



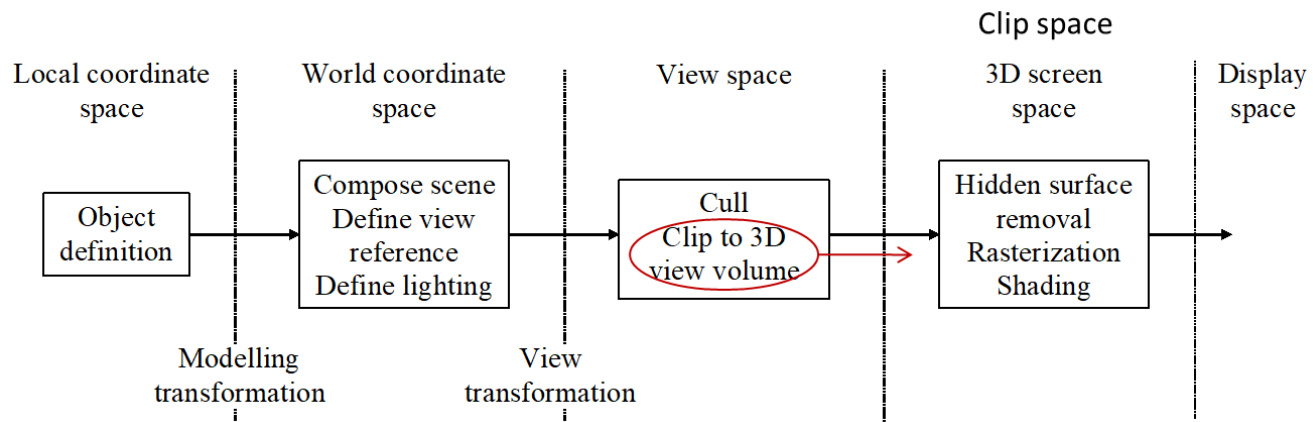
The
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COM3503/4503/6503: 3D Computer Graphics

Lecture 6: The graphics pipeline

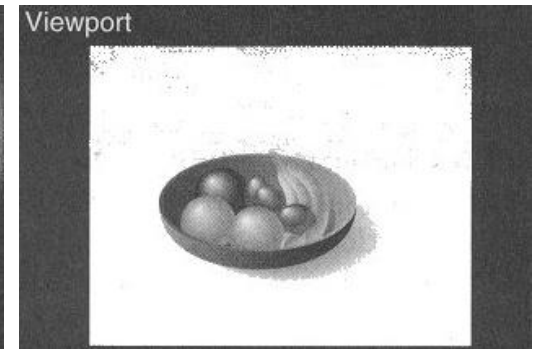
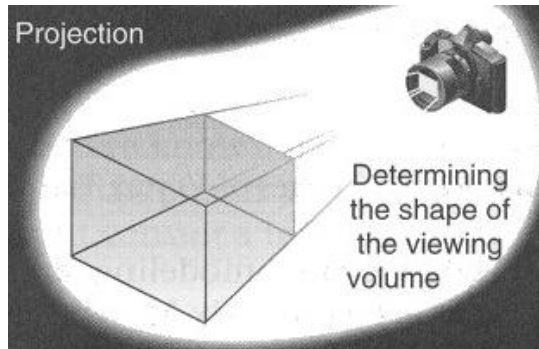
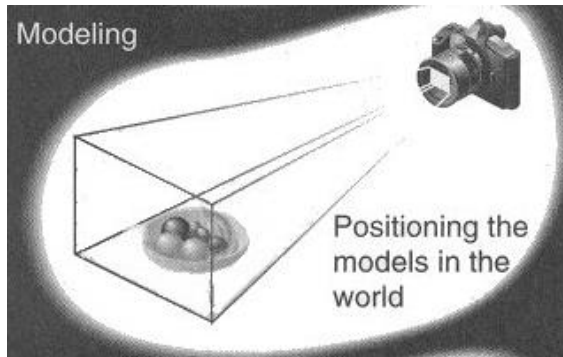
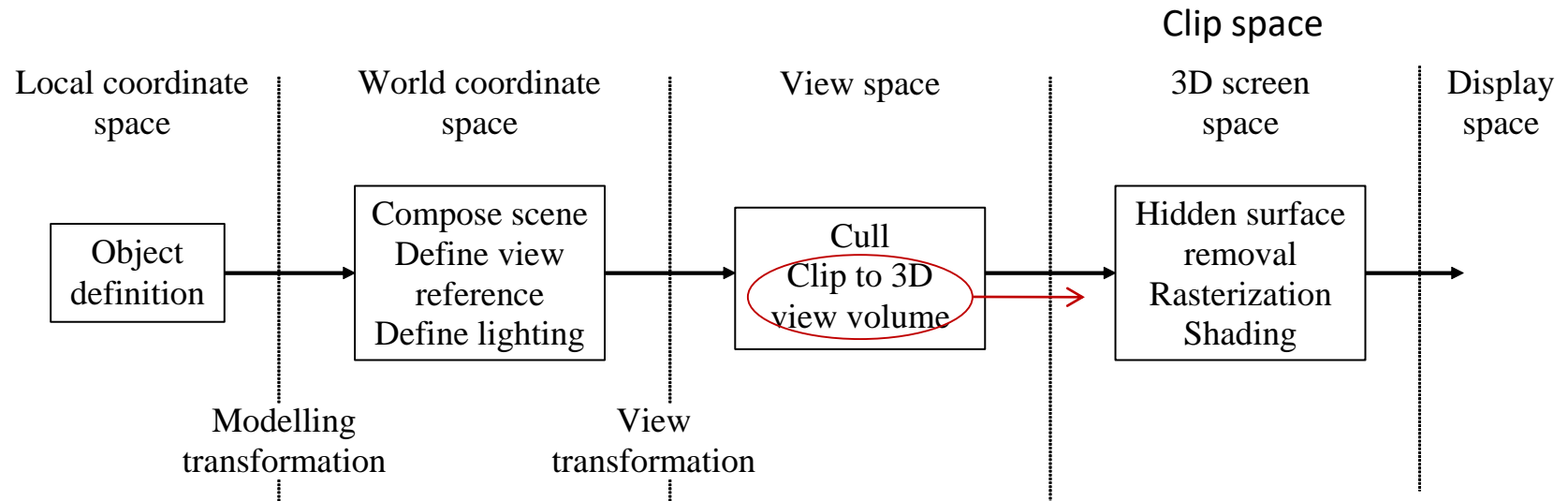
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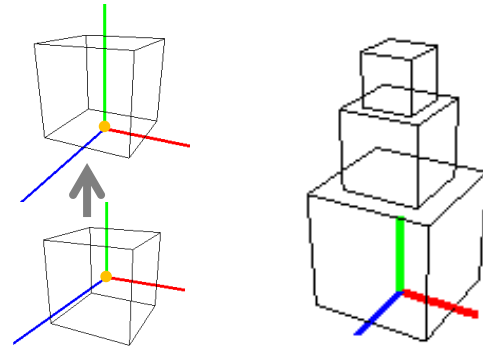
1. Coordinate spaces

- A graphics pipeline takes a description of a scene in 3D space and maps it into a 2D projection on the display space.

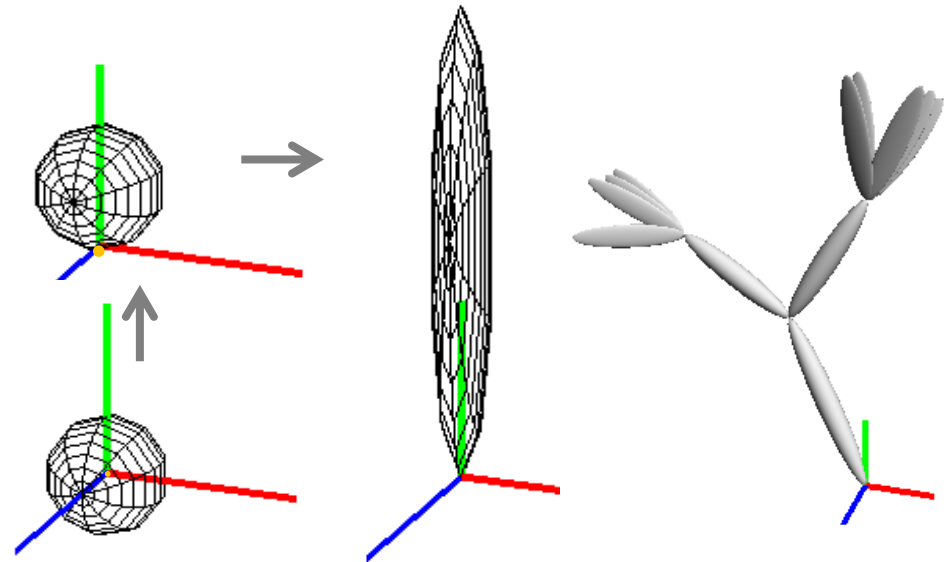


2. Local Coordinate System (LCS)

- Store vertices of a polygon mesh object with respect to some point located in, on, or near the object
- Promotes modelling flexibility
- Transform in LCS to produce basic object shape
 - Put coordinate frame at a sensible point to ease joining with other objects
 - Scaling can cause normal calculation complexities (e.g. for lighting), there is an argument that the object should be defined at the right scale
- Supports object instantiation



