
MODULE *crackers7*

EXTENDS *Naturals, FiniteSets*
 CONSTANTS *Things, People*
 VARIABLES *desires, holds*

$Init \triangleq \wedge desires = [p \in People \mapsto \{\}]$
 $\wedge holds = [p \in People \mapsto \{\}]$

RECURSIVE $_SetOrdinals(-, -)$
 $_SetOrdinals(s, f) \triangleq$ IF $s = \{\}$
 THEN f
 ELSE LET $e \triangleq$ CHOOSE $x \in s : \text{TRUE}$
 IN $_SetOrdinals(s \setminus \{e\}, [f \text{ EXCEPT } ![e] = \text{Cardinality}(s)])$

$SetOrdinals(S) \triangleq _SetOrdinals(S, [x \in S \mapsto 0])$

$ResourceOrdinals \triangleq SetOrdinals(Things)$
 $ChooseBefore(a, b) \triangleq ResourceOrdinals[a] < ResourceOrdinals[b]$

$Held(t) \triangleq \exists p \in People : t \in holds[p]$

$Desire(p) \triangleq \wedge holds[p] \neq \{\} \Rightarrow desires[p] \neq \{\}$
 $\wedge \exists t \in Things :$
 $\wedge t \notin desires[p]$
 $\wedge desires' = [desires \text{ EXCEPT } ![p] = desires[p] \cup \{t\}]$
 $\wedge \text{UNCHANGED } holds$

$Acquire(p) \triangleq \exists t \in desires[p] :$
 $\wedge \neg Held(t)$
 $\wedge \neg \exists t2 \in desires[p] : t2 \notin holds[p] \wedge ChooseBefore(t2, t)$
 $\wedge holds' = [holds \text{ EXCEPT } ![p] = holds[p] \cup \{t\}]$
 $\wedge \text{UNCHANGED } desires$

$Satiated(p) \triangleq \wedge desires[p] \neq \{\}$
 $\wedge \forall t \in desires[p] : t \in holds[p]$
 $\wedge desires' = [desires \text{ EXCEPT } ![p] = \{\}]$
 $\wedge \text{UNCHANGED } holds$

$TidyUp(p) \triangleq \wedge desires[p] = \{\}$
 $\wedge \exists t \in holds[p] :$
 $\wedge holds' = [holds \text{ EXCEPT } ![p] = holds[p] \setminus \{t\}]$
 $\wedge \text{UNCHANGED } desires$

$Relinquish(p) \triangleq \exists t \in desires[p] :$
 $\wedge t \notin holds[p]$
 $\wedge \exists t2 \in holds[p] :$
 $\wedge ChooseBefore(t, t2)$
 $\wedge holds' = [holds \text{ EXCEPT } ![p] = holds[p] \setminus \{t2\}]$

\wedge UNCHANGED *desires*

$$\begin{aligned} \text{Next} \triangleq & \exists p \in \text{People} : \\ & \vee \text{Desire}(p) \\ & \vee \text{Acquire}(p) \\ & \vee \text{Satiated}(p) \\ & \vee \text{TidyUp}(p) \\ & \vee \text{Relinquish}(p) \end{aligned}$$

$$\begin{aligned} \text{TidiesUp} \triangleq & \neg \exists p \in \text{People} : \\ & \wedge \text{desires}[p] \neq \{\} \\ & \wedge \exists l \in \text{holds}[p] : l \notin \text{desires}[p] \end{aligned}$$

$$\text{Exclusivity} \triangleq \neg \exists p, q \in \text{People} : p \neq q \wedge (\text{holds}[p] \cap \text{holds}[q]) \neq \{\}$$

$$\begin{aligned} \text{Ordering} \triangleq & \wedge \forall x, y, z \in \text{Things} : \\ & \text{ChooseBefore}(x, y) \wedge \text{ChooseBefore}(y, z) \Rightarrow \text{ChooseBefore}(x, z) \\ & \wedge \forall x \in \text{Things} : \neg \text{ChooseBefore}(x, x) \end{aligned}$$

$$\text{Spec} \triangleq \text{Init} \wedge \Box[\text{Next}]_{\langle \text{desires}, \text{holds} \rangle}$$
