

測位航法学会 平成23年度全国大会 セミナー②

GNSS Precise Positioning with RTKLIB

Part 2

2011-4-25,26 @東京海洋大学品川 楽水会館



東京海洋大学 高須 知二

Timetable

1. GPS/GNSS	April 25	9:30-10:40
2. Signal and Receiver		10:50-12:00
3. Standard Positioning		13:00-15:10
4. RTKLIB		15:30-16:40

5. RTK	April 26	9:30-10:30
6. PPP		10:40-11:50
7. RTK System		13:00-14:20
8. Advanced Topics		14:40-16:10

5. RTK

Precise Positioning

	Standard Positioning (code-based)	Precise Positioning (carrier-based)
Observables	Pseudorange (Code)	Carrier-Phase + Pseudorange
Receiver Noise	30 cm	3 mm
Multipath	30 cm - 30 m	1 - 3 cm
Sensitivity	High (<20dBHz)	Low (>35dBHz)
Discontinuity	No Slip	Cycle-Slip
Ambiguity	-	Estimated/Resolved
Receiver	Low-Cost (~\$100)	Expensive (~\$20,000)
Accuracy (RMS)	3 m (H), 5 m (V) (Single) 1 m (H), 2 m (V) (DGPS)	5 mm (H), 1 cm (V) (Static) 1 cm (H), 2 cm (V) (RTK)
Application	Navigation, Timing, SAR,...	Survey, Mapping, ...

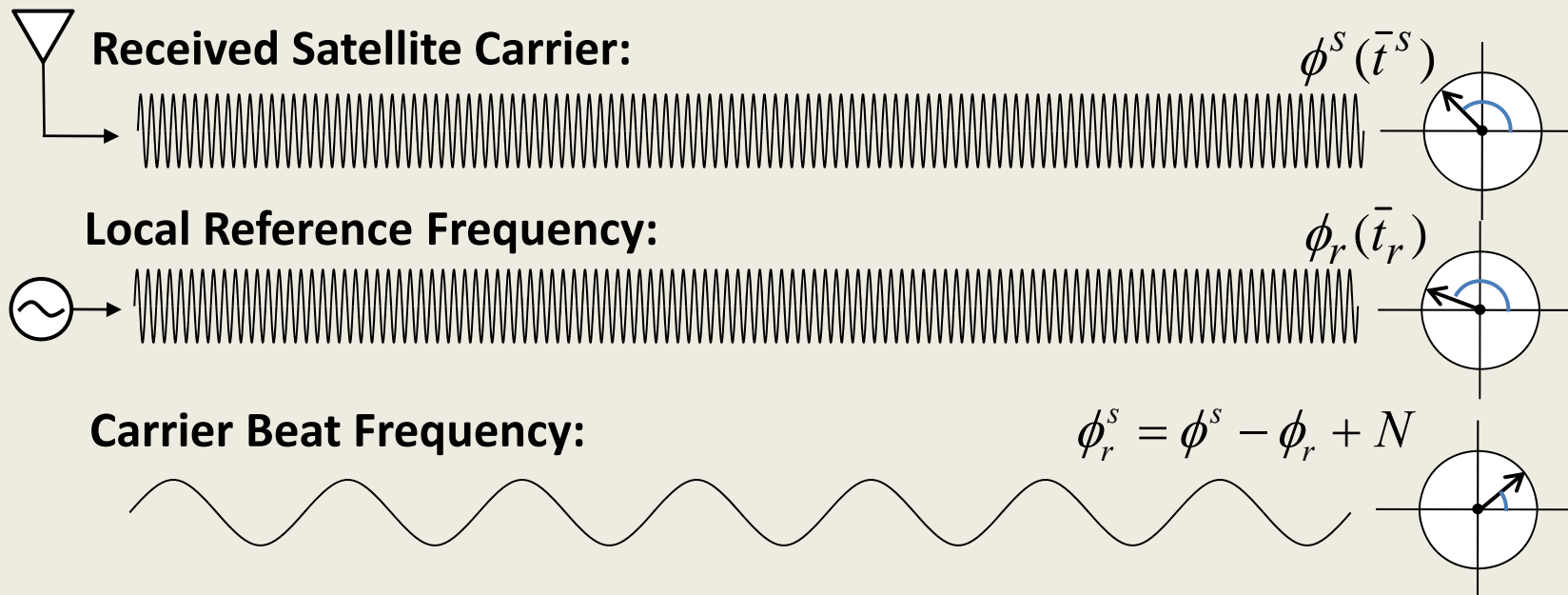
Carrier-Phase

Definition:

$$\phi_r^s = \phi^s - \phi_r + N$$

(cycle)

... actually being a measurement on the beat frequency between the received carrier of the satellite signal and a receiver-generated reference frequency. (*RINEX 2.10*)



Carrier-Phase Model (1)

Carrier-Phase:

$$\begin{aligned}\phi_r^s &= \phi_r(t_r) - \phi^s(t^s) + N_r^s + \varepsilon_\phi & (\phi_{r,0} = \phi_r(t_0), \phi_0^s = \phi^s(t_0)) \\ &= (f(t_r + dt_r - t_0) + \phi_{r,0}) - (f(t^s + dT^s - t_0) + \phi_0^s) + N_r^s + \varepsilon_\phi \\ &= \frac{c}{\lambda}(t_r - t^s) + \frac{c}{\lambda}(dt_r - dT^s) + (\phi_{r,0} - \phi_0^s + N_r^s) + \varepsilon_\phi & \text{(cycle)} \\ \Phi_r^s &\equiv \lambda\phi_r^s = c(t_r - t^s) + c(dt_r - dT^s) + \lambda(\phi_{r,0} - \phi_0^s + N_r^s) + \lambda\varepsilon_\phi \\ &= \underbrace{\rho_r^s + c(dt_r - dT^s) - I_r^s + T_r^s}_{\text{Carrier-Phase Bias}} + \underbrace{\lambda B_r^s}_{\text{Other}} + \underbrace{d_r^s}_{\text{Correction Terms}} + \varepsilon_\phi & \text{(m)}\end{aligned}$$

Pseudorange:

$$P_r^s = \underbrace{\rho_r^s + c(dt_r - dT^s) + I_r^s + T_r^s}_{\text{Carrier-Phase Bias}} + \varepsilon_P$$

Carrier-Phase Model (2)

Carrier-Phase Bias:

$$\underline{B_r^S} = \phi_{r,0} - \phi_0^S + N_r^S \quad (\text{cycle})$$

N_r^S : Integer Ambiguity

$\phi_{r,0}$: Receiver Initial Phase

ϕ_0^S : Satellite Initial Phase

Other Correction Terms:

$$\underline{d_r^S} = -\mathbf{d}_{r,pco}^T \mathbf{e}_{r,enu}^S + \left(\mathbf{E}_{sat \rightarrow ecef} \mathbf{d}_{pco}^S \right)^T \mathbf{e}_r^S + d_{r,pcv} + d_{pcv}^S - \mathbf{d}_{disp}^T \mathbf{e}_{r,enu}^S + d_{pw} + d_{rel} \quad (\text{m})$$

$\mathbf{d}_{r,pco}$: Receiver Antenna Phase Center Offset

$d_{r,pcv}$: Receiver Antenna Phase Center Variation

\mathbf{d}_{pco}^S : Satellite Antenna Phase Center Offset

d_{pcv}^S : Satellite Antenna Phase Center Variation

\mathbf{d}_{disp} : Site Displacement

d_{pw} : Phase Wind-up Effect

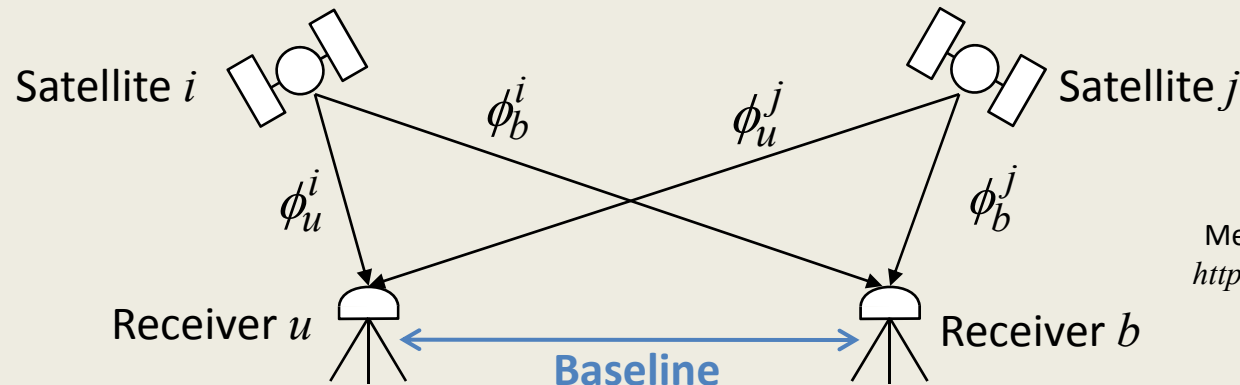
d_{rel} : Relativistic Effect

DD (Double Difference)

$$\begin{aligned}
 \Phi_{ub}^{ij} &\equiv \lambda((\phi_u^i - \phi_b^i) - (\phi_u^j - \phi_b^j)) \\
 &= \rho_{ub}^{ij} + c(dt_{ub}^{ij} - dT_{ub}^{ij}) - I_{ub}^{ij} + T_{ub}^{ij} + \lambda B_{ub}^{ij} + d_{ub}^{ij} + \varepsilon_{\Phi} \\
 &= \rho_{ub}^{ij} - I_{ub}^{ij} + T_{ub}^{ij} + \lambda N_{ub}^{ij} + d_{ub}^{ij} + \varepsilon_{\Phi} \\
 dt_{ub}^{ij} &= dt_u^{ij} - dt_b^{ij} = 0, dT_{ub}^{ij} = dT_{ub}^i - dT_{ub}^j \approx 0 \\
 B_{ub}^{ij} &= (\phi_{u,0} - \phi_0^i + N_u^i) - (\phi_{b,0} - \phi_0^i + N_b^i) - (\phi_{u,0} - \phi_0^j + N_u^j) + (\phi_{b,0} - \phi_0^j + N_b^j) = N_{ub}^{ij}
 \end{aligned}$$

(short Baseline and same antenna type)

$$\begin{aligned}
 \Phi_{ub}^{ij} &\approx \rho_{ub}^{ij} + \lambda N_{ub}^{ij} + \varepsilon_{\Phi} \\
 I_{ub}^{ij} &= I_{ub}^i - I_{ub}^j \approx 0, T_{ub}^{ij} = T_{ub}^i - T_{ub}^j \approx 0, d_{ub}^{ij} = d_{ub}^i - d_{ub}^j \approx 0
 \end{aligned}$$



Memo for Misra & Enge:
<http://gpspp.sakura.ne.jp/diary200608.htm>

Carrier-based Relative Positioning

Nonlinear-LSE:

Parameter Vector:

$$\mathbf{x} = (\mathbf{r}_u^T, N_{ub}^{s_2s_1}, N_{ub}^{s_3s_1}, \dots, N_{ub}^{s_ms_1})^T$$

Measurement Vector:

$$\mathbf{y} = (\mathbf{y}_{t_1}^T, \mathbf{y}_{t_2}^T, \dots, \mathbf{y}_{t_n}^T)^T$$

Meas Model, Design Matrix:

$$\mathbf{h}(\mathbf{x}) = (\mathbf{h}_{t_1}(\mathbf{x})^T, \mathbf{h}_{t_2}(\mathbf{x})^T, \dots, \mathbf{h}_{t_n}(\mathbf{x})^T)^T$$

$$\mathbf{H} = (\mathbf{H}_{t_1}^T, \mathbf{H}_{t_2}^T, \dots, \mathbf{H}_{t_n}^T)^T$$

Meas Error Covariance:

$$\mathbf{R} = \text{blkdiag}(\mathbf{R}_{t_1}, \mathbf{R}_{t_2}, \dots, \mathbf{R}_{t_n})$$

Solution (Static/Float):

$$\hat{\mathbf{x}} = \mathbf{x}_0 + (\mathbf{H}^T \mathbf{R}^{-1} \mathbf{H})^{-1} \mathbf{H}^T \mathbf{R}^{-1} (\mathbf{y} - \mathbf{h}(\mathbf{x}_0))$$

$$\mathbf{y}_{t_k} = (\Phi_{ub,t_k}^{s_2s_1}, \Phi_{ub,t_k}^{s_3s_1}, \dots, \Phi_{ub,t_k}^{s_ms_1})^T$$

$$\mathbf{h}_{t_k}(\mathbf{x}) = \begin{pmatrix} \rho_{u,t_k}^{s_2s_1} - \rho_{b,t_k}^{s_2s_1} + \lambda N_{ub}^{s_2s_1} \\ \rho_{u,t_k}^{s_3s_1} - \rho_{b,t_k}^{s_3s_1} + \lambda N_{ub}^{s_3s_1} \\ \vdots \\ \rho_{u,t_k}^{s_ms_1} - \rho_{b,t_k}^{s_ms_1} + \lambda N_{ub}^{s_ms_1} \end{pmatrix}$$

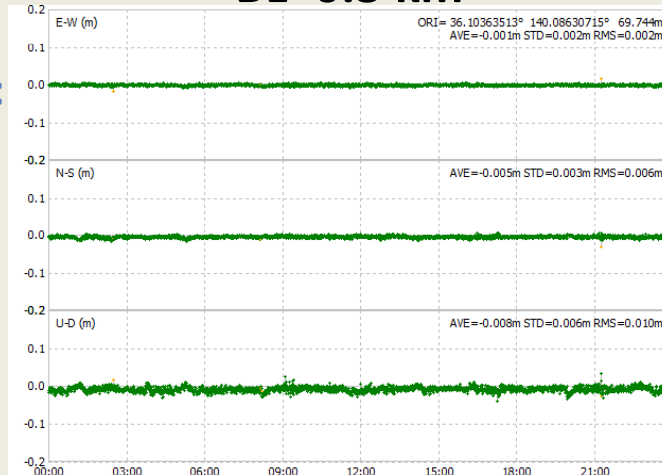
$$\mathbf{H}_{t_k} = \begin{pmatrix} -\mathbf{e}_{u,t_k}^{s_2s_1 T} & \lambda & 0 & \dots & 0 \\ -\mathbf{e}_{u,t_k}^{s_3s_1 T} & 0 & \lambda & \dots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ -\mathbf{e}_{u,t_k}^{s_ms_1 T} & 0 & 0 & \dots & \lambda \end{pmatrix}$$

$$\mathbf{R}_{t_k} = \begin{pmatrix} 4\sigma_\phi^2 & 2\sigma_\phi^2 & \dots & 2\sigma_\phi^2 \\ 2\sigma_\phi^2 & 4\sigma_\phi^2 & \dots & 2\sigma_\phi^2 \\ \vdots & \vdots & \ddots & \vdots \\ 2\sigma_\phi^2 & 2\sigma_\phi^2 & \dots & 4\sigma_\phi^2 \end{pmatrix}$$

