



The  
University  
Of  
Sheffield.

## COM3503/4503/6503: 3D Computer Graphics

### Lecture 13: Texture: part 3



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[http://commons.wikimedia.org/wiki/File:Liquorice\\_allsorts\\_2010.jpg](http://commons.wikimedia.org/wiki/File:Liquorice_allsorts_2010.jpg)

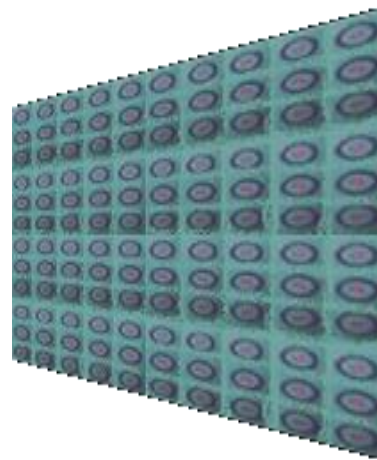
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# 1. Introduction

- 2D texture colour/diffuse mapping pastes a bitmap picture (texture) onto the surface of an object
- There are a range of approaches for pasting the 2D texture on the surface of a 3D object



2D  
mapping

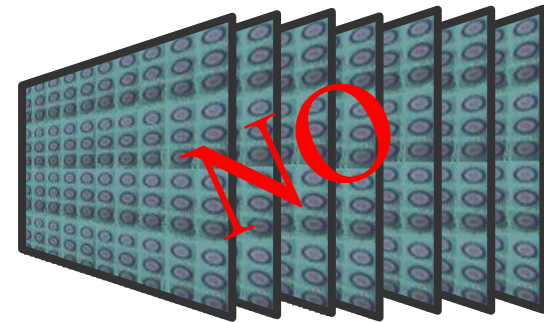


# 1. Introduction

- 3D texture mapping places an object inside a 3D pattern
- The 3D pattern is NOT represented as an array of 2D textures
  - This would be memory inefficient
  - Many values would remain unused
- Instead, the pattern is usually represented as a procedure...



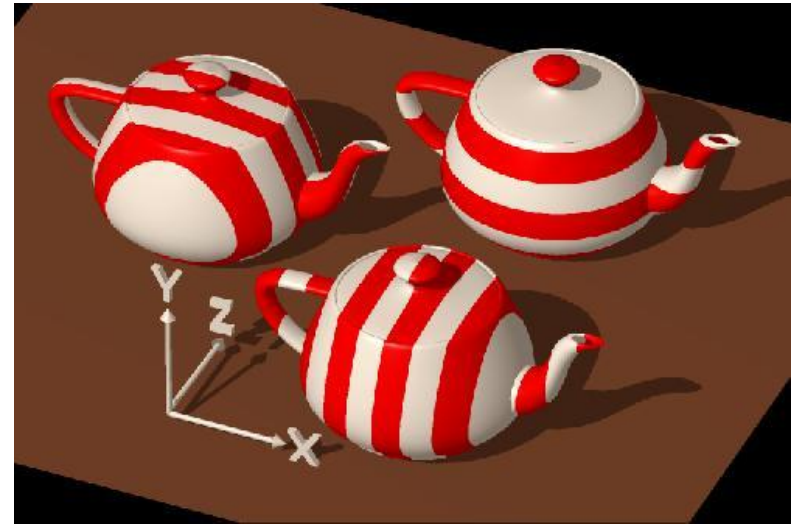
3D  
mapping



## 2. 3D texture mapping ('Solid texture') [Perlin,85; Peachey,85]

- For 3D texture mapping, all that is required to texture a point is a 3D coordinate
- A texture function  $f(x,y,z)$  is evaluated for each 3D coordinate  $(x_w, y_w, z_w)$
- Example function:

```
if trunc(z) is even {  
    colour of point is red  
}  
else {  
    colour of point is white  
}
```
- Example:  $z = 2.4 \rightarrow \text{red}$
- Example:  $z = 1.9 \rightarrow \text{white}$



Left teapot:

if  $\text{trunc}(z)$  is even then red; else white

Middle teapot:

if  $\text{trunc}(x)$  is even then red; else white

Right teapot:

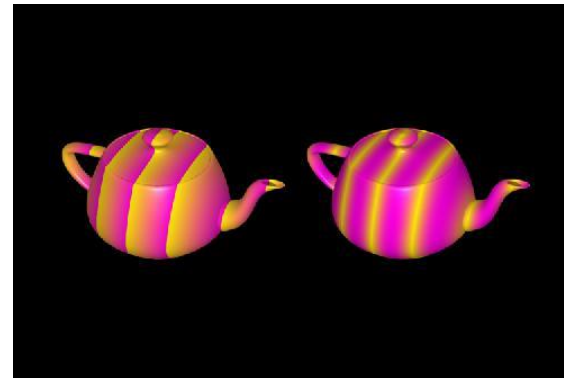
if  $\text{trunc}(y)$  is even then red; else white

## 2. 3D texture mapping

- Left teapot →
  - use  $x$  and  $y$  to compute radial distance from axis through teapot centre
  - If  $\text{trunc}(\text{result})$  is even then red; else white



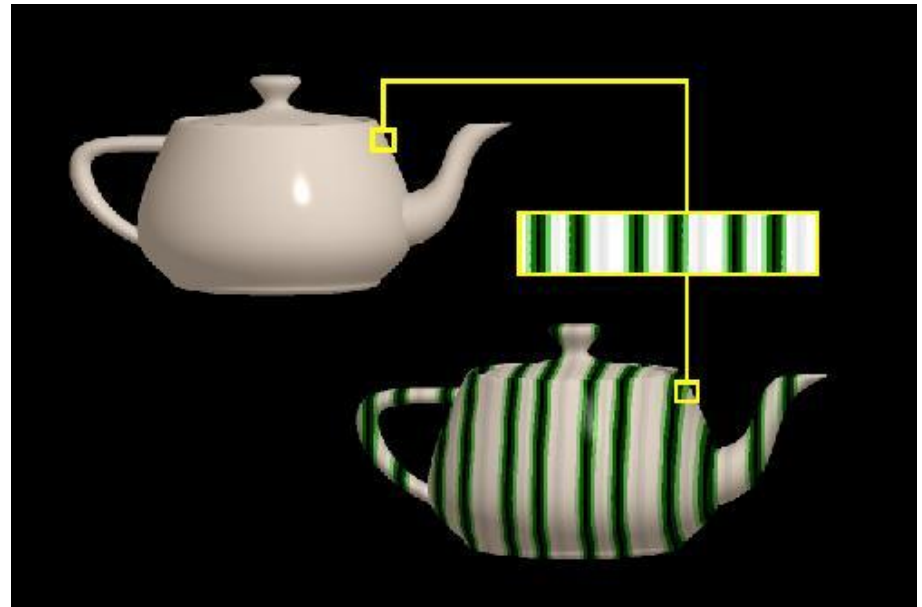
- More complex functions can be used:
  - Left:  $\text{mod}(x, a)/a$ .
  - Right:  $(\sin(x)+1)/2$