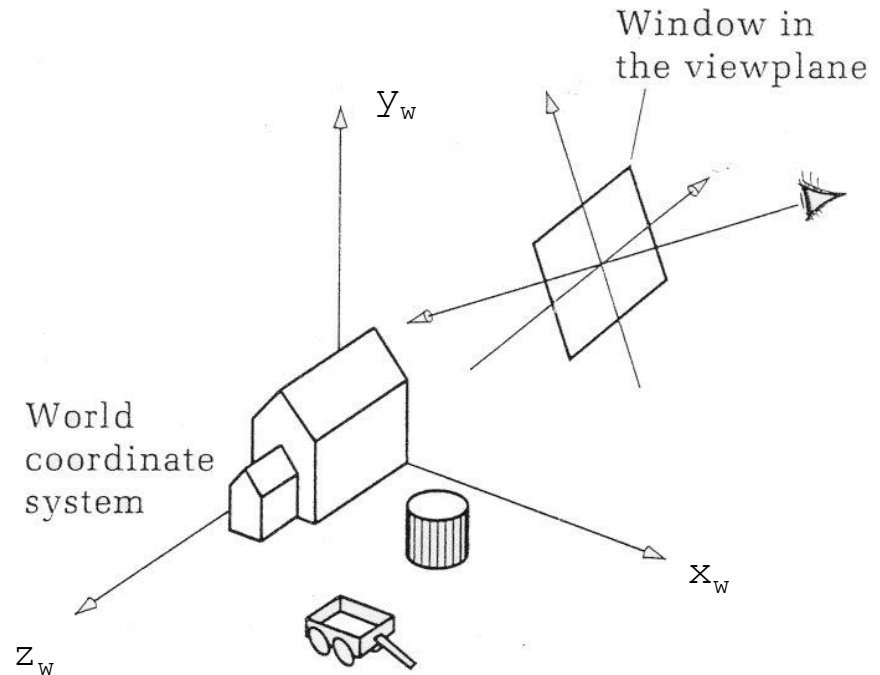
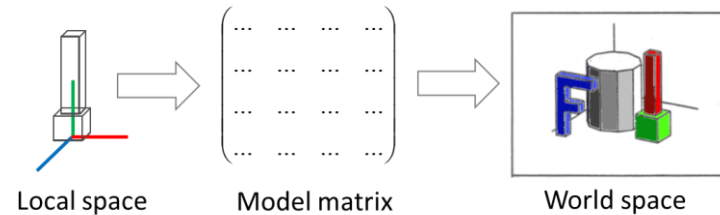
If cube side=1, shifting up produces a cube of height 1 with base centred on origin



If radius=1, shifting up produces a sphere of height 2 with south pole at origin

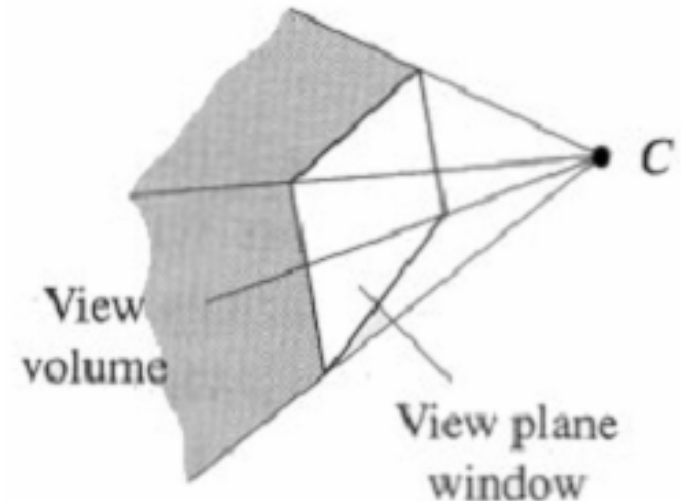
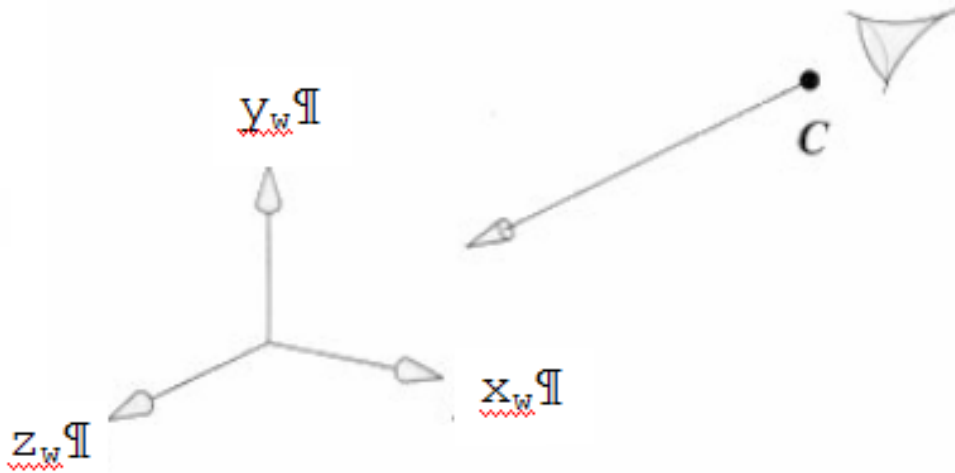
3. World Coordinate System (WCS)

- To create a scene, transform all objects into one common, global coordinate system
 - Right handed system
- Define light source(s) and camera(s)
- Specify surface attributes, e.g. texture and colour of objects (see later lecture)



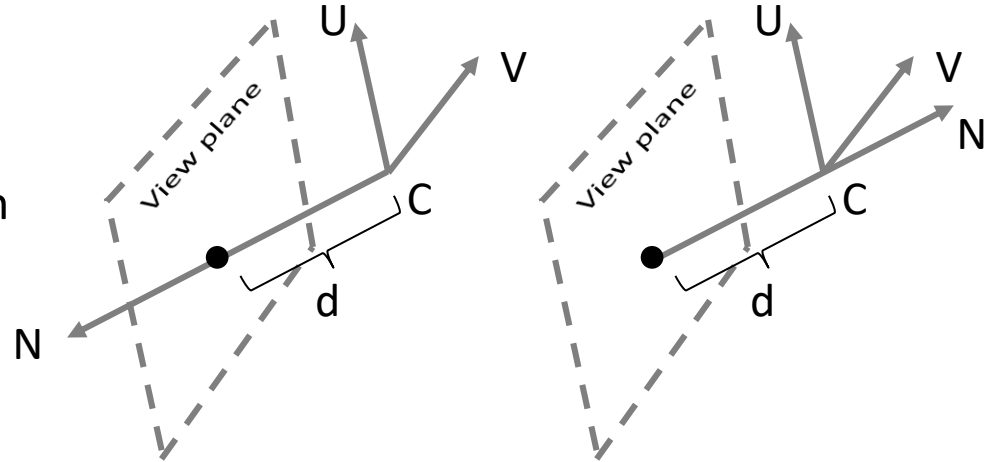
4. Defining view space

- (Alternative names: Camera space, eye space)
- Establish viewing parameters
 - viewpoint, viewing direction and a view volume
- The view frustum is the field of view



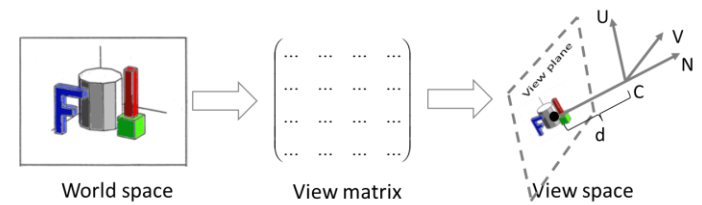
4.1 The camera

- The camera can be positioned anywhere in the WCS, pointed in any direction and rotated about the viewing direction
 - Left handed system
 - (Or right handed system)
- A view point **C**
- A view coordinate system:
 - z • **N** – viewing direction
 - y • **U** – ‘up’ vector
 - x • **V** – cross product of **N** and **U**
- A view plane (parallel to **V** and **U**) onto which the scene is projected
 - **d** – distance from **C**