\mathbf{r}_b : Fixed Base-Station Position

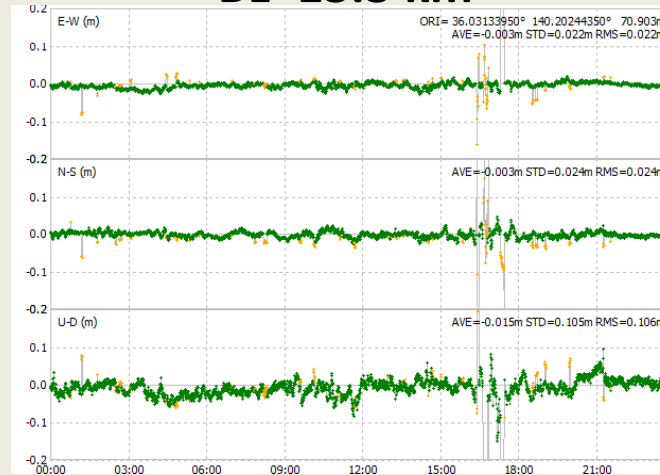
Effect of Baseline Length

BL=0.3 km



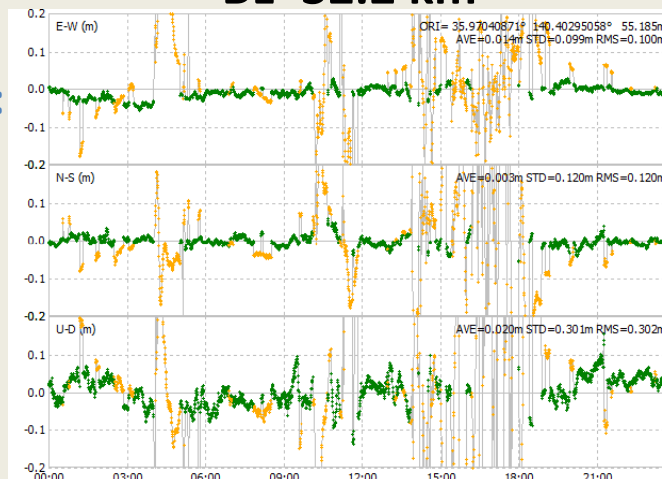
RMS Error:
E: 0.2cm
N: 0.6cm
U: 1.0cm
Fix Ratio:
99.9%

BL=13.3 km



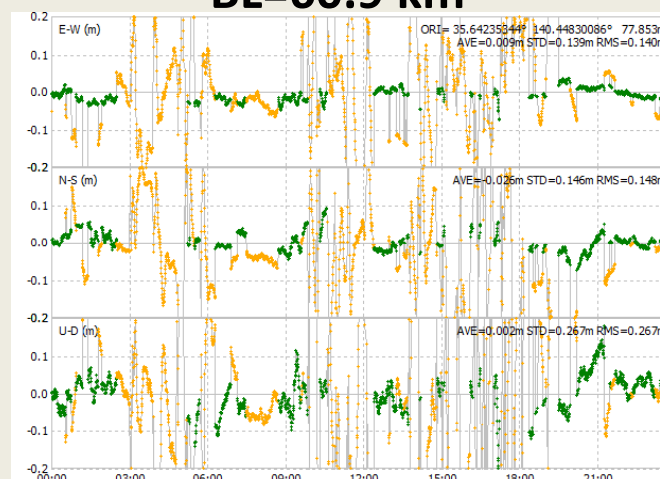
RMS Error:
E: 2.2cm
N: 2.4cm
U: 10.6cm
Fix Ratio:
94.2%

BL=32.2 km



RMS Error:
E: 10.0cm
N: 12.0cm
U: 30.2cm
Fix Ratio:
64.3%

BL=60.9 km



RMS Error:
E: 14.0cm
N: 14.8cm
U: 26.7cm
Fix Ratio:
44.4%

(24 hr Kinematic ●: Fixed Solution ●: Float Solution)

Integer Ambiguity Resolution

- **Objectives**
 - More accurate than float solutions
 - Fast converge of solutions
- **Many AR Strategies**
 - Simple Integer rounding
 - Multi-frequency wide-lane and narrow-lane generation
 - Search in coordinate domain
 - Search in ambiguity domain
 - AFM, FARA, LSAST, LAMBDA, ARCE, HB-L³, Modified Cholesy Decomposition, Null Space, FAST, OMEGA, ...

ILS (Integer Least Square Estimation)

Problem:

$$\begin{aligned} \mathbf{x} &= (\mathbf{a}^T, \mathbf{b}^T)^T, \mathbf{H} = (\mathbf{A}, \mathbf{B}) \\ \mathbf{y} &= \mathbf{H}\mathbf{x} + \mathbf{v} = \mathbf{A}\mathbf{a} + \mathbf{B}\mathbf{b} + \mathbf{v} \\ \tilde{\mathbf{x}} &= \arg \min_{\mathbf{a} \in \mathbf{Z}^n, \mathbf{b} \in \mathbf{R}^m} (\mathbf{y} - \mathbf{H}\mathbf{x})^T \mathbf{Q}_y^{-1} (\mathbf{y} - \mathbf{H}\mathbf{x}) \end{aligned}$$

Strategy:

(1) Conventional LSE

$$\hat{\mathbf{x}} = \begin{pmatrix} \hat{\mathbf{a}} \\ \hat{\mathbf{b}} \end{pmatrix} = \mathbf{Q}_x \mathbf{H}^T \mathbf{Q}_y^{-1} \mathbf{y}, \mathbf{Q}_x = \begin{pmatrix} \mathbf{Q}_a & \mathbf{Q}_{ab} \\ \mathbf{Q}_{ba} & \mathbf{Q}_b \end{pmatrix} = (\mathbf{H}^T \mathbf{Q}_y \mathbf{H})^{-1}$$

(2) **Search Integer Vector** with Minimum Squared Residuals

$$\tilde{\mathbf{a}} = \arg \min_{\mathbf{a} \in \mathbf{Z}^n} (\hat{\mathbf{a}} - \mathbf{a})^T \mathbf{Q}_a^{-1} (\hat{\mathbf{a}} - \mathbf{a})$$

(3) Improve solution

$$\tilde{\mathbf{b}} = \hat{\mathbf{b}} - \mathbf{Q}_{ba} \mathbf{Q}_a^{-1} (\hat{\mathbf{a}} - \tilde{\mathbf{a}})$$

LAMBDA

Teunissen, P.J.G. (1995)

The least-squares ambiguity decorrelation adjustment: a method for fast GPS integer ambiguity estimation. *Journal of Geodesy*, Vol. 70, No. 1-2, pp. 65-82.

- **ILS Estimation with:**

- Shrink Integer Search Space with "Decorrelation"
- Efficient Tree Search Strategy
- Similar to *Closest Point Search with LLL Lattice Basis Reduction* Algorithm

$$\check{\mathbf{a}} = \arg \min_{\mathbf{a} \in \mathbf{Z}^n} (\hat{\mathbf{a}} - \mathbf{a})^T \mathbf{Q}_a^{-1} (\hat{\mathbf{a}} - \mathbf{a})$$



$$\hat{\mathbf{z}} = \mathbf{Z}^T \hat{\mathbf{a}}, \mathbf{Q}_z = \mathbf{Z}^T \mathbf{Q}_a \mathbf{Z}$$

$$\check{\mathbf{z}} = \arg \min_{\mathbf{z} \in \mathbf{Z}^n} (\hat{\mathbf{z}} - \mathbf{z})^T \mathbf{Q}_z^{-1} (\hat{\mathbf{z}} - \mathbf{z})$$

$$\check{\mathbf{a}} = \mathbf{Z}^{-T} \check{\mathbf{z}}$$

RTK (Real-time Kinematic)

- **Technique with Carrier-based Relative Positioning**
 - Real-time Position of Rover Antenna
 - Transmit Reference Station Data to Rover via Comm. Link
 - **OTF** (On-the-Fly) Integer Ambiguity Resolution
 - Typical Accuracy: $1 \text{ cm} + 1 \text{ ppm} \times \text{BL RMS (Horizontal)}$
 - Applications:
Land Survey, Construction Machine Control, Precision Agriculture etc.



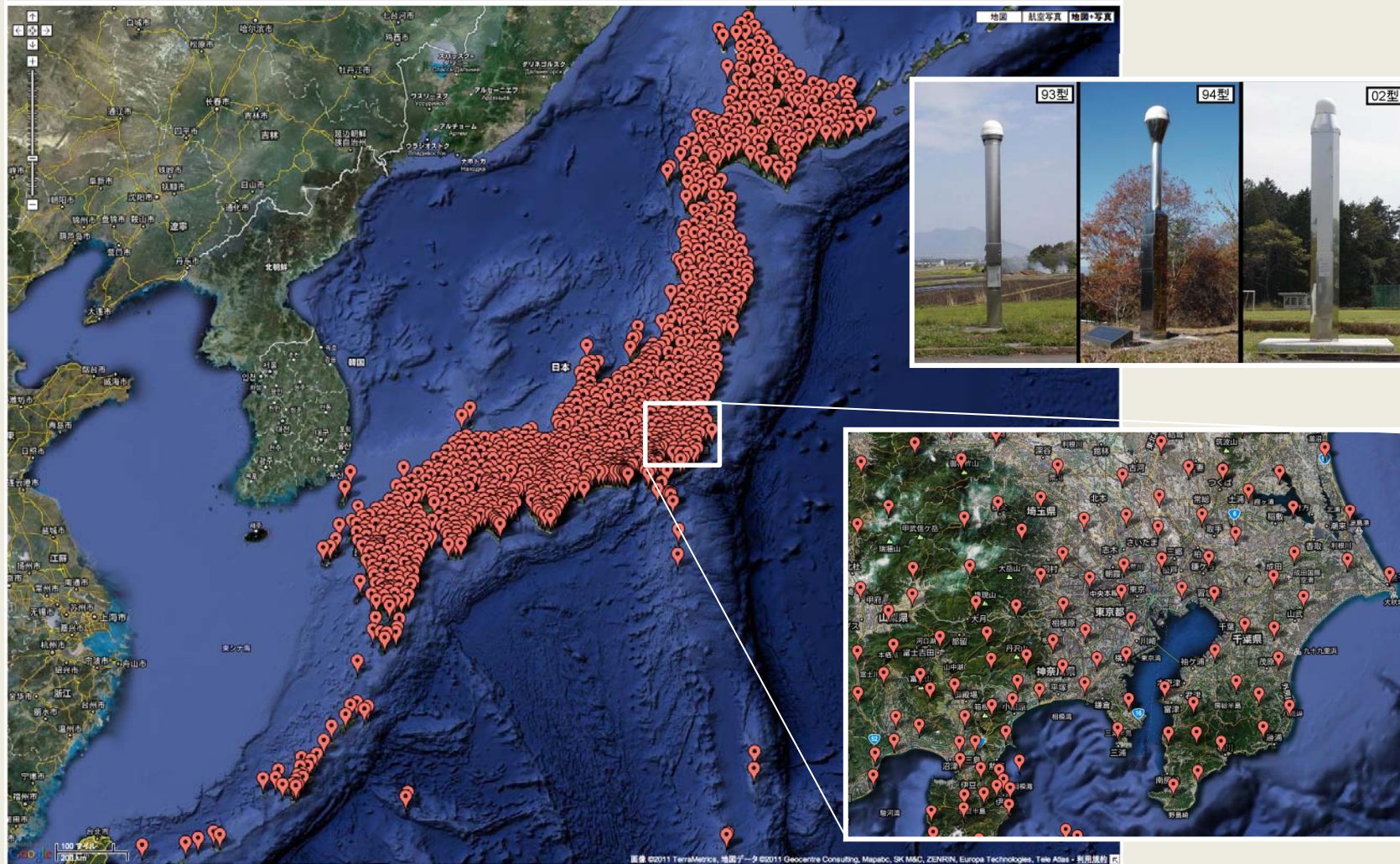
NRTK (Network RTK)

- **Extension of RTK**
 - RTK without User Reference Station
 - Sparse Networked Reference Stations
 - Correction Messages via Mobile-Phone Network
 - Format: **VRS**, **FKP**, MAC, RTCM 2.3, RTCM 3.1
 - Server S/W: Trimble GPSNet, GEO++ GNSMART, ...
 - NTRIP Networked Transport of RTCM via Internet Protocol
- **NRTK Service in Japan**
 - GEONET: ~1200 Reference Stations by GSI
 - NGDS (www.gpsdata.co.jp), JENOBAs (www.jenoba.jp)

GEONET

GEONET STATIONS MAP by Google Map : [GEONET Stations](http://geonet.stations)

IGS Map | Home



The station coordinates are based on the 72 stations on 2007/1/1 provided by GSI. Height: ellipsoidal height (WGS84)

(<http://terras.gsi.go.jp/ja/index.htm>)

5. RTK: Exercise

RTK of Driving Vehicle

- **Objective**

RTK of Driving Vehicle

- **Program**

...¥rtklib_2.4.0¥bin¥rtknavi.exe

...¥rtklib_2.4.1b¥bin¥rtknavi.exe

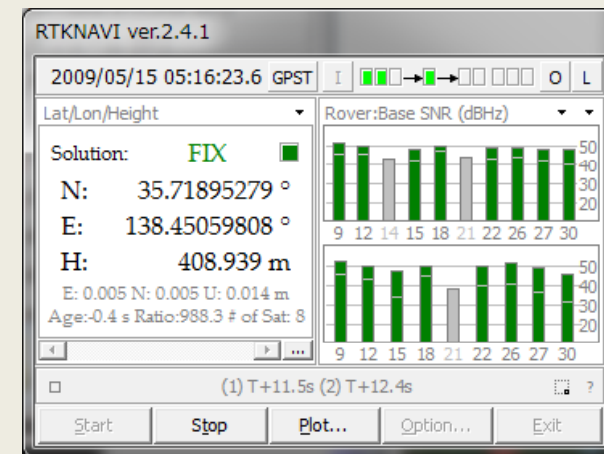
- **Data**

...¥seminar¥sample2¥

oemv_2009515c.gps (NovAtel)

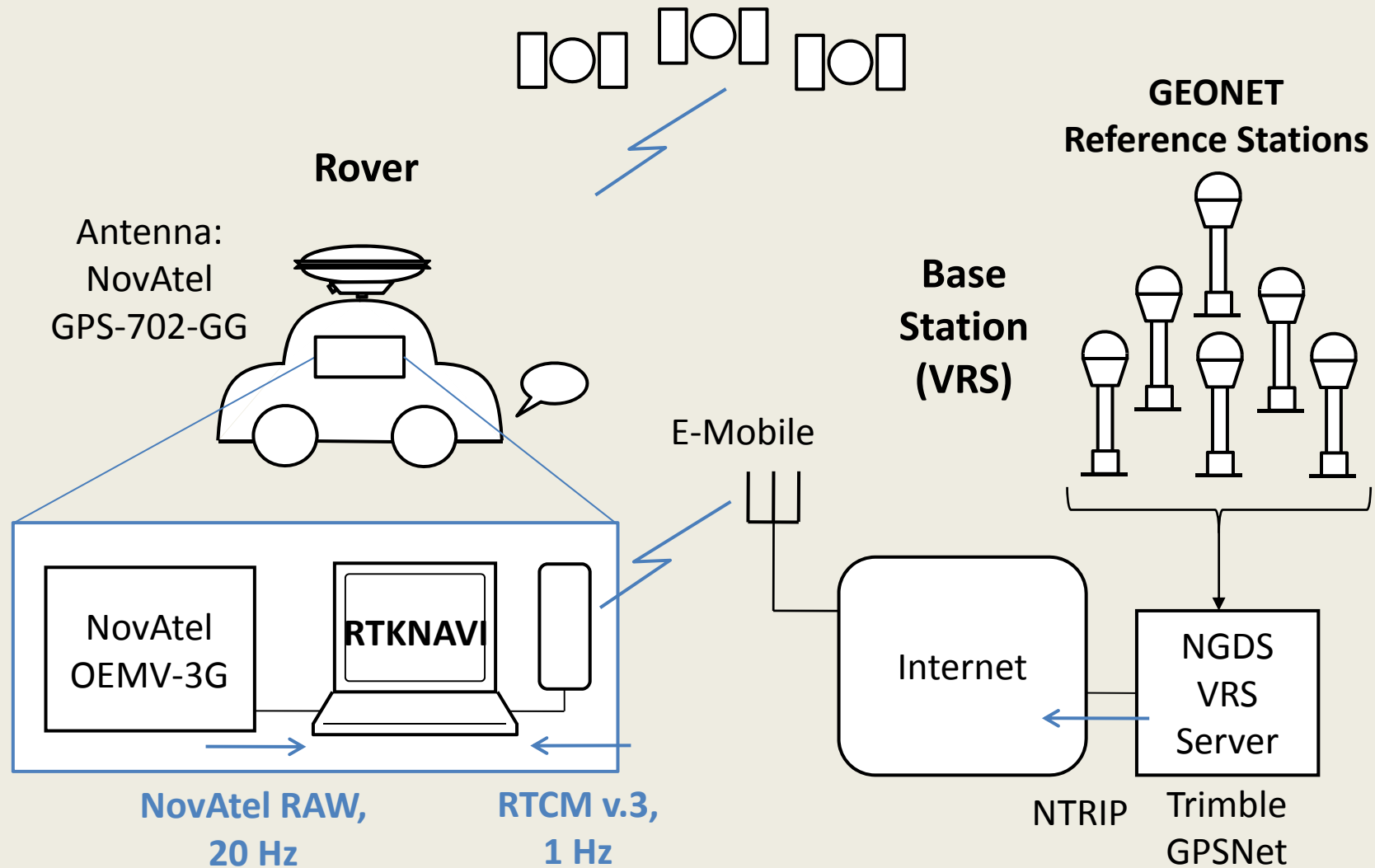
0263_20090515c.rtc3 (VRS)

