

There is no real number which squares to give  $-1$ . However, we can define an object which squares to  $-1$ . This is traditionally called  $i$  in mathematics and  $j$  in physics and engineering (to avoid confusion with  $i$  meaning an electrical current), so  $i^2 = -1$ . Thus we find that

- the square roots of  $-1$  are  $i$  and  $-i$
- the square roots of  $-4$  are  $2i$  and  $-2i$

and so on.

We call real multiples of  $i$  (that is,  $ai$  for some real number  $a$ ) *imaginary numbers*.

We can visualise imaginary numbers as lying along a number line like the ordinary real number line, but at right angles to it. These two number lines together form a plane called the complex plane.