Jamin, Michigan State Univ, 2013

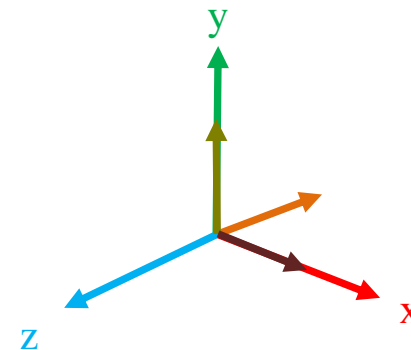
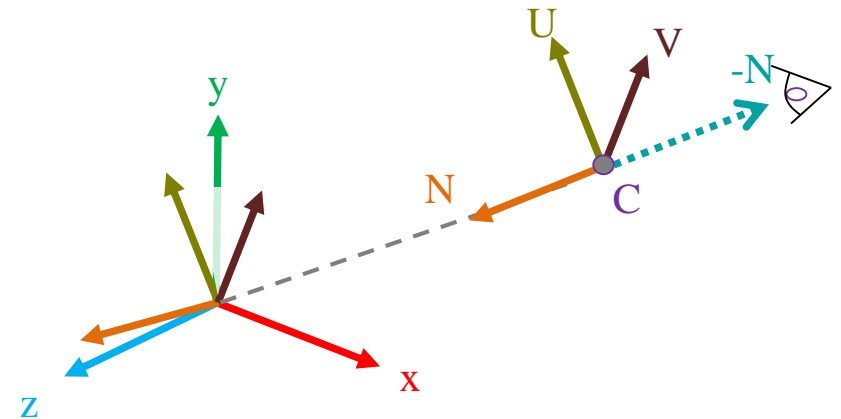
4.2 World to view coordinates



- Transform world coordinates to view coordinates

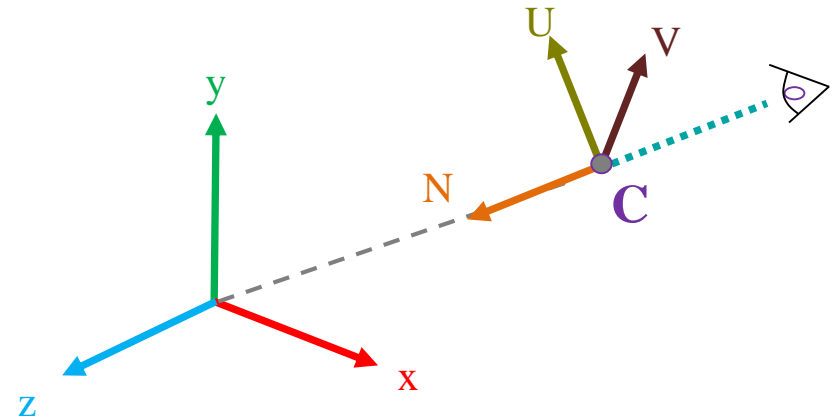
$$\begin{pmatrix} x_v \\ y_v \\ z_v \\ 1 \end{pmatrix} = T_{view} \begin{pmatrix} x_w \\ y_w \\ z_w \\ 1 \end{pmatrix}$$

- Translate **C** to world origin
- Rotate **UVN** to align with world axes
 - N** is on negative Z axis
- Inverse of these processes converts world coordinates to view coordinates
 - Need to change z coordinate too



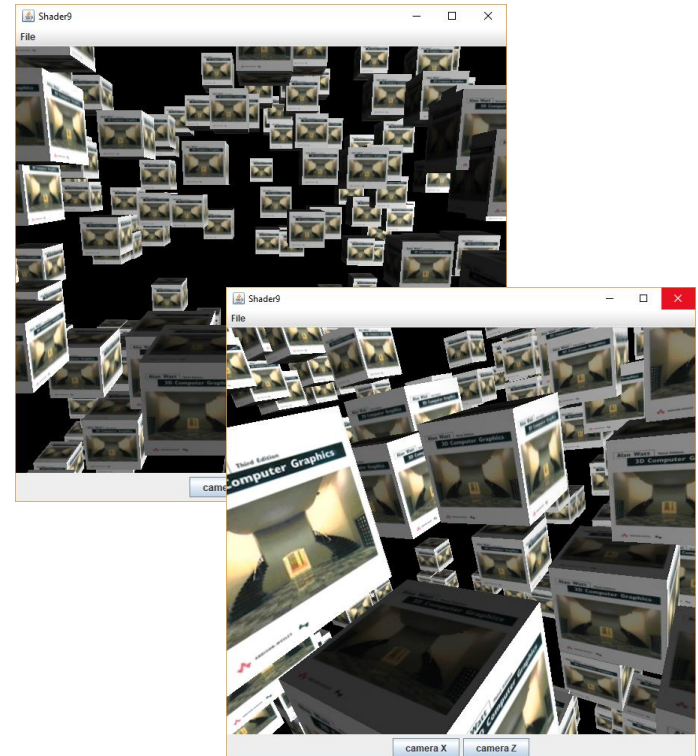
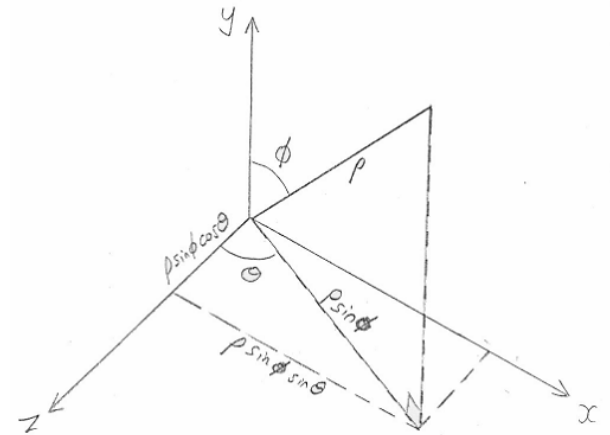
4.3 User interface considerations

- **C** is specified as a 3D coordinate
- **N** can be calculated by giving a 3D coordinate to look at
- **U** and **V** are more problematic
- User specifies **U'**, e.g. (0,1,0)
 - $V = U' \times N$
 - $U = V \times N$
 - Known as Gram-Schmidt process
- **C, U, V, N** can now be used to form the view matrix
- (Note if **N** specified in opposite direction:
 - $V = N \times U'$; $U = N \times V$)



4.3.1 Example camera system

- Camera position at a fixed radius could be controlled by a mouse by using two angles (θ , ϕ) in a spherical coordinate system centred on the world origin
- We can create a camera that stays in one position, but can point in any direction
 - Stand still and move your head around to look in different directions
 - Again, controlled by mouse and two angles
- Can also add ability to move in direction the camera is looking or sideways/up/down



4.4 Culling (= back-face elimination)

- Compare orientation of each polygon with viewpoint direction and remove polygons that are facing away from the camera

- visible = $N_p \cdot S > 0$

$$N_p \cdot S = |N_p| |S| \cos\theta$$

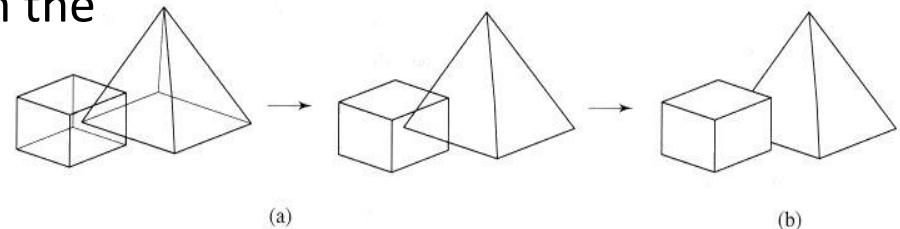
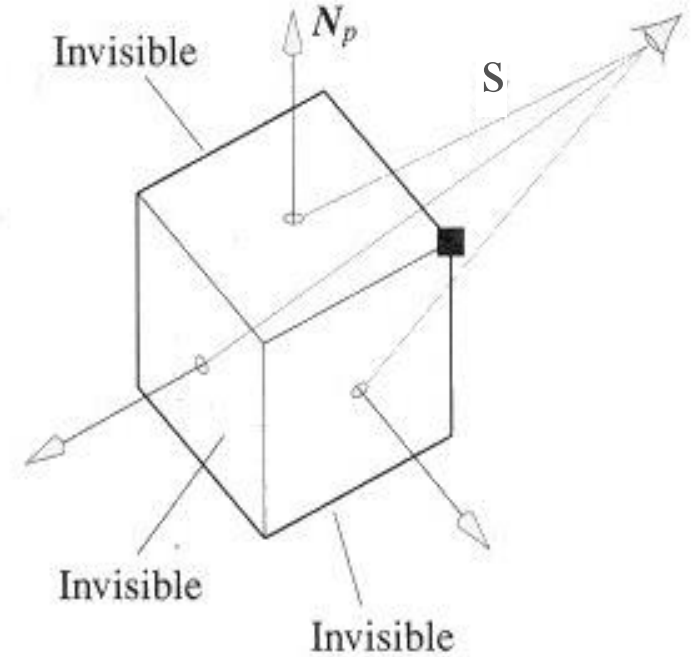
where

