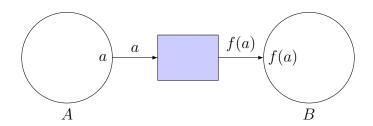
Functions: Graphing in the Cartesian Plane

Video companion

1 Introduction

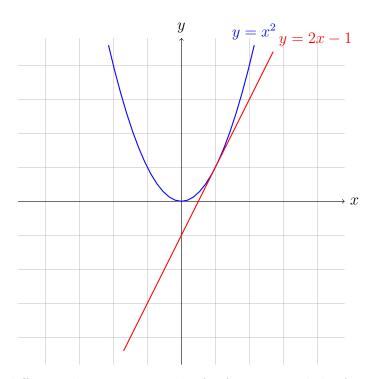
Last time: abstract depiction of a function as a machine

$$f:A\to B$$



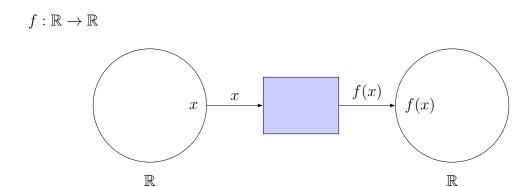
This video: graphs of functions

$$f: \mathbb{R} \to \mathbb{R}$$



You will learn the difference between a graph of a function and the function itself.

2 Map real line to real line



A function is a formula, a rule for how to operate the machine.

$$f(x) = 2x - 1$$

$$f(1) = 2(1) - 1 = 1$$

$$f(0) = 2(0) - 1 = -1$$

$$f(5.1) = 2(5.1) - 1 = 9.2$$

More complicated formulas, like absolute value:

$$g(x) = |x|$$

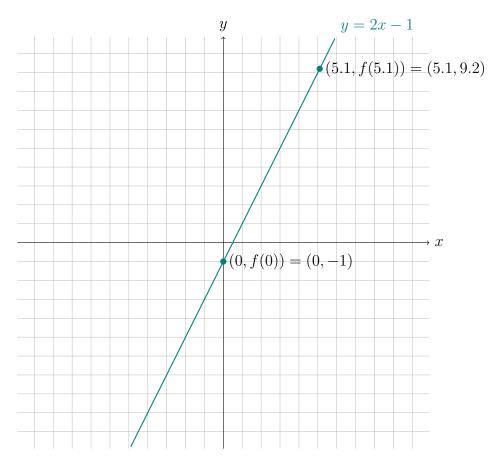
$$= \begin{cases} x & x \ge 0 \\ -x & x < 0 \end{cases}$$

Both f and g are functions, with a formula for how to compute the result.

2

3 What is a graph?

Graph of the function $f: \mathbb{R} \to \mathbb{R}$



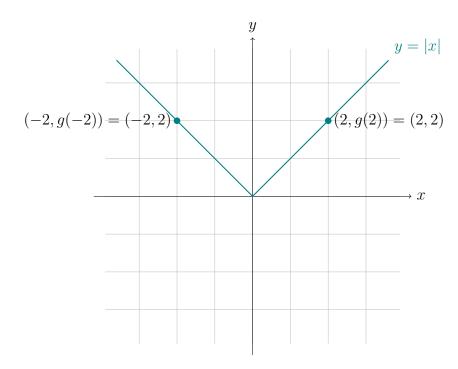
If g is a function : $\mathbb{R} \to \mathbb{R}$, the graph of $g = \{(x, y) \in \mathbb{R}^2 : y = g(x)\}$

4 Examples

Absolute value function

$$g(x) = |x|$$

$$= \begin{cases} x & x \ge 0 \\ -x & x < 0 \end{cases}$$

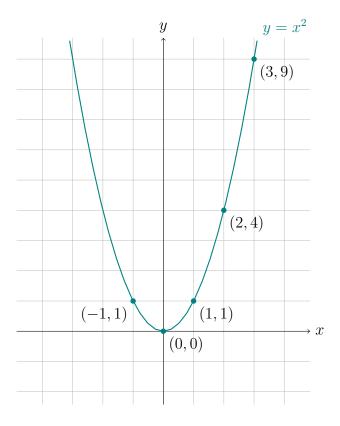


Quadratic function

$$h(x) = x^2$$

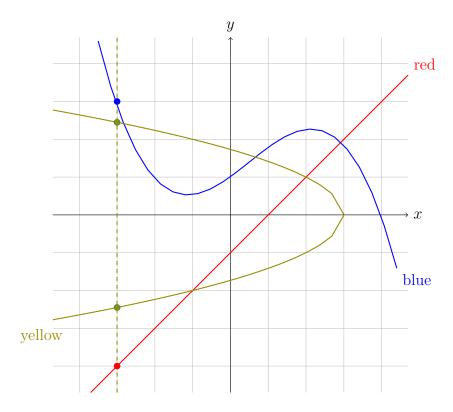
Graph a function by testing input and output pairs, see a pattern, and try to draw a curve through it. This is similar to *querying* in supervised learning.

Table of values:



 $h(x) = x^2$ is a quadratic function.

5 Vertical line test



Red and blue could be graphs of functions. Yellow could not be the graph of a function because it violates the *vertical line test*, which states that *any vertical line intersects the graph of a function once*.