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## 2. 3D texture mapping

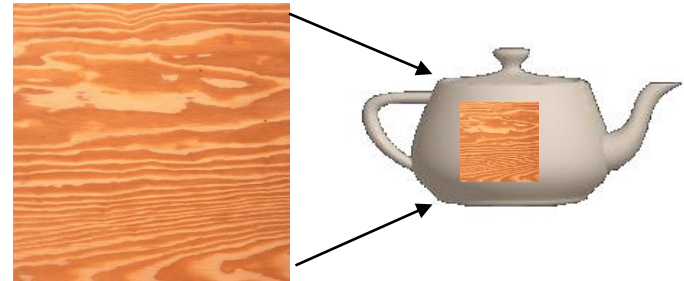
- Here a colour table is used
- Function:
  - the fractional part of the x coordinate (0.0 .. 0.99) multiplied by number of elements in colour table (256)
  - process repeats



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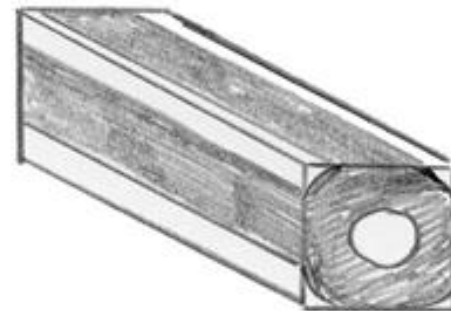
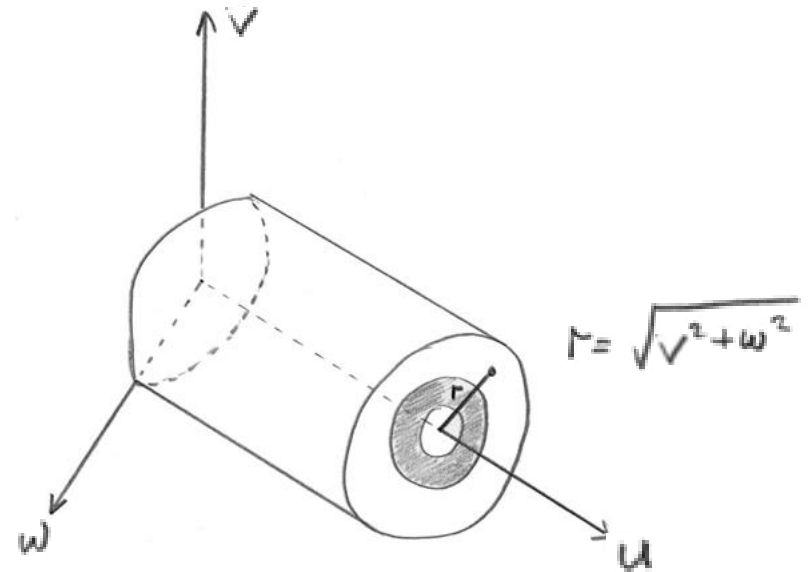
## 2.1 Example: wood

- We want to model the appearance of wood
- 2D texture mapping:
  - Take a photo of a wood surface and paste it on to a model
  - Limited to using the photograph (or photographs)
- 3D texture mapping (solid texture)
  - Create a function that produces the pattern of colour variation
  - A good function can produce endless patterns



## 2.1 Example: wood

- Start by defining a function based on a cylinder
- In  $u, v, w$  space,  
if  $\text{trunc}(r)$  is even then dark brown  
else light brown
- Map  $x, y, z$  of object to the  $u, v, w$  space  
the texture function is defined in
  - A scale function may be required if  
the  $x, y, z$  space is large in comparison  
to the  $u, v, w$  space

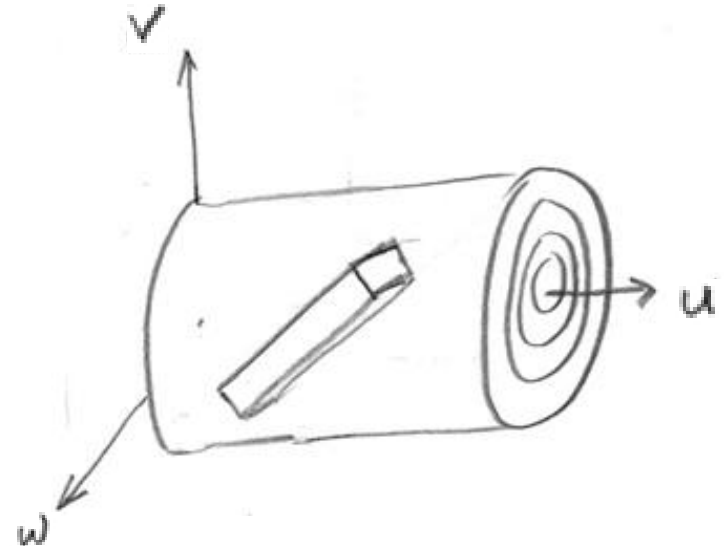


$$(u, v, w) \leftarrow (x_w, y_w, z_w)$$



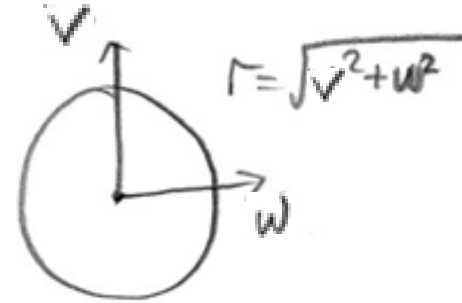
## 2.1 Example: wood

- We can remove the regularity of the function in a number of ways:
- Tilt (i.e. rotate) the  $(x, y, z)$  coordinate before using in the function
  - $(u, v, w) \leftarrow \text{Tilt}(x, y, z)$

