# Dissecting Different Flavors of Generic Programming in One Haskell Universe

**Presented to Galois** 

Sean Leather

Utrecht University

August 27, 2013

## What is Generic Programming?

In programming languages, the adjective "generic" is heavily overloaded.

- Java/C# generics
- C++ templates
- Ada generic packages

## What is Generic Programming?

The goal is often the same.

A higher level of abstraction than "normally" available

The technique is also often the same.

Some form of parameterization and instantiation

# **Examples of Generic Programming**

```
Java/C#:
public class Stack<T>
{
   public void push(T item) {...}
   public T pop() {...}
}
```

# **Examples of Generic Programming**

```
C++:
template < typename T, typename Compare >
T& min(T& a, T& b, Compare comp) {
  if (comp(b, a))
    return b;
  return a;
}
```

## Generic Programming in Haskell

#### In other words:

- ullet Java-style generics pprox parametric polymorphism
- ullet C++ templates pprox ad-hoc polymorphism

#### In Haskell:

- Both forms already exist.
- We don't call them generics because they're native to the language.

#### Datatype-generic programming:

- Abstract over the structure of a datatype
- Also known as "polytypism" and "shape-/structure-polymorphism"

## **Datatypes**

$$\mathbf{data} \ \mathsf{D} \ \mathsf{p} = \mathsf{Alt}_1 \ | \ \mathsf{Alt}_2 \ \mathsf{Int} \ \mathsf{p}$$

#### A datatype can have:

- Parameters: type variables (≥ 0)
- Alternatives: unique constructors (≥ 0)
- Fields: types for each constructor (≥ 0)

#### Non-syntactic features:

- Recursion
- Nesting

There are other features of datatypes, but we will consider only the above as a foundation for looking at the structure.

## Structure of Datatypes: Sums

First structural element: alternatives.

data 
$$AltEx_2 = A_1 Int \mid A_2 Char$$

Note that the above is similar to a standard type:

And we can, in fact, model  $AltEx_2$  as:

**type** AltEx
$$_2'$$
 = Either Int Char

with the following "smart" constructors:

$$a_1 :: Int \rightarrow AltEx_2'$$
  
 $a_1 = Left$ 

$$a_2 :: \mathsf{Char} \to \mathsf{AltEx}_2'$$

$$a_2 = Right$$

## Structure of Datatypes: Sums

When talking about alternatives in structural sense, we often call them sums. Either is the basic binary sum type. For conciseness, we use this (identical) binary sum type:

data 
$$a : +: b = L a \mid R b$$

What about a type with < 2 alternatives?

data 
$$AltEx_3 = B_1 Int \mid B_2 Char \mid B_3 Float$$

The simplest solution is to nest one binary sum inside another:

type 
$$AltEx_3' = Int :+: (Char :+: Float)$$

Note that:

$$b_3 :: \mathsf{Float} \to \mathsf{AltEx}_3'$$
  
 $b_3 = \mathsf{R} \circ \mathsf{R}$ 

# Structure of Datatypes: Products

Next: fields.

data  $FldEx_2 = FldEx_2$  Int Char

Again, note the similarity to a standard type, the pair:

$$data (,) a b = (,) a b$$

And again, we model  $FldEx_2$  similarly:

**type** 
$$FldEx_2' = (,)$$
 Int Char

with the smart constructor:

$$\mathsf{fldEx}_2' :: \mathsf{Int} \to \mathsf{Char} \to \mathsf{FldEx}_2'$$
$$\mathsf{fldEx}_2' = (,)$$

## Structure of Datatypes: Products

The pair type is the basic binary product type. For symmetry with sums, we will use the following type:

data 
$$a : \times : b = a : \times : b$$

And more than two fields...

data 
$$FldEx_3 = FldEx_3$$
 Int Char Float

... are modeled by nested binary products:

**type** 
$$FldEx'_3 = Int : x: (Char : x: Float)$$

with the smart constructor:

$$\begin{array}{l} \mathsf{fldEx}_3' :: \mathsf{Int} \to \mathsf{Char} \to \mathsf{Float} \to \mathsf{FldEx}_3' \\ \mathsf{fldEx}_3' \times \mathsf{y} \ \mathsf{z} = \mathsf{x} : \!\! \times \!\! : (\mathsf{y} : \!\! \times \!\! : \mathsf{z}) \end{array}$$

# Structure of Datatypes: Sums of Products

To "sum" it all up, recall the first datatype example:

data 
$$D p = Alt_1 | Alt_2 Int p$$

We can define an identical type using the sum and product types we have just discussed:

```
type Rep_D p = U :+: Int :\times: p
```

#### Notes:

- We use the "unit" type data U = U (identical to the standard type
   () to represent an alternative without fields.
- :+: is **infixr** 5, and :x: is **infixr** 6, so we can write Rep<sub>D</sub> naturally, without unnecessary parentheses.