RTKNAVI



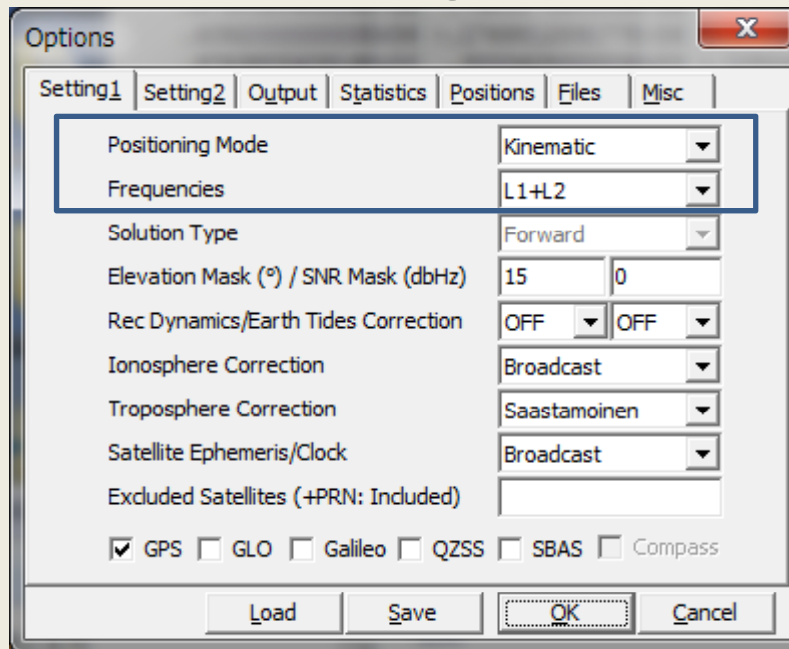
NovAtel OEMV-3G,
GPS-702-GG

RTK Configuration



RTKNAVI - Options

Setting1

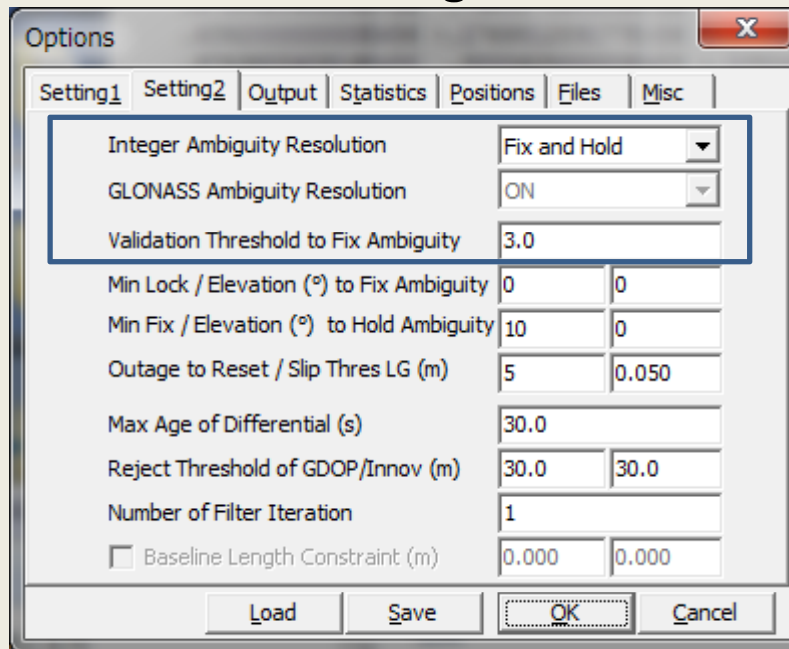


The 'Setting1' tab of the RTKNAVI Options dialog box contains the following settings:

Setting	Value
Positioning Mode	Kinematic
Frequencies	L1+L2
Solution Type	Forward
Elevation Mask (°) / SNR Mask (dbHz)	15 / 0
Rec Dynamics/Earth Tides Correction	OFF / OFF
Ionosphere Correction	Broadcast
Troposphere Correction	Saastamoinen
Satellite Ephemeris/Clock	Broadcast
Excluded Satellites (+PRN: Included)	
GPS	<input checked="" type="checkbox"/>
GLO	<input type="checkbox"/>
Galileo	<input type="checkbox"/>
QZSS	<input type="checkbox"/>
SBAS	<input type="checkbox"/>
Compass	<input type="checkbox"/>

Buttons: Load, Save, OK, Cancel

Setting2

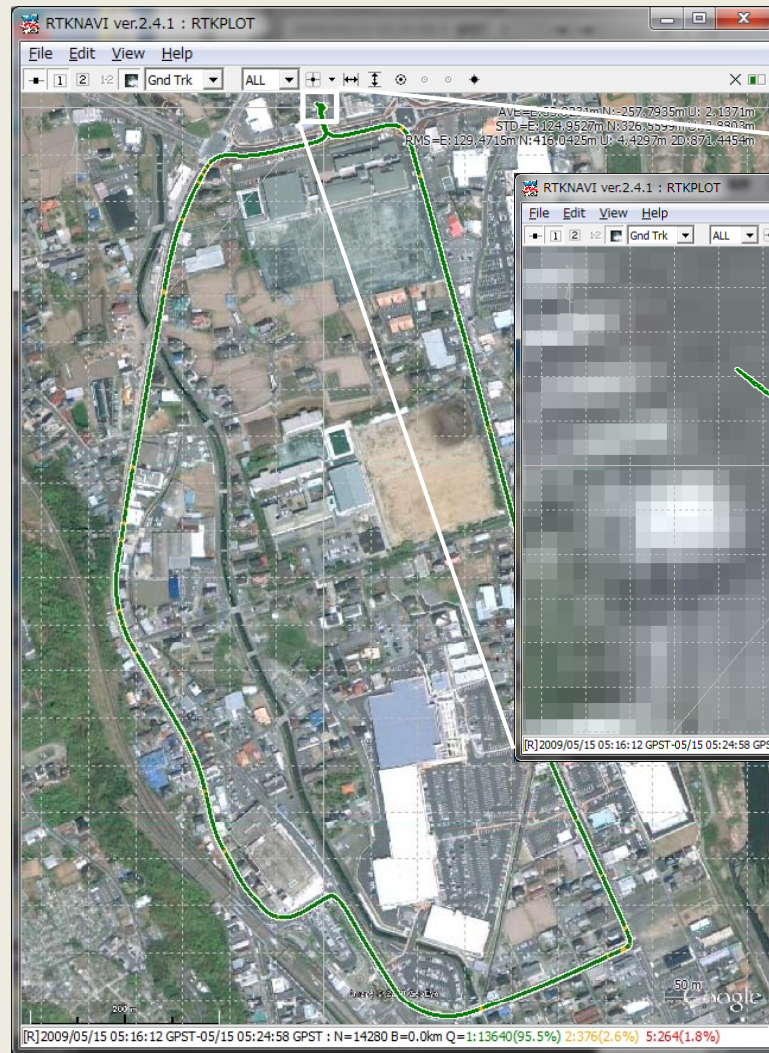


The 'Setting2' tab of the RTKNAVI Options dialog box contains the following settings:

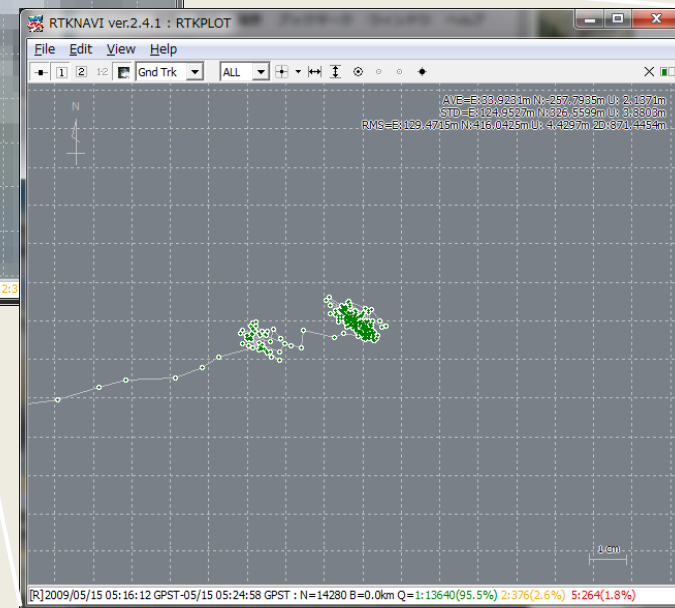
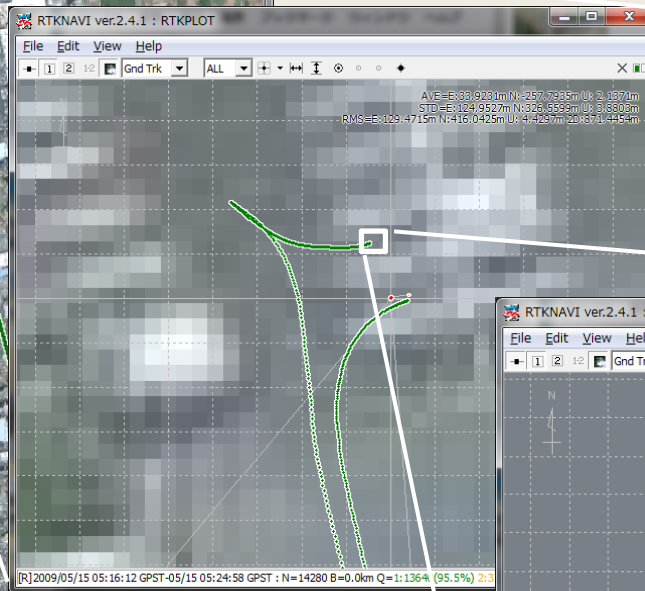
Setting	Value
Integer Ambiguity Resolution	Fix and Hold
GLONASS Ambiguity Resolution	ON
Validation Threshold to Fix Ambiguity	3.0
Min Lock / Elevation (°) to Fix Ambiguity	0 / 0
Min Fix / Elevation (°) to Hold Ambiguity	10 / 0
Outage to Reset / Slip Thres LG (m)	5 / 0.050
Max Age of Differential (s)	30.0
Reject Threshold of GDOP/Innov (m)	30.0 / 30.0
Number of Filter Iteration	1
Baseline Length Constraint (m)	0.000 / 0.000

Buttons: Load, Save, OK, Cancel

RTK Solutions



RTKPLOT 2.4.1 (Real-time Plot Mode)



6. PPP

PPP (Precise Point Positioning)

- **Feature**

- with Single Receiver (No Reference Station)
- Efficient Analysis for Many Receivers
- Precise Ephemeris
- Conventionally Post-Processing

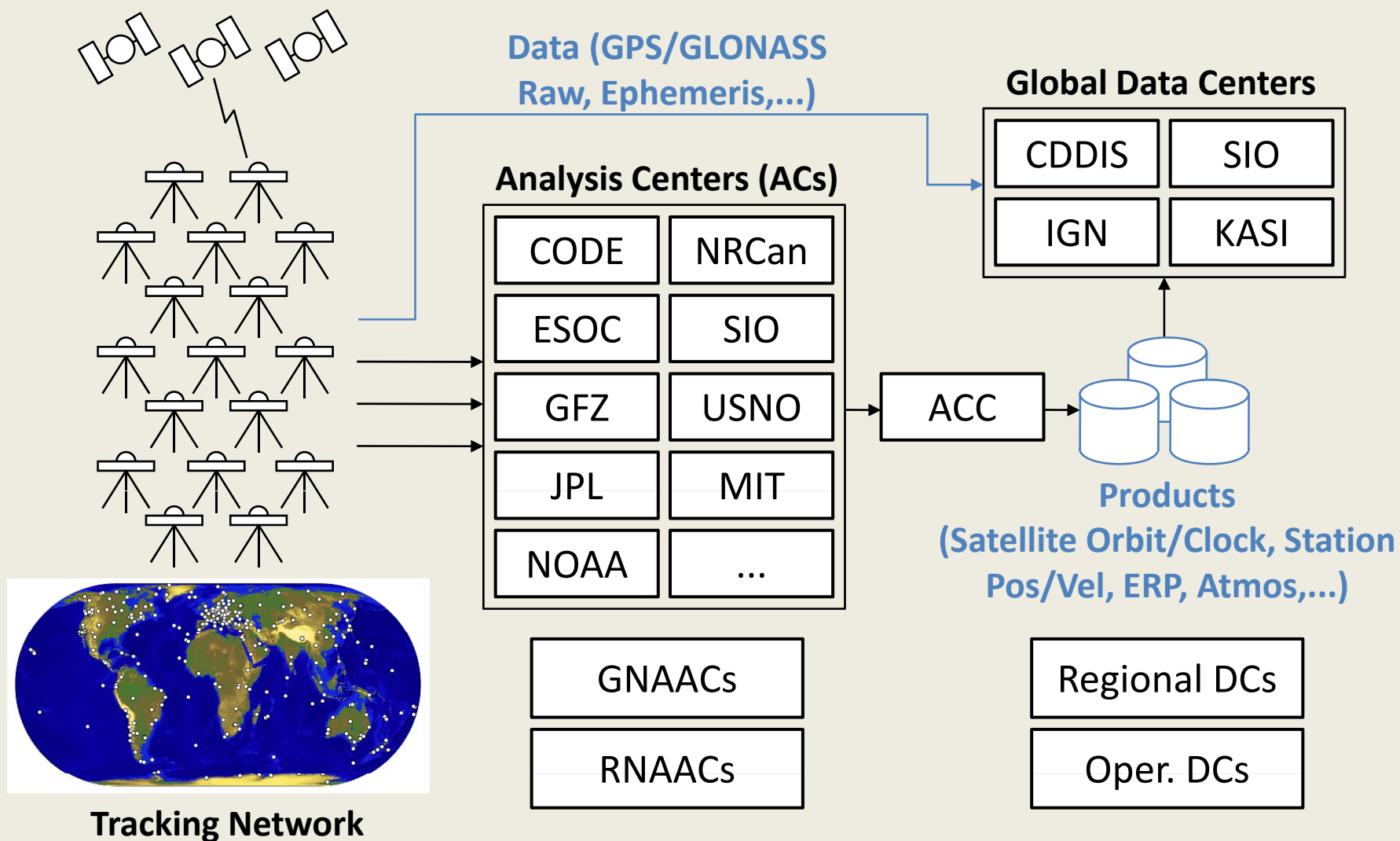
- **Applications**

- GPS Seismometer
- GPS Meteorology
- POD (Precise Orbit Determination) of LEO Satellite
- Precise Time Transfer

Precise Ephemeris

- **Precise Satellite Orbit and Clock**
 - By Post-Processing or in Real-time
 - Observation Data of Tracking Stations World-Wide
- **Data Format**
 - Orbit: NGS SP3
 - Clock: NGS SP3 or RINEX Clock Extension
- **Contents**
 - Orbit: ECEF-Positions of Satellite Mass Center
 - Clock: Clock-biases wrt Time Scale Aligned to GPS Time

IGS (International GNSS Service)



