

**UNIVERSITY OF LIMERICK**  
**OILLSCOIL LUIMNIGH**  
**FACULTY OF SCIENCE AND ENGINEERING**  
**DEPARTMENT OF ELECTRONIC & COMPUTER ENGINEERING**

**MODULE CODE:** CE6021  
**MODULE TITLE:** MACHINE VISION  
**SEMESTER:** AUTUMN 2022  
**DURATION OF EXAM:** 2 ½ HOURS  
**LECTURER:** DR. TONY SCANLAN

**INSTRUCTION TO CANDIDATES:**

**ANSWER 4 OF 5 QUESTIONS.**

**EACH QUESTION CARRIES 20 MARKS. YOU WILL BE MARKED OUT OF 80.**

**THIS EXAM PAPER IS WORTH 45% OF THE FINAL MODULE RESULT.**

**READ EACH PROBLEM COMPLETELY AND THOROUGHLY BEFORE BEGINNING TO WORK ON IT.**

**INCLUDE ANY GRAPH PAPER OR ADDITIONAL SHEETS WITH YOUR SCRIPT.**

**CLEARLY MARK YOUR FINAL ANSWERS TO QUESTIONS.**

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## Q1

- (a) A simple pinhole camera has a distance of 0.2m from the aperture to the rear surface of the camera where the image is formed. What is the optimum aperture diameter  $d$  when the wavelength of light is  $\lambda = 700\text{nm}$ ?

[5 marks]

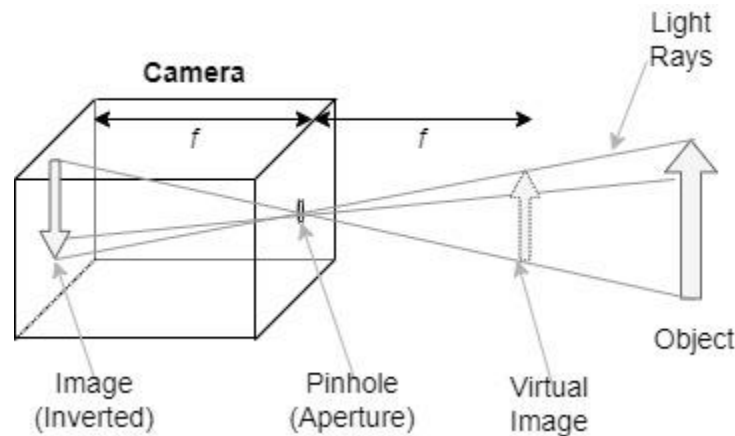


Figure 1.

- (b) Give brief answers to the following questions.

- i. What effect is typically seen in images captured by camera with a slow shutter speed?
- ii. Calculate the approximate depth of field for a camera with F-number 1.8, allowable circle of confusion  $1\mu\text{m}$ , focal length 13.5mm and a subject distance of 15m (Given the formula  $D \approx \frac{2NCU^2}{f^2}$ ).
- iii. What physical principle do digital cameras use to convert incident light into electrical current?
- iv. Briefly explain how alising occurs in digital images.
- v. Briefly explain how a rolling shutter in a digital image sensor can cause distortion in the image of a high speed object in motion (e.g. helicopter blades).

[8 marks]

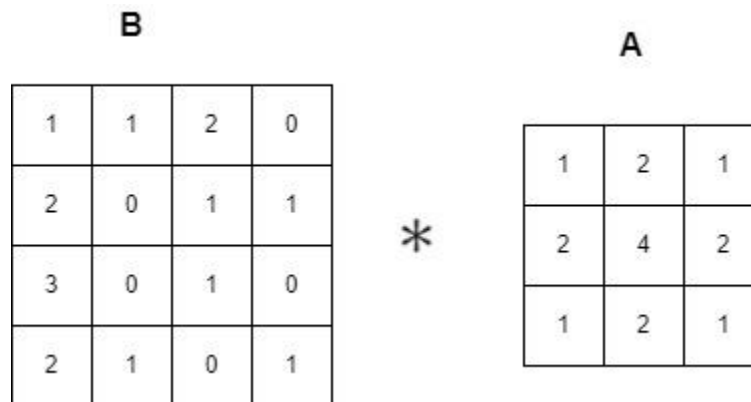
- (c) Given a wide angle camera with a  $90^\circ$  field of view how many pixels are needed to be able to resolve a 5cm wide feature at a distance of 30m?

[7 marks]

**Q2**

(a)

- i. What is the fundamental difference between the convolution and cross correlation operations?
- ii. Determine the result of convolving the 3x3 kernel **A** with the 4x4 image **B** shown in Figure 2. You must demonstrate how the convolution can be carried efficiently using Separable convolution.

**[4 Marks]**Figure 2.

(b)

- i. How is an edge in an image defined?
- ii. What is the general principle used to find edges in images?
- iii. What effect can image noise have on an edge detector and how can the effect of noise be mitigated?
- iv. List the four main steps in the Canny algorithm.

**[4 Marks]**

- (c) Describe the Harris Corner algorithm. Write your answer as pseudo code showing the key steps to detect corners in an image.

