

Covariance and confidence intervals

The asymptotic covariance matrix of $\hat{\pi}$ can be approximated by the inverse of the observed Fisher information matrix, I :

$$I(\pi'|\mathbf{x}, \mathbf{y}) = -\frac{\partial^2 \ell(\pi')}{\partial \pi' \partial \pi'^T}$$

$$\text{Cov}(\hat{\pi}_p, \hat{\pi}_q) = [I^{-1}(\hat{\pi}')]_{pq}$$

with variance and correlation given by

$$\text{Var}(\hat{\pi}_j) = \sigma_j^2 = \left\{ \text{Cov}(\hat{\pi}) \right\}_{jj}$$

$$\text{Corr}(\hat{\pi}_p, \hat{\pi}_q) = \frac{\text{Cov}(\hat{\pi}_p, \hat{\pi}_q)}{\sqrt{\sigma_p^2 \sigma_q^2}}$$