Image Processing Lab

Sem 1

Lab 2: Basics of Signal Processing

16/08/2018

 $1.\mathrm{Try}$ to complete the lab questions during the lab time (in lab submission)

2.Please do not copy programs.

1. Basic Signal Operations

Let x[n] be a signal with x[n] = [1, 2, 5, 6, 3, 2, 1, 1, 1]Sketch the following signals:

(a)
$$x[n-4]$$

(b)
$$x[-n]$$

(c)
$$x[2-n]$$

(d)
$$2x[n]$$

(e)
$$x[3n]$$

(f)
$$x[n/3]$$

2. 1-D convolution

Perform the following 1-D convolutions between signals x[n] and h[n]:

(a)
$$x[n] = [1, 1, 1, 1, 1]$$
, $h[n] = [0, 0, 1, 1, 1, 1, 1, 1, 0]$

(b)
$$x[n] = (-0.5)^n u[n-4]$$
, $h[n] = 4^n[2-n]$

(c) Consider the evaluation of
$$y[n] = x_1[n] * x_2[n] * x_3[n]$$

where, $x_1[n] = (0.5)^n u[n]$, $x_2[n] = u[n-3]$, $x_3[n] = \delta[n] - \delta[n-1]$.

Hint: You have to define the range of n appropriately.

3. 2-D convolutions

Perform the following 2-D convolutions and comment on the kind of filtering obtained in the result.

(a)

$$X = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 6 & 7 & 8 \end{bmatrix}, H = \begin{bmatrix} 1 & -2 & -1 \\ 1 & 0 & -1 \\ 1 & 2 & -1 \end{bmatrix}$$

(b) Use the cameraman image as input and the kernel to be

$$H = \frac{1}{9} \left[\begin{array}{rrr} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{array} \right]$$

(c) Use the cameraman image as input and the kernel to be

$$H = \left[\begin{array}{rrr} 0 & -1 & 0 \\ -1 & 4 & -1 \\ 0 & -1 & 0 \end{array} \right]$$

4. Convolution as multiplication

Prove that convolution in spatial domain is multiplication in frequency domain by applying FFT.

- (a) Find the FFT of the cameraman image and display the magnitude spectrum
- (b) Find the FFT of the kernel in question 3(b)
- (c) Multiply the two FFTs and take Inverse FFT of the product
- (d) Compare it with your result in question 3(b)