

# lecture

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**Definition 1** (NP-hard). every problem in NP can be efficiently reduced to any other problem in np hard

max cut game: each node is a player, each player decides if they want to move to the other side to increase the total score

this is equal to the local search for maxcut

**Definition 2.** ppad complete (?), pls complete (?)

**Definition 3** (pls class). has 3 algos that are efficient over input size.

1. initialization
2. evaluation
3. locally opt checker - report local opt or return better

**Definition 4** (pls reduction). start from problem that is hard, transform into new algo in poly time, from  $\pi_1$  to  $\pi_2$ .

w requirements,

1. every  $x \in \pi_1$  maps to  $A(x) \in \pi_2$
2. maps every local optimum  $A(x)$  to  $x$

if you can pls reduce max cut to a new problem and you claim to find local optimum in the new problem, then it would be a contradiction