

# ECE250: Signals & Systems

## Monsoon 2023

### Mid-Semester Examination

Date: 1/10/2023

Duration: 1.30 Hours

Total Points: 24 Points

### Instructions

- Please do not plagiarize. Any act of plagiarism will be dealt with strictly as per the institute's policy.
- Please provide proper mathematical justifications with your answers. No marks will be awarded without a valid justification.

[CO2] Q1: Let  $h(t)$  be the rectangular pulse shown in Figure-1(a), and let  $x(t)$  be the impulse train depicted in Figure-1(b). That is,

$$x(t) = \sum_{k=-\infty}^{+\infty} \delta(t - kT)$$

Compute and Sketch for  $y(t) = x(t) * h(t)$ , for the given values T: (a)  $T=2$

(b)  $T=4$

Also find Time period of  $y(t)$  in each cases.

[2×(3+1+1) Points]

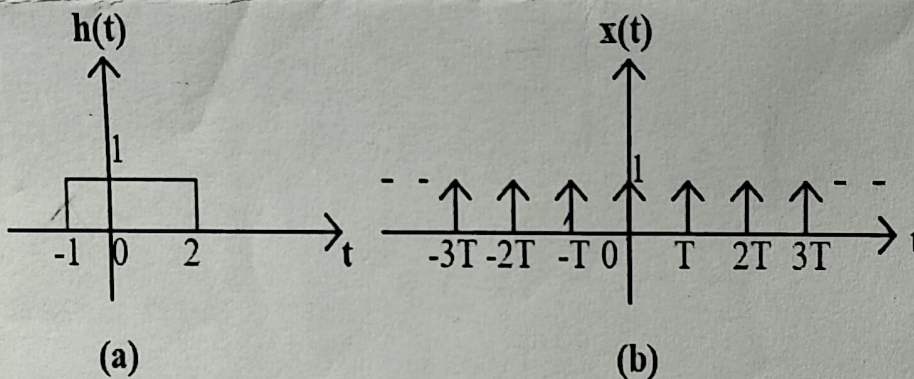


Figure 1

[CO2] Q2: Let  $x[n] = 2^n u[-n-3]$  and  $h[n] = \left(\frac{1}{5}\right)^n u[n+3]$  then compute  $y[n] = x[n] * h[n]$ .

[5 Points]

[CO2] Q3: Determine whether each of the following statements concerning LTI systems is true or false.

Justify your answers with proper explanation.

[5×1 Points]

- (a) If  $h(t)$  is the impulse response of an LTI system and  $h(t)$  is periodic and nonzero, the system is unstable.
- (b) If  $|h[n]| \leq K$  for each  $n$ , where  $K$  is a given number, then the LTI system with  $h[n]$  as its impulse response is stable.



- (c) If a discrete-time LTI system has an impulse response  $h[n]$  of finite duration, the system is stable.
- (d) If an LTI system is causal, it is stable.
- (e) The cascade of a non-causal LTI system with a causal one is necessarily non-causal.

**Q4:** Consider a vector space of all continuous time finite energy signals. This vector space is defined over the Field  $\mathbb{C}$  (the set of complex numbers). Let us define a map  $\langle, \rangle$  as:

$$\langle f(t), g(t) \rangle = \int_{-\infty}^{+\infty} f(t) \cdot \overline{g(t)} \cdot dt$$

Where  $(\overline{\phantom{x}})$  represent conjugate of the signal.

- (a) Write the properties of the inner product. **[2 Points]**
- (b) Prove that the above defined map satisfies all the properties of a valid inner product. **[2 Points]**