

HW Linear Programming

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1. Solving the following linear program using simplex method

$$\max Z = 3x_1 + 6x_2 + 2x_3$$

$$\begin{cases} 3x_1 + 4x_2 + x_3 \leq 2 \\ x_1 + 3x_2 + 2x_3 \leq 1 \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0 \end{cases}$$

augmented
→
form

$$\max Z = 3x_1 + 6x_2 + 2x_3$$

$$3x_1 + 4x_2 + x_3 + s_1 = 2$$

$$x_1 + 3x_2 + 2x_3 + s_2 = 1$$

$$s_1, s_2, x_1, x_2, x_3 \geq 0$$

	x_1	x_2	x_3	s_1	s_2	β_i
2	(3)	4	1	1	0	$2/3$
1	1	3	2	0	1	1
0	3	6	2	0	0	

	b	x_1	x_2	x_3	s_1	s_2	β_i
	$2/3$	1	$4/3$	$1/3$	$1/3$	0	$2/4$
	$1/3$	0	($5/3$)	$5/3$	$-1/3$	1	$1/5$
$-Z$	-2	0	2	1	-1	0	

	b	x_1	x_2	x_3	s_1	s_2	β_i
	$2/5$	1	0	-1	$3/5$	$-4/5$	
	$1/5$	0	1	1	$-1/5$	$3/5$	
$-Z$	$-12/5$	0	0	-1	$-3/5$	$-6/5$	

$$Z = \frac{12}{5} \quad \left(\frac{2}{5}, \frac{1}{5}, 0 \right)$$