IGS Products

Product		Final (IGS)	Rapid (IGR)	Ultra-Rapid (IGU)		Broadcast
				Observed	Predicted	
Accuracy	Orbit	~2.5cm	~2.5cm	~3cm	~5cm	~100cm
	Clock	~75ps RMS ~20ps STD	~75ps RMS ~25ps STD	~150ps RMS ~50ps STD	~3ns RMS ~1.5ns STD	~5ns RMS ~2.5ns STD
Latency		12-18 days	17-41 hours	3-9 hours	realtime	realtime
Updates		every Thursday	at 17 UTC daily	at 03, 09, 15, 21 UTC	at 03, 09, 15, 21 UTC	-
Sample Interval	Orbit	15min	15min	15min	15min	daily
	Clock	Sat: 30s Stn: 5min	5min	15min	15min	daily

(2009/8, <http://igscb.jpl.nasa.gov/>)

Iono-free LC (Linear Combination)

$$C = a\Phi_1 + b\Phi_2 + cP_1 + dP_2 (\Phi_1 = \lambda_1\phi_1, \Phi_2 = \lambda_2\phi_2)$$

	LC	Coefficients				Wave Length (cm)	Ionos Effect wrt L1	Typical Noise (cm)
		<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>			
L1	L1 Carrier-Phase	1	0	0	0	19.0	1.0	0.3
L2	L2 Carrier-Phase	0	1	0	0	24.4	1.6	0.3
LC/L3	Iono-Free Phase	C_1	C_2	0	0	-	0.0	0.9
LG/L4	Geometry-Free Phase	1	-1	0	0	-	0.6	0.4
WL	Wide-Lane Phase	λ_W / λ_1	$-\lambda_W / \lambda_2$	0	0	86.2	1.3	1.7
NL	Narrow-Lane Phase	λ_N / λ_1	λ_N / λ_2	0	0	10.7	1.3	1.7
MW	Melbourne-Wübbena	λ_W / λ_1	$-\lambda_W / \lambda_2$	λ_N / λ_1	λ_N / λ_2	86.2	0.0	21
MP1	L1-Multipath	$2C_2 - 1$	$-2C_2$	1	0	-	0.0	30
MP2	L2-Multipath	$-2C_1$	$2C_1 - 1$	0	1	-	0.0	30

$$C_1 = f_1^2 / (f_1^2 - f_2^2), C_2 = -f_2^2 / (f_1^2 - f_2^2), \lambda_W = 1 / (1/\lambda_1 - 1/\lambda_2), \lambda_N = 1 / (1/\lambda_1 + 1/\lambda_2)$$

Tropospheric Model

Tropospheric Delay:

$$T = m_h(El)ZHD + m_w(El)ZWD$$

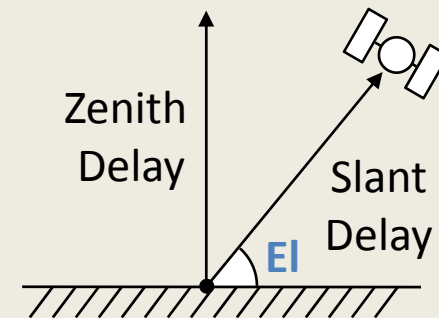
$$ZHD = \frac{0.0022768 p}{1 - 0.00266 \cos 2\phi - 2.8 \times 10^{-7} H}$$

: Zenith Hydrostatic Delay (m)

ZWD : Zenith Wet Delay (m)

$m_h(El)$: Hydrostatic Mapping Function

$m_w(El)$: Wet Mapping Function



ZWD to PWV (Precipitable Water Vapor):

$$T_m = 70.2 + 0.72T$$

$$PWV = \frac{1 \times 10^5}{R_v \left(k_2 - k_1 \frac{m_v}{m_d} + \frac{k_3}{T_m} \right)} ZWD$$

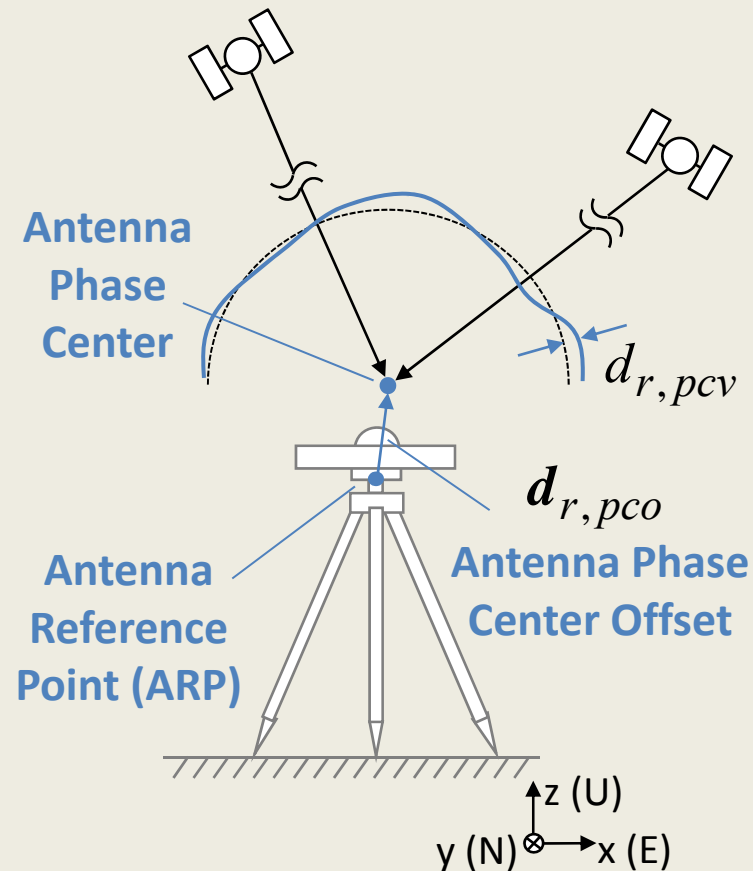
$$R_v = 461, k_1 = 77.6,$$

$$k_2 = 71.98, k_3 = 3.754 \times 10^5$$

$$m_v = 18.0152, m_d = 28.9644$$

Antenna PCV (Phase Center Variation)

Receiver Antenna Phase Center:



Antenna Phase Center Variation (PCV)

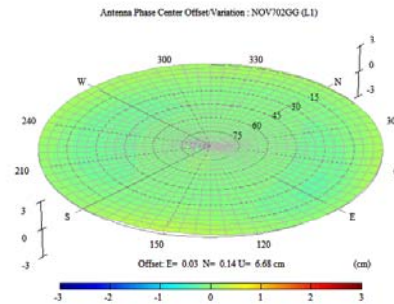
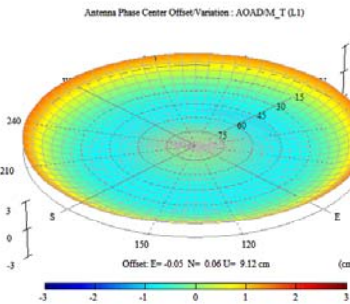
Choke-Ring Type



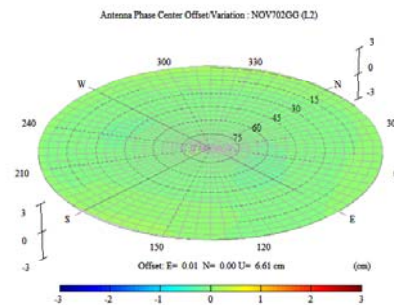
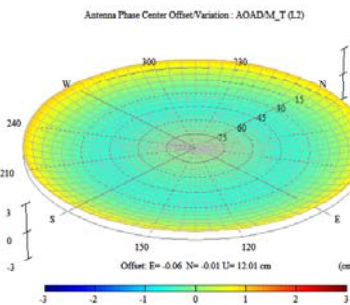
Zero-Offset Type



L1



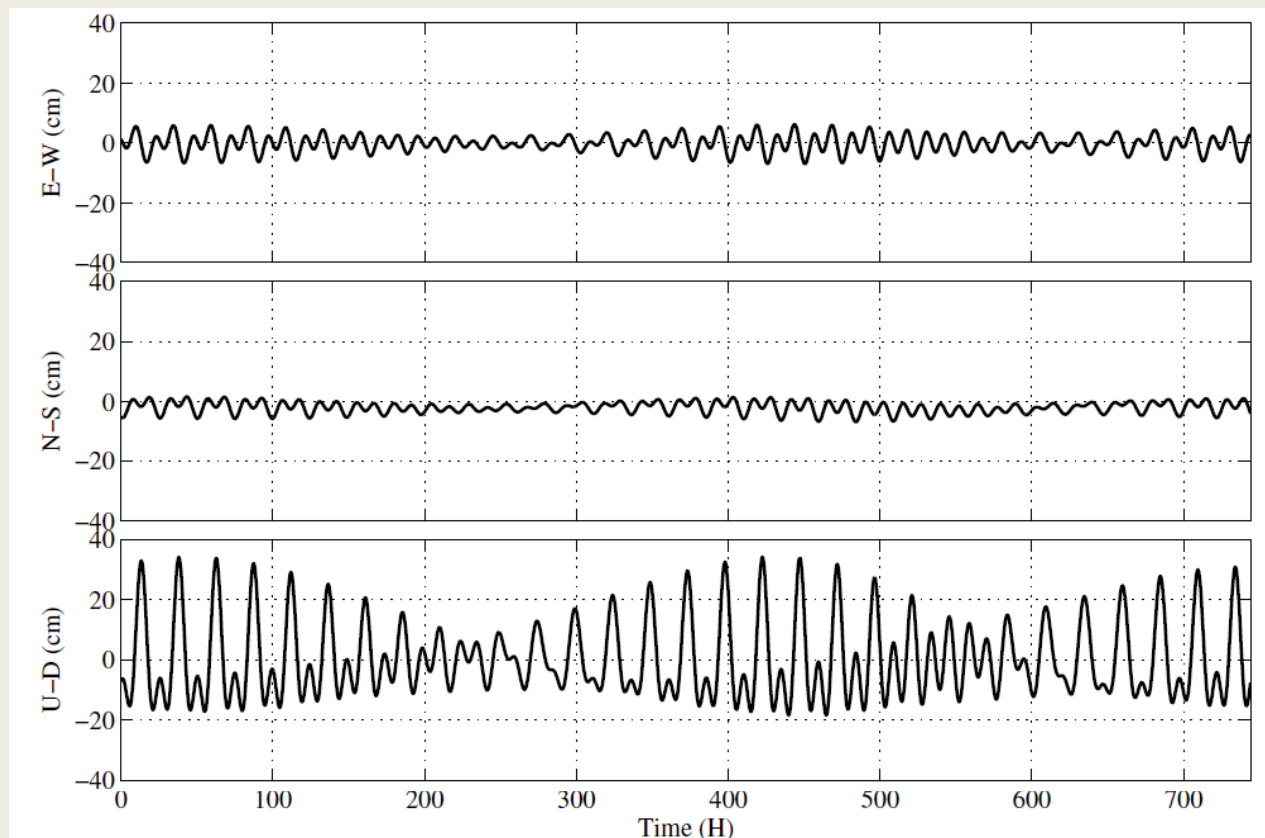
L2



IGS Absolute Antenna Model (IGS05.PCV)

Earth Tides

Solid Earth Tide, Ocean Tide Loading, Pole Tide, Atmospheric Loading

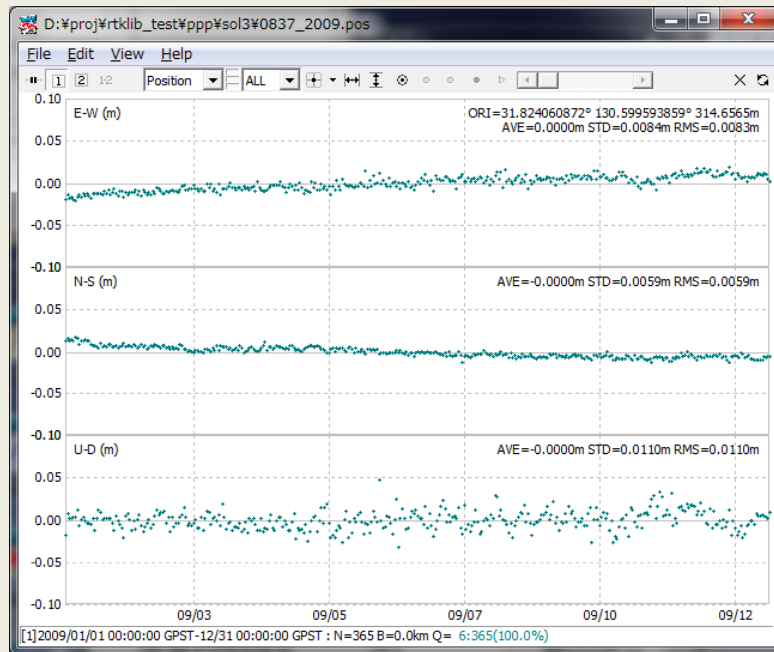


IERS Conventions 1996 + NAO99.b, 2007/1/1-1/31, TSKB

Static PPP vs Kinematic PPP

Static PPP Results

Station: GEONET 0837

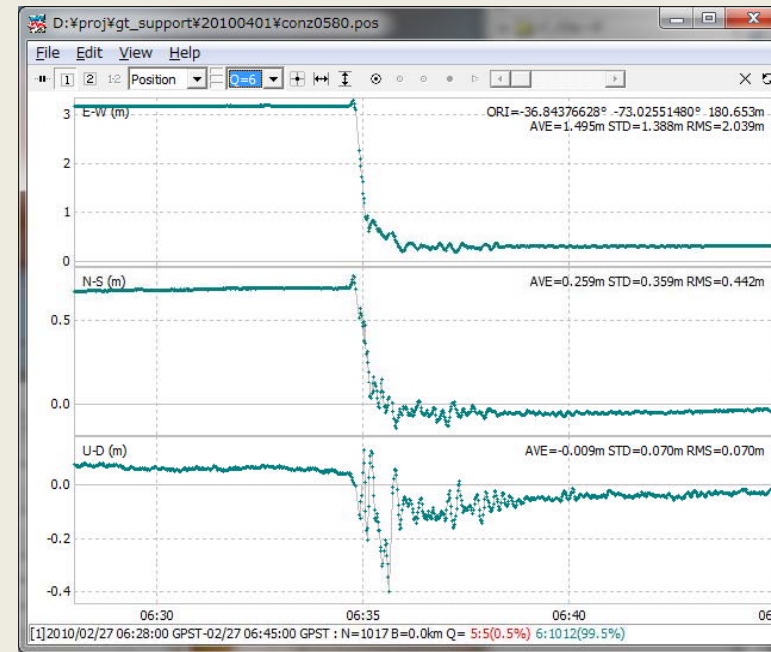


2009/1/1-2009/12/31

Interval: 1day

Kinematic PPP Results

Station: IGS CONZ



2010/2/27 6:28-6:45 GPST

Interval: 1 s

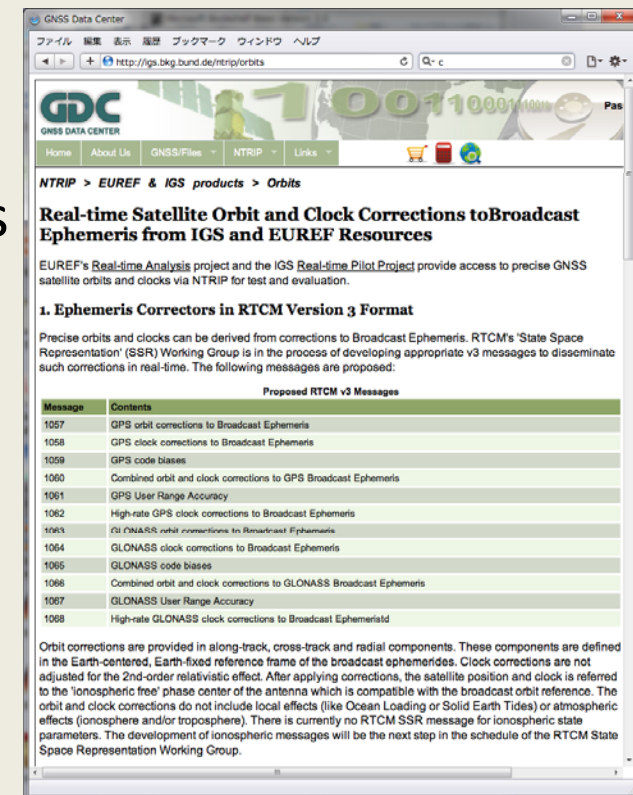
Real-time PPP

Commercial RT-PPP/GDPS Services

Service	Provider	Communication		Ref. Stations	Orbit/ Clock	Engine	Accuracy
		Coverage	Link				
StarFire	NavCom	World-wide	3 GEO L-band	60	1 min/ 1-2 s	JPL RTG	<10 cm H <15 cm V (1 sigma)
OmniSTAR XP/HP+	Fuguro	World-wide (Land)	6 GEO L-band	100	1 min/ 10 s	Fuguro	dm-class
SeaSTAR XP/G2		World-wide (Sea)	6 GEO L-band	100	1 min/ 10 s	Fuguro/ ESOC (G2)	dm-class
VERIPOS Ultra/Apex	VERIPOS	World-wide	7 GEO L-band	80	30 s/ 30 s	JPL/ ESOC	10 cm H 20 cm V (95%)