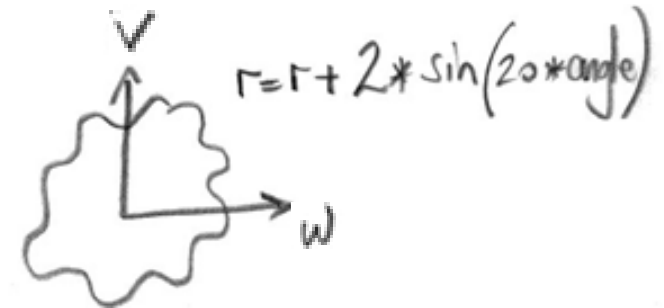


## 2.1 Example: wood

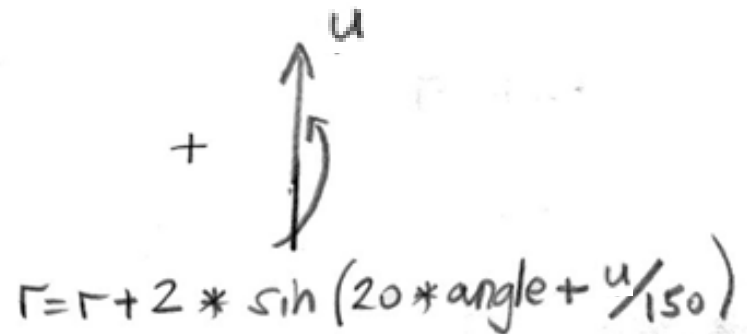
- We can remove the regularity of the function in a number of ways:
- Alter the calculation of  $r$ :



- E.g. by adding a sine wave

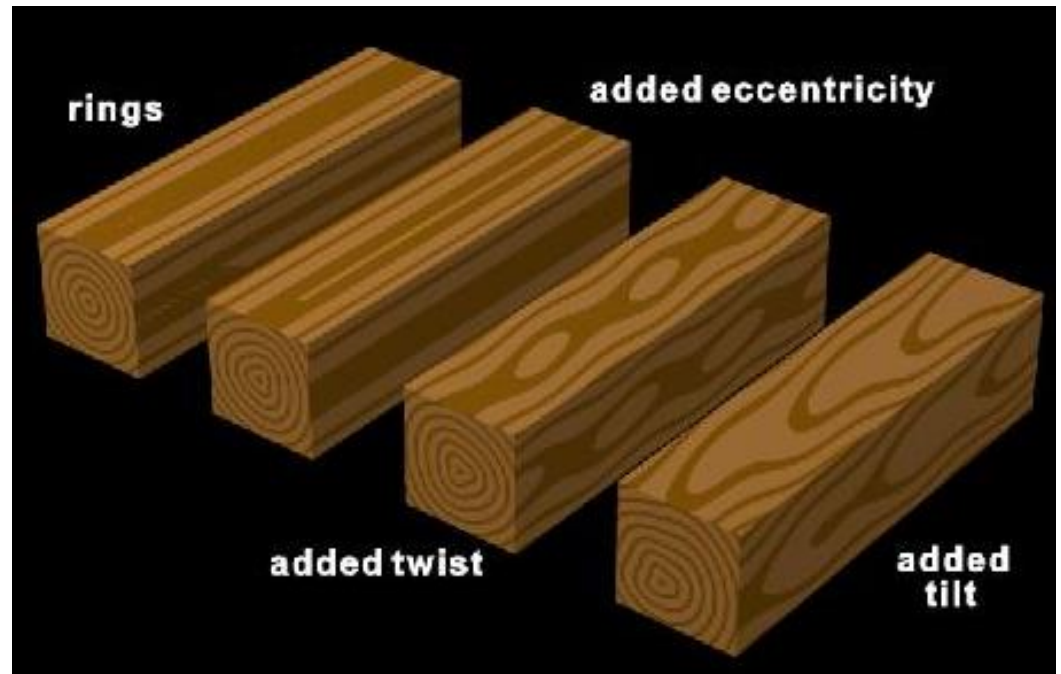
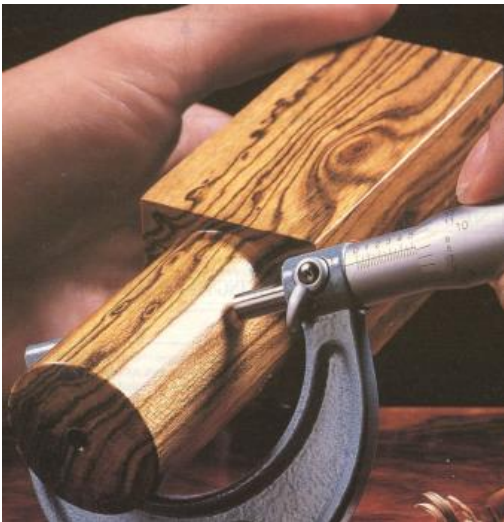


- E.g. by adding a twist with respect to the  $u$  axis



## 2.1 Example: wood

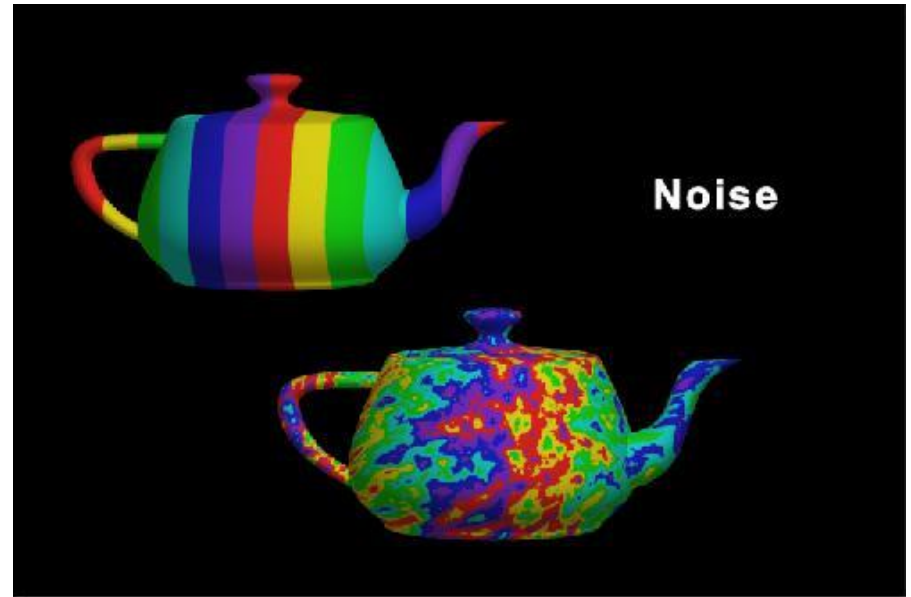
- These are all combined to give the final result
- However, the result is still too regular in appearance