# Structure of Datatypes: Isomorphism

So, we think we can model datatypes. But how do we know  $\operatorname{\mathsf{Rep}}_\mathsf{D}$  accurately models  $\mathsf{D}$  ?

We define an isomorphism: two total functions that convert between types.

```
\begin{array}{ll} \text{from}_D :: D \ p \rightarrow \text{Rep}_D \ p \\ \text{from}_D \ \text{Alt}_1 &= L \ U \\ \text{from}_D \ (\text{Alt}_2 \ i \ p) &= R \ (i : \times : p) \\ \text{to}_D :: \text{Rep}_D \ p \rightarrow D \ p \\ \text{to}_D & (L \ U) &= \text{Alt}_1 \\ \text{to}_D & (R \ (i : \times : p)) = \text{Alt}_2 \ i \ p \end{array}
```

This allows us to convert terms between (1) the familiar datatype and (2) the structure representation used for generic operations.

## Structure of Datatypes: Constructors

Oh, but there's one more thing...

You may have noticed the representation lacked any information about the constructors (e.g. the names).

That's easily repaired with another datatype:

```
data Ca = CStringa
```

We modify the representation to store constructor names:

```
 \begin{aligned} &\textbf{type} \; \mathsf{Rep}_{\mathsf{D}} \; \mathsf{p} = \mathsf{C} \; \mathsf{U} \; \text{:+:} \; \mathsf{C} \; (\mathsf{Int} \; \text{:} \times : \mathsf{p}) \\ &\mathsf{from}_{\mathsf{D}} \; \mathsf{Alt}_1 \qquad = \mathsf{L} \; (\mathsf{C} \; \text{"Alt1"} \; \mathsf{U}) \\ &\mathsf{from}_{\mathsf{D}} \; (\mathsf{Alt}_2 \; \mathsf{i} \; \mathsf{p}) = \mathsf{R} \; (\mathsf{C} \; \text{"Alt2"} \; (\mathsf{i} \; \text{:} \times : \mathsf{p})) \end{aligned}
```

We could also put additional metadata (e.g. fixity) into C.

## Generic Functions

Okay, so we have a structure representation. But what can we do with it?

#### Generic functions

- Defined on each possible case of the structure representation
- Work for every datatype that has an isomorphism with a structure representation

Example: show ::  $a \rightarrow String$ 

## Generic Functions: show

We define a show function for each possible structure case.

#### Unit:

$$\begin{array}{l} \mathsf{show}_U :: U \to \mathsf{String} \\ \mathsf{show}_U \ U = \texttt{""} \end{array}$$

#### Constructor name:

$$\begin{array}{l} \mathsf{show}_\mathsf{C} :: (\mathsf{a} \to \mathsf{String}) \to \mathsf{C} \; \mathsf{a} \to \mathsf{String} \\ \mathsf{show}_\mathsf{C} \; \mathsf{show}_\mathsf{a} \; (\mathsf{C} \; \mathsf{nm} \; \mathsf{a}) = \\ \text{"("} \# \; \mathsf{nm} \# \text{" "} \# \; \mathsf{show}_\mathsf{a} \; \mathsf{a} \# \text{")"} \end{array}$$

#### Binary product:

$$show_{\times} :: (a \rightarrow String) \rightarrow (b \rightarrow String) \rightarrow a : \times: b \rightarrow String \\ show_{\times} show_{a} show_{b} (a : \times: b) = show_{a} a # " " # show_{b} b$$

#### Binary sum:

$$\begin{array}{l} \mathsf{show}_+ :: (\mathsf{a} \to \mathsf{String}) \to (\mathsf{b} \to \mathsf{String}) \to \mathsf{a} : +: \mathsf{b} \to \mathsf{String} \\ \mathsf{show}_+ \ \mathsf{show}_\mathsf{a} \ \_ (\mathsf{L} \ \mathsf{a}) = \mathsf{show}_\mathsf{a} \ \mathsf{a} \\ \mathsf{show}_+ \ \_ \ \mathsf{show}_\mathsf{b} \ (\mathsf{R} \ \mathsf{b}) = \mathsf{show}_\mathsf{b} \ \mathsf{b} \end{array}$$