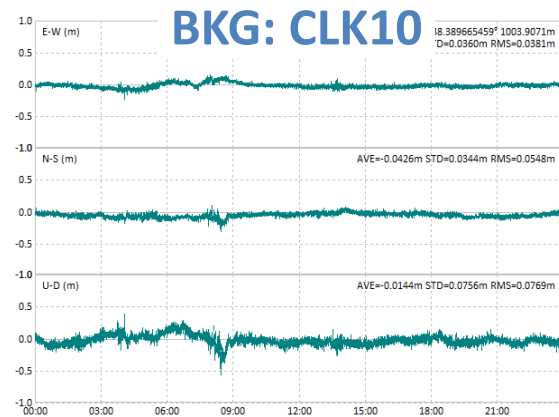
IGS Real-time Ephemeris

- **Developed by IGS-RTTP**
 - RTCM v.3 MT1057-1068 (SSR)
 - Corrections to broadcast ephemeris
 - Real-time NTRIP stream
 - Interval: 10 s, Latency: 5 - 10 s
 - GPS and GLONASS
- **Analysis Strategy**
 - Orbit: fixed to IGU or estimated
 - Clock: estimated with IGS real-time tracking network

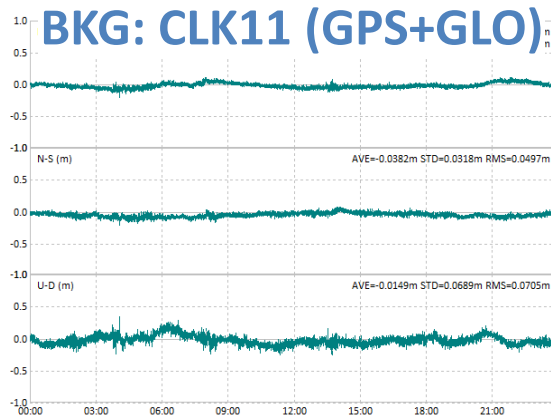


<http://igs.bkg.bund.de>

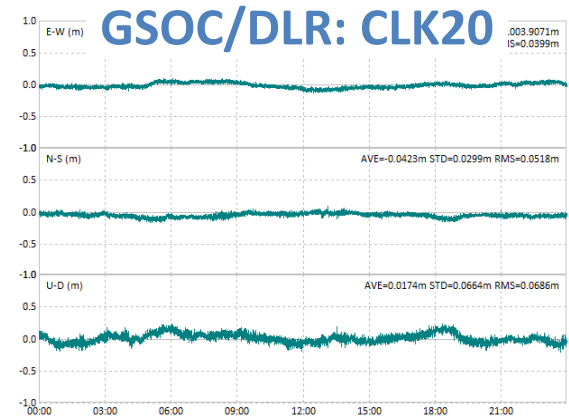
RT-PPP Performance with IGS



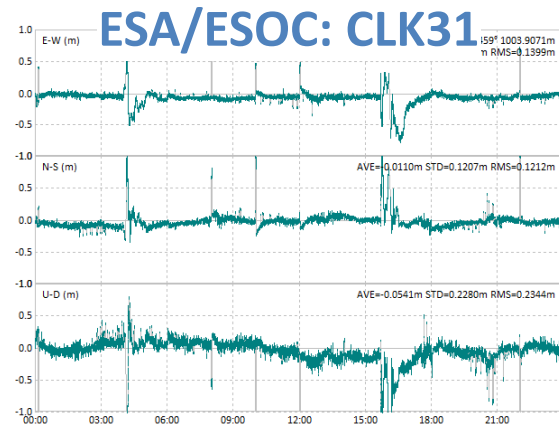
RMS: 3.8, 5.5, 7.7cm



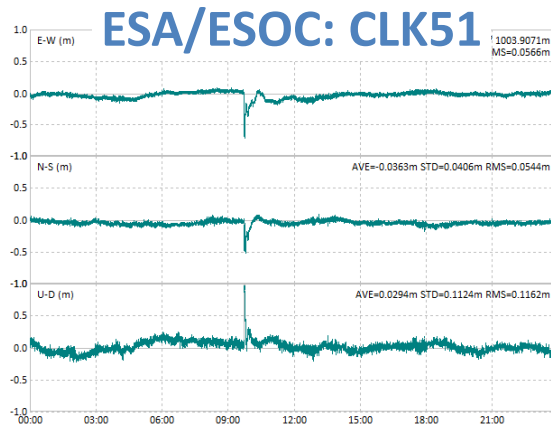
RMS: 3.8, 5.0, 7.1cm



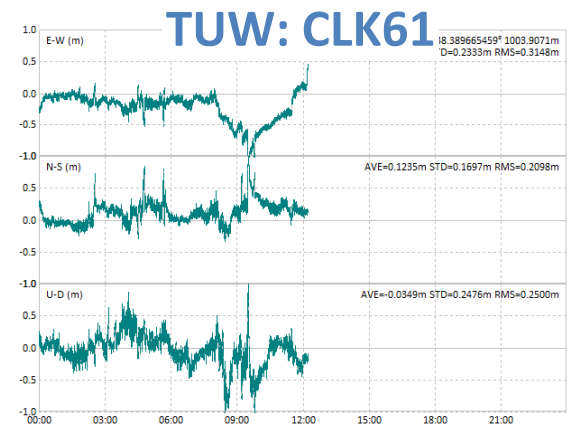
RMS: 4.0, 5.2, 6.9cm



RMS: 14.0, 12.1, 23.4cm



RMS: 5.7, 5.4, 11.6cm



RMS: 23.3, 21.0, 25.0cm

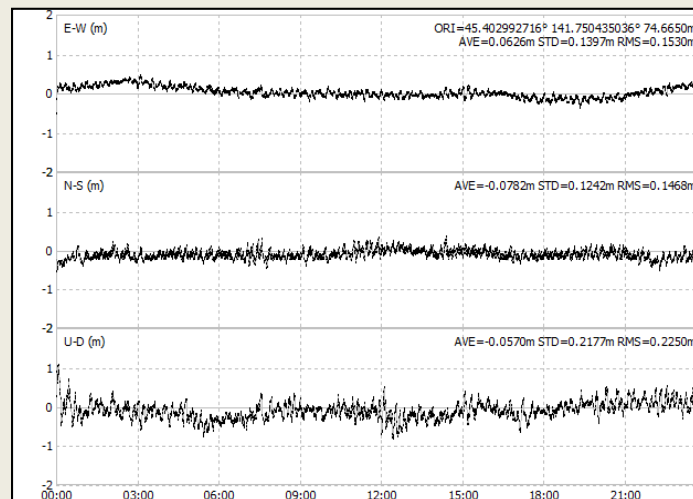
2010/9/18 0:00-23:59, 1Hz, Kinematic PPP, NovAtel OEMV-3+GPS-702, RTKLIB 2.4.1

JAXA QZSS LEX-PPP Experiment

- **Implementation for LEX-PPP user algorithm**
 - Based on Real-time PPP by RTKLIB 2.4.1
 - Support QZSS LEX Message Type 10, 11
 - Support LEX-Receiver (Furuno LPY-10000) Message
- **Preliminary Evaluation**

GEONET 0001 Wakkanai,
2010/8/3 0:00:00-23:59:30

**RMS Error E/N/U:
15.2, 14.2, 21.6 cm
(Dual Frequency)**



(T.Takasu, Space Sciences and Technology Conference , 2011)

6. PPP: Exercise

PPP Analysis for Reference Point

- **Objective**

PPP Analysis for Reference Point

- **Program**

...¥rtklib_2.4.0¥bin¥rtkpost.exe

...¥rtklib_2.4.1b¥bin¥rtkpost.exe

- **Data**

...¥seminar¥sample4¥

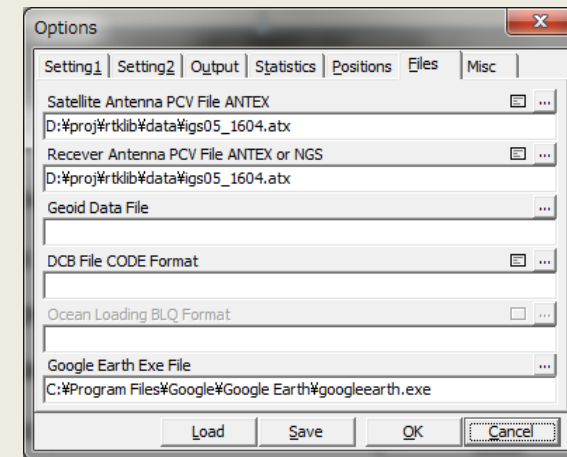
09160700.11o, 09160700.11n (RINEX)

21100700.11o, 21100700.11n (RINEX)

igs16265.sp3 (Precise Orbit)

igs16265.clk_30s (Precise Clock)

RTKPOST



Date:

2011/3/11 GPST
(GPS week 1626-5, DOY 070)

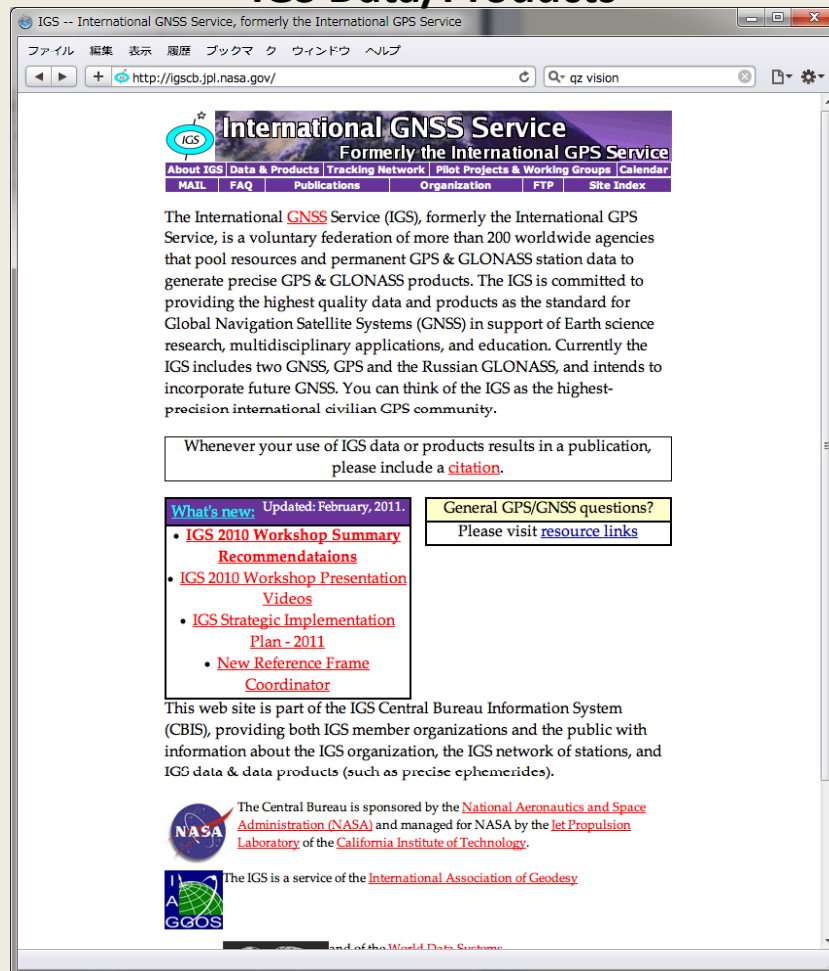
GEONET Station:

