SGD Algorithm to predict movie ratings

There will be some functions that start with the word "grader" ex: grader_matrix(), grader_mean(), grader_dim() etc, you should not change those function definition.

Every Grader function has to return True.

- 1. Download the data from here
- 2. The data will be of this format, each data point is represented as a triplet of user_id, movie_id and rating

user_id	movie_id	rating
77	236	3
471	208	5
641	401	4
31	298	4
58	504	5
235	727	5

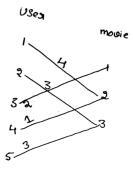
Task 1

Predict the rating for a given (user_id, movie_id) pair

Predicted rating \hat{y}_{ij} for user i, movied j pair is calcuated as $\hat{y}_{ij} = \mu + b_i + c_j + u_i^T v_j$, here we will be finding the best values of b_i and c_j using SGD algorithm with the optimization problem for N users and M movies is defined as

$$L = \min_{b,c,\{u_i\}_{i=1}^N,\{v_j\}_{j=1}^M} \quad \alpha(\sum_j \sum_k v_{jk}^2 + \sum_i \sum_k u_{ik}^2 + \sum_i b_i^2 + \sum_j c_i^2) + \sum_{i,j \in I^{train}} (y_{ij} - \mu - b_i - c_j - u_i^T v_j)^2$$

- μ : scalar mean rating
- b_i : scalar bias term for user i
- c_i: scalar bias term for movie j
- u_i: K-dimensional vector for user i
- v_i : K-dimensional vector for movie j
- *. We will be giving you some functions, please write code in that functions only.
- *. After every function, we will be giving you expected output, please make sure that you get that output.
 - 1. Construct adjacency matrix with the given data, assuming its weighted un-directed bi-partited graph and the weight of each edge is the rating given by user to the movie



you can construct this matrix like $A[i][j] = r_{ij}$ here i is user_id, j is movieid and \$r{ij}\$ is rating given by user ito the moviej\$

Hint: you can create adjacency matrix using csr_matrix

1. We will Apply SVD decomposition on the Adjaceny matrix link1, link2 and get three matrices U, \sum, V such that $U \times \sum \times V^T = A$, if A is of dimensions $N \times M$ then

U is of $N \times k$,

 \sum is of $k\times k$ and

V is $M \times k$ dimensions.

- *. So the matrix U can be represented as matrix representation of users, where each row u_i represents a k-dimensional vector for a user
- *. So the matrix V can be represented as matrix representation of movies, where each row v_j represents a k-dimensional vector for a movie.
- 2. Compute μ , μ represents the mean of all the rating given in the dataset.(write your code in def m_u())

- 3. For each unique user initilize a bias value B_i to zero, so if we have N users B will be a N dimensional vector, the i^{th} value of the B will corresponds to the bias term for i^{th} user (write your code in def initialize())
- 4. For each unique movie initilize a bias value C_j zero, so if we have M movies C will be a M dimensional vector, the j^{th} value of the C will corresponds to the bias term for j^{th} movie (write your code in def initialize())
- 5. Compute dL/db_i (Write you code in def derivative_db())
- 6. Compute dL/dc_j(write your code in def derivative_dc()
- 7. Print the mean squared error with predicted ratings.

```
for each epoch:
    for each pair of (user, movie):
        b_i = b_i - learning_rate * dL/db_i
        c_j = c_j - learning_rate * dL/dc_j
predict the ratings with formula
```

```
\hat{y}_{ii} = \mu + b_i + c_j + dot\_product(u_i, v_j)
```

1. you can choose any learning rate and regularization term in the range 10^{-3} to 10^2

2. **bonus**: instead of using SVD decomposition you can learn the vectors \mathbf{u}_i , \mathbf{v}_j with the help of SGD algo similar to \mathbf{b}_i and \mathbf{c}_j

Task 2

As we know U is the learned matrix of user vectors, with its i-th row as the vector ui for user i. Each row of U can be seen as a "feature vector" for a particular user.

The question we'd like to investigate is this: do our computed per-user features that are optimized for predicting movie ratings contain anything to do with gender?

The provided data file user_info.csv contains an is_male column indicating which users in the dataset are male. Can you predict this signal given the features U?

Note 1: there is no train test split in the data, the goal of this assignment is to give an intution about how to do matrix factorization with the help of SGD and application of truncated SVD. for better understanding of the collaborative fillerting please check netflix case study.