**[12 Marks]**

## Q3

(a) Give brief answers to the following questions:

- i. List some qualities (four) of a good feature detector.
- ii. Give some applications (two) that keypoints obtained using feature detection can be used for.
- iii. What does it mean when a feature detector is described as scale invariant?
- iv. Which function is commonly used as the canonical function for generating scale spaces?
- v. What is the key principle that enables scale invariant feature detectors reliably detect features at one scale only?
- vi. How is the Laplacian scale space formed (List the components or give your answer in the form of an equation)?
- vii. How can the Laplacian scale space be formed in a computationally efficient manner?
- viii. What simple algorithm can be used to find local maxima across a scale space?
- ix. What advantage does the Harris Laplacian detector have over the basic Laplacian detector?
- x. Explain how the difference of Gaussians scale invariant detector is more computationally efficient than the Laplacian scale space detector?

[14 marks]

(b) In the SIFT algorithm a pixel with a calculated magnitude of  $\mu = 15$  is to be divided between the 4 nearest histograms (centres as shown in figure 3). Calculate the contribution to the histogram with centre (2,0) using bilinear interpolation.

[6 marks]

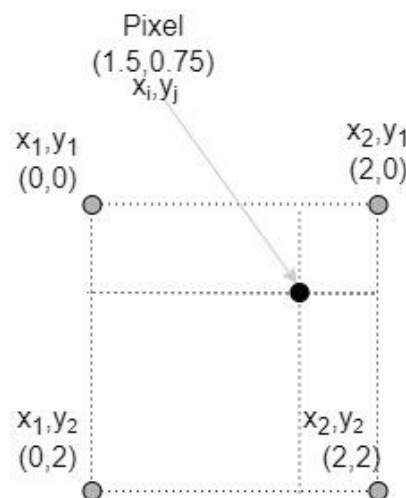


Figure 3.

**Q4**

(a) Give Brief answers to the following questions:

- i. Define the term supervised learning.
- ii. What are the three key components in a supervised learning system?
- iii. What is the difference between Classification and Regression?
- iv. Briefly define what the term “Generalisation” means for classifiers?

**[4 marks]**

(b) Give brief answers to the following questions about the K Nearest Neighbours (KNN) classifier.

- i. What computation takes place during prediction with KNN?
- ii. How does the value of K affect the overfitting behaviour of the classifier?

**[4 marks]**

(c) Give brief answers to the questions below.

- i. Briefly explain the curse of dimensionality?
- ii. What is the implication for image classification (using pixels as features) due to the curse of dimensionality?

**[4 marks]**

(d) Given a data matrix  $X = \begin{bmatrix} \vdots & \dots & \vdots \\ x_1 & \dots & x_n \\ \vdots & \dots & \vdots \end{bmatrix}$  with  $n$  data sample vectors  $x_i$  of dimension  $d$ .

- i. Briefly outline the steps necessary to obtain the principal components for the matrix of samples  $X$ . (You can give your answer in the form of pseudo code and/or mathematical equations)
- ii. Briefly explain how images can be compressed and uncompressed using the principal component analysis.

**[8 marks]**

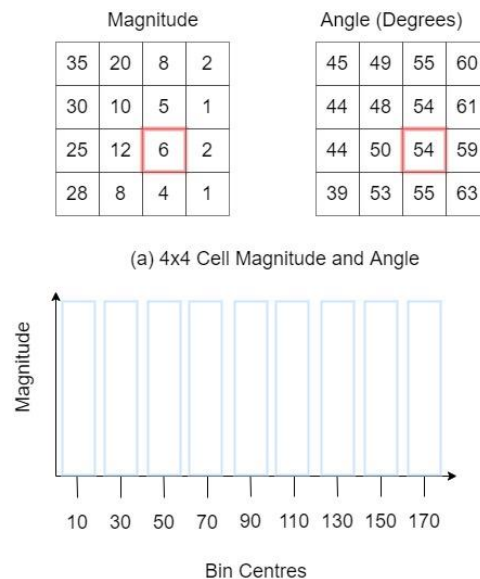
**Q5**

- (a) Briefly describe how the Histogram of Orientated Gradients descriptor can be used to build a pedestrian detector.

**[4 marks]**

- (b) Given the gradient information (Magnitude and Angle) for a 4 x 4 pixel cell (as shown in Figure 3) and assuming that the magnitude is to be interpolated between the two nearest neighbouring histogram bins.

- Determine which bin centres will have some magnitude assigned by the pixel in the red square.
- Calculate the individual magnitudes that will be assigned to each of the bins

**[6 marks]****Figure 3.**

- (c) If a Histograms of Orientated Gradients (HOG) based detector is comprised of: cells of size 8 x 8 pixels, blocks of 2 x 2 cells, histograms with 9 orientations in each cell and an image patch size of 176 x 64 pixels.

- Calculate how many blocks does the detector window contain (assuming the blocks overlap by 1 cell)?
- Calculate the length of the HOG descriptor?

**[6 marks]**

- (d) Briefly describe how the Bag of features representation is generated for an image.

**[4 marks]**

*Additional Information for Q5:*

Convolution Formula: For any size image  $i$ , kernel of size  $k$  and stride  $s$  the output size  $o$  is given by

$$o = \left\lfloor \frac{i-k}{s} \right\rfloor + 1 \quad (\text{all values } (i, k, o, s) \text{ are in pixels})$$