KI2: Künstliche Intelligenz - SS22 Al Project: Rush Hour 1

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Abstract

In this programming assignment, we were tasked with using the A^* algorithm to solve instances of the Rush Hour puzzle. This involved implementing a graph-search version of A^* , along with three heuristics. Our implementation was tested on several Rush Hour puzzles.

1.1 Algorithm

For finding the best possible solution for the Rush Hour Puzzle the A* Algorithm is used in this project. With a weighted graph of search nodes, starting from one specific point, it finds a path to the goal with the smallest costs, which would be the exit of the red car in this case. The A* algorithm uses an open and closed list to ensure, that nodes are not visited twice. For each step the algorithm has to determine which node to expand next. This is evaluated with the lowest overall costs, this is done by minimizing f(n) = g(n) + h(n). In this project the cost for one move is always 1, so the path costs are equal to the depth of the node. The heuristic is calculated for each node individually. In this project for sorting the nodes according to their overall costs a PriorityQueue was used. This Queue automatically sorts all inserted nodes according to a specific comparator. In the closed list every node which is already expanded is stored. In this list every node can only be once, so a Set was used to implement that.

1.2 Heuristics

The heuristics should analyse the current state of the puzzle and make an estimation of how many moves would be necessary when visiting the current node. For the heuristics it is important to never overestimate the real costs (moves needed). As a result the heuristic would not be admissible and therefore the solution found may not be optimal.

1.2.1 Zero-Heuristic

The project already implemented a Zero Heuristic, which returns zero for each node. Using A^* with this heuristic is equivalent to breadth-first search.

1.2.2 Distance Heuristic

We also considered the distance from the goal car the exit as a possible heuristic (the results are also included below). When investigate this heuristic one can see that this would not be admissible for all possible puzzles. Because one car can move as far as possible in one move, the distance could possibly overestimate the real costs and not find an optimal solution. Therefore this heuristic is not admissable. See also Chapter 1.3

1.2.3 Blocking Heuristic

As second heuristic a blocking heuristic was considered. It counts all others cars, blocking the exit for the red car. Each car counts one, because at least one move would be required to get is out of the way. This value plus one for the goal car (to move the goal car to the exit, one move is required) is the result for a state.

1.2.4 Advanced Heuristic

In the advanced heuristic the blocking heuristic was extended, to not only count the cars blocking the goal car, but also the cars which block these cars again, and the cars which again block these, and so forth. The idea behind this algorithm was to count all blocking cars in a recursive way.

For considering the blocking cars in a recursive way, much information is needed to accomplish a correct value. First we counted all blocking cars of our goal car again and did the recursive call only for those cars. Each car had to be tested for moving backwards and forwards and then the overall count of which is the lowest of both was chosen. This was done because there could be more possible solutions and we want the minimum required moves. Next we had to determine whether a car has enough space to move out of the way, is blocked by another car or by a wall of the game. When a blocking car is found the recursive call is done. In order to not produce an endless recursion a list with all cars already considered was taken into account. Although this means that cars can be never counted twice, so if one car blocks three others it is only counted once and then considered to have been moved out of the way. This is also necessary to not overestimate the real costs.

We also tried the add the distance to the Value calculated for the Advanced Heuristic, but this lead of course to the same problem as mentioned beforhand in Chapter 1.2.2.

1.3 Consistent and Admissible

Both Blocking and our Advanced Heuristic are consistent and therefore also admissible. A heuristic is consistent if its estimate is always less than or equal to the estimated distance from any neighbouring vertex to the goal, plus the cost of reaching that neighbour. A heuristic is admissible if it never overestimates the cost of reaching the goal, for example the cost it estimates to reach the goal is not higher than the lowest possible cost from the current point in the path.

As we count each car once, and it is counted to have at least one move to be moved out of the way of our goal car, the estimated cost is always smaller or equal to the actual cost as it has to be moved at least once. Here the length of the move is not of importance.

1.4 Results

In the following table the results for all five heuristics can be seen (Zero - Blocking - Distance - Advanced - Advanced Distance). Note that the Heuristics using the Distance are performing quite good but are not admissible. It can be seen that some results get much worse results comparing to the admissible heuristics, because it did not find the optimal solution. We accomplished an admissible heuristic with our Advanced Heuristic which performs considerable better than the blocking heuristic. When running the project it can clearly be seen, that the more difficult the puzzle gets, the longer it takes the algorithm to find a possible solution because many recursive calls are needed for all possible states of the puzzle. In this matter the blocking heuristic is the one which obviously performs better.