N_p is the polygon normal

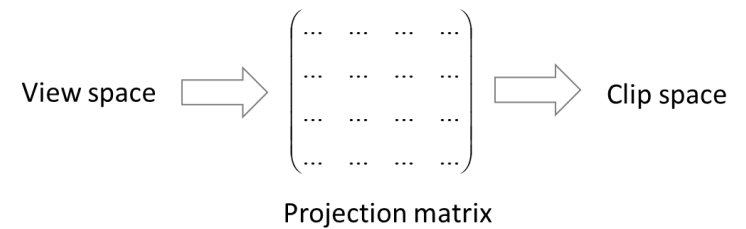
S is the 'line of sight' vector (use any vertex on the polygon for simplicity)

θ is the angle between N_p and S

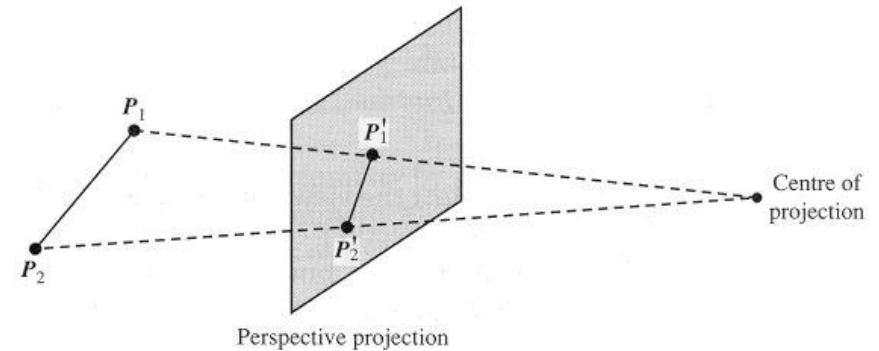
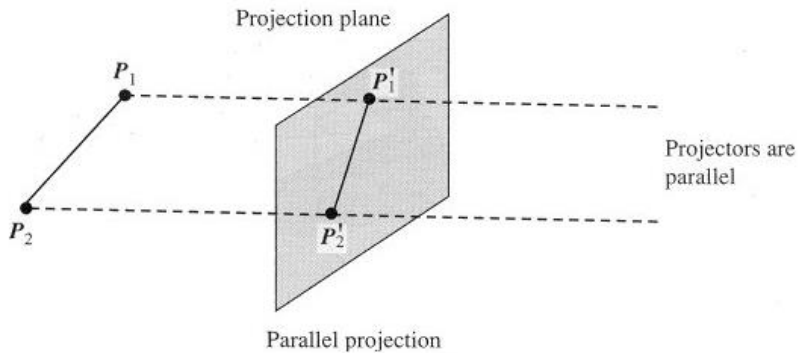
- (a) Culling only removes complete polygons that are facing away from the camera
- (b) HSR deals with the general problem of partial obscuration



5. Projection



- This is the conversion from view space to clip space (and 3D screen space)
- Two basic projections:
 - Orthographic (or parallel) and Perspective



5.1 Orthographic projection

- Used in CAD, where measurement is important

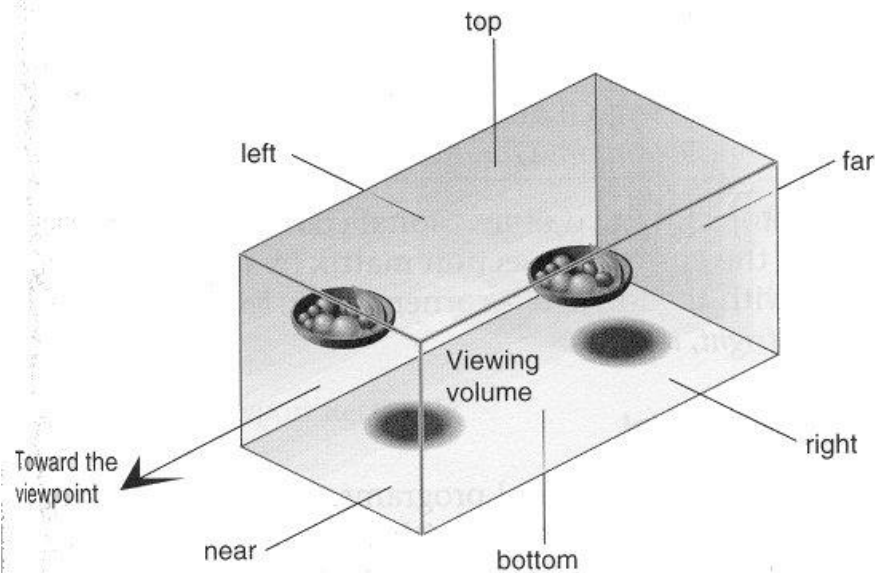
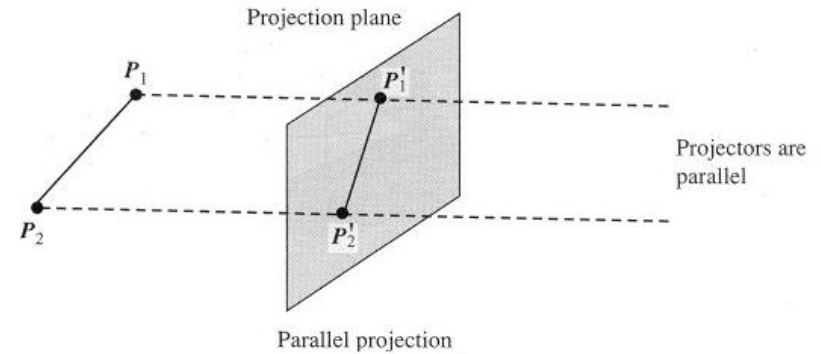
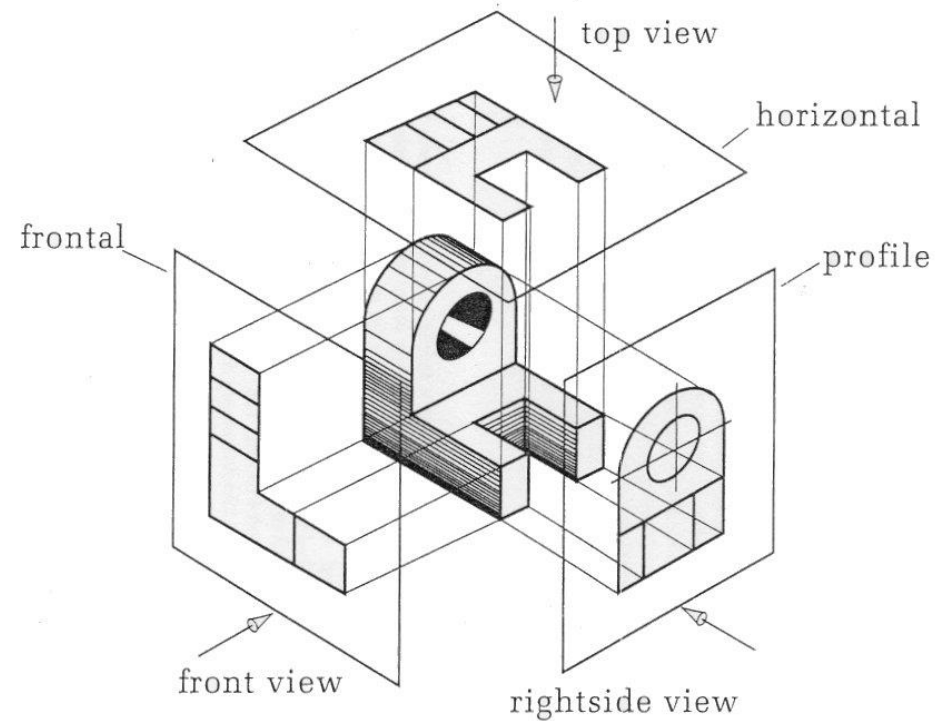
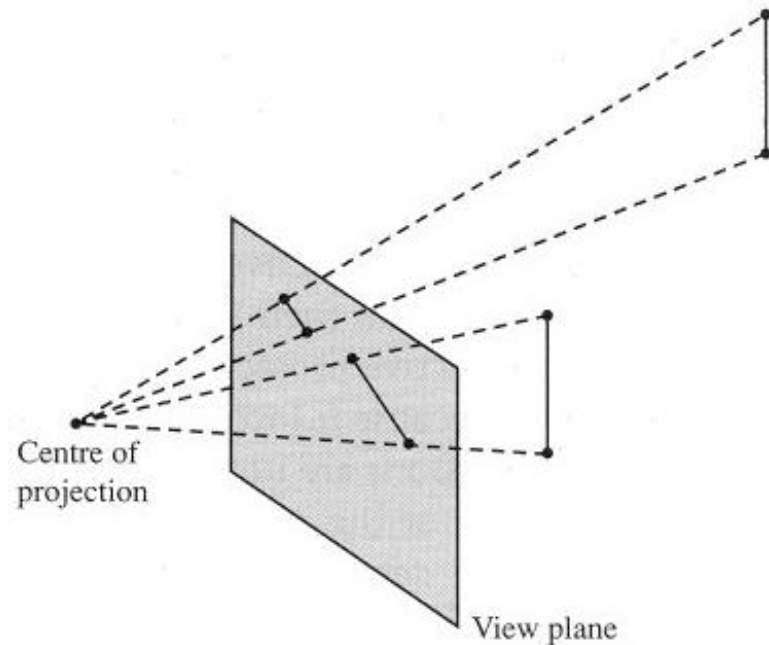