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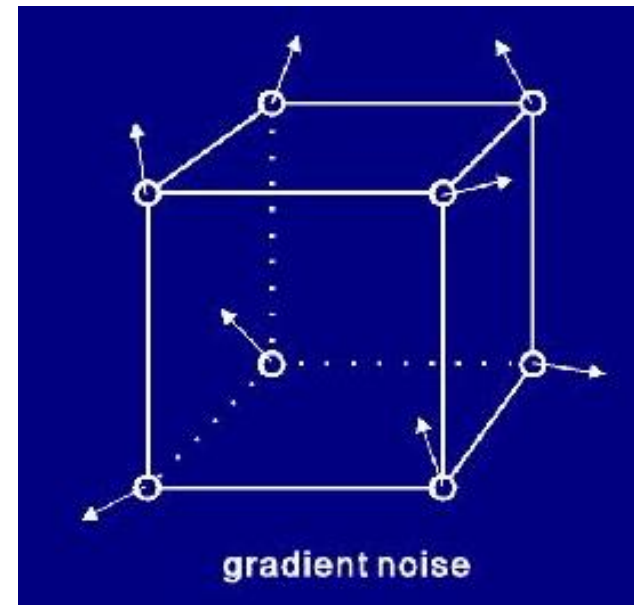
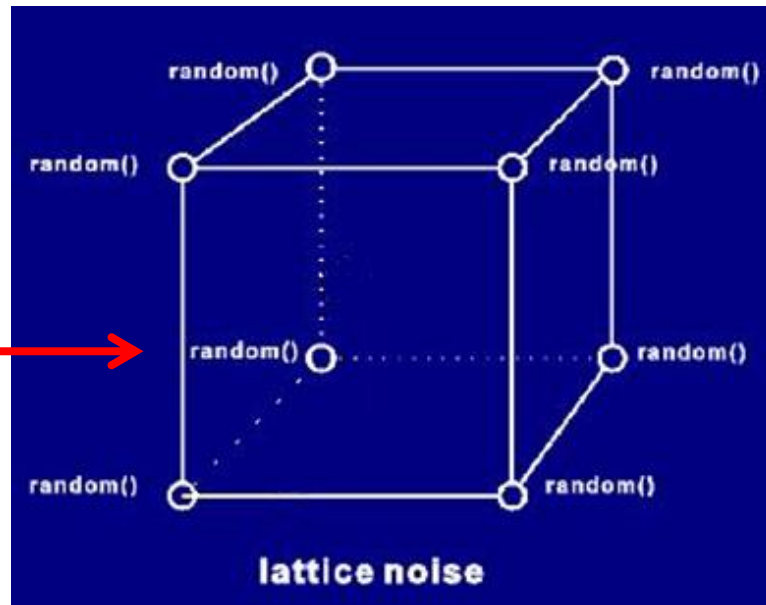
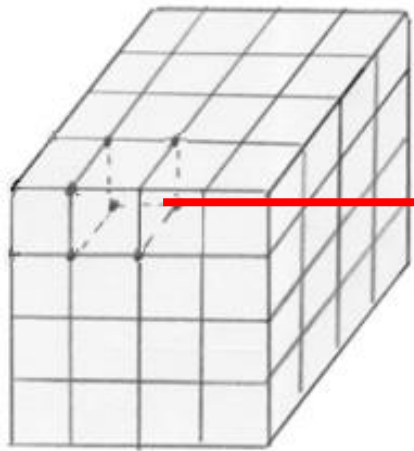
## 2.2 Adding noise

- To remove the regular appearance, we can add randomness (i.e. noise) to the function
- But, needs to be controllable. Need to be able to:
  - Intuitively control the amount of noise to give different effects
  - Use same values every time the object is drawn



## 2.2 Adding noise

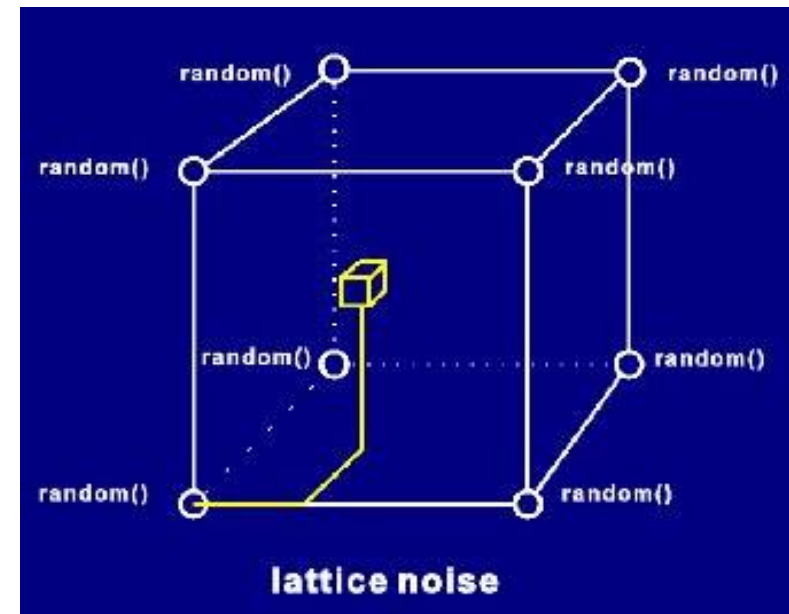
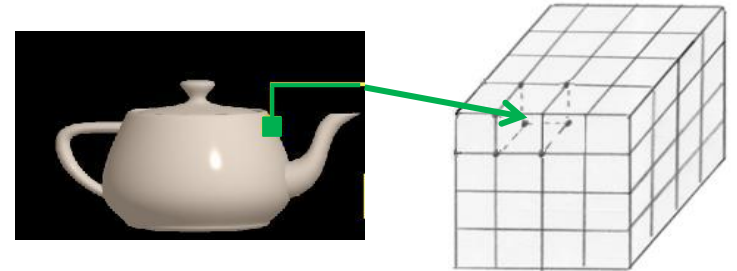
- The noise is generated once and stored in a low resolution grid ( $u, v, w$ )
- Lattice noise: random value at each point in a 3D grid
- Gradient noise: random unit vector for each lattice point



