



# Swarm intelligence

<http://cs.ulb.ac.be/public/teaching/infoh414>

[mdorigo@ulb.ac.be](mailto:mdorigo@ulb.ac.be)

Marco Dorigo

FNRS Research Director

IRIDIA

Université Libre de Bruxelles



# Course organization

- Subjects
  - Swarm intelligence basics
  - Particle swarm optimization
  - Ant colony optimization
  - Swarm robotics
- Projects:
  - Details will be given later

# What is swarm intelligence?

Swarm intelligence is the complex global behavior shown by a distributed system that arises from the self-organized local interactions between its constituent agents



# Insects, Social Insects, and Ants

- $10^{18}$  living insects (rough estimate)
- ~2% of all insects are social
- Social insects are:
  - All ants
  - All termites
  - Some bees
  - Some wasps
- 50% of all social insects are ants
- Avg weight of one ant between 1 and 5 mg
- Tot weight ants ~ Tot weight humans
- Ants have colonized Earth for over 100 million years, *Homo sapiens sapiens* for approximately 100,000 years

# Ants



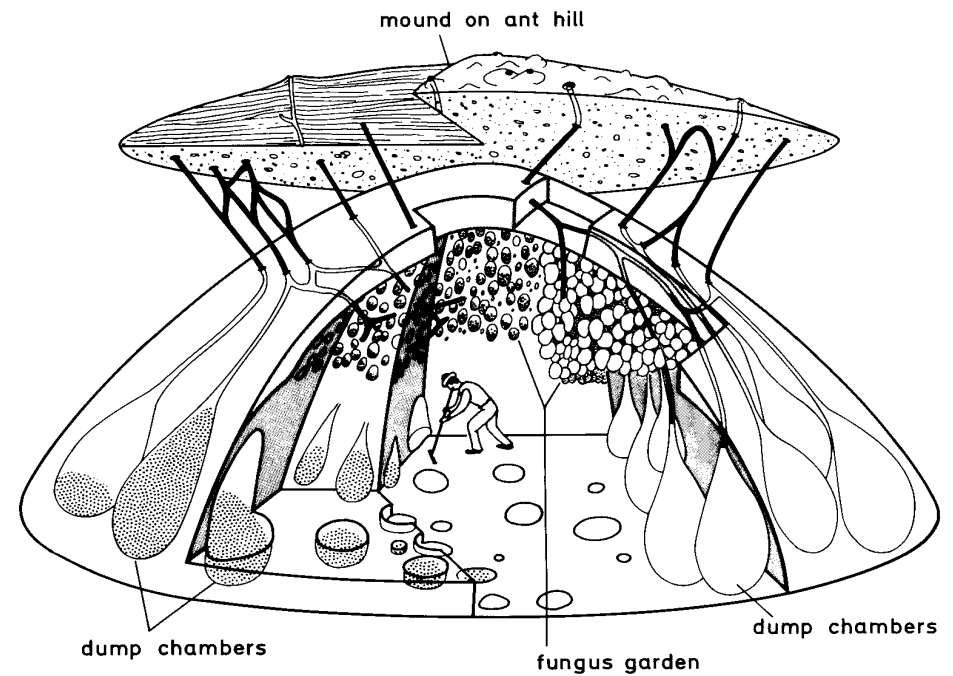
Leaf cutter,  
fungus growing  
ants

Breeding ants

Weaver ants

# Ants

- Fungus growers
- Breeding ants
- Weaver ants
- Harvesting ants
- Army ants
- Slavemaker ants





# Ant Colony Societies

- Ant colony size: from as few as 30 to millions of workers
- Work division:
  - Reproduction --> queen
  - Defense --> soldiers
  - Food collection --> specialized workers
  - Brood care --> specialized workers
  - Nest brooming --> specialized workers
  - Nest building --> specialized workers



# How Do Ants and Social Insects Coordinate their Activities?

- **Self-organization:**
  - Set of dynamical mechanisms whereby **structure appears at the global level** as the result of **interactions among lower-level components**
  - The rules specifying the interactions among the system's constituent units are executed on the basis of **purely local information**, without reference to the global pattern, which is an **emergent property of the system** rather than a property imposed upon the system by an external ordering influence





# Self-organization

## Four basic ingredients:

- Multiple interactions
- Randomness
- Positive feedback
  - E.g., recruitment and reinforcement
- Negative feedback
  - E.g., limited number of available foragers



