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B.Tech. / M.Tech. (Integrated) DEGREE EXAMINATION, DECEMBER 2023

21MAB101T – CALCULUS AND LINEAR ALGEBRA

(For the candidates admitted from the academic year 2023 - 2024)

Note:

- (i) **Part - A** should be answered in OMR sheet within first 40 minutes and OMR sheet should be handed over to hall invigilator at the end of 40th minute.

(ii) **Part – B** and **Part - C** should be answered in answer booklet.

Time: 3 Hours

Max. Marks: 75

PART – A (20 × 1 = 20Marks)

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Answer ALL Questions

1 1 1

1. If 1 and 3 are eigen values of $A = \begin{bmatrix} 1 & 0 & -1 \\ 1 & 2 & 1 \\ 2 & 2 & 3 \end{bmatrix}$, then the eigen values of A^3 are

- (A) 1, 2, 3 (B) 1, 4, 9
(C) 1, 8, 27 (D) 1, 8, 9

1 2 1

2. The characteristic equation of $A = \begin{bmatrix} 4 & 5 & 1 \\ 2 & 1 & -2 \\ 1 & 2 & 1 \end{bmatrix}$ is

- (A) $\lambda^3 - 6\lambda^2 + 6\lambda - 11 = 0$ (B) $\lambda^3 + 6\lambda^2 + 6\lambda + 11 = 0$
 (C) $\lambda^3 - 6\lambda^2 + 6\lambda + 6 = 0$ (D) $\lambda^3 - 5\lambda^2 + 6\lambda - 10 = 0$

1 3 1

3. The quadratic form of $A = \begin{bmatrix} 0 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$ is

- (A) $3x_1^2 + 3x_2^2 + 3x_3^2 - 2x_1x_2 + 2x_2x_3 - x_1x_3$
(B) $6x_1^2 + 3x_2^2 + 3x_3^2 - 4x_1x_2 - 2x_2x_3 + 4x_1x_3$
(C) $6x_1^2 + 3x_2^2 + 3x_3^2 + 2x_1x_2 + 2x_2x_3 + x_1x_3$
(D) $3x_1^2 + 3x_2^2 + 3x_3^2 + 4x_1x_2 + 2x_2x_3 + 4x_1x_3$

1 3 1

4. If 6 is one of the eigen values of $A = \begin{pmatrix} 3 & -1 & 1 \\ -1 & 5 & -1 \\ 1 & -1 & 3 \end{pmatrix}$, then other eigen values

are

1 2 2

5. If $u = x^3 + y^3 + z^3 - 3xyz$, then $\frac{\partial^2 u}{\partial x^2}$ is

- (A) $3x^2 - 3yz$ (B) $6x$
 (C) $6x - 3yz$ (D) $3x^2 + 3y^2 + 3z^2 - 3yz$

8 3 4

- b. Find the envelope of the family of straight line $\frac{x}{a} + \frac{y}{b} = 1$ where a and b are connected by the relation $ab=c^2$ where c is a constant.

25. a. Test the convergence of the series $\frac{1}{1.2.3} + \frac{3}{2.3.4} + \frac{5}{3.4.5} + \dots \infty$.

8 3 5

(OR)

- b. Discuss the convergence of the series $1 + \frac{2!}{2^2} + \frac{3!}{3^3} + \frac{4!}{4^4} + \dots \infty$.

8 3 5

PART - C (1 × 15 = 15 Marks)

Answer ANY ONE Questions

Marks BL CO

26. Reduce the quadratic form $3x_1^2 + 2x_2^2 + 3x_3^2 - 2x_1x_2 - 2x_2x_3$ to canonical form and find the rank, index signature and nature of the quadratic form.

15 3 1

27. Find the extreme values of $f(x, y) = x^3y^2(1-x-y)$.

15 4 2

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