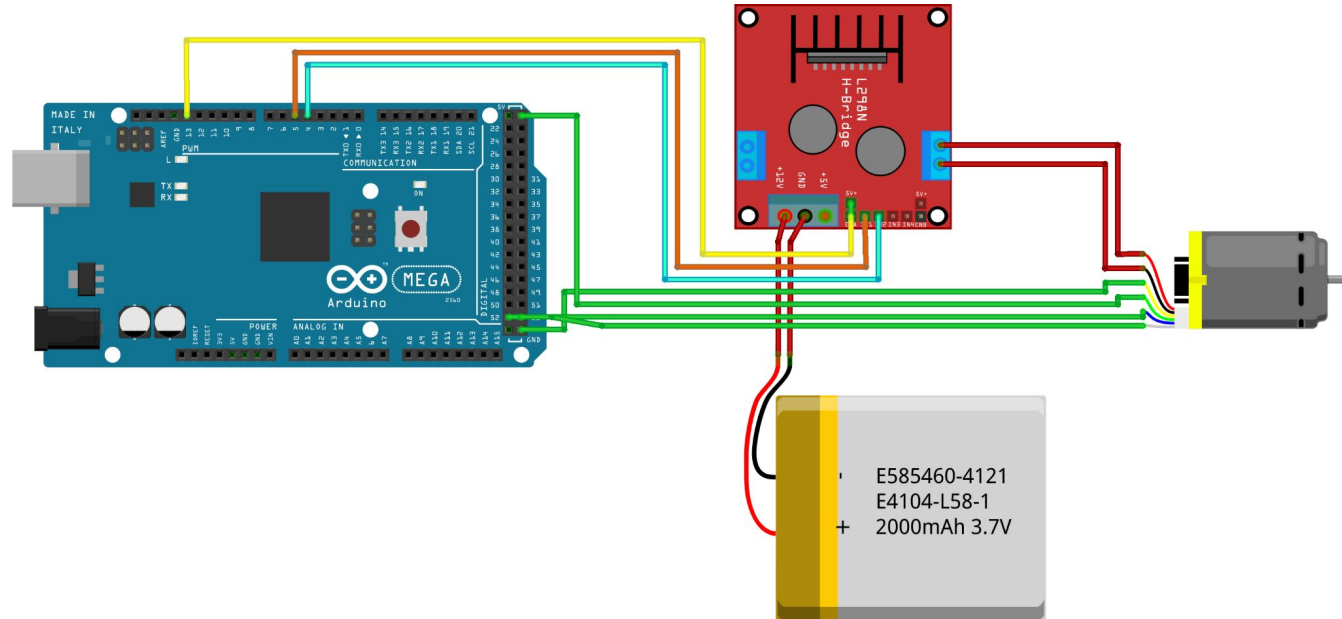
➤ Bound the error

➤ Bound the components

- ❖ We designed an exercise for you
- ❖ Implement a motor class
 - Includes a PID controller
- ❖ We gift you all the other modules :)



- ❖ Design problem
 - Comms with PC
 - Motor Control (Direction and Speed)
 - Encoder



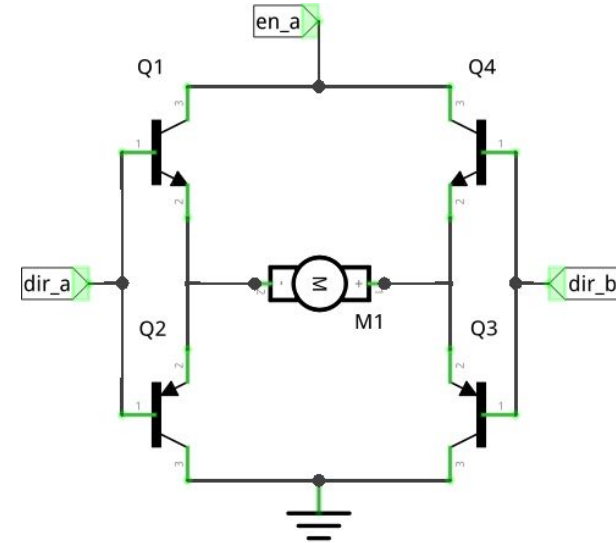
❖ UART library

- Initializes Serial communication
 - 19200 bit/sec
 - 8-bit data
- Allows single/multiple byte transmissions
 - {put/get}Char()
 - {put/get}String(buf)