020916: Minamikata
92110: Tsukuba

Acknowledgment: Sample Data are provided by GSI and IGS

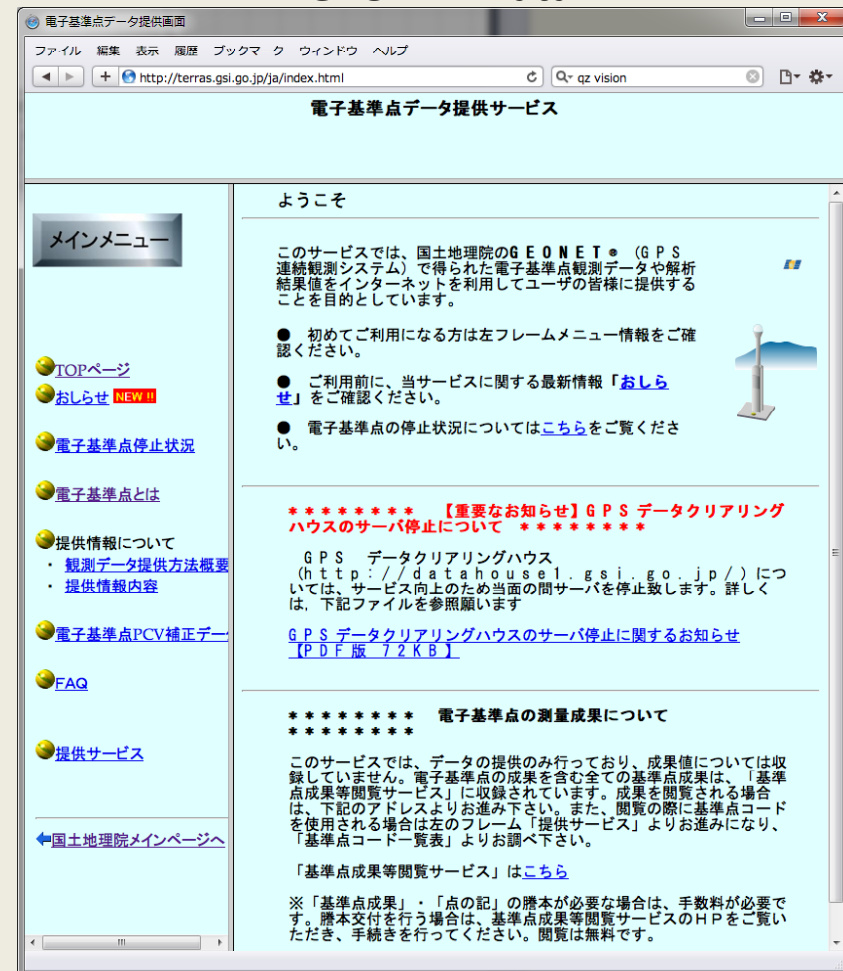
Online GNSS Data Sources

IGS Data/Products



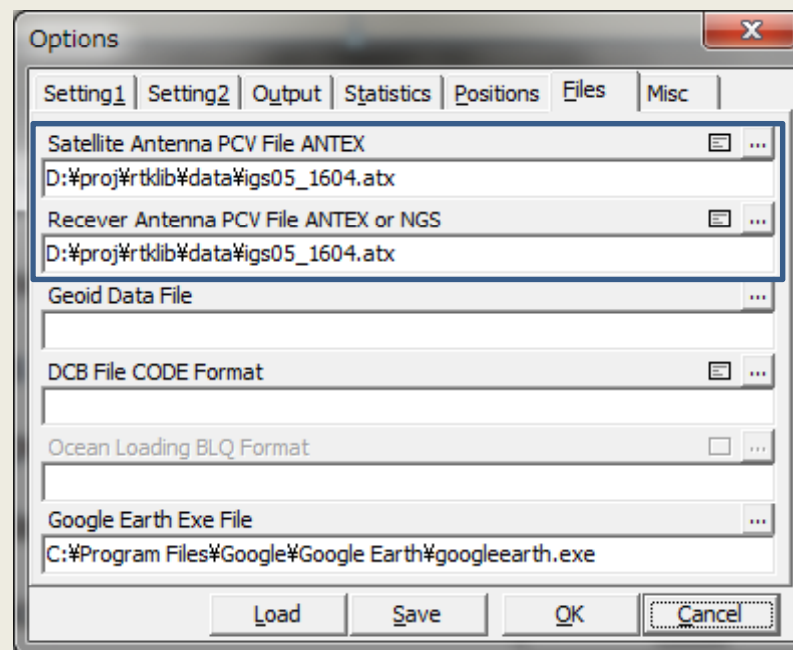
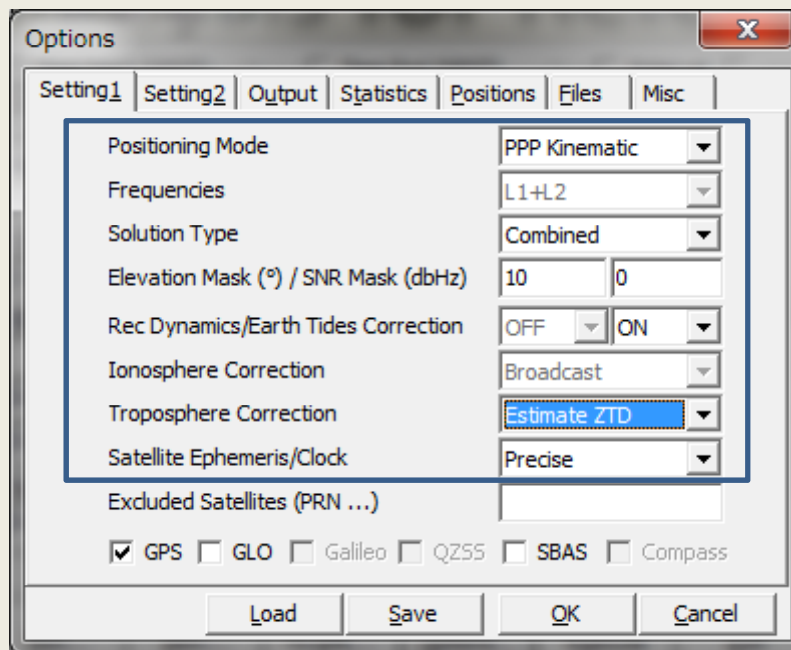
<http://igscb.jpl.nasa.gov>

GEONET Data



<http://terras.gsi.go.jp/ja/index.html>

RTKPOST - Options



7. RTK System

RTK Application



Geodetic Survey



Construction
Machine Control



Precision Agriculture



ITS (Intelligent
Transport System)



Mobile Mapping
System



Sports

Considerations for RTK System

- **Rover**
 - Single vs. Dual-freq, Update Rate, GNSS, Receiver-cost
 - CPU Power for external processing
 - INS-integration for obstacles
- **Reference Station**
 - Baseline-Length vs. Performance
 - Self-provided vs. NRTK Service
 - Coverage, Receiver-cost, Operational-cost, Service-fee
- **Communication Link**
 - Coverage, Band-width, Latency, Link-cost

CPU-power, Bandwidth, Latency

- **CPU-power**

- ~2 ms/epoch for dual-freq RTK on Intel Core 2 Q 2.4 GHz
- ~20ms/epoch for single-freq RTK on ARM 600 MHz
- H/W DP floating-point is necessary

- **Bandwidth**

- ~3 kbps for 1 Hz GPS only, RTCM 3
- ~20 kbps for 1 Hz GPS+GLO+QZS+SBAS, JAVAD GREIS

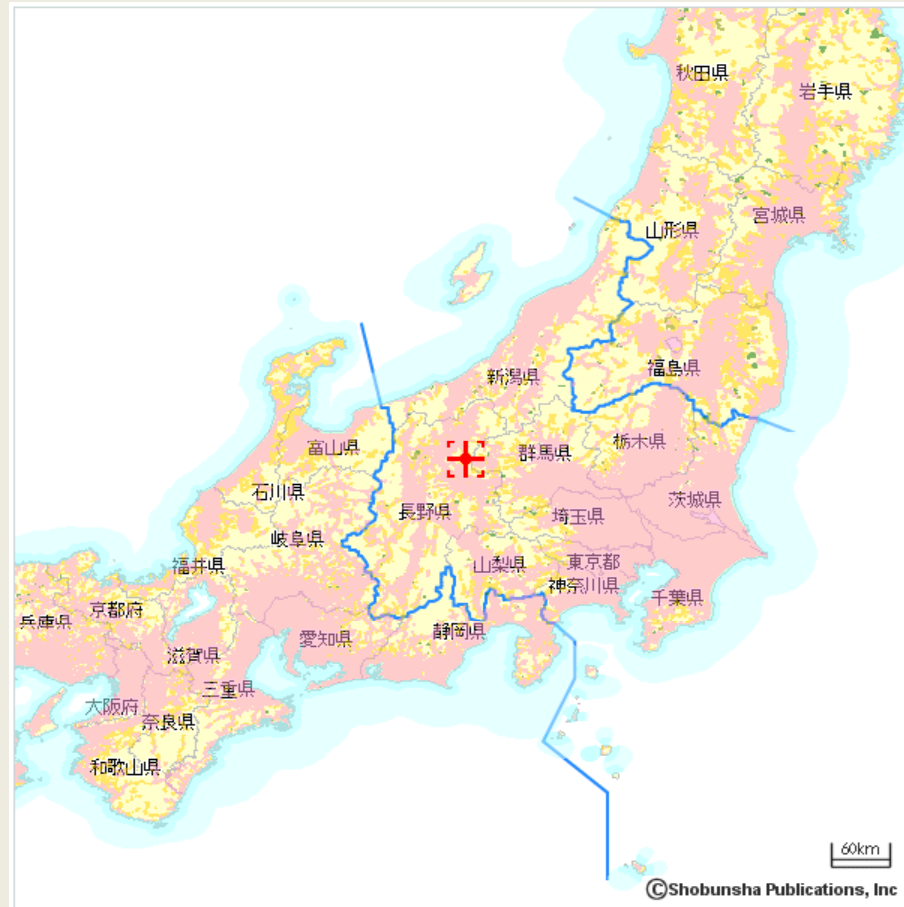
- **Latency**

- > 5 s Latency degrades RTK performance
- "Low-latency" vs. "Matched" Solution

Communication Link for RTK

- **Local (<300 m)**
 - Serial, USB, LAN, ... (wired)
 - Radio Modem, WiFi, ZigBee, DSRC, ... (wireless)
- **Regional (<1,000 km)**
 - Analog-phone, ISDN, Dedicated Link, ... (wired)
 - Mobile-phone (Analog, 2G, 3G, ...), ... (wireless)
- **Global (<10,000 km)**
 - Internet
 - GEO Satellite Link (Inmarsat, WideStar II, ...)
 - LEO Satellite Link (Iridium, Orbicom, ...)

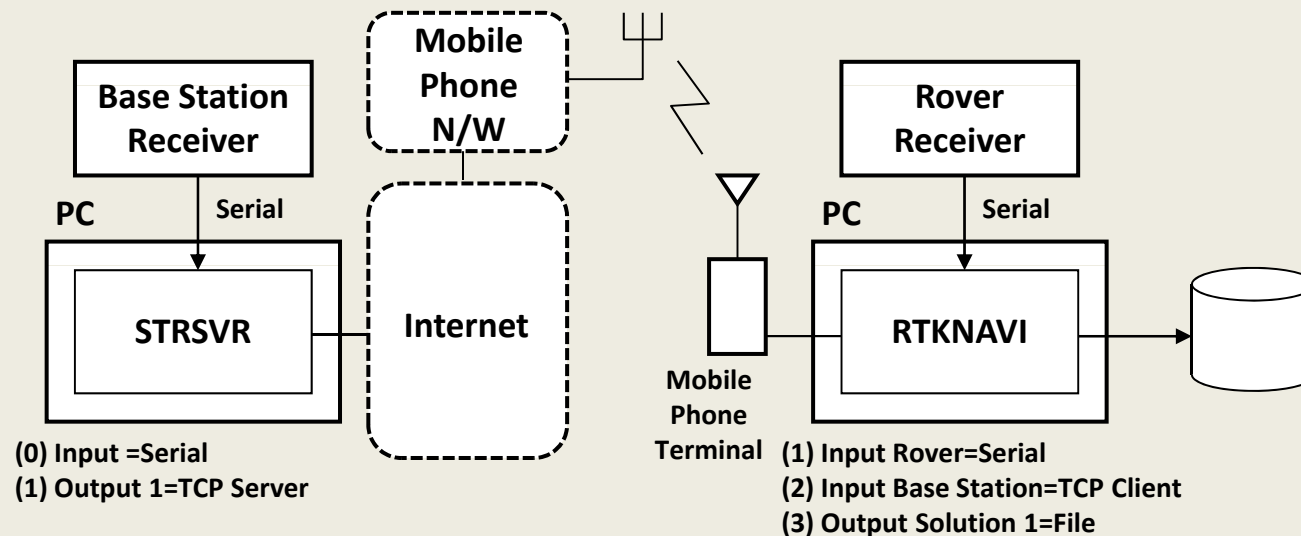
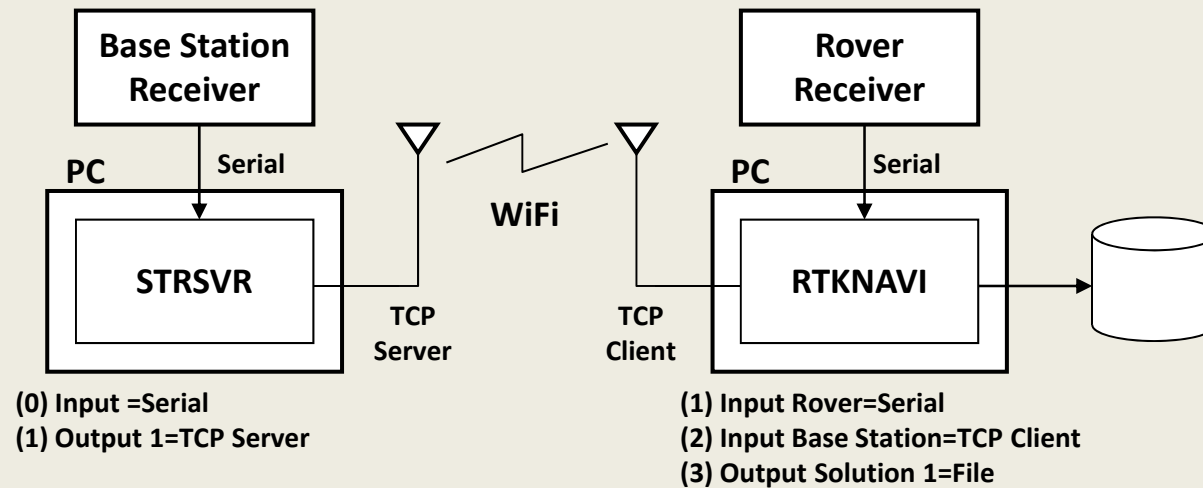
Coverage by Mobile-phone N/W



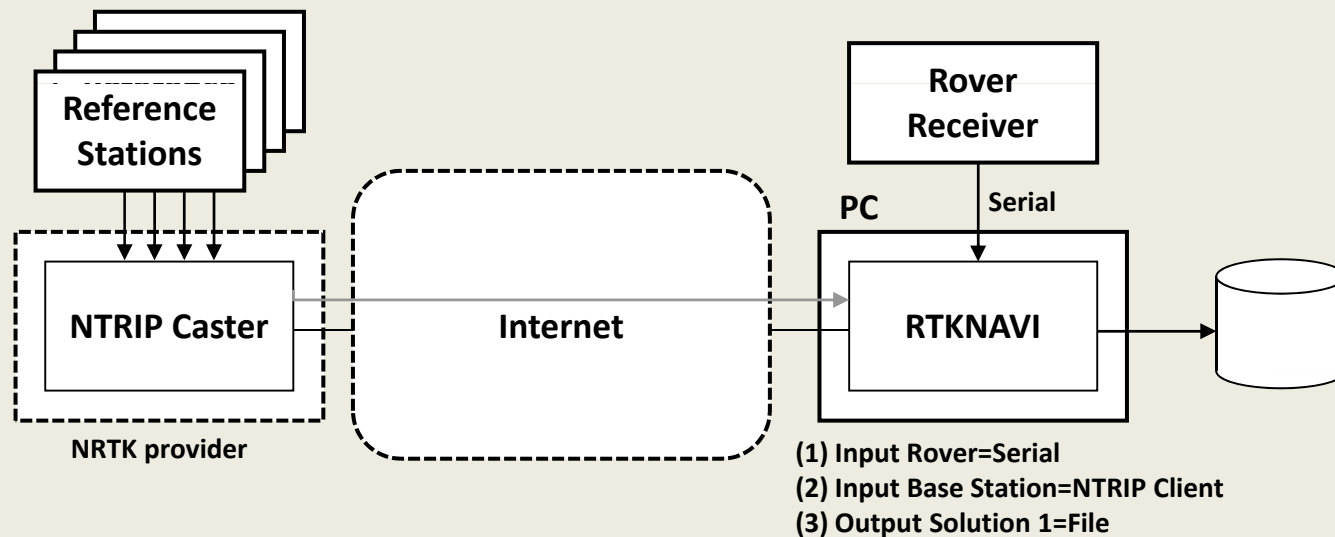
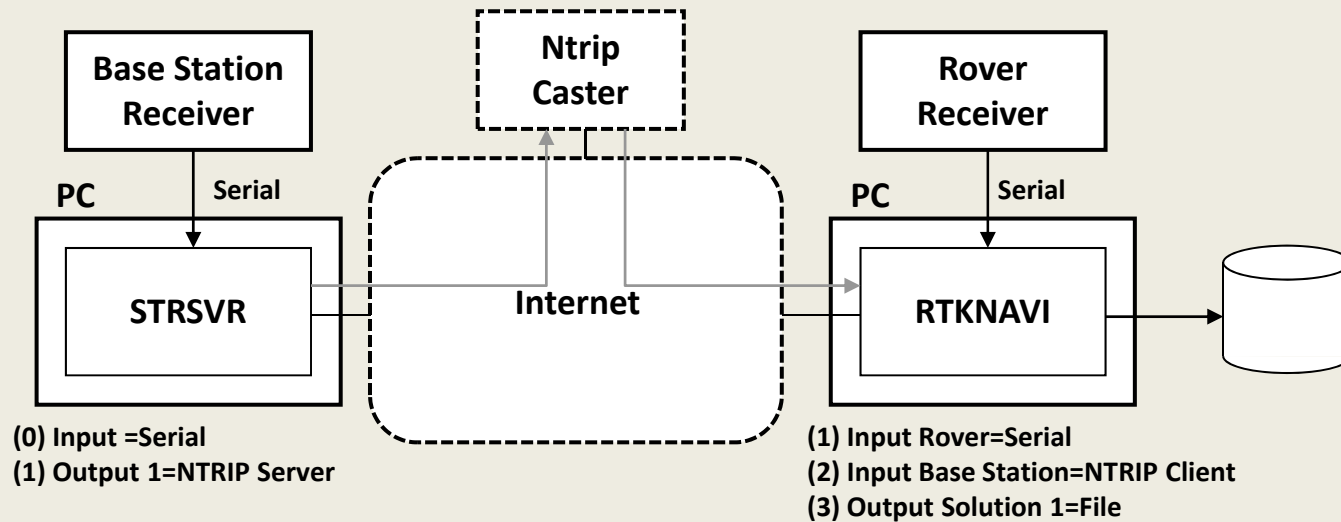
NTT docomo FOMA (2008/9)

(<http://servicearea.nttdocomo.co.jp>)