# How Do Social Insects Achieve Self-organization?

- **Communication is necessary**
- **Two types of communication:**
  - **Direct:** antennation, trophallaxis (food or liquid exchange), mandibular contact, visual contact, chemical contact, etc.
  - **Indirect:** two individuals interact indirectly when one of them modifies the environment and the other responds to the new environment at a later time  
This is called **stigmergy**



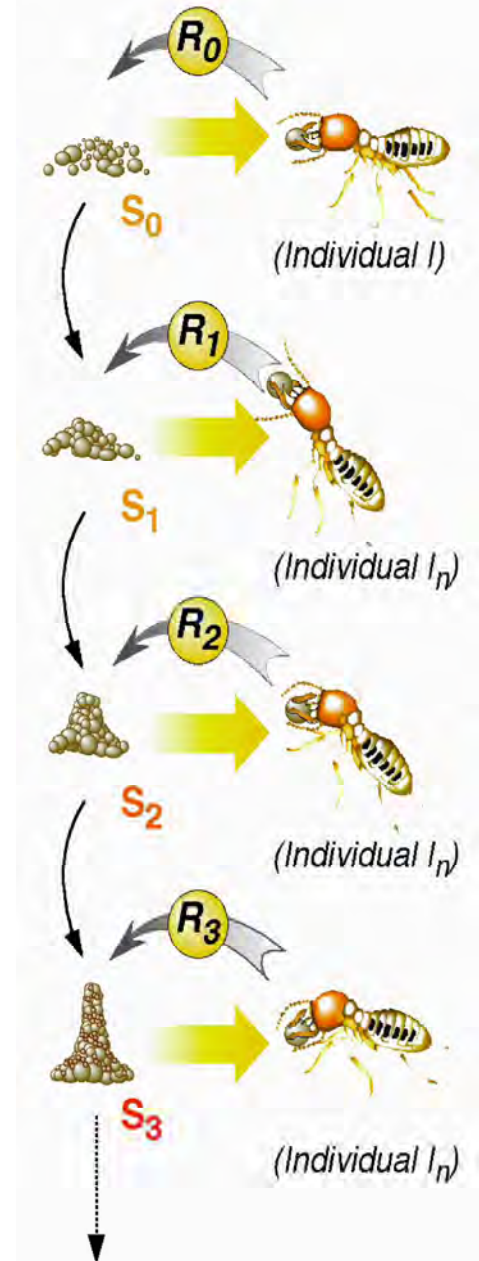
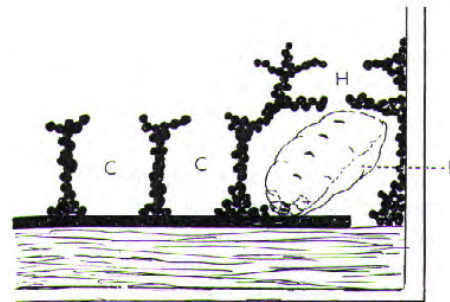
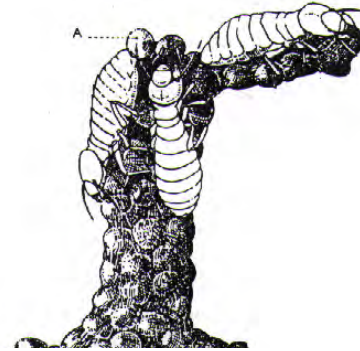
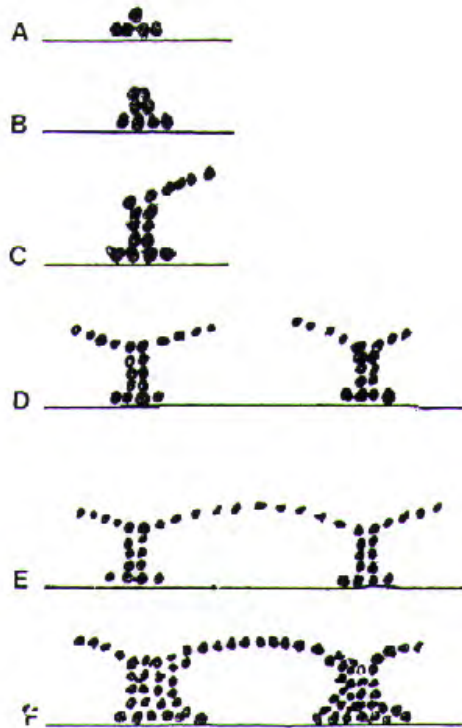
# Stigmergy

- “La coordination des tâches, la régulation des constructions ne dépendent pas directement des ouvriers, mais des constructions elles-mêmes. ***L’ouvrier ne dirige pas son travail, il est guidé par lui.*** C’est à cette stimulation d’un type particulier que nous donnons le nom du **STIGMERGIE** (*stigma*, pique; *ergon*, travail, oeuvre = oeuvre stimulante).” Grassé P. P., 1959
- [“The coordination of tasks and the regulation of constructions does not depend directly on the workers, but on the constructions themselves. ***The worker does not direct his work, but is guided by it.*** It is to this special form of stimulation that we give the name **STIGMERGY** (*stigma*, sting; *ergon*, work, product of labour = stimulating product of labour).”]