All in all our heuristics performed as expected. The only surprising thing was to see that for some individual puzzles some 'lesser' heuristics performed better or just as good, but overall worse. As the puzzles are listed roughly in order of difficulty it was interesting to see how the algorithm behaved. The more cars clustered in one spot, the harder it was for the algorithm to get to a solution whereas for the human eye clusters were detected easily and resolved with more ease. In comparison, the more dependencies on blocking cars were found, the harder it was for the human eye and mind to have an overview over the situation as only a few moves could be thought through before moving.

| | br.fac | 2,186 | 2,340 | 1,613 | 1,627 | 1,774 | 1,901 | 2,018 | 1,411 | 1,715 | 1,558 | 1,324 | 1,502 | 1,608 | 1,759 | 1,331 | 1,473 | 1,376 | 1,350 | 1,359 | 1,992 | 1,306 | 1,338 | 1,257 | 1,459 | 1,414 | 1,372 | 1,323 | 1,221 | 1,335 | 1,242 | 1,256 | 1,170 | 1,209 | 1,214 | 1,215 | 1,190 | 1,152 | 1,181 | 1,178 | |
|------------------|--------|----------|----------|-------|-------|-------|-------|-------|-------|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--|
| | dpth | ∞ | ∞ | 15 | 6 | 6 | 11 | 13 | 12 | 12 | 18 | 25 | 17 | 19 | 18 | 23 | 22 | 24 | 25 | 22 | 11 | 21 | 27 | 33 | 25 | 28 | 28 | 29 | 30 | 31 | 33 | 38 | 38 | 41 | 44 | 44 | 45 | 47 | 49 | 50 | |
| AdvancedDistance | nodes | 959 | 1570 | 3410 | 206 | 398 | 2465 | 18272 | 212 | 1549 | 8186 | 4554 | 3024 | 22037 | 26809 | 2869 | 15631 | 7752 | 6934 | 3224 | 3926 | 1162 | 10358 | 9354 | 40432 | 55422 | 26062 | 13807 | 2203 | 31109 | 6299 | 28248 | 2674 | 13938 | 29199 | 29998 | 15613 | 5827 | 22723 | 23861 | |
| | br.fac | 2,196 | 2,248 | 1,686 | 1,781 | 1,896 | 2,025 | 2,027 | 1,641 | 1,791 | 1,602 | 1,329 | 1,546 | 1,761 | 1,727 | 1,337 | 1,510 | 1,375 | 1,352 | 1,364 | 1,992 | 1,315 | 1,343 | 1,308 | 1,463 | 1,432 | 1,379 | 1,344 | 1,253 | 1,340 | 1,255 | 1,265 | 1,176 | 1,213 | 1,217 | 1,218 | 1,195 | 1,164 | 1,186 | 1,178 | |
| | dpth | ∞ | 6 | 14 | 6 | 6 | 10 | 13 | 12 | 12 | 17 | 25 | 17 | 16 | 18 | 23 | 21 | 25 | 25 | 22 | 10 | 21 | 27 | 29 | 25 | 27 | 28 | 28 | 30 | 31 | 32 | 37 | 37 | 41 | 44 | 44 | 44 | 47 | 48 | 20 | |
| Advanced | nodes | 991 | 2643 | 3688 | 409 | 899 | 2287 | 19262 | 972 | 2468 | 8001 | 4961 | 4656 | 19842 | 44531 | 3171 | 16879 | 10451 | 7202 | 3482 | 1973 | 1301 | 11322 | 10163 | 42408 | 54025 | 29348 | 15462 | 4299 | 34569 | 0902 | 28863 | 2683 | 15743 | 31437 | 32553 | 15739 | 8919 | 22597 | 23908 | |
| | br.fac | 2,625 | 2,681 | 1,639 | 2,255 | 2,284 | 2,239 | 1,955 | 1,840 | 1,839 | 1,608 | 1,324 | 1,564 | 1,763 | 1,758 | 1,337 | 1,509 | 1,408 | 1,384 | 1,364 | 2,115 | 1,331 | 1,408 | 1,301 | 1,463 | 1,433 | 1,372 | 1,338 | 1,286 | 1,331 | 1,251 | 1,251 | 1,165 | 1,232 | 1,221 | 1,225 | 1,195 | 1,174 | 1,183 | 1,167 | |
