

### Given Data:

Reservoir Area,  $A = 2.4 \text{ km}^2 = 2.4 \times 10^6 \text{ m}^2$ ,

Reservoir Capacity,  $V = 5 \times 10^6 \text{ m}^3$ ,

Effective Head,  $H = 100 \text{ m}$ ,

Efficiencies:  $\eta_p = 0.95$ ,  $\eta_t = 0.90$ ,  $\eta_g = 0.85$ ,

Total Efficiency,  $\eta = \eta_p \cdot \eta_t \cdot \eta_g = 0.95 \cdot 0.90 \cdot 0.85 = 0.72675$ ,

Gravitational Acceleration,  $g = 9.81 \text{ m/s}^2$ ,

Load Supplied:  $P = 15000 \text{ kW} = 1.5 \times 10^7 \text{ W}$ ,

Time Supplied:  $t = 3 \text{ hours} = 3 \cdot 3600 = 10800 \text{ s}$ .

### Part i: Total Electrical Energy Generated

The total energy is calculated as:

$$E = \eta \cdot \rho \cdot g \cdot H \cdot V,$$

where  $\rho = 1000 \text{ kg/m}^3$ .

Substitute the values:

$$E = 0.72675 \cdot 1000 \cdot 9.81 \cdot 100 \cdot (5 \times 10^6).$$

$$E = 3.56 \times 10^{12} \text{ J}.$$

Convert joules to kilowatt-hours:

$$E_{\text{kWh}} = \frac{E}{3.6 \times 10^6} = \frac{3.56 \times 10^{12}}{3.6 \times 10^6} = 988,541.67 \text{ kWh}.$$

**Answer:** The total electrical energy generated is:

$$E = 988,541.67 \text{ kWh}.$$

### Part ii: Fall in Reservoir Level

The energy consumed is:

$$E_{\text{consumed}} = P \cdot t = 1.5 \times 10^7 \cdot 10800 = 1.62 \times 10^{11} \text{ J}.$$

The volume of water used is:

$$V_{\text{used}} = \frac{E_{\text{consumed}}}{\eta \cdot \rho \cdot g \cdot H}.$$

Substitute values:

$$V_{\text{used}} = \frac{1.62 \times 10^{11}}{0.72675 \cdot 1000 \cdot 9.81 \cdot 100}.$$

$$V_{\text{used}} = 2.28 \times 10^4 \text{ m}^3.$$

The fall in reservoir level is:

$$\text{Fall in Level} = \frac{V_{\text{used}}}{A} = \frac{2.28 \times 10^4}{2.4 \times 10^6}.$$

$$\text{Fall in Level} = 0.0095 \text{ m} = 9.5 \text{ mm}.$$

**Answer:** The fall in reservoir level is:

$$\text{Fall in Level} = 9.5 \text{ mm}.$$

## Hydroelectric Plant Discharge and Capacity Estimation

The weekly discharge of a typical hydroelectric plant is as follows:

Day	Sun	Mon	Tue	Wed	Thu	Fri	Sat
Discharge (m <sup>3</sup> /s)	500	520	850	800	875	900	546

The plant has an effective head of 15 m and an overall efficiency of 85%. The plant operates at a 40% load factor.

### i. Average Daily Discharge

The average daily discharge is calculated as:

$$\text{Average daily discharge} = \frac{\text{Sum of daily discharges}}{\text{Number of days}}$$

$$\text{Average daily discharge} = \frac{500 + 520 + 850 + 800 + 875 + 900 + 546}{7} = \frac{4491}{7} = 641.57 \text{ m}^3/\text{s}$$

### ii. Pondage Required

Pondage refers to the storage required to regulate the flow variations across days. First, calculate the deviations from the average daily discharge:

$$\text{Deviation for each day} = \text{Discharge for that day} - \text{Average discharge}$$

For positive deviations:

$$\text{Pondage required (m}^3\text{)} = \text{Sum of positive deviations} \times \text{Seconds per day}$$