# Stigmergy

*Stimulation of worker  
by the performance  
they have achieved*

Grassé P. P., 1959





# Stigmergy

## Example: Termites Building their Nest



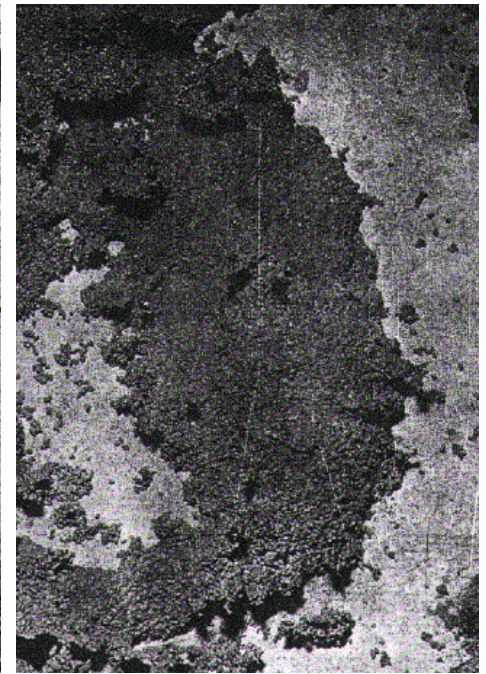
**1 h 18'**  
**after start**



**3 h 23'**  
**after start**



**5 h 15'**  
**after start**



**8 h 13'**  
**after start**



# Termites' Nest



# Sign-based Stigmergy

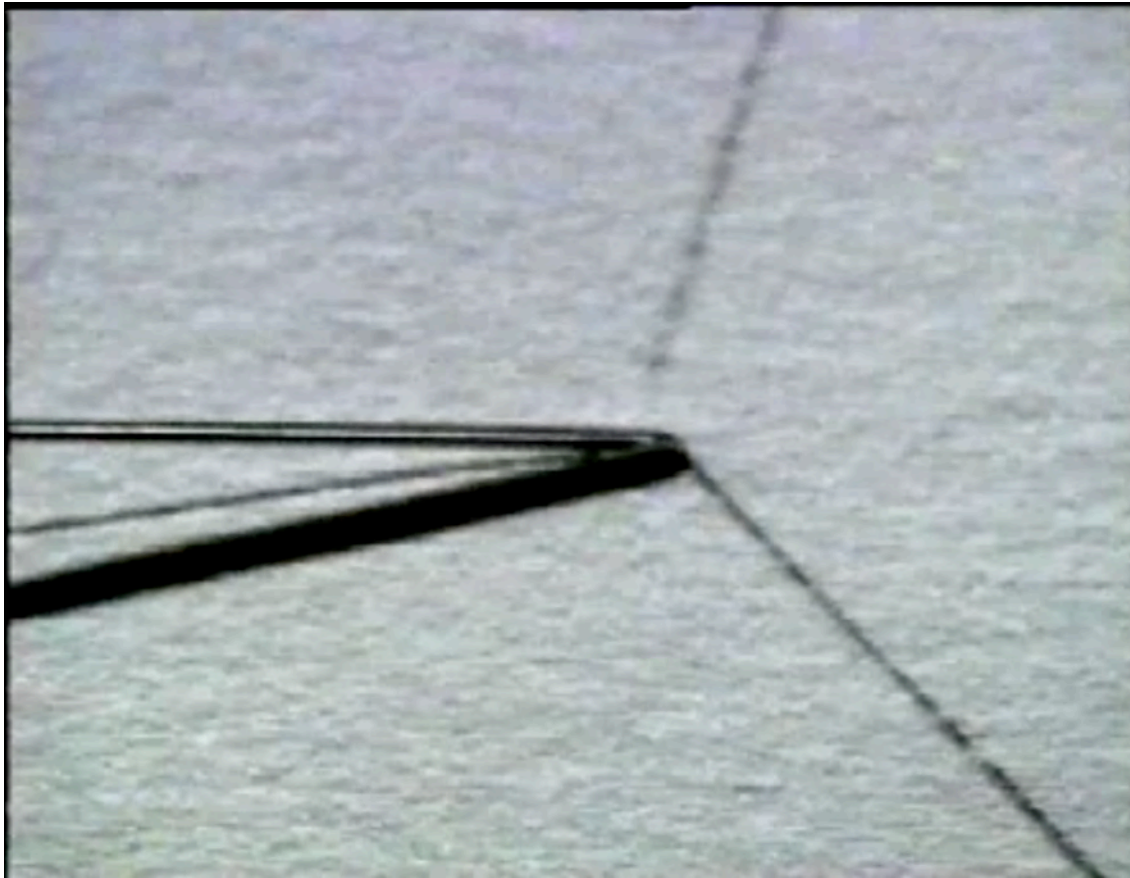