Figure 3-15 Orthographic Viewing Volume



5.2 Perspective projection

- A perspective projection is the more common choice in computer graphics
- A perspective projection incorporates foreshortening
 - Relative dimensions are not preserved
 - Enables perception of depth



5.3 False perspective

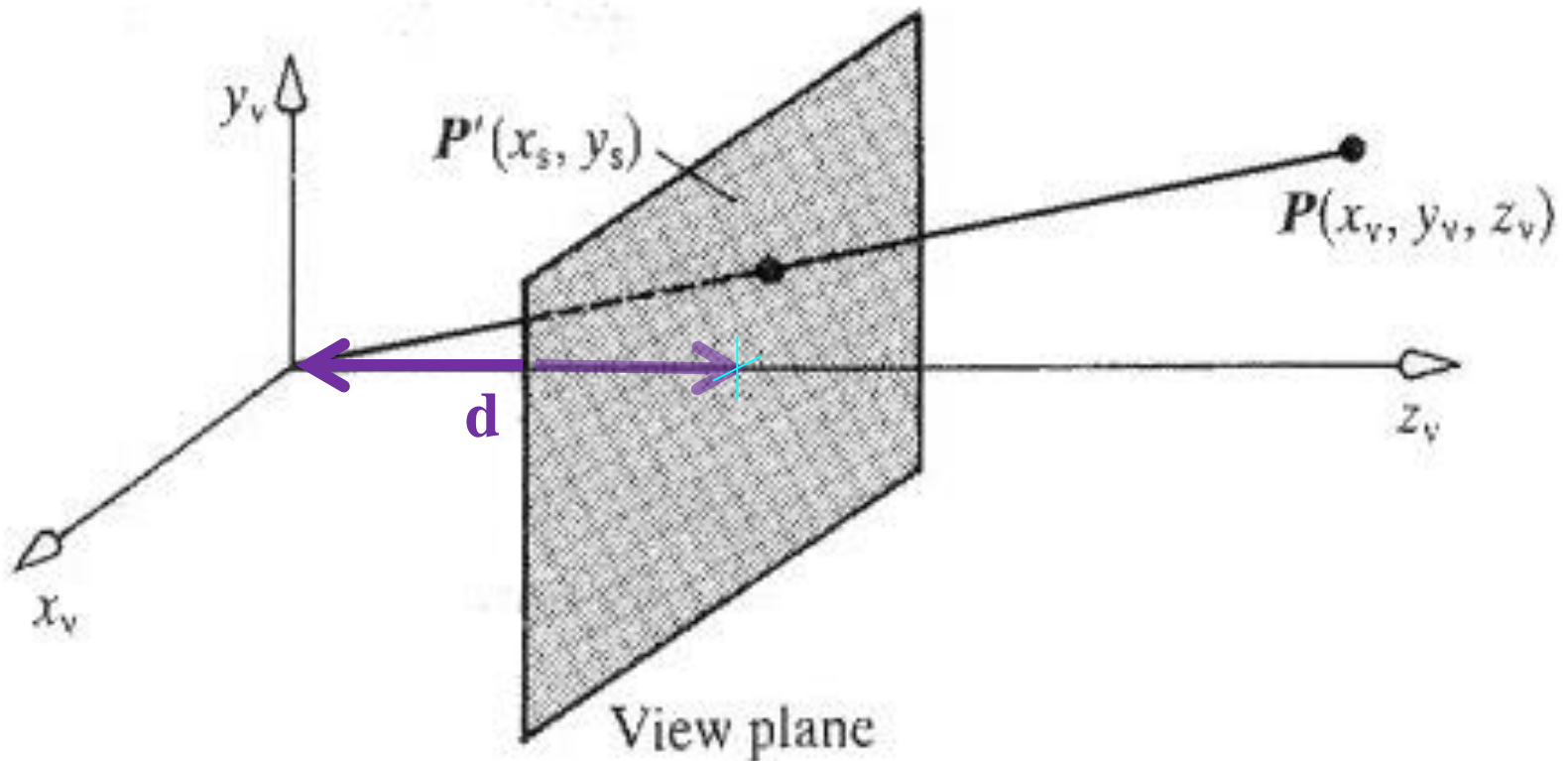
- *Satire on False Perspective*, William Hogarth, 1754, engraving
- “Whoever makes a DESIGN without the Knowledge of PERSPECTIVE will be liable to such Absurdities as are shewn in this Frontispiece”
- Some ‘errors’:
 - The man in the foreground's fishing rod's line passes behind that of the man behind him.
 - The sign is moored to two buildings, one in front of the other, with beams that show no difference in depth
 - The sign is overlapped by two distant trees.
 - The man climbing the hill is lighting his pipe with the candle of the woman leaning out of the upper story window.
 - The crow perched on the tree is massive in comparison to it.
 - ...