❖ Timer library

- Allows precise loop timings
 - Set to 10ms/loop

- ❖ Brushed DC Motors requires H-Bridge circuit
 - 2 signals for direction
 - 1 signal for speed (Pulse Width Modulation)
- ❖ Digital I/O library
 - Allows binary signal generation
 - dir_a and dir_b
- ❖ PWM library
 - Allows 2^8 PWM configurations
 - en_a



❖ Brushed DC may include angular velocity sensor

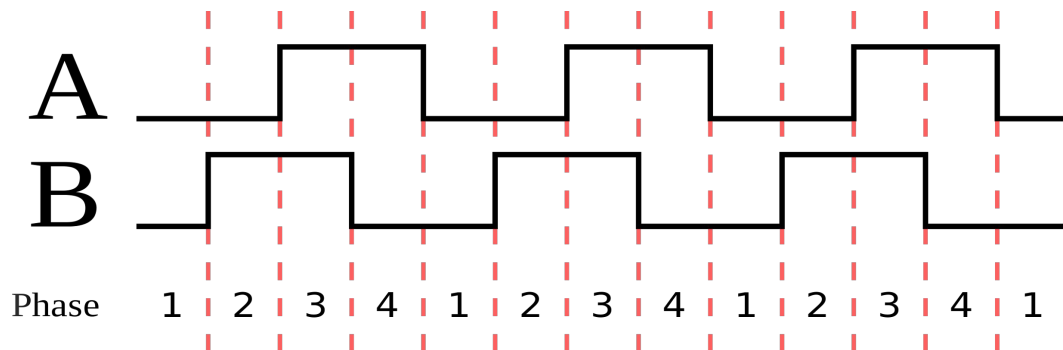
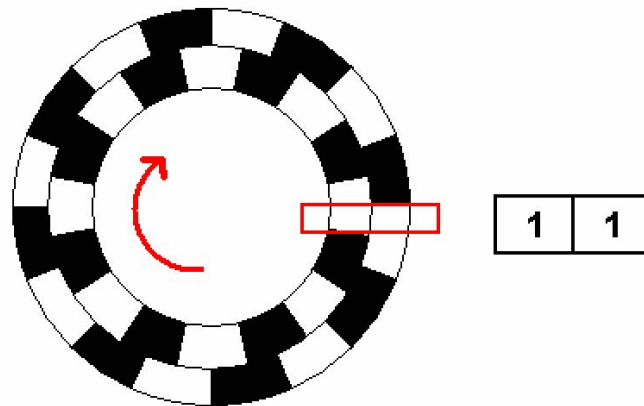
➤ Incremental quadrature encoder

❖ Encoder library

➤ Allows 1 encoder port (pin 52, 53)

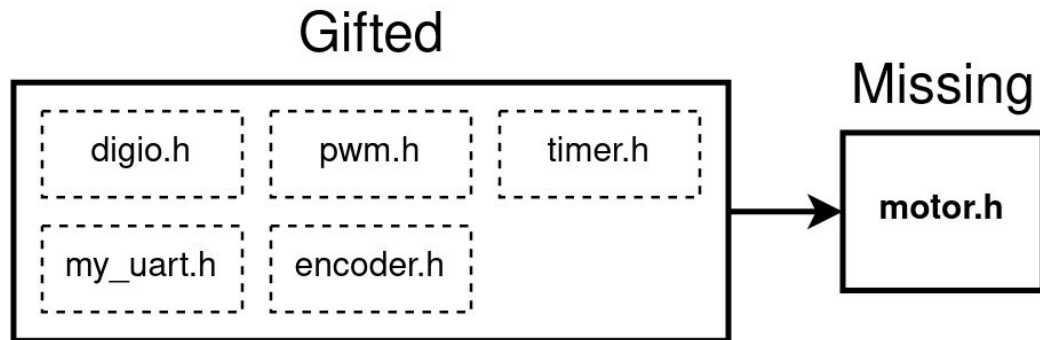
➤ Asynchronous update

➤ Refer to previous lectures for details



- ❖ Last missing section
- ❖ Abstract the motor interface
 - H-bridge for control
 - Encoder for closed loop feedback

- ❖ Design a Motor class that:
 - Allows for multiple controls:
 - PWM Open Loop
 - PID
 - **Computes** PID corrections



- ❖ For simplicity:
 - DigIO only handles Register E
 - Bit 4 -> pin 2
 - Bit 5 -> pin 3
 - More on the code...
 - PWM only handles pin 13
 - Encoder mapped to pins 52 and 53

- ❖ Motor constructor takes:
 - Dir_a, dir_b regE bits
 - PID parameters (Kp, Ki, Kd)