## Example: Trail Following in Ants

While walking, ants and termites:

- May deposit a pheromone on the ground
- Follow with high probability pheromone trails they sense on the ground

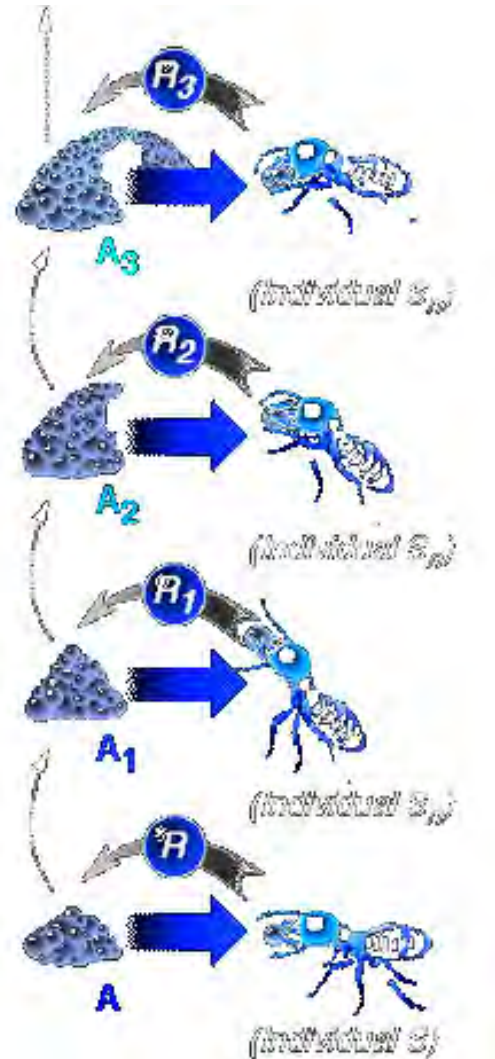
# Pheromone Trail Following

Ants and termites follow pheromone trails

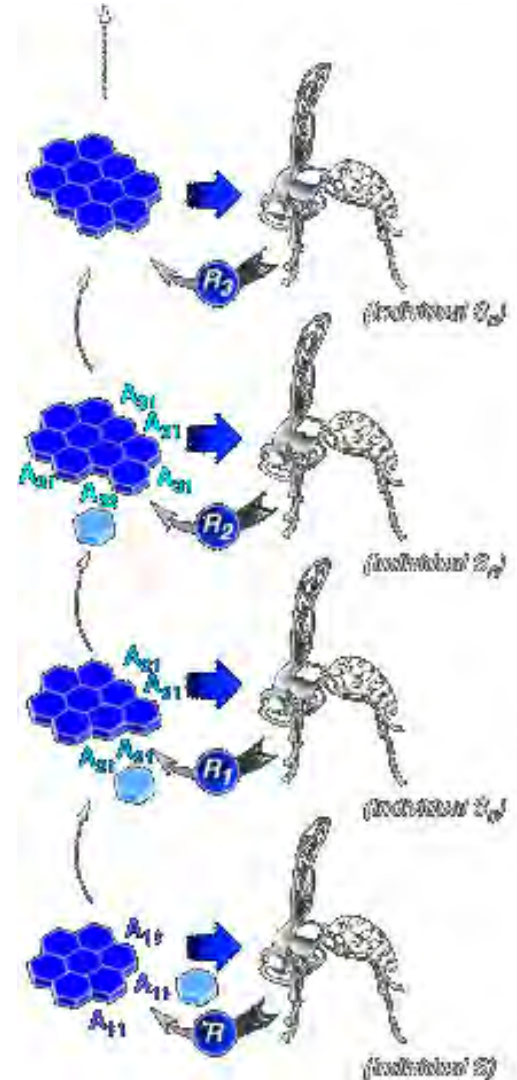




# Quantitative vs. Qualitative Stigmergy