For each day:

$$\text{Sun: } 500 - 641.57 = -141.57 \quad (\text{negative, ignored})$$

$$\text{Mon: } 520 - 641.57 = -121.57 \quad (\text{negative, ignored})$$

$$\text{Tue: } 850 - 641.57 = 208.43 \quad (\text{positive deviation})$$

$$\text{Wed: } 800 - 641.57 = 158.43 \quad (\text{positive deviation})$$

$$\text{Thu: } 875 - 641.57 = 233.43 \quad (\text{positive deviation})$$

$$\text{Fri: } 900 - 641.57 = 258.43 \quad (\text{positive deviation})$$

$$\text{Sat: } 546 - 641.57 = -95.57 \quad (\text{negative, ignored})$$

Total positive deviation:

$$208.43 + 158.43 + 233.43 + 258.43 = 858.72 \text{ m}^3/\text{s}$$

Pondage required:

$$\text{Pondage required} = 858.72 \times 86400 = 74,177,612.8 \text{ m}^3$$

### iii. Installed Capacity of Proposed Plant

The installed capacity is calculated using the formula for power:

$$\text{Power (W)} = \rho \cdot g \cdot Q \cdot H \cdot \eta$$

Where:

$$\rho = 1000 \text{ kg/m}^3 \quad (\text{density of water}), \quad g = 9.81 \text{ m/s}^2 \quad (\text{gravity}),$$

$$Q = 900 \text{ m}^3/\text{s} \quad (\text{maximum discharge}), \quad H = 15 \text{ m}, \quad \eta = 0.85$$

Substituting the values:

$$\text{Power (W)} = 1000 \cdot 9.81 \cdot 900 \cdot 15 \cdot 0.85 = 112,569,750 \text{ W}$$

Converting to MW:

$$\text{Power (MW)} = \frac{112,569,750}{10^6} = 112.57 \text{ MW}$$

Considering the load factor:

$$\text{Installed Capacity (MW)} = \frac{\text{Power}}{\text{Load factor}} = \frac{112.57}{0.40} = 281.43 \text{ MW}$$

## i. Average Daily Discharge

The average daily discharge is calculated as:

$$\text{Average daily discharge} = \frac{\text{Sum of daily discharges}}{\text{Number of days}}$$

Substituting the values:

$$\text{Average daily discharge} = \frac{500 + 520 + 850 + 800 + 875 + 900 + 546}{7} = 713 \text{ m}^3/\text{s}$$

## ii. Pondage Required

Pondage refers to the storage required to regulate the flow variations across days. First, calculate the deviations from the average daily discharge:

$$\text{Deviation for each day} = \text{Discharge for that day} - \text{Average discharge}$$

For positive deviations:

$$\text{Pondage required (m}^3\text{)} = \text{Sum of positive deviations} \times \text{Seconds per day}$$

For each day:

$$\text{Sun: } 500 - 713 = -213 \quad (\text{negative, ignored})$$

$$\text{Mon: } 520 - 713 = -193 \quad (\text{negative, ignored})$$

$$\text{Tue: } 850 - 713 = 137 \quad (\text{positive deviation})$$

$$\text{Wed: } 800 - 713 = 87 \quad (\text{positive deviation})$$

$$\text{Thu: } 875 - 713 = 162 \quad (\text{positive deviation})$$

$$\text{Fri: } 900 - 713 = 187 \quad (\text{positive deviation})$$

$$\text{Sat: } 546 - 713 = -167 \quad (\text{negative, ignored})$$

Total positive deviation:

$$137 + 87 + 162 + 187 = 573 \text{ m}^3/\text{s}$$

Pondage required:

$$\text{Pondage required} = 573 \times 86400 = 49,507,200 \text{ m}^3$$

## iii. Installed Capacity

The installed capacity is calculated using the formula for power:

$$\text{Power (W)} = \rho \cdot g \cdot Q \cdot H \cdot \eta$$

Where:

$$\rho = 1000 \text{ kg/m}^3 \quad (\text{density of water}), \quad g = 9.81 \text{ m/s}^2 \quad (\text{gravity}),$$

$$Q = 900 \text{ m}^3/\text{s} \quad (\text{maximum discharge}), \quad H = 15 \text{ m}, \quad \eta = 0.85$$

Substituting the values:

$$\text{Power (W)} = 1000 \cdot 9.81 \cdot 900 \cdot 15 \cdot 0.85 = 112,569,750 \text{ W}$$

Converting to MW:

$$\text{Power (MW)} = \frac{112,569,750}{10^6} = 112.57 \text{ MW}$$

Considering the load factor:

$$\text{Installed Capacity (MW)} = \frac{\text{Power}}{\text{Load factor}} = \frac{112.57}{0.40} = 281.43 \text{ MW}$$