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## 2.2 Adding noise

- Given a floating point  $(x,y,z)$  object position, this is mapped to a floating point  $(u,v,w)$
- The noise value  $n(u,v,w)$  is calculated using interpolation from surrounding grid points
- $n(u,v,w)$  can be used to alter  $f(u,v,w)$  in the procedural texture function
  - The  $(u,v,w)$  spaces in each may need mapping between, e.g. scaling
- Each time an object is rendered,  $(x,y,z)$  will generate the same  $(u,v,w)$  and thus the same  $n(u,v,w)$
- Thus for  $n(x,y,z)$ :
  - $\text{map}(x,y,z)$  to  $(u,v,w)$
  - $\text{return } n(u,v,w)$

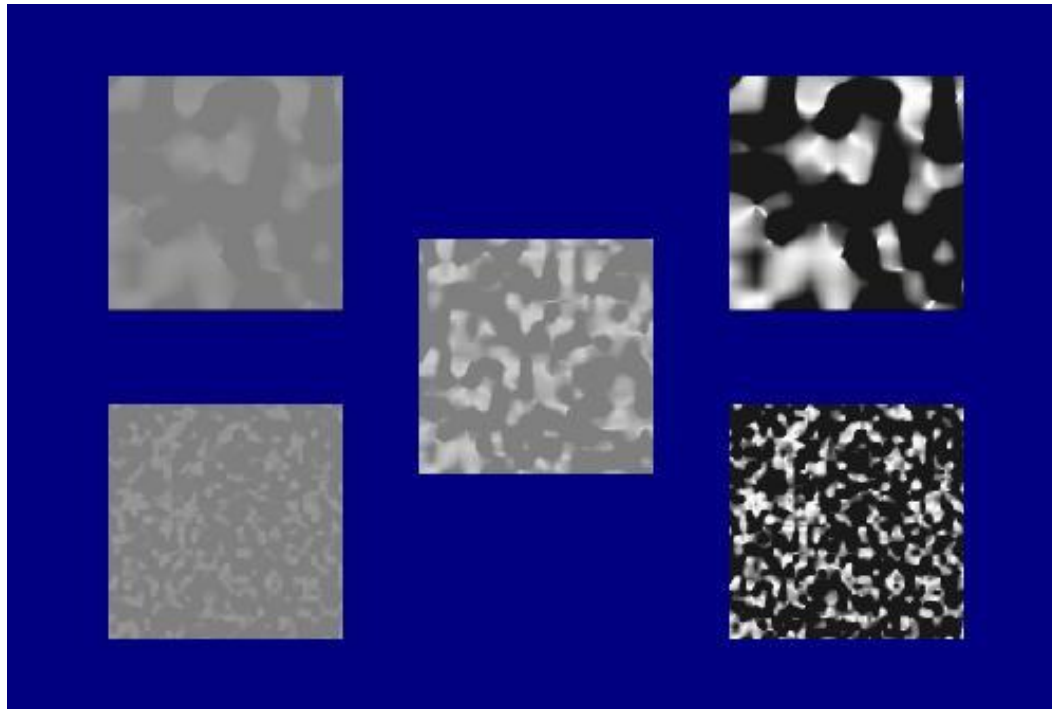


## 2.2 Adding noise

- For more control,  $\text{noise}(x,y,z)$  can be rewritten as

$$\text{noise}(f*x, f*y, f*z) * a$$

where  $f$  controls the frequency and  $a$  controls the amplitude

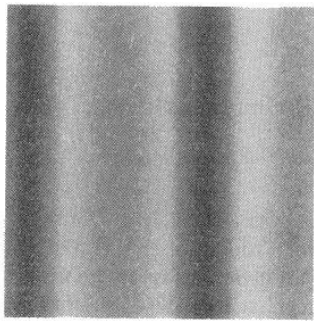


2D slice of a noise  
grid, The  
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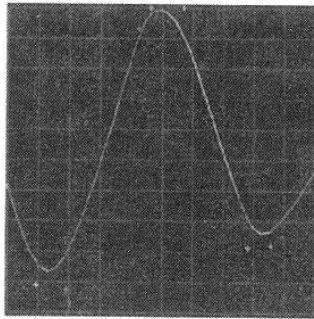


## 2.3 Example: marble

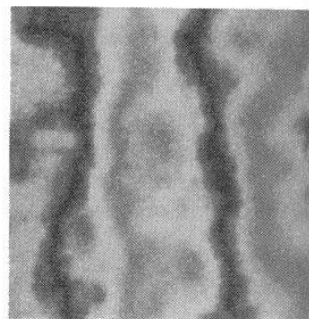
- A colour spline (b) is mapped to shades of grey (a)
- When turbulence is added, we get (c). In 3D, we get (d)
- $\text{marble}(x) = \text{marble\_colour}(\sin(x + \text{turbulence}(x)))$ ;



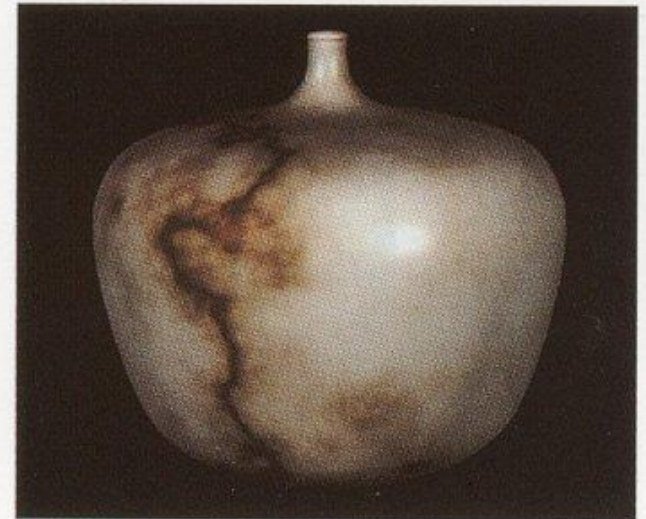
(a)



(b)