## Generic Functions: show

We can define a show function for  $Rep_D$  (assuming show<sub>Int</sub>):

```
\begin{split} &\mathsf{show}_{\mathsf{Rep}_D} :: (\mathsf{p} \to \mathsf{String}) \to \mathsf{Rep}_D \; \mathsf{p} \to \mathsf{String} \\ &\mathsf{show}_{\mathsf{Rep}_D} \; \mathsf{show}_{\mathsf{p}} = \\ &\mathsf{show}_+ \; \big( \mathsf{show}_C \; \mathsf{show}_U \big) \; \big( \mathsf{show}_C \; \big( \mathsf{show}_\times \; \mathsf{show}_{\mathsf{Int}} \; \mathsf{show}_{\mathsf{p}} \big) \big) \end{split}
```

The show function for D is just a hop away:

```
\begin{aligned} \mathsf{show}_D :: (\mathsf{p} \to \mathsf{String}) \to \mathsf{D} \; \mathsf{p} \to \mathsf{String} \\ \mathsf{show}_D \; \mathsf{show}_{\mathsf{p}} = \mathsf{show}_{\mathsf{Rep}_D} \; \mathsf{show}_{\mathsf{p}} \circ \mathsf{from}_D \end{aligned}
```

## Generic Functions: show

```
\begin{aligned} \mathsf{show}_{\mathsf{Rep}_D} &:: (\mathsf{p} \to \mathsf{String}) \to \mathsf{Rep}_D \; \mathsf{p} \to \mathsf{String} \\ \mathsf{show}_{\mathsf{Rep}_D} &\: \mathsf{show}_{\mathsf{p}} = \\ &\: \mathsf{show}_+ \; \big( \mathsf{show}_\mathsf{C} \; \mathsf{show}_\mathsf{U} \big) \; \big( \mathsf{show}_\mathsf{C} \; \big( \mathsf{show}_\times \; \mathsf{show}_\mathsf{Int} \; \mathsf{show}_\mathsf{p} \big) \big) \end{aligned}
```

#### Some observations:

- This is a sort of predictable pattern (or recipe) for defining show functions on structure representations.
- The functions are recursive but not in the usual way because the argument types differ.
- Each datatype can have a unique structure representation, and we want to support all combinations, generically.

## Generic Functions, Generically

In order to jump into "true" genericity (where the structure is a parameter instead of a pattern), we need several additional things:

 Polymorphic recursion – functions with a common scheme that reference each other and allow types to change in the calls

```
\begin{array}{lll} \mathsf{show}_{\mathsf{U}} :: & \mathsf{U} & \to \mathsf{String} \\ \mathsf{show}_{\mathsf{C}} :: ... \Rightarrow \mathsf{C} \ \mathsf{a} & \to \mathsf{String} \\ \mathsf{show}_{+} :: ... \Rightarrow \mathsf{a} : \!\!\! + \!\!\! : \mathsf{b} \to \mathsf{String} \\ & \dots \end{array}
```

A common encoding for isomorphisms

## Polymorphic Recursion

There are several ways to encode polymorphic recursion. We will use type classes.

- Standard classes already use polymorphic recursion for deriving instances: Show, Eq, etc.
- The class declaration specifies the type signature.
- Each recursive case is specified by an instance of the class.

A simplified definition of the Show class:

#### class Show a where

show ::  $a \rightarrow String$ 

## Polymorphic Recursion

The instances for each structure representation case:

Unit:

instance Show U where show = show<sub>U</sub>

Constructor name:

instance Show a  $\Rightarrow$  Show (C a) where show = show<sub>C</sub> show

Binary product:

**instance** (Show a, Show b) 
$$\Rightarrow$$
 Show (a :×: b) **where** show = show $_{\times}$  show show

Binary sum:

instance (Show a, Show b) 
$$\Rightarrow$$
 Show (a :+: b) where show = show<sub>+</sub> show show

## Polymorphic Recursion

```
Now, recall \mathsf{show}_{\mathsf{Rep}_D}: \mathsf{show}_{\mathsf{Rep}_D}: \mathsf{show}_{\mathsf{Rep}_D}:: (\mathsf{p} \to \mathsf{String}) \to \mathsf{Rep}_D \mathsf{p} \to \mathsf{String} \mathsf{show}_{\mathsf{Rep}_D} \mathsf{show}_{\mathsf{p}} \mathsf{show}_{\mathsf{p}}
```

