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MODULE *crackers7a*

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EXTENDS *Naturals, FiniteSets*  
 CONSTANTS *Things, People*  
 VARIABLES *desires, holds*

$Init \triangleq \wedge desires = [p \in People \mapsto \{\}]$   
 $\wedge holds = [p \in People \mapsto \{\}]$

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RECURSIVE  $\_SetOrdinals(-, -)$   
 $\_SetOrdinals(s, f) \triangleq$  IF  $s = \{\}$   
     THEN  $f$   
     ELSE LET  $e \triangleq$  CHOOSE  $x \in s : \text{TRUE}$   
     IN  $\_SetOrdinals(s \setminus \{e\}, [f \text{ EXCEPT } ![e] = \text{Cardinality}(s)])$

$SetOrdinals(S) \triangleq \_SetOrdinals(S, [x \in S \mapsto 0])$

$ResourceOrdinals \triangleq SetOrdinals(Things)$   
 $ChooseBefore(a, b) \triangleq ResourceOrdinals[a] < ResourceOrdinals[b]$

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$Held(t) \triangleq \exists p \in People : t \in holds[p]$

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$Desire(p) \triangleq \wedge holds[p] \neq \{\} \Rightarrow desires[p] \neq \{\}$   
 $\wedge \exists t \in Things :$   
 $\wedge t \notin desires[p]$   
 $\wedge desires' = [desires \text{ EXCEPT } ![p] = desires[p] \cup \{t\}]$   
 $\wedge \text{UNCHANGED } holds$

$Acquire(p) \triangleq \exists t \in desires[p] :$   
 $\wedge \neg Held(t)$   
 $\wedge \neg \exists t2 \in desires[p] : t2 \notin holds[p] \wedge ChooseBefore(t2, t)$   
 $\wedge holds' = [holds \text{ EXCEPT } ![p] = holds[p] \cup \{t\}]$   
 $\wedge \text{UNCHANGED } desires$

$Satiated(p) \triangleq \wedge desires[p] \neq \{\}$   
 $\wedge \forall t \in desires[p] : t \in holds[p]$   
 $\wedge desires' = [desires \text{ EXCEPT } ![p] = \{\}]$   
 $\wedge \text{UNCHANGED } holds$

$TidyUp(p) \triangleq \wedge desires[p] = \{\}$   
 $\wedge \exists t \in holds[p] :$   
 $\wedge holds' = [holds \text{ EXCEPT } ![p] = holds[p] \setminus \{t\}]$   
 $\wedge \text{UNCHANGED } desires$

$Relinquish(p) \triangleq \exists t \in desires[p] :$   
 $\wedge t \notin holds[p]$   
 $\wedge \exists t2 \in holds[p] :$   
 $\wedge ChooseBefore(t, t2)$   
 $\wedge holds' = [holds \text{ EXCEPT } ![p] = holds[p] \setminus \{t2\}]$

$\wedge$  UNCHANGED *desires*

$$\begin{aligned} Next \triangleq & \exists p \in People : \\ & \vee Desire(p) \\ & \vee Acquire(p) \\ & \vee Satiated(p) \\ & \vee TidyUp(p) \\ & \vee Relinquish(p) \end{aligned}$$

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$$\begin{aligned} TidiesUp \triangleq & \neg \exists p \in People : \\ & \wedge desires[p] \neq \{\} \\ & \wedge \exists l \in holds[p] : l \notin desires[p] \end{aligned}$$

$$Exclusivity \triangleq \neg \exists p, q \in People : p \neq q \wedge (holds[p] \cap holds[q]) \neq \{\}$$

$$\begin{aligned} Ordering \triangleq & \wedge \forall x, y, z \in Things : \\ & ChooseBefore(x, y) \wedge ChooseBefore(y, z) \Rightarrow ChooseBefore(x, z) \\ & \wedge \forall x \in Things : \neg ChooseBefore(x, x) \end{aligned}$$


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$$Spec \triangleq Init \wedge \Box [Next]_{\langle desires, holds \rangle}$$


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