## ECE UY 3613, Spring 2024, Homework #1

Released on 01/25/2024, no submission, solutions will be released on 02/02/2024

Review Questions: 11, 13, 23 Problems: 4, 5, 7, 8, 20, 24, 33

- **R11.** Suppose there is exactly one packet switch between a sending host and a receiving host. The transmission rates between the sending host and the switch and between the switch and the receiving host are  $R_1$  and
- **R13.** Suppose users share a 2 Mbps link. Also suppose each user transmits continuously at 1 Mbps when transmitting, but each user transmits only 20 percent of the time. (See the discussion of statistical multiplexing in **Section 1.3.**)
  - a. When circuit switching is used, how many users can be supported?
  - **b.** For the remainder of this problem, suppose packet switching is used. Why will there be essentially no queuing delay before the link if two or fewer users transmit at the same time? Why will there be a queuing delay if three users transmit at the same time?
  - **c.** Find the probability that a given user is transmitting.
  - **d.** Suppose now there are three users. Find the probability that at any given time, all three users are transmitting simultaneously. Find the fraction of time during which the queue grows.

- **P4.** Consider the circuit-switched network in **Figure 1.13**. Recall that there are four circuits on each link. Label the four switches A, B, C, and D, going in the clockwise direction.
  - **a.** What is the maximum number of simultaneous connections that can be in progress at any one time in this network?
  - **b.** Suppose that all connections are between switches A and C. What is the maximum number of simultaneous connections that can be in progress?
  - **c.** Suppose we want to make four connections between switches A and C, and another four connections between switches B and D. Can we route these calls through the four links to accommodate all eight connections?
- **P5.** Review the car-caravan analogy in **Section 1.4**. Assume a propagation speed of 100 km/hour.
  - **a.** Suppose the caravan travels 175 km, beginning in front of one tollbooth, passing through a second tollbooth, and finishing just after a third tollbooth. What is the end-to-end delay?
  - **b.** Repeat (a), now assuming that there are eight cars in the caravan instead of ten.

- P7. In this problem, we consider sending real-time voice from Host A to Host B over a packet-switched network (VoIP). Host A converts analog voice to a digital 64 kbps bit stream on the fly. Host A then groups the bits into 56-byte packets. There is one link between Hosts A and B; its transmission rate is 10 Mbps and its propagation delay is 10 msec. As soon as Host A gathers a packet, it sends it to Host B. As soon as Host B receives an entire packet, it converts the packet's bits to an analog signal. How much time elapses from the time a bit is created (from the original analog signal at Host A) until the bit is decoded (as part of the analog signal at Host B)?
- **P8.** Suppose users share a 10 Mbps link. Also suppose each user requires 200 kbps when transmitting, but each user transmits only 10 percent of the time. (See the discussion of packet switching versus circuit switching in Section 1.3.)
  - **a.** When circuit switching is used, how many users can be supported?
  - **b.** For the remainder of this problem, suppose packet switching is used. Find the probability that a given user is transmitting.
  - **c.** Suppose there are 120 users. Find the probability that at any given time, exactly n users are transmitting simultaneously. (*Hint:* Use the binomial distribution.)
  - **d.** Find the probability that there are 51 or more users transmitting simultaneously.

**P20.** Consider the throughput example corresponding to **Figure 1.20(b)**. Now suppose that there are M client-server pairs rather than 10. Denote  $R_s$ ,  $R_c$ , and R for the rates of the server links, client links, and network link. Assume all other links have abundant capacity and that there is no other traffic in the network besides the traffic generated by the M client-server pairs. Derive a general expression for throughput in terms of  $R_s$ ,  $R_c$ , R and M.

**P24.** Suppose you would like to urgently deliver 50 terabytes data from Boston to Los Angeles. You have available a 100 Mbps dedicated link for data transfer. Would you prefer to transmit the data via this link or instead use FedEx over-night delivery? Explain.

**P33.** Consider sending a large file of F bits from Host A to Host B. There are three links (and two switches) between A and B, and the links are uncongested (that is, no queuing delays). Host A segments the file into segments of S bits each and adds 80 bits of header to each segment, forming packets of L = 80 + S bits. Each link has a transmission rate of R bps. Find the value of S that minimizes the delay of moving the file from Host A to Host B. Disregard propagation delay.