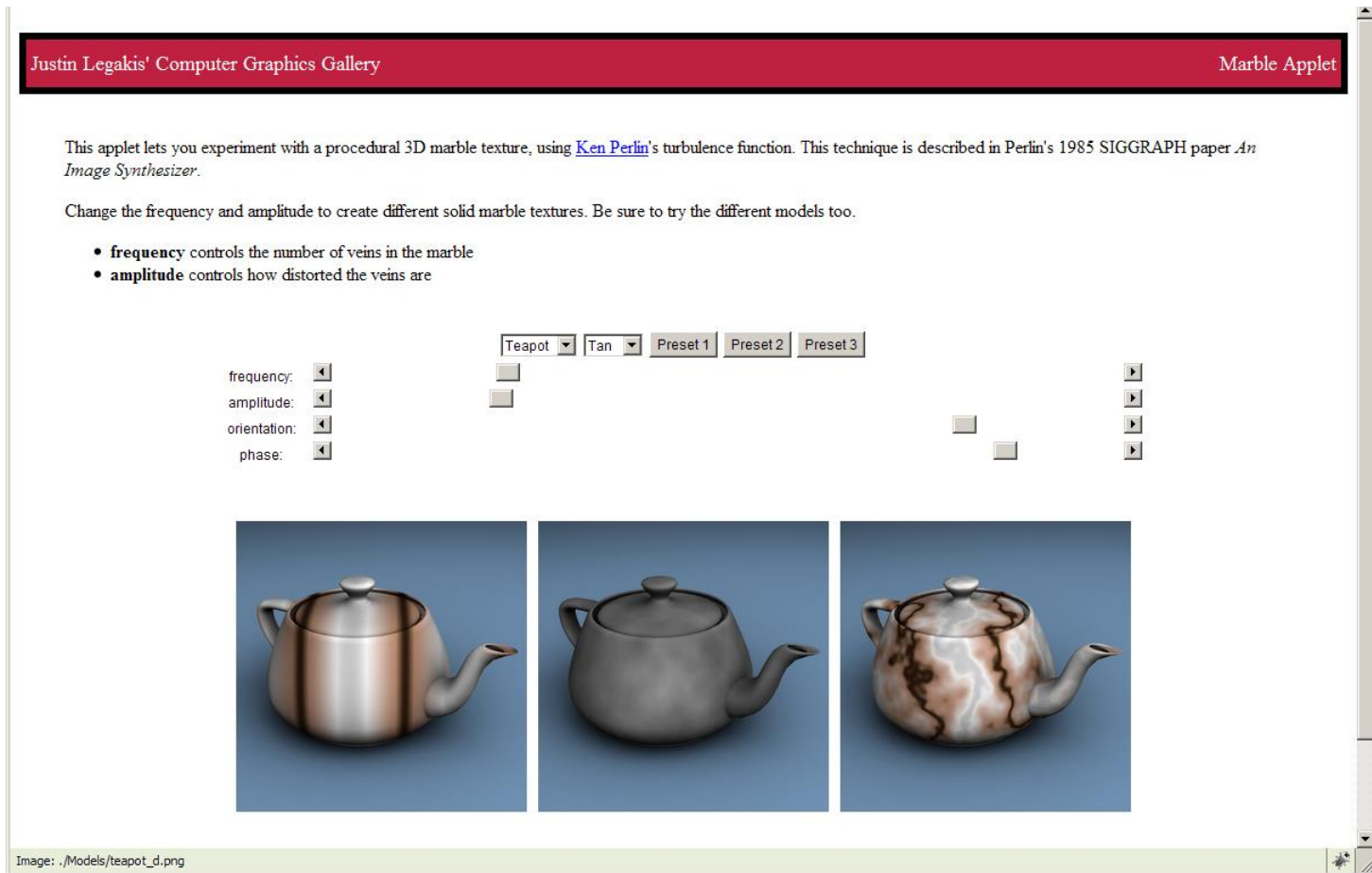
(c)



(d) **Figure 8.21** Imitating marble – the classic example of three-dimensional procedural texture.

