22MAT121-Discrete Mathematics AIE-B

SET-A

- 1. Find the contrapositive, converse and inverse of the following statement: " n is an even number whenever n is a perfect number." [3 marks]
- 2. show that $(p \land (p \rightarrow q)) \rightarrow q$ is a tautology without using the truth table. [3 marks]
- 3. Let P(x), Q(x) and R(x) are the statements "x is a professor", "x is ignorant" and "x is vain". Represent the following statements using quantifiers, logical connectives, P(x), Q(x) and R(x).
 - (a) No professors are ignorant.
 - (b) All ignorant people are vain.
 - (c) There is a professor who is ignorant and vain.

[4 Marks]

SET-B

- 1. Let P(x), Q(x) and R(x) are the statements "x is a clear explanation", "x is satisfactory" and "x is an excuse". Represent the following statements using quantifiers, logical connectives, P(x), Q(x) and R(x).
 - (a) All clear explanations are satisfactory.
 - (b) Some excuses are unsatisfactory.
 - (c) Some excuses are neither satisfactory nor a clear explanation.

[4 Marks]

- 2. Find the contrapositive, converse and inverse of the following statement: " n is an odd number is necessary for n is a prime number." [3 marks]
- 3. show that $(\neg q \land (p \rightarrow q)) \rightarrow \neg p$ is a tautology without using the truth table. [3 marks]

SET-C

1. show that $p \leftrightarrow q \equiv (p \land q) \lor (\neg p \land \neg q)$ without using the truth table.

[3 marks]

- 2. Let P(x), Q(x) and R(x) are the statements "x is a baby", "x is illogical" and "x can manage a dog". Represent the following statements using quantifiers, logical connectives, P(x), Q(x) and R(x).
 - (a) Babies are illogical.
 - (b) illogical persons can't manage a dog.
 - (c) Babies are either illogical or can manage a dog.

[4 Marks]

3. Find the contrapositive, converse and inverse of the following statement: " n is an solitary number is sufficient for n is a even number." [3 marks]