Limbertwig LateralAlgebra.app

Parker Emmerson

June 2023

1 Limbertwig Kernel

2 Lateral Algebra

Let F be an abstract field whose elements will serve as symbols representing variables in a lateral algebra. The lateral algebra \mathcal{L} is a parametric algebraic system which is characterized by operations \oplus and \otimes .

The operations \oplus and \otimes combine two elements in the following way:

$$(x \oplus y) \otimes z = x \otimes z \oplus y \otimes z$$

where $x,y,z\in F$ and operators satisfy the following "list associativity" property:

$$(x \oplus y) \otimes (z \oplus w) = (x \otimes z) \oplus (y \otimes z) \oplus (x \otimes w) \oplus (y \otimes w).$$

$$(x \oplus y) \otimes (z \oplus w) = \left(\frac{r(\alpha - \Delta)}{z\Theta}\right) \oplus \frac{r(\alpha + \Delta)}{z\Theta}\right) \otimes \left(\frac{1}{1 - \frac{v^2}{c^2}} \oplus z\Theta\right)$$

$$=\frac{1}{1-\frac{v^2}{c^2}}\otimes\frac{r(\alpha-\Delta))}{z\Theta)}\oplus\frac{1}{1-\frac{v^2}{c^2}}\otimes\frac{r(\alpha+\Delta))}{z\Theta)}\oplus z\Theta\otimes\frac{r(\alpha-\Delta))}{z\Theta)}\oplus z\Theta\otimes\frac{r(\alpha+\Delta))}{z\Theta)}$$

$$\begin{split} &=\frac{r(\alpha-\Delta))}{z\Theta(1-\frac{v^2}{c^2})}\,\oplus\,\frac{r(\alpha+\Delta))}{z\Theta(1-\frac{v^2}{c^2})}\,\oplus\,\frac{z\Theta r(\alpha-\Delta))}{z\Theta}\,\oplus\,\frac{z\Theta r(\alpha+\Delta)}{z\Theta}\\ &=\frac{r(\alpha-\Delta))}{z\Theta(1-\frac{v^2}{c^2})}\,\oplus\,\frac{r(\alpha+\Delta))}{z\Theta(1-\frac{v^2}{c^2})}\,\oplus\,r(\alpha-\Delta))\,\oplus\,r(\alpha+\Delta))\\ &=\frac{r^2(-\Delta^2+\alpha^2)}{z\Theta(1-\frac{v^2}{c^2})} \end{split}$$

3 Package

$$\begin{array}{l} \Lambda \rightarrow N \rangle \left\{ \sigma, \mathbf{g_a}, \mathbf{b}, \mathbf{c}, \mathbf{d}, \mathbf{e}, \dots \sim \right\} \left\langle \rightleftharpoons \Lambda \rightarrow \right. \\ \exists \ L \rightarrow N, value, value \dots \left\langle \exists L \rightarrow \left\{ \left\langle \sim \rightarrow \heartsuit \rightarrow \epsilon \right\rangle \left\langle \rightleftharpoons \heartsuit \right\rangle \right\rangle \rightarrow \\ \left\{ \uparrow \Rightarrow \alpha_i \right\} \left\langle \rightleftharpoons \forall \alpha_i \right\rangle \bigcirc \rightarrow \left\{ \right\} \left\langle \rightleftharpoons \uparrow \rightarrow \left\{ \mathbf{x} \Rightarrow \mathbf{g_a} \right\} \left\langle \rightleftharpoons \mathbf{x} \rightarrow \left\{ \mathbf{x} \Rightarrow \mathbf{b} \right\} \left\langle \rightleftharpoons \mathbf{x} \rightarrow \left\{ \mathbf{x} \Rightarrow \mathbf{c} \right\} \left\langle \rightleftharpoons \mathbf{x} \rightarrow \left\{ \mathbf{x} \Rightarrow \mathbf{d} \right\} \left\langle \rightleftharpoons \mathbf{x} - \right\rangle \right. \\ \left\{ \mathbf{x} \Rightarrow \mathbf{e} \right\} \left\langle \rightleftharpoons \mathbf{x} \rightarrow \left\{ \mathbf{x} \Rightarrow \mathbf{c} \right\} \left\langle \rightleftharpoons \mathbf{x} \rightarrow \left\{ \mathbf{x} \Rightarrow \mathbf{d} \right\} \left\langle \rightleftharpoons \mathbf{x} - \right\rangle \right. \\ \left\{ \mathbf{x} \Rightarrow \mathbf{e} \right\} \left\langle \rightleftharpoons \mathbf{x} \rightarrow \left\{ \mathbf{c} \rightarrow \nabla \rightarrow \epsilon \right\rangle \left\langle \rightleftharpoons \mathbf{c} \rightarrow \right\rangle \rightarrow \\ \exists \ n \in N \ s.t. \ \mathcal{L}_f \left(\uparrow r \alpha s \Delta \eta \right) \wedge \overline{\mu} \\ \left\{ \overline{g} (ab c d e \dots \ \forall \quad) \neq \Omega \right. \\ \Rightarrow \mathcal{L}_f \left(\uparrow r \alpha s \Delta \eta \right) \wedge \overline{\mu} \left\{ \overline{g} (ab c d e \dots \ \forall \quad) \neq \Omega \right. \\ \Leftrightarrow \mathcal{O} \left\{ \begin{array}{c} \mu \in \infty \Rightarrow (\Omega \ \forall \) \otimes (\Delta \oplus H_{im}^\circ) \\ \Rightarrow \ \forall \vdots \ \heartsuit \Rightarrow \overline{\mu}, \ \overline{g} (ab c d e \dots \ \forall \quad) \\ \Leftarrow \Lambda \cdot \forall \otimes (\Delta \oplus H_{im}^\circ) \Rightarrow \otimes \stackrel{\sim}{\oplus} \heartsuit \right\} \end{array}$$

4 Rewrite