(1) (2) This is a contradiction, so In the prime factorisations our original assumption of  $m^2$  and  $n^2$ , 2 occurs to an that  $\sqrt{2}$  is rational must be even power. wrong. 3 **(4**) But prime factorisations Multiply across to get are unique, so 2 should  $2n^2 = m^2$ . appear to the same power in both  $2n^2$  and  $m^2$ . (5) (6) That is, we can write Suppose, for a  $\sqrt{2} = \frac{m}{n}$  where m and n are contradiction, that  $\sqrt{2}$  is integers and where  $n \neq 0$ . rational. (7) (8) In the prime factorisation So  $\sqrt{2}$  is irrational. of  $2n^2$ , 2 occurs to an odd power.

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Squaring, we have  $2 = \frac{m^2}{n^2}$ .