Note 2: Check if scaling of U, V matrices improve the metric

Reading the csv file

```
import pandas as pd
import numpy as np

data=pd.read_csv('ratings_train.csv')
data.head()
```

Out[104		user_id	item_id	rating
	0	772	36	3
	1	471	228	5
	2	641	401	4
	3	312	98	4
	4	58	504	5

Create your adjacency matrix

Grader function - 1

```
In [107...
          def grader matrix(matrix):
             assert(matrix.shape==(943,1681))
             return True
           grader matrix(adjacency matrix)
Out[107... True
         SVD decompostion
         Sample code for SVD decompostion
In [108...
           from sklearn.utils.extmath import randomized_svd
           import numpy as np
           matrix = np.random.random((20, 10))
           U, Sigma, VT = randomized svd(matrix, n components=5, n iter=5, random state=None)
           print(U.shape)
           print(Sigma.shape)
           print(VT.T.shape)
          (20, 5)
          (5,)
          (10, 5)
         Write your code for SVD decompostion
In [109...
          U, Sigma, VT = randomized svd(adjacency matrix, n components=5, n iter=5, random state=None)
           print(U.shape)
           print(Sigma.shape)
           print(VT.T.shape)
          (943, 5)
          (5,)
          (1681, 5)
         Compute mean of ratings
In [110...
           def m u(ratings):
               '''In this function, we will compute mean for all the ratings'''
               # you can use mean() function to do this
               # check this (https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.mean.html) link for more de
```

```
return ratings.mean()
In [111...
           mu=m_u(data['rating'])
            print(mu)
           3.529480398257623
          Grader function -2
In [112...
           def grader mean(mu):
              assert(np.round(mu,3)==3.529)
              return True
            mu=m u(data['rating'])
            grader_mean(mu)
Out[112... True
         Initialize B<sub>i</sub> and C<sub>i</sub>
          Hint: Number of rows of adjacent matrix corresponds to user dimensions (B_i), number of columns of adjacent matrix corresponds to movie
          dimensions (C<sub>i</sub>)
In [113...
           def initialize(dim):
                '''In this function, we will initialize bias value 'B' and 'C'.'''
                # initalize the value to zeros
                # return output as a list of zeros
                return np.zeros(dim)
In [114...
            dim= adjacency_matrix.shape[0]
            b i=initialize(dim)
In [115...
            dim= adjacency matrix.shape[1]
            c j=initialize(dim)
          Grader function -3
In [116...
```

```
def grader_dim(b_i,c_j):
    assert(len(b_i)==943 and np.sum(b_i)==0)
    assert(len(c_j)==1681 and np.sum(c_j)==0)
    return True
grader_dim(b_i,c_j)
```

Out[116... True

Compute dL/db_i

$$L = \min_{b,c,\{u_i\}_{i=1}^N,\{v_j\}_{j=1}^M} \quad \alpha(\sum_j \sum_k v_{jk}^2 + \sum_i \sum_k u_{ik}^2 + \sum_i b_i^2 + \sum_j c_i^2) + \sum_{i,j \in I^{train}} (y_{ij} - \mu - b_i - c_j - u_i^T v_j)^2$$

- μ : scalar mean rating
- b_i: scalar bias term for user i
- c_i: scalar bias term for movie j
- u_i: K-dimensional vector for user i
- v_i: K-dimensional vector for movie j

```
def derivative_db(user_id, item_id, rating,U,V,mu,alpha):
    '''In this function, we will compute dL/db_i'''
    first_term = 2*b_i[user_id]*alpha
    second_term = 2*(rating - mu - b_i[user_id] - c_j[item_id] - np.dot(U[user_id], V.T[item_id]))
    derivative = first_term - second_term
    return np.amin(derivative)
```

Grader function -4

```
def grader_db(value):
    assert(np.round(value, 3)==-0.931)
    return True
U1, Sigma, V1 = randomized_svd(adjacency_matrix, n_components=2,n_iter=5, random_state=24)
# Please don't change random state
# Here we are considering n_componets = 2 for our convinence
```

```
alpha=0.01
value=derivative_db(312,98,4,U1,V1,mu,alpha)
grader_db(value)

Out[118... True
```

```
Compute dL/dc_j
```

```
def derivative_dc(user_id,item_id,rating,U,V,mu,alpha):
    '''In this function, we will compute dL/dc_j'''
    first_term = 2*alpha*c_j[item_id]
    second_term = 2*(rating - mu - b_i[user_id] - c_j[item_id] - np.dot(U[user_id], V.T[item_id]))
    derivative = first_term - second_term
    return np.amin(derivative)
```