http://en.wikipedia.org/wiki/Satire_on_False_Perspective

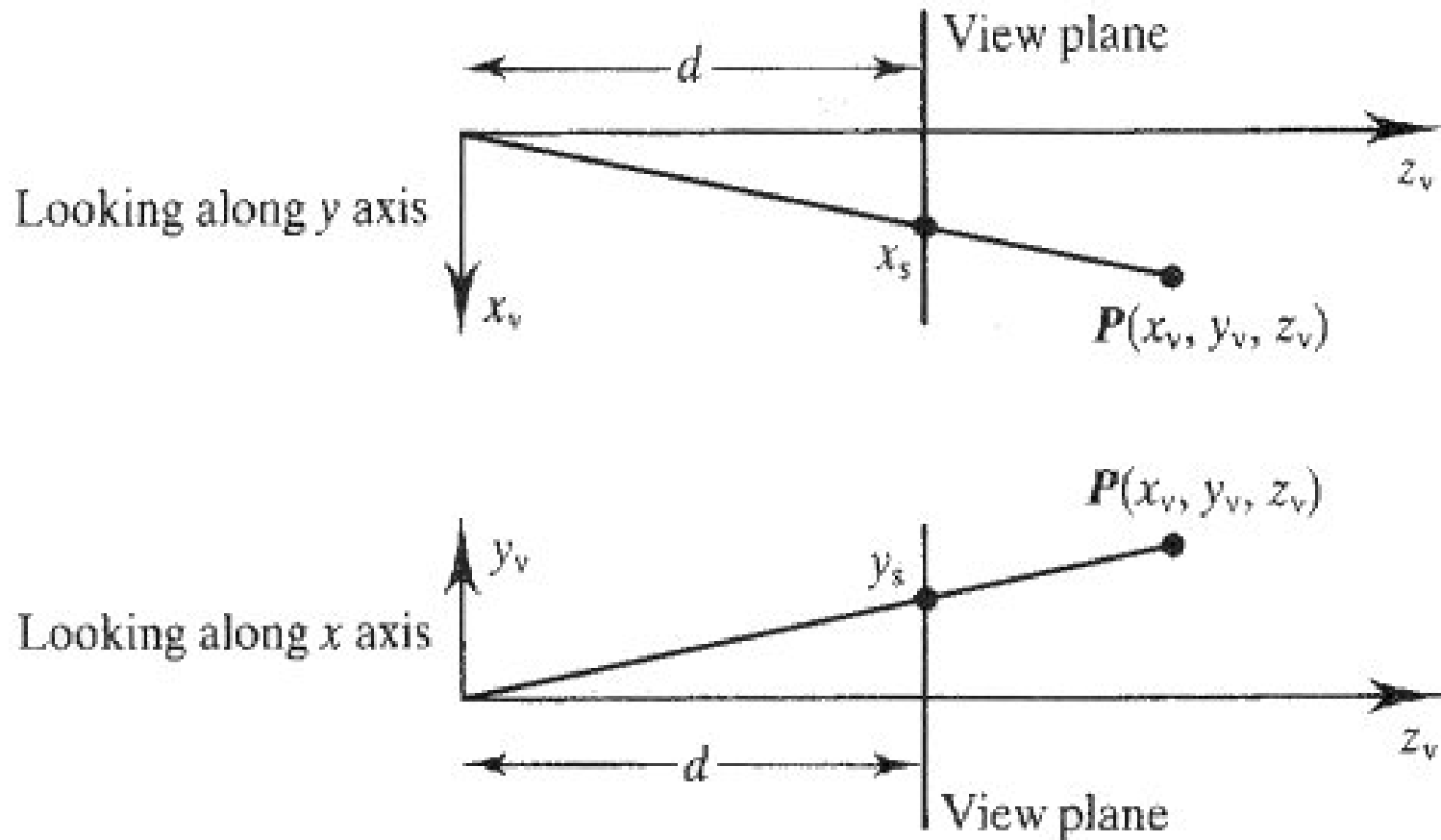
5.4 Deriving a perspective projection

- Define a focal distance, d
 - Distance from camera to view plane



5.4 Deriving a perspective projection

- Similar triangles gives: $\frac{x_s}{d} = \frac{x_v}{z_v}$ $\frac{y_s}{d} = \frac{y_v}{z_v}$



5.4 Deriving a perspective projection

$$\frac{x_s}{d} = \frac{x_v}{z_v} \quad \frac{y_s}{d} = \frac{y_v}{z_v}$$

- Rearranging, setting $w = zv/d$, and using homogeneous coordinates:

$$\begin{pmatrix} X \\ Y \\ Z \\ w \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 1/d & 0 \end{pmatrix} \begin{pmatrix} x_v \\ y_v \\ z_v \\ 1 \end{pmatrix}$$

T_{pers}

- The perspective divide is clear; screen coordinates are given by:

$$x_s = X/w$$

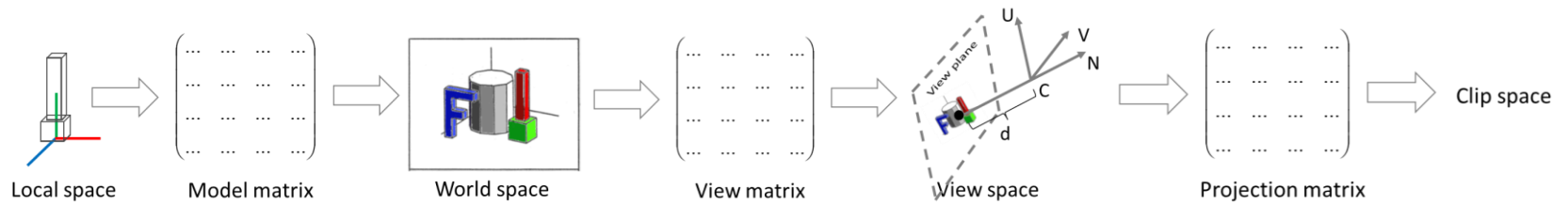
$$y_s = Y/w$$

$$z_s = Z/w$$

A more complex
perspective matrix used
in practice is shown in
the Appendix.

5.5 Combining the matrices

- Every vertex v_i is transformed by ModelViewProjection matrix
- This is done in the vertex shader

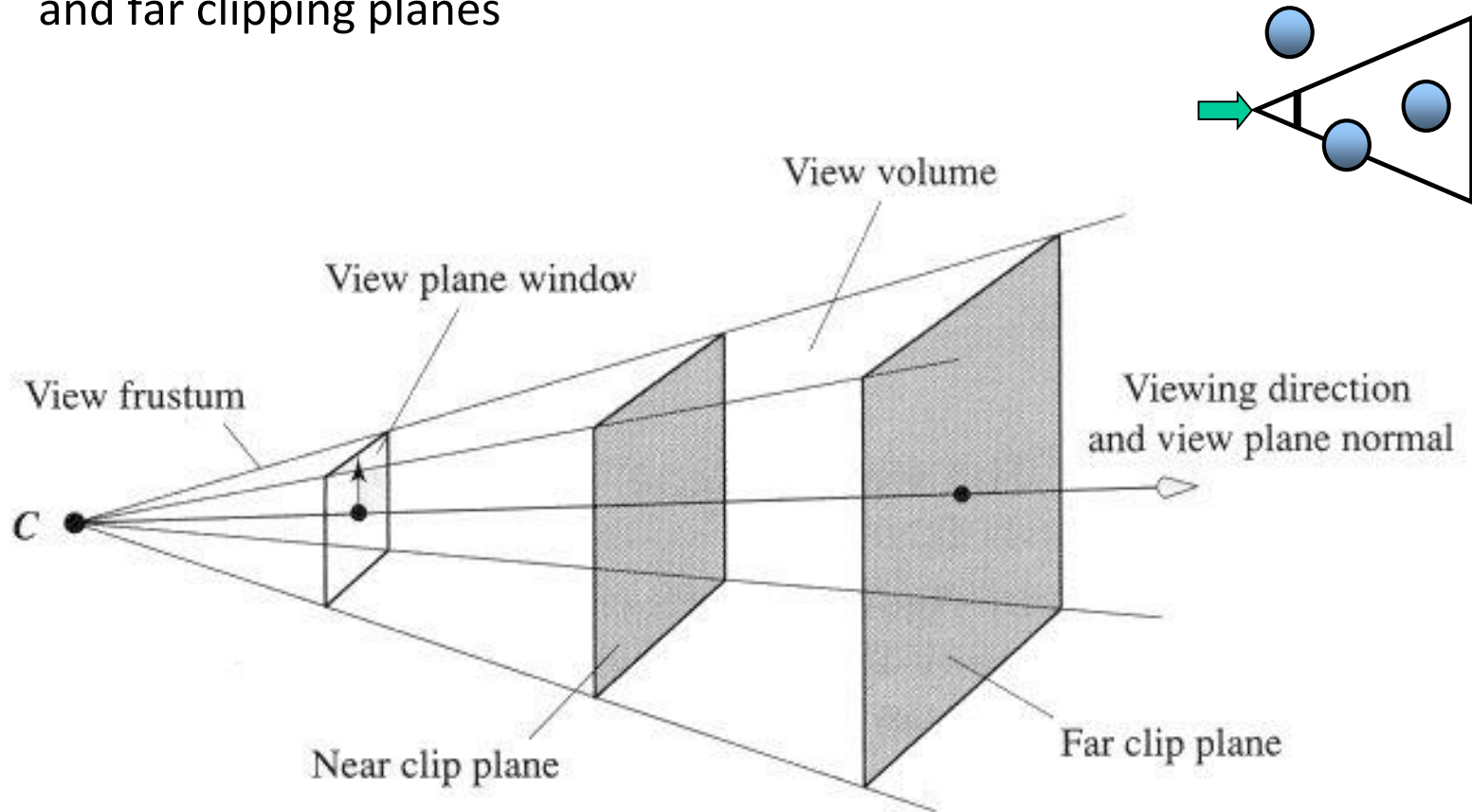


$$\text{MVPmatrix} = \text{projection} * \text{view} * \text{model}$$

$$\text{transformed_vertex_position} = \text{MVPmatrix} * \text{vertex_position}$$