| | dpth | 6 | 6 | 15 | 6 | 11 | 11 | 14 | 13 | 12 | 18 | 26 | 17 | 18 | 18 | 23 | 21 | 25 | 25 | 22 | 11 | 21 | 26 | 30 | 25 | 28 | 59 | 29 | 31 | 32 | 33 | 39 | 40 | 41 | 44 | 43 | 45 | 48 | 49 | 53 | |
| Distance | nodes | 9561 | 11407 | 4249 | 2707 | 15724 | 12786 | 24401 | 6064 | 3269 | 13721 | 6017 | 5541 | 62786 | 59925 | 3175 | 16791 | 18025 | 12179 | 3453 | 7171 | 1631 | 25421 | 11546 | 43034 | 78720 | 35803 | 18224 | 10859 | 38130 | 8014 | 30663 | 3175 | 27331 | 39998 | 33469 | 18339 | 15154 | 24530 | 24878 | |
| | br.fac | 2,857 | 2,663 | 1,699 | 2,057 | 2,433 | 2,510 | 2,035 | 1,925 | 1,835 | 1,651 | 1,338 | 1,562 | 1,816 | 1,776 | 1,337 | 1,513 | 1,425 | 1,375 | 1,364 | 2,095 | 1,327 | 1,401 | 1,309 | 1,463 | 1,440 | 1,386 | 1,351 | 1,293 | 1,345 | 1,259 | 1,268 | 1,178 | 1,233 | 1,226 | 1,224 | 1,198 | 1,177 | 1,187 | 1,178 | |
| | dpth | ∞ | ∞ | 14 | 6 | 6 | 6 | 13 | 12 | 12 | 17 | 25 | 17 | 16 | 17 | 23 | 21 | 24 | 25 | 22 | 10 | 21 | 26 | 29 | 25 | 27 | 28 | 28 | 30 | 31 | 32 | 37 | 37 | 40 | 43 | 43 | 44 | 47 | 48 | 50 | |
| Blocking | nodes | 6856 | 4044 | 4059 | 1281 | 5075 | 2929 | 20143 | 5381 | 3200 | 12739 | 5778 | 5457 | 31112 | 39873 | 3171 | 17597 | 16575 | 10540 | 3463 | 3116 | 1535 | 22294 | 10343 | 42796 | 61820 | 33715 | 17448 | 9813 | 37766 | 7675 | 30623 | 2800 | 23243 | 34899 | 32919 | 17182 | 14245 | 23526 | 24236 | |
| | br.fac | 3,066 | 3,378 | 1,788 | 2,301 | 2,888 | 2,791 | 2,202 | 1,957 | 1,947 | 1,675 | 1,347 | 1,642 | 1,916 | 1,880 | 1,338 | 1,529 | 1,436 | 1,392 | 1,367 | 2,438 | 1,332 | 1,421 | 1,338 | 1,467 | 1,455 | 1,396 | 1,359 | 1,313 | 1,345 | 1,264 | 1,270 | 1,182 | 1,249 | 1,228 | 1,225 | 1,206 | 1,179 | 1,192 | 1,179 | |
| | dpth | ∞ | ∞ | 14 | 6 | 6 | 6 | 13 | 12 | 12 | 17 | 25 | 17 | 16 | 17 | 23 | 21 | 24 | 25 | 22 | 10 | 21 | 26 | 29 | 25 | 27 | 28 | 28 | 30 | 31 | 32 | 37 | 37 | 40 | 43 | 43 | 44 | 47 | 48 | 20 | |
| Zero | nodes | 11589 | 24081 | 7731 | 3203 | 21390 | 15992 | 52493 | 6461 | 6116 | 15890 | 6694 | 11677 | 69130 | 97411 | 3180 | 21560 | 19560 | 13839 | 3610 | 12593 | 1650 | 31244 | 18382 | 45187 | 80491 | 40135 | 20228 | 14809 | 38385 | 8580 | 32409 | 3155 | 36459 | 37447 | 33989 | 22309 | 15268 | 28374 | 24708 | |
| | name | Jam-1 | Jam-2 | Jam-3 | Jam-4 | Jam-5 | Jam-6 | Jam-7 | Jam-8 | Jam-9 | Jam-10 | Jam-11 | Jam-12 | Jam-13 | Jam-14 | Jam-15 | Jam-16 | Jam-17 | Jam-18 | Jam-19 | Jam-20 | Jam-21 | Jam-22 | Jam-23 | Jam-24 | Jam-25 | Jam-26 | Jam-27 | Jam-28 | Jam-29 | Jam-30 | Jam-31 | Jam-32 | Jam-33 | Jam-34 | Jam-35 | Jam-36 | Jam-37 | Jam-38 | Jam-39 | |

Table 1.1: Comparison of Heuristics. Zero - Blocking - Distance - Advanced - Advanced Distance