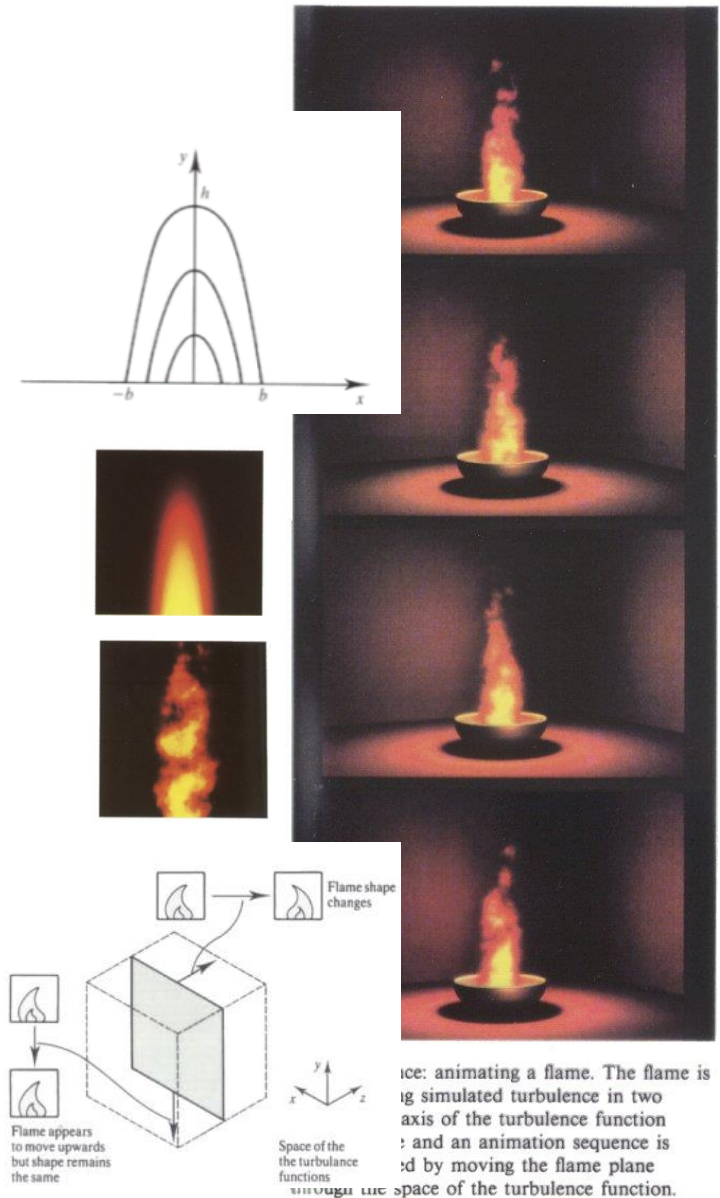


<http://legakis.net/justin/MarbleApplet/>

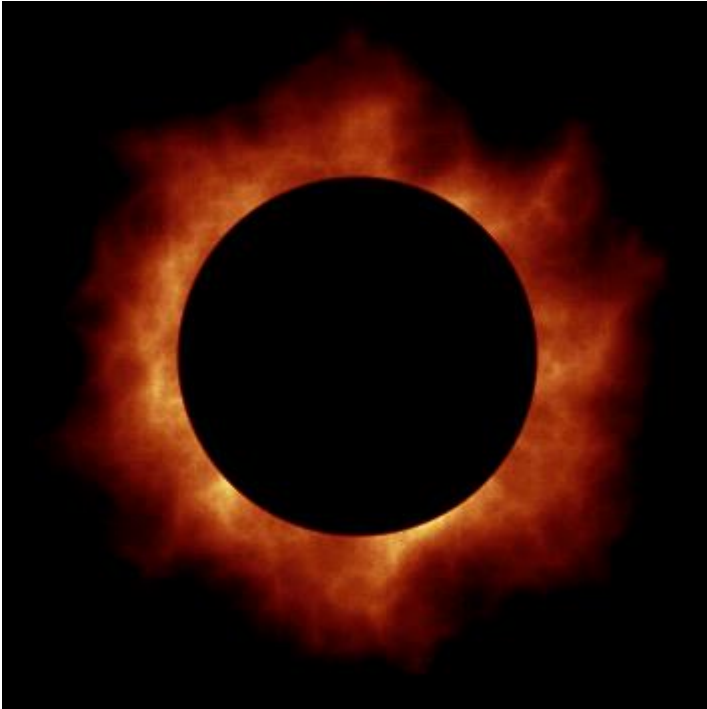


## 2.4 Noise and time

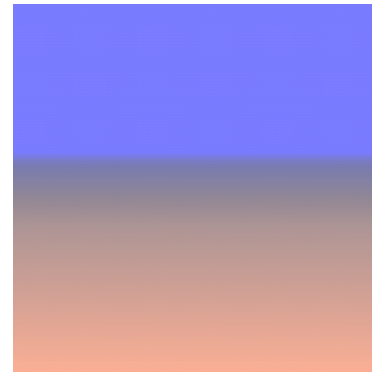
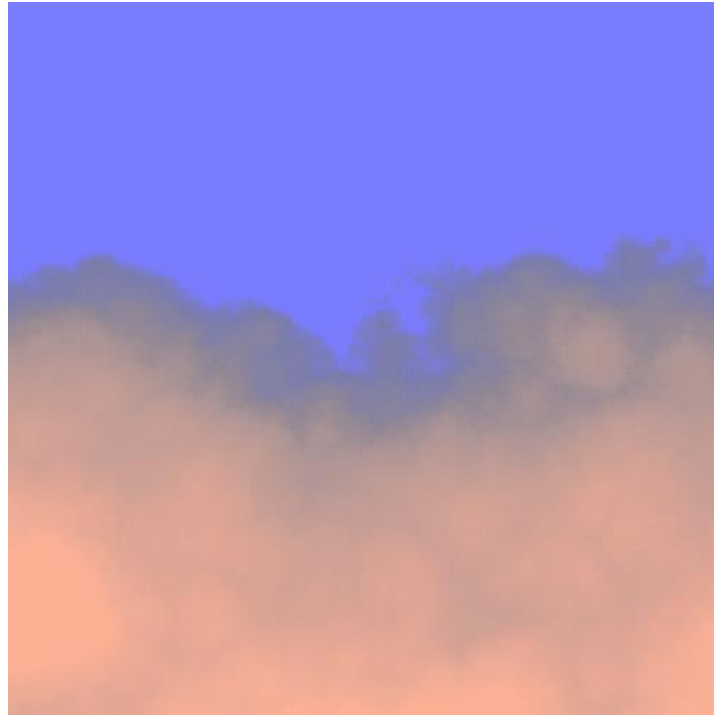
- A noise function (i.e. a noise grid) can also be used in conjunction with one or more 2D texture maps
- Example: Texture map of flame
  - or procedural model of flame's colours
- Use the noise function to add turbulence to the texture
  - $u, v$  noise plane alters the texture
  - $w$  axis acts as time
  - vary  $w$  over time will change the noise profile over time
- (Alternative: play animation of real flame on a billboard polygon)



## 2.4 Noise and time



Ken Perlin



## 2.5 3D texture mapping versus 2D texture mapping

- 2D texture mapping
  - A 2D texture map can be compressed or stretched depending on the mapping, especially if the object is deforming
  - 2D texture mapping is awkward for non-trivial topologies
  - Advantage: easy to produce lots of 2D textures, e.g. photographs
- 3D texture mapping
  - Based on a function  $f(x,y,z)$ , so can be generated to any level of detail for any topology
  - Extra work required if object is deforming
  - Can be difficult to design complex colour patterns – lots of trial and error