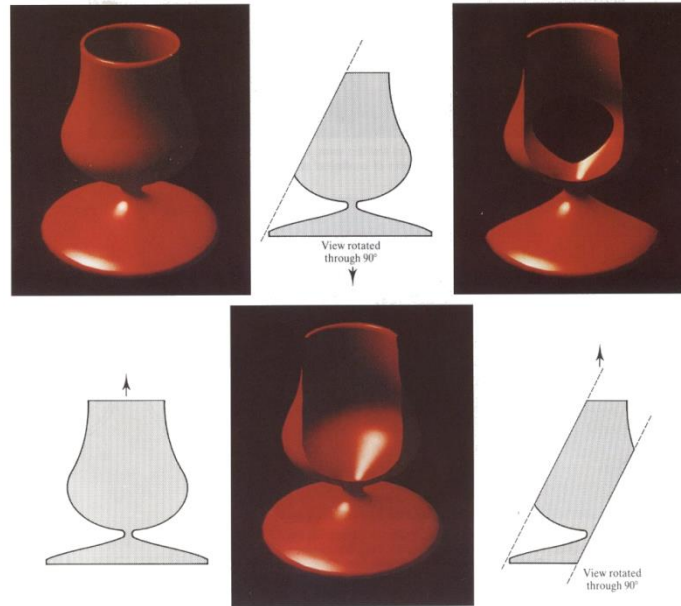
6. The view volume

- Defined by a view plane window, has a finite width and height, and near and far clipping planes



6.1 Clipping planes

- Near plane clips things 'behind' the camera
- Far plane clips distant things
 - In games, use 'fog' to blend out



2 A view volume interacting with a shaded object. Bringing near and far planes into coincidence with an object; (*centre*) near plane coincides; (*right*) both planes coincide with the object.



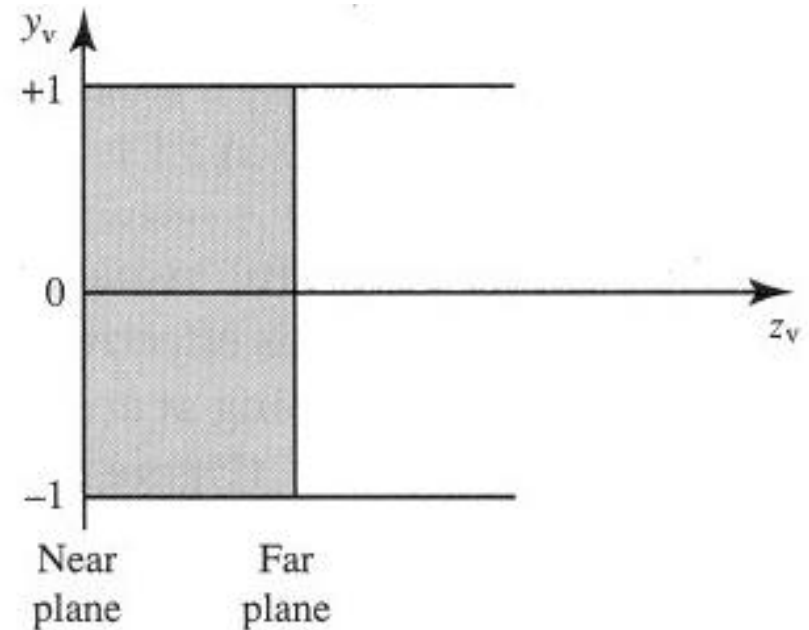
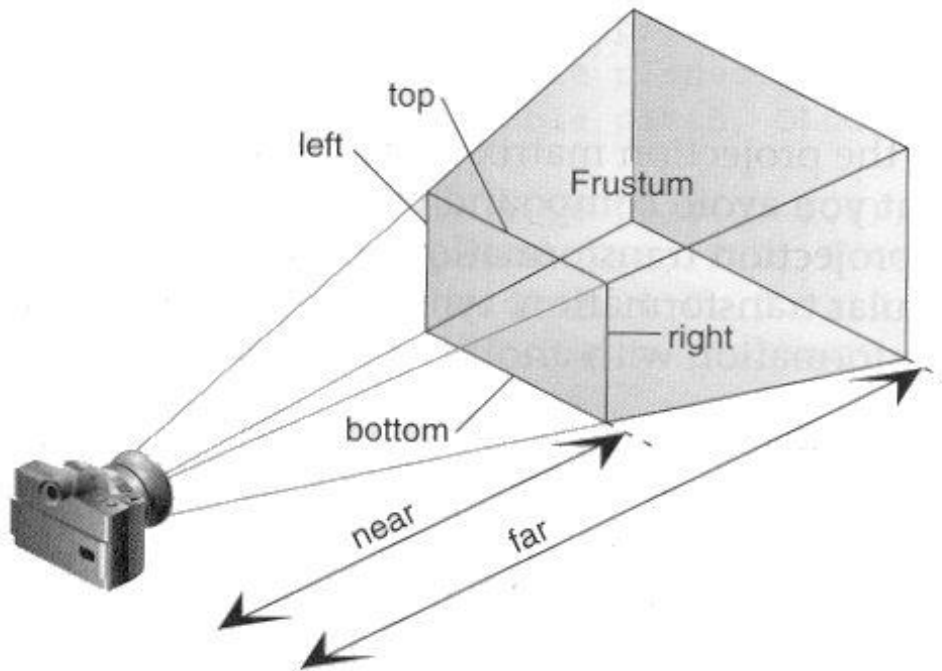
Finite view volume



Finite view volume + fog

7. 3D Screen space

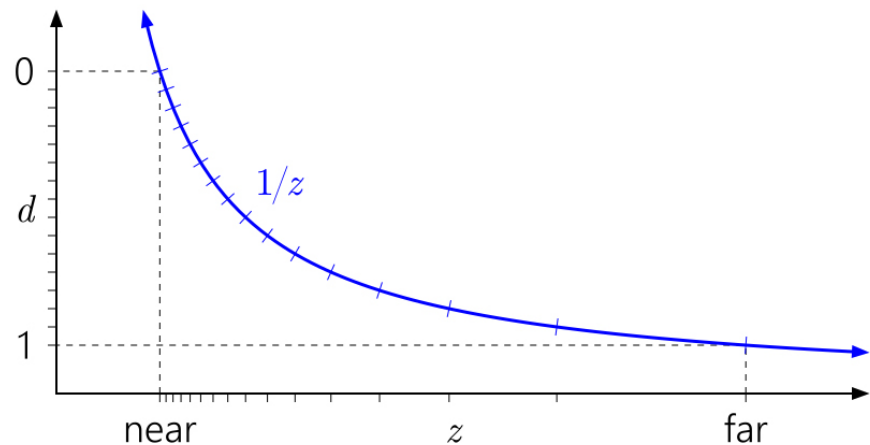
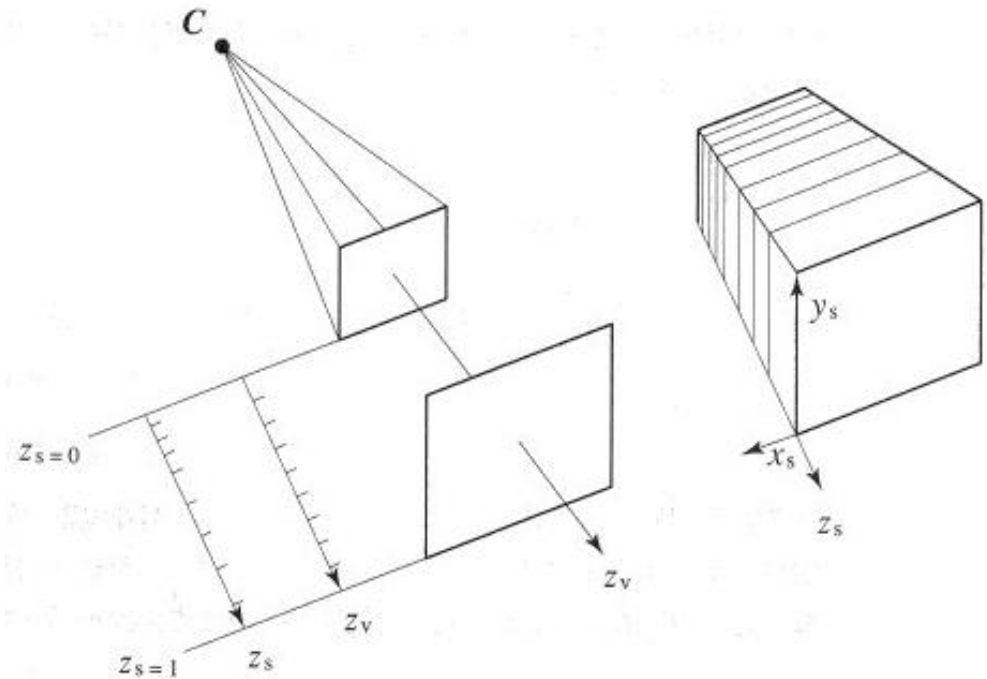
- We need depth information to decide what's in front
- View space (x_s, y_s, z_s) is transformed into a box-shaped space (x_s, y_s) (-1 to +1), with z_s as the depth (0 to 1), which supports easy clipping