Grader function - 5

```
def grader_dc(value):
    assert(np.round(value,3)==-2.929)
    return True
U1, Sigma, V1 = randomized_svd(adjacency_matrix, n_components=2,n_iter=5, random_state=24)
# Please don't change random state
# Here we are considering n_componets = 2 for our convinence
alpha=0.01
value=derivative_dc(58,504,5,U1,V1,mu, alpha)
grader_dc(value)
```

Out[120... True

Compute MSE (mean squared error) for predicted ratings

for each epoch, print the MSE value

```
for each epoch:
    for each pair of (user, movie):
        b i = b i - learning rate * dL/db i
```

c_j = c_j - learning_rate * dL/dc_j

```
predict the ratings with formula
        \hat{y}_{ii} = \mu + b_i + c_i + dot product(u_i, v_i)
In [121...
          from sklearn.metrics import mean squared error
          from tadm import tadm
          epoch = 15
          learning rate = 0.001
          alpha = 0.001
          MSEs = []
          for i in range(epoch):
               predicted ratings = []
               for user, item, rating in tqdm(zip(data['user id'], data['item id'], data['rating'])):
                   b i[user] = b i[user] - learning rate * derivative db(user, item, rating, U1, V1, mu, alpha)
                   c j[item] = c j[item] - learning rate * derivative dc(user, item, rating, U1, V1, mu, alpha)
                   y pred = mu + b i[user] + c j[item] + np.dot(U1[user], V1.T[item])
                   predicted ratings.append(y pred)
               MSEs.append(mean squared error(data['rating'], predicted ratings))
         89992it [00:02, 33681.50it/s]
         89992it [00:02, 32871.70it/s]
         89992it [00:02, 35082.72it/s]
```

```
89992it [00:02, 33681.50it/s]
89992it [00:02, 32871.70it/s]
89992it [00:02, 35082.72it/s]
89992it [00:02, 32657.45it/s]
89992it [00:02, 33125.01it/s]
89992it [00:02, 33909.32it/s]
89992it [00:02, 36038.60it/s]
89992it [00:02, 36233.50it/s]
89992it [00:02, 34924.44it/s]
89992it [00:02, 34924.44it/s]
89992it [00:02, 36917.42it/s]
89992it [00:02, 36996.77it/s]
89992it [00:02, 37675.27it/s]
89992it [00:02, 37162.47it/s]
89992it [00:02, 37340.43it/s]
```

Plot epoch number vs MSE

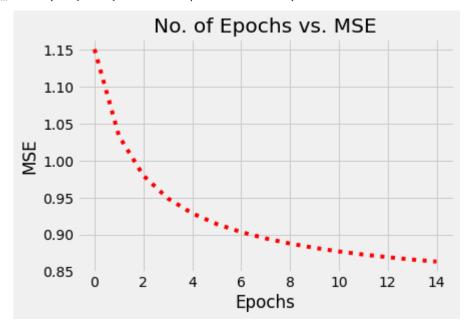
epoch number on X-axis

• MSE on Y-axis

```
import matplotlib.pyplot as plt
from matplotlib import style

plt.style.use('fivethirtyeight')
plt.plot(list(range(epoch)), MSEs, color='r', linestyle='dotted')
plt.xlabel('Epochs')
plt.ylabel('MSE')
plt.title('No. of Epochs vs. MSE')
```

Out[122... Text(0.5, 1.0, 'No. of Epochs vs. MSE')



Task 2

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Note 2: Check if scaling of U, V matrices improve the metric

```
In [123...
          data = pd.read csv('user info.txt')
In [124...
          from sklearn.preprocessing import Normalizer
          U normalized = Normalizer().fit(U1)
          U normalized = U normalized.transform(U1)
In [125...
          df = pd.DataFrame({'user_id' : data['user_id'].unique(),
                               'U1' : U normalized[:, 0],
                               'U2' : U normalized[:, 1],
                               'is male' : data['is male']})
In [126...
          X = df.drop(['is_male'], axis=1)
          y = df['is male']
In [127...
          from sklearn.linear model import LogisticRegression
          from sklearn.metrics import f1 score
          clf = LogisticRegression(random state=42).fit(X, y)
          y pred = clf.predict(X)
In [128...
          print('The F1 score for our model is : ', f1 score(data['is male'], y pred))
         The F1 score for our model is: 0.8307501549907006
```