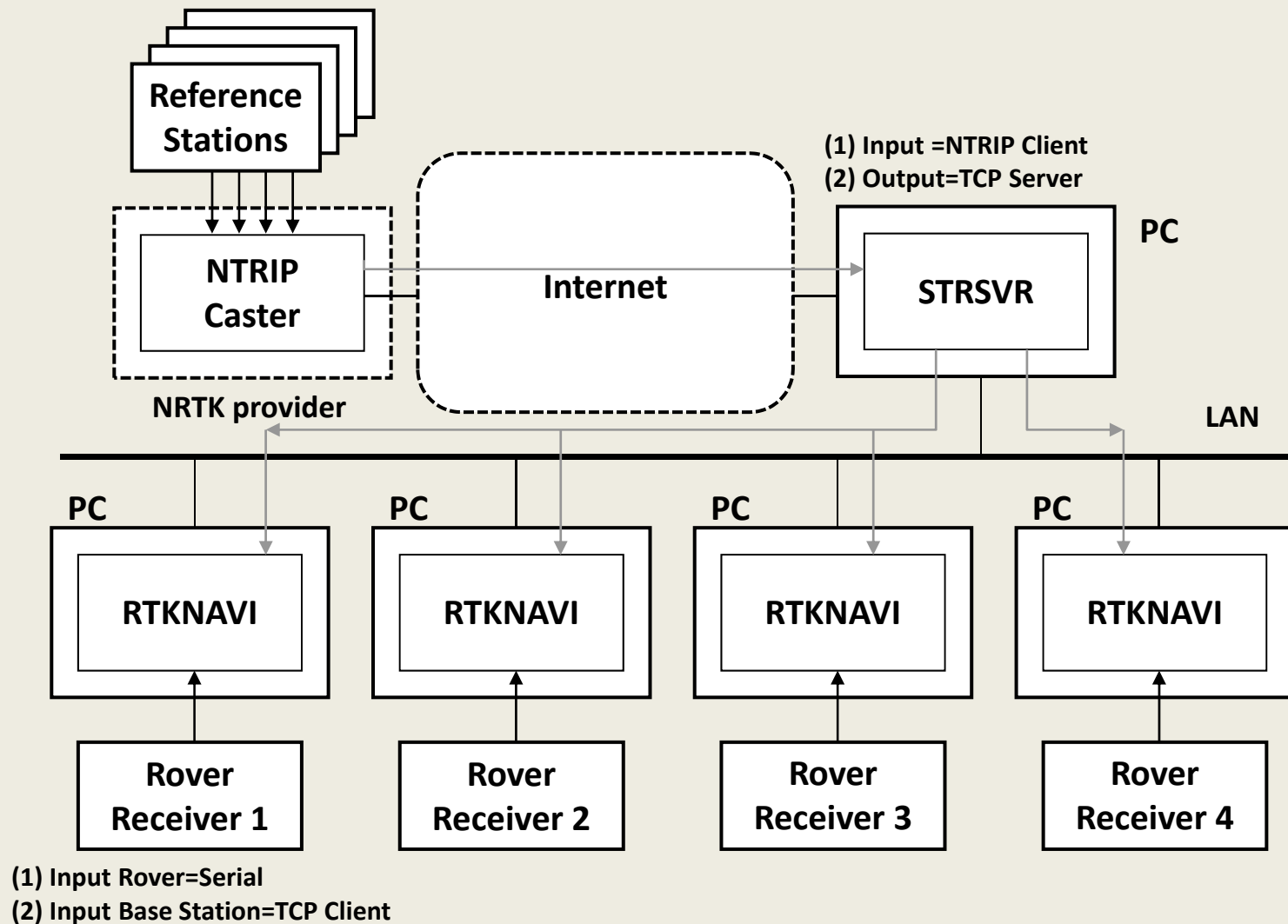
RTK Configurations (1)



RTK Configuration (2)



RTK Configuration (3)



7. RTK System: Exercise

Communication Link for RTK

- **Objective**

Network Connection for RTK

- **Program**

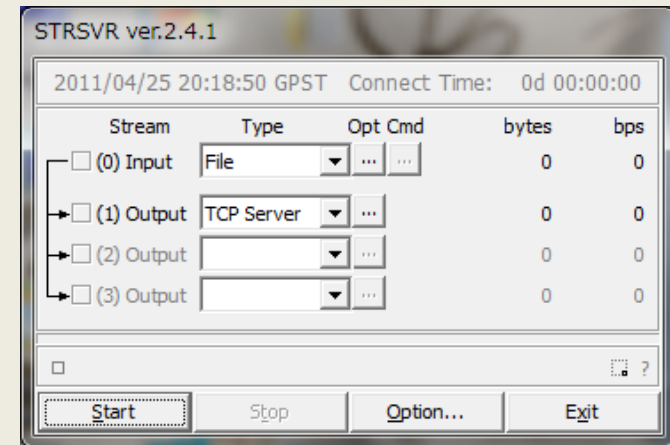
...¥rtklib_2.4.1b¥bin¥rtknavi.exe

...¥rtklib_2.4.1b¥bin¥strsvr.exe

- **Stream (TCP Client)**

JAV1: 192.168.1.173: 2101 (Format: Javad)

JAV2: 192.168.1.173: 2102 (Format: Javad)



STRSVR

Acknowledgment:

Sample data were captured by JAVAD DELTA and FURUNO LPY-10000 receiver provided by JAXA

Network Configuration

RTKNAVI 2.4.1b (TCP Client)

STRSVR (TCP server)

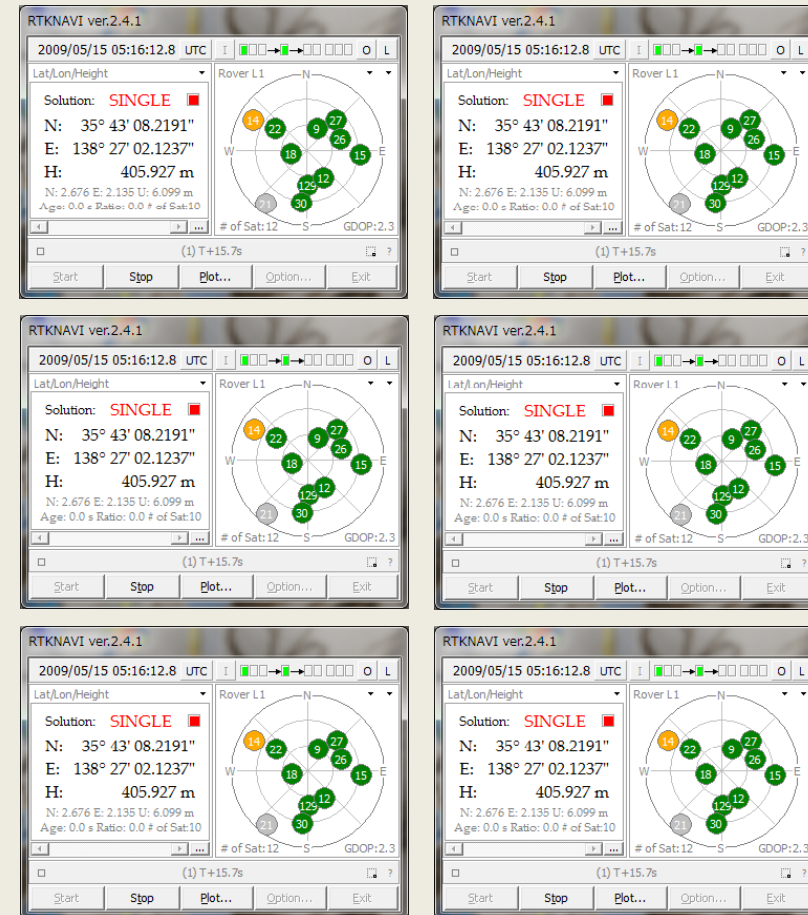
Javad

Javad

Format:
Javad
Javad

192.168.1.173:2101 (Javad1)

192.168.1.173:2102 (Javad2) Javad2: 35.666496867 139.792366358 59.3696



8. Advanced Topics

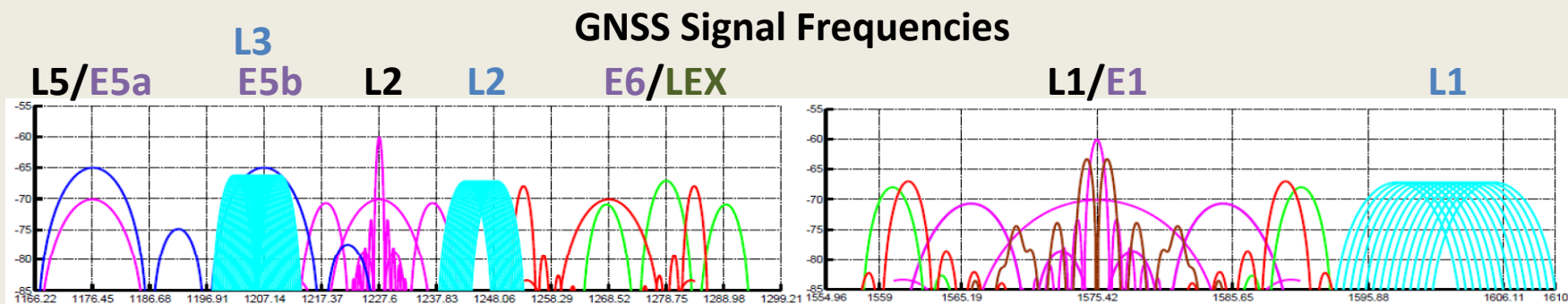
Advanced Topics

- **Multi-GNSS RTK**
- **Long-Baseline RTK**
- **INS-Aided RTK**
- **Ambiguity Resolution for PPP**
- **"CM-Accuracy Anywhere"**

GNSS Evolution

Number of Planned GNSS Satellites

System	2010	2013	2016	2019
GPS	31	32	32	32
GLONASS	23 (+2)	24 (+3)	24 (+3)	24 (+3)
Galileo	0	4	18	27 (+3)
Compass	6	12	30	32 (+3)
QZSS	1	1	7	7
IRNSS	0	7	7	7
SBAS	7	8	11	11
Total	68	88	129	140



(Y.Yang, COMPASS: View on Compatibility and Interoperability, 2009)

Multi-GNSS RTK Performance

RTK Performance: Baseline 13.3 km, Instantaneous AR

		El Mask=15°				El Mask=30°			
GPS	Galileo	Fixing Ratio	RMS Error (cm)			Fixing Ratio	RMS Error (cm)		
			E-W	N-S	U-D		E-W	N-S	U-D
L1	-	49.7%	4.6	8.1	19.0	23.3%	71.4	115.0	289
GPS L1+L2	-	99.0%	1.4	1.3	1.9	87.6%	3.4	10.5	15.5
L1,L2,L5	-	99.0%	1.4	1.3	1.9	87.3%	3.4	10.5	15.6
L1	E1	98.8%	1.3	1.2	1.9	90.1%	1.2	2.1	2.7
GPS+GAL L1	E1	98.9%	1.4	1.2	1.7	98.7%	1.2	1.0	1.6
L1,L2	E1	98.9%	1.4	1.2	1.7	98.7%	1.2	1.0	1.6
L1,L2,L5	E1,E5a, E5b	98.9%	1.5	1.3	2.0	98.9%	1.3	1.1	1.8

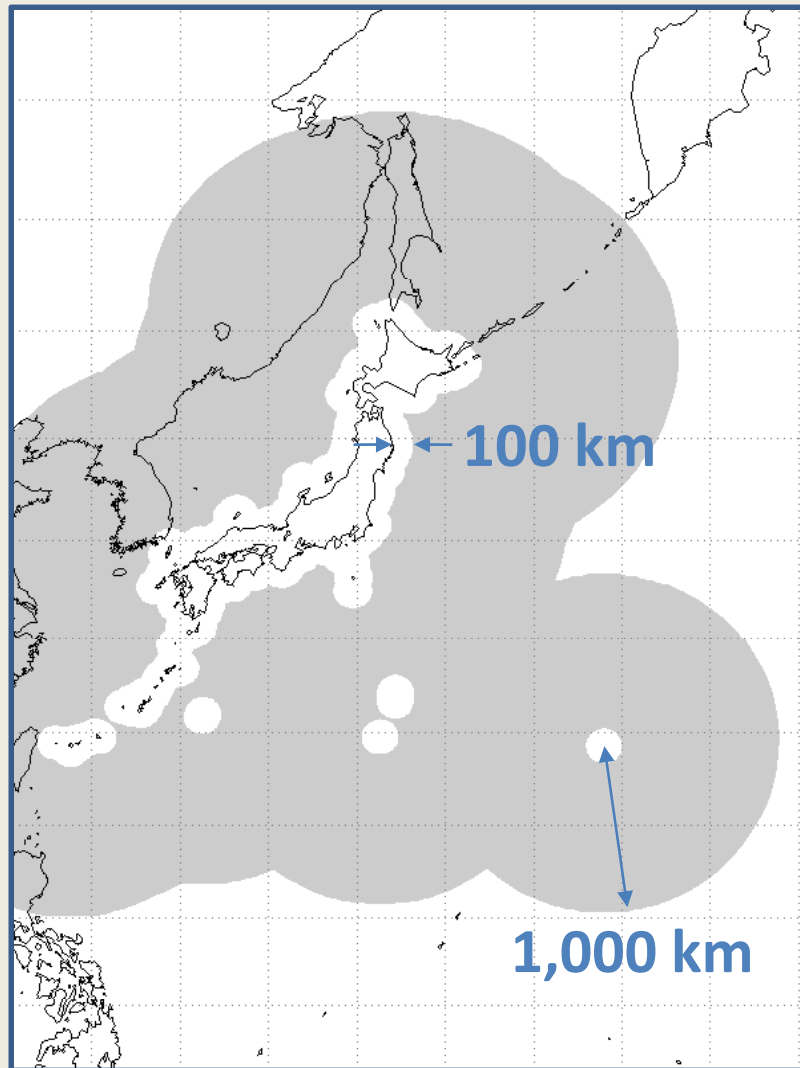
Multi-GNSS Receiver

- **Moore's Law**
 - More correlators
 - More tracking channels
 - More powerful embedded CPU
- **Consumer-grade Multi-GNSS Receiver**
 - SkyTraq: GPS + GLONASS
 - STMicro: GPS + GLONASS
 - Broadcom: GPS + GLONASS + QZSS
 - u-blox: GPS + Galileo

Issues for Multi-GNSS RTK

- **Multi-GNSS Integration Issue**
 - Time-system, Coordinate-system
 - Receiver H/W Biases
- **Multi-code System Issue**
 - L1C/A-L1P(Y)-L1Cd-L1Cp, L2P(Y)-L2C, L5I-L5Q
 - Quarter cycle phase-shift problem
- **GLONASS FDMA Issue**
 - Receiver Inter-channel biases (Receiver Interoperability)
 - Calibration Message Standard
 - Antenna Calibration