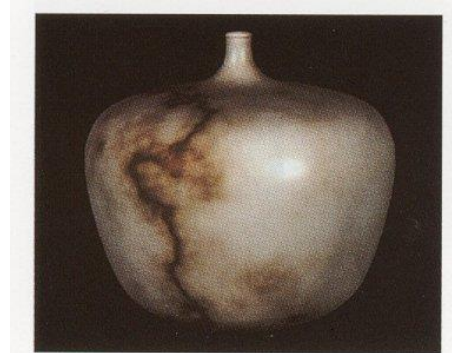
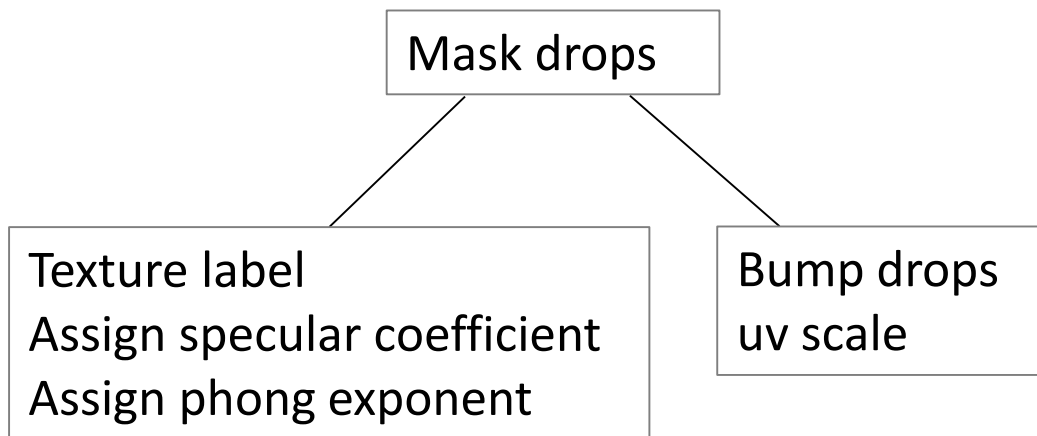


Figure 8.21 Imitating marble – the classic example of three-dimensional procedural texture.

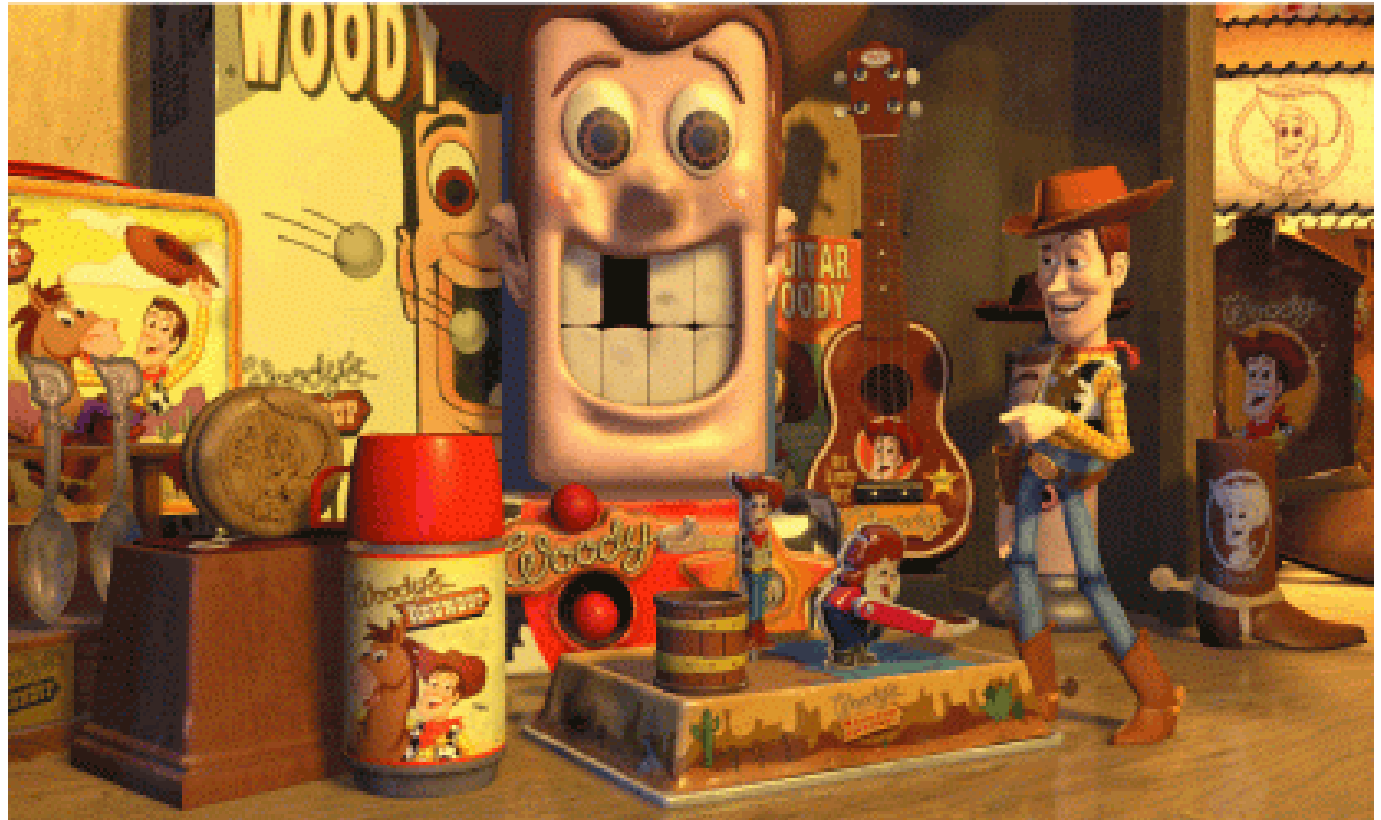
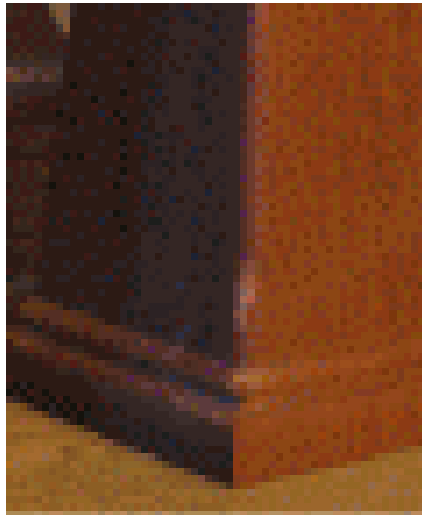
Watt, 00

### 3. Combining texture maps

- Texture maps can be combined to produce more complex effects
- Based on the idea of shade trees
  - (Cook, 84), shading language, RenderMan (Pixar)



## 4. Textures for 'dirt'



If you look closely, you can see yellowed printed material, little scratches, and paint worn off metal surfaces that tell you this collection is old but well-maintained.

Toy Story 2, Pixar, 99



## 5. Summary

- Most common *texture mapping* approach is to apply 2D texture maps to polygon mesh objects – texture colour mapping
- *Other approaches*:
  - environment mapping
  - bump mapping
  - normal mapping
  - displacement mapping
  - 3D texture mapping
- *Texture trees (based on shade trees)*: Organise combination of texturing effects