Compare to the new version that is now possible:

```
\begin{array}{l} \mathsf{show}'_{\mathsf{Rep}_D} :: \mathsf{Show} \ \mathsf{p} \Rightarrow \mathsf{Rep}_D \ \mathsf{p} \to \mathsf{String} \\ \mathsf{show}'_{\mathsf{Rep}_D} = \mathsf{show} \end{array}
```

To define the show function for D , we still need to define another function:

```
\begin{aligned} \mathsf{show}_D' &:: \mathsf{Show} \ \mathsf{p} \Rightarrow \mathsf{D} \ \mathsf{p} \to \mathsf{String} \\ \mathsf{show}_D' &= \mathsf{show}_{\mathsf{Rep}_D}' \circ \mathsf{from}_D \end{aligned}
```

#### Next goal:

• Define one show function that knows how to convert any type T to its structure representation type  $Rep_T$ , given an isomorphism between T and  $Rep_T$ .

We define a class of function pairs.

- We again use a type class, but with the addition of a type family.
- Each function pair implements an isomorphism between a datatype  $\mathsf{T}$  and its structure representation  $\mathsf{Rep}_\mathsf{T}$ :

$$\mathsf{from} :: \mathsf{T} \to \mathsf{Rep}_\mathsf{T} \qquad \qquad \mathsf{to} :: \mathsf{Rep}_\mathsf{T} \to \mathsf{T}$$

- Each requires two types, so each instance must have two types (unlike the Show instances which needed only the structure representation type).
- Rep<sub>T</sub> is precisely determined by T, so really we only need one unique type and a second type derivable from the first.
- In this case, a (1) multiparameter type class with a functional dependency and a (2) type class with a type family are equally expressive. (It's a matter of taste, really.)

#### The type class:

#### class Generic a where

#### **type** Rep a

```
from :: a \rightarrow Rep a to :: Rep a \rightarrow a
```

- Rep is a type family or, more precisely, an associated type synonym.
- Think of Rep as a function on types. Given a unique type (index)
   T, you get a type (synonym) Rep T.
- Note that Rep T need not be different from Rep U even though T and U are different.
- Concretely: two datatypes may have the same representation.

We need Generic instances for every datatype that we want to use with generic functions.

The instance for D uses definitions that we've already seen:

```
\label{eq:constraints} \begin{split} & \textbf{instance} \; \mathsf{Generic} \; (\mathsf{D} \; \mathsf{p}) \; \textbf{where} \\ & \textbf{type} \; \mathsf{Rep} \; (\mathsf{D} \; \mathsf{p}) = \mathsf{Rep}_{\mathsf{D}} \; \mathsf{p} \\ & \mathsf{from} = \mathsf{from}_{\mathsf{D}} \\ & \mathsf{to} \; = \mathsf{to}_{\mathsf{D}} \end{split}
```

- Other instances are defined similarly.
- In fact, Rep T, from, and to are precisely determined by the definition of T, so these instances can be automatically generated (e.g. using Template Haskell or a preprocessor).

## The Generic show Function

#### Finally:

```
gshow :: (Show (Rep a), Generic a) \Rightarrow a \rightarrow String gshow = show \circ from
```

## GP in General

- Datatype-generic programming:
  - Datatype is the parameter
  - Instantiation gives you a large class of generic functions
- Many generic functions:
  - Pretty-printing ( show ) and parsing ( read )
  - Compression, serialization, and the reverse
  - Comparison, equality
  - ► Folds (catamorphisms), unfolds (anamorphisms), maps, zips, zippers
  - Traversals, updates, queries
- Many different libraries:
  - Instant Generics presented here
  - Generic Deriving GHC ≥ 7.2, similar to Instant Generics
  - ▶ EMGM maintained by me
  - Regular folds, etc.
  - Multirec mutually recursive datatypes, folds, etc.
  - Scrap Your Boilerplate (SYB) GHC, traversals, queries
  - **-** ...

### References

#### Generic Programming in Haskell:

- Johan Jeuring, Sean Leather, José Pedro Magalhães, Alexey Rodriguez Yakushev. Libraries for Generic Programming in Haskell. AFP 2008. pp. 165-229, 2009.
- Generic Deriving: http://www.haskell.org/haskellwiki/GHC.Generics