Long-Baseline RTK



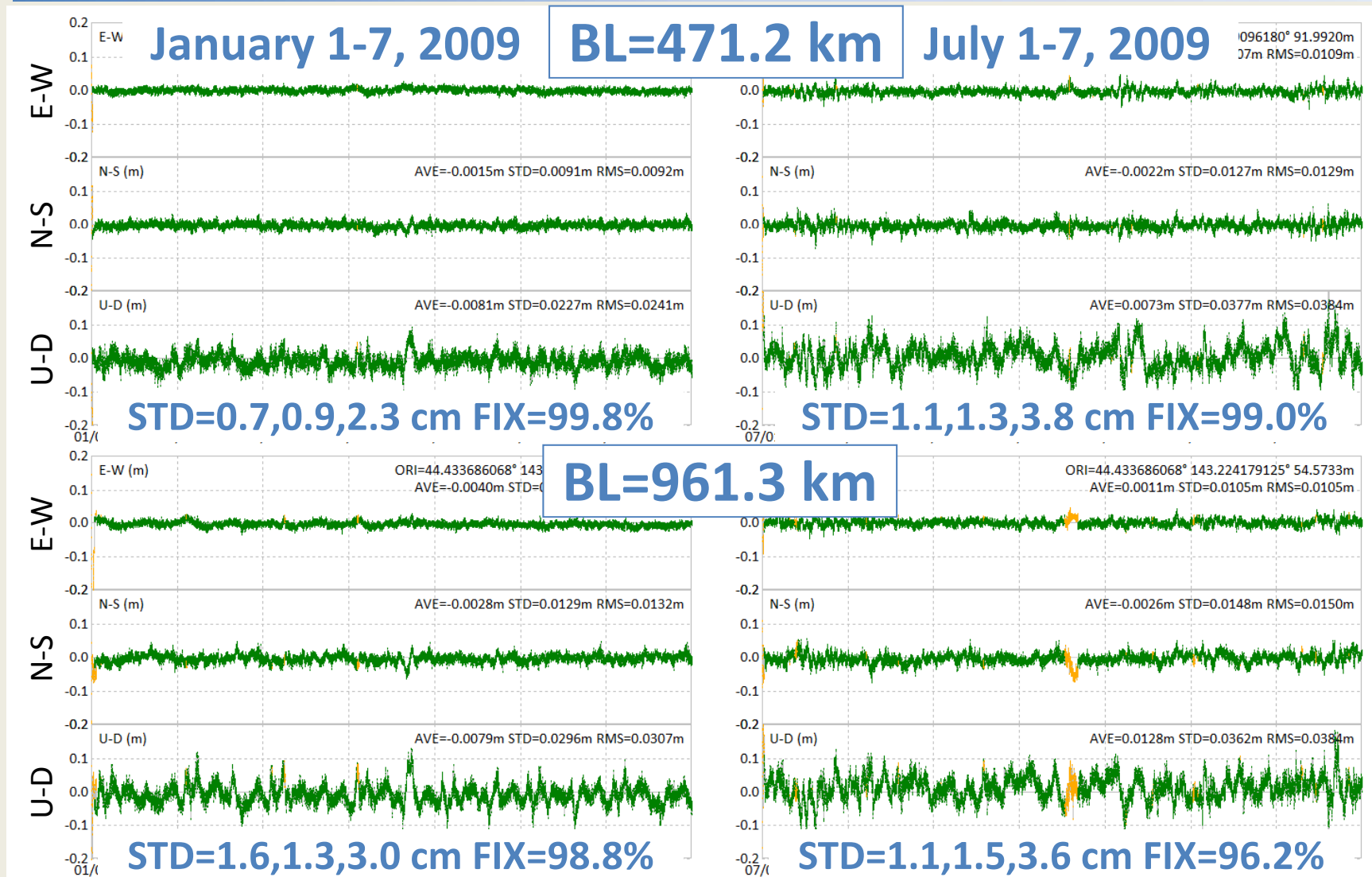
**GPS Tsunami
Monitoring System
(Currently ~15 km off-shore)**

<http://www.tsunamigps.com>

Long-Baseline RTK Strategy

	BL (km)	Error Elimination				Strategy
		Ephem	Ionos	Tropos	Others	
S	0 – 10	Broadcast	-	-	-	Conventional RTK
M	10 – 100	Broadcast	Dual-Freq	-	-	
			Interpolation		-	Network RTK
L	100 – 1,000	Real-time Precise (IGU)	Dual-Freq	Estimate ZTD + MF	Earth Tides	Long-Baseline RTK
VL	>1,000	Non-RT Precise (IGR, IGS)	Dual-Freq	Estimate ZTD + MF	Earth Tides, Ph-WU	Post- Processing or PPP

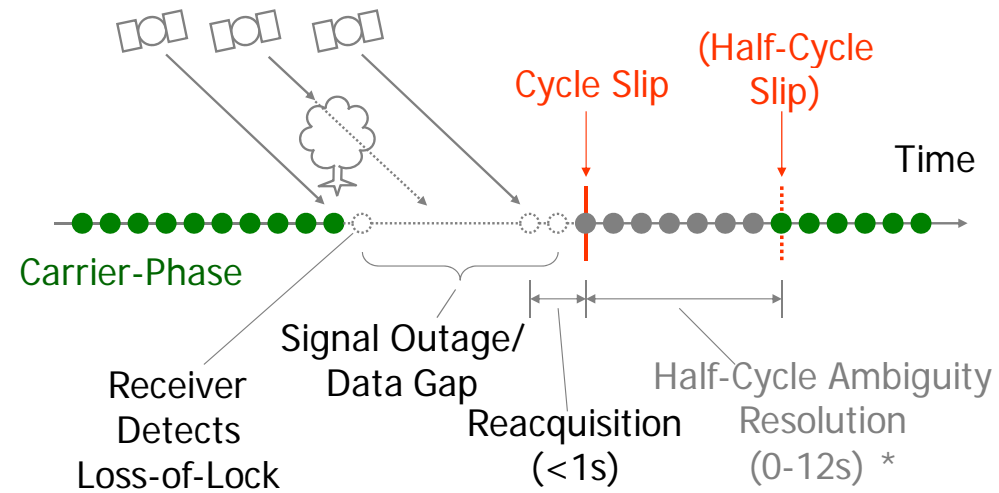
Long-Baseline RTK with RTKLIB



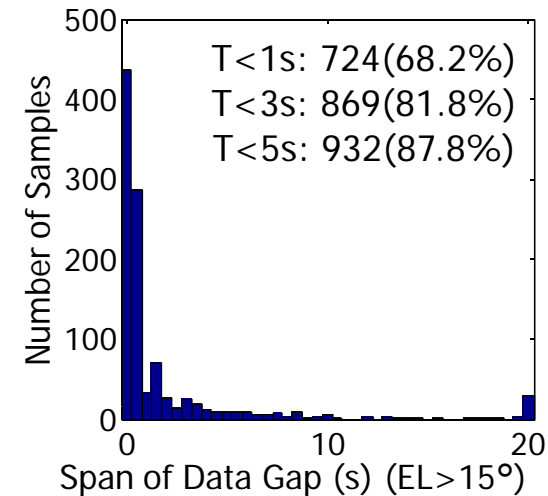
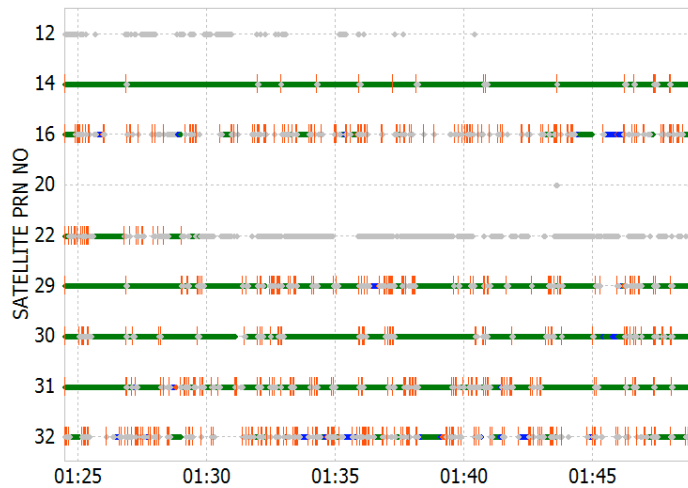
Mobile AP issues for RTK

- **Cycle-Slips**
 - Frequent cycle-slip with around obstacles
 - Miss-detection of cycle-slip
- **Low Solution Availability**
 - Long acquisition time by weak signal (Low C/N0)
 - Half-cycle ambiguity resolution with Costas-PLL
 - Low fixing ratio
- **High Noise Level**
 - High multipath level even in carrier-phase
 - Jamming by RFI

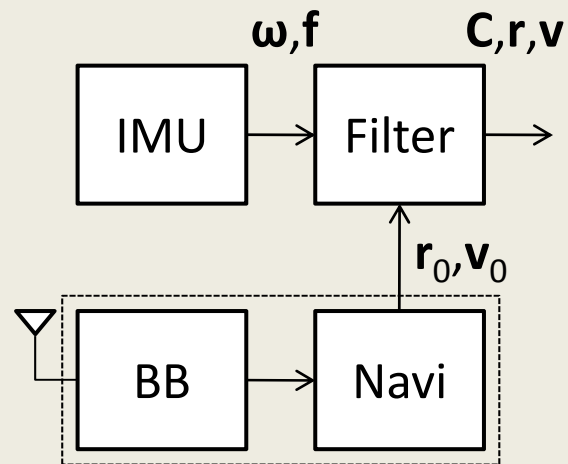
Cycle-Slips



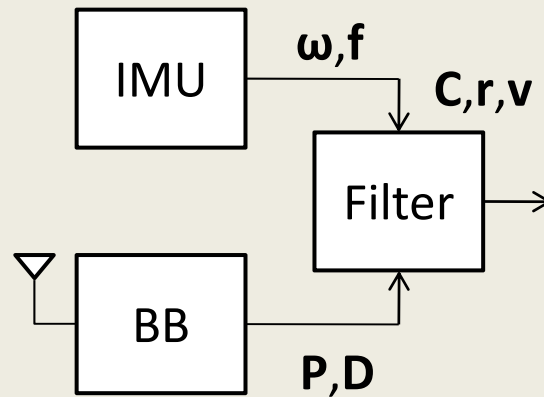
* Depend on Receiver



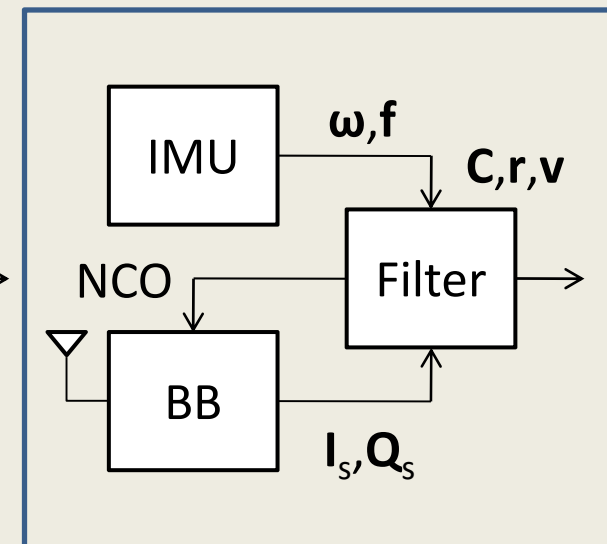
INS-Aided RTK



Loosely-Coupled
Integration



Tightly-Coupled
Integration



Deep Integration
(Ultra-Tightly)

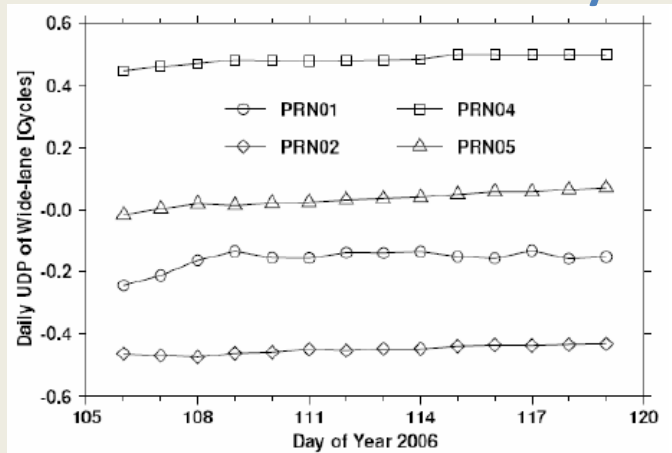
High sensitivity
(DLL, PLL)
Slip resistance

Ambiguity Resolution for PPP

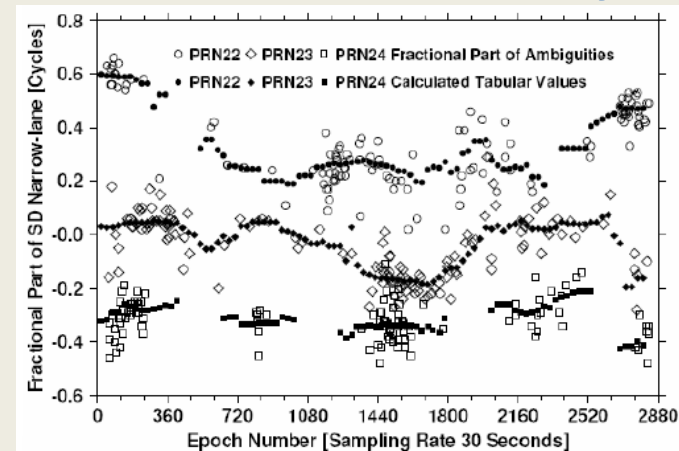
- with AR for PPP
 - Improve Convergence Time
 - Improve Accuracy of Static Solution (EW, UD)
 - Improve Stability of Kinematic Solution
- Difficulties of AR for PPP
 - Unknown Satellite Initial Phase Biases
 - Effect of Precise Orbit/Clock Error
 - Effect of Ionospheric Delay
 - Code/Phase Bias Instability
 - Multipath Effect at Reference Station Network

M.Ge et al., EGU 2007

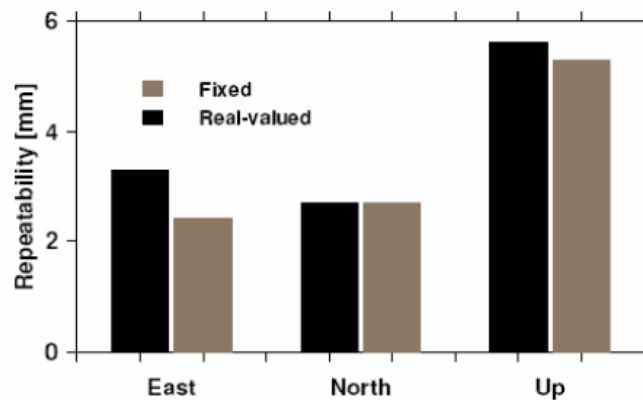
WL Phase Bias Stability



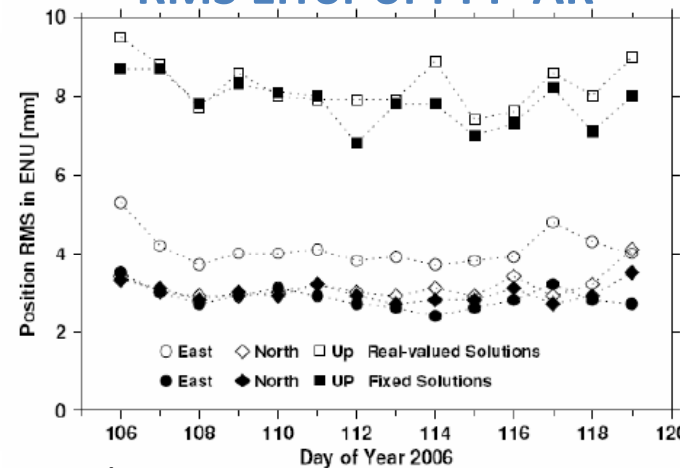
NL Phase Bias Stability



Repeatability of PPP-AR



RMS Error of PPP-AR



M.Ge et al., Resolution of GPS carrier-phase ambiguity in precise point positioning, EGU Assembly 2007

D.Laurichesse, ION 2010

- Real-Time Implementation of PPP-AR
 - Network WL ambiguity fixing
 - Parameter estimation by EKF with iono-free code/phase: phase-clock, code-phase-bias, ZTD, station position, orbit correction to IGU, phase ambiguity
 - Orbit construction + high-rate clock generation
- Evaluation of Accuracy
 - Orbit: 4cm, code-clock: 5 cm, phase-clock: 1cm
- RT-PPP with AR ("CNES Integer PPP")
 - 1 cm HRMS

"CM-Accuracy Anywhere"

Requirement	Target in 2020	Developing/Future Technologies
Coverage	Global (world-wide)	Precise Ephemeris with AR, Broadcast via GEO/QZSS Satellite
Latency	Real-time (1 s)	Real-time Multi-GNSS Orbit/Clock Estimation
Accuracy	1 cm (HRMS) 2 cm (VRMS)	Local iono/tropos corrections (land) Iono estimation by triple-freq (sea)
Availability	99 % (open-sky)	Multi-GNSS 30 Sats + triple-freq
	95 % (urban)	Multi-GNSS 30 Sats + INS-aided PLL, slip-resistant
TTF	10 s (land)	Local iono/tropos corrections
	1 min (sea)	Iono estimation by triple-freq
User Cost	< \$100	No patent problem, need killer-AP

8. Advanced Topics: Q & A