OpenGL red book

7.1 The relationship between z_v and z_s

- Interpolating along a line in view space (eye space) is not the same as interpolating this line in 3D screen space
- As z_v approaches the far clipping plane, z_s approaches 1 more rapidly
- Thus objects get distorted towards the back of the view frustum



<https://developer.nvidia.com/content/depth-precision-visualized>

7.2 3D Screen space

- *Later Lecture:* Rendering processes:
 - Rasterisation – decide which pixels are covered by polygons.
 - Hidden surface removal (HSR) – decide what is in front.
 - Shading – decide what colour things are.

Vertex shader

- uses
ModelViewProjection
matrix to transform
vertex positions into
3D screen space

Primitive assembly and clipping

Rasterisation

- interpolates vertex
values for a polygon to
produce a set of
fragments for the
inside of the polygon

Fragment shader

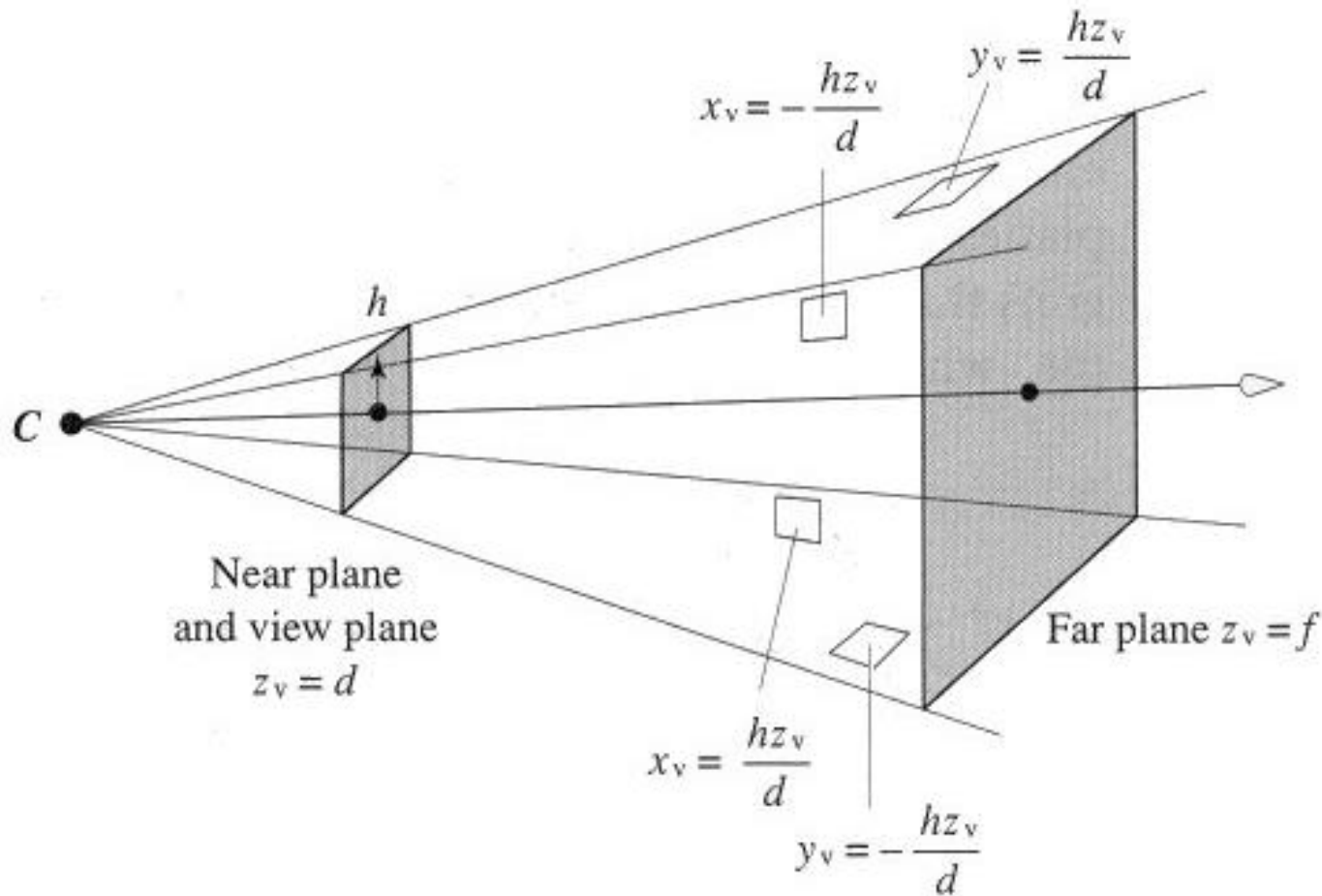
- calculates final values
for the fragment which
are written to relevant
buffers, e.g. pixel colour
and depth value

8. Summary

- Using a local coordinate system to define objects supports the idea of object instantiation
- Individual objects are brought together in the (global) world space
- The conversion from world to view space involves translation and rotation
- The conversion from view space to screen space is called *projection*
- A ModelViewProjection matrix is used to transform vertices from local space to 3D screen space

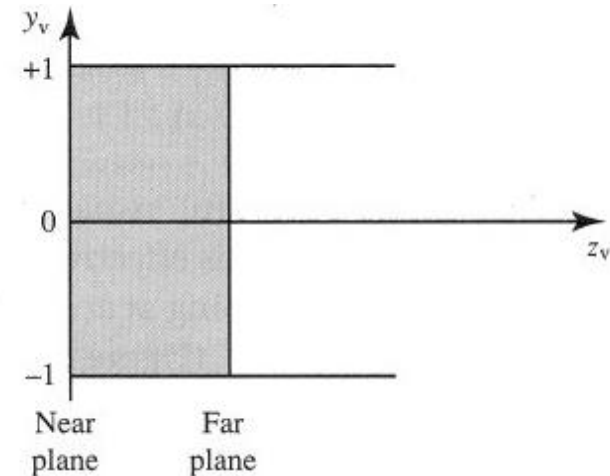
A1. The view volume

- Simplify diagram by setting width = height = $2h$



A.2 3D screen space

- (Newman and Sproull, 73)
- Useful properties:
 - Image plane width and height map to $[-1..1]$
 - Points on the image plane should map to $z_s = 0$
 - Points on the far clip plane should map to $z_s = 1$
 - Intersections of lines and planes in view space should map to their intersections in screen space
 - Straight lines should transform to straight lines
 - Planes should transform to planes
- This is the case if $z_s = A + B/z_v$
- Using the properties above as constraints, together with the view volume, leads to:



$$x_s = d \frac{x_v}{hz_v}$$

$$y_s = d \frac{y_v}{hz_v}$$

$$z_s = \frac{f(1 - d/z_v)}{(f - d)}$$

A.3 Matrix form

- Using homogeneous coordinates we can write:

$$\begin{pmatrix} X \\ Y \\ Z \\ w \end{pmatrix} = \begin{pmatrix} d/h & 0 & 0 & 0 \\ 0 & d/h & 0 & 0 \\ 0 & 0 & f/(f-d) & -df/(f-d) \\ 0 & 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} x_v \\ y_v \\ z_v \\ 1 \end{pmatrix} = T_{pers} \begin{pmatrix} x_v \\ y_v \\ z_v \\ 1 \end{pmatrix}$$

A.4 Decomposing the transformation

- To see what is happening, we can break the view to screen space into two parts:

$$T_{pers} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & f/(f-d) & -df/(f-d) \\ 0 & 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} d/h & 0 & 0 & 0 \\ 0 & d/h & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$= T_{pers2} T_{pers1}$$

- T_{pers1} scales by d/h in x and y , so that the side clipping planes are of the form $x=z$ and $y=z$
- T_{pers2} maps the regular pyramid into a box, with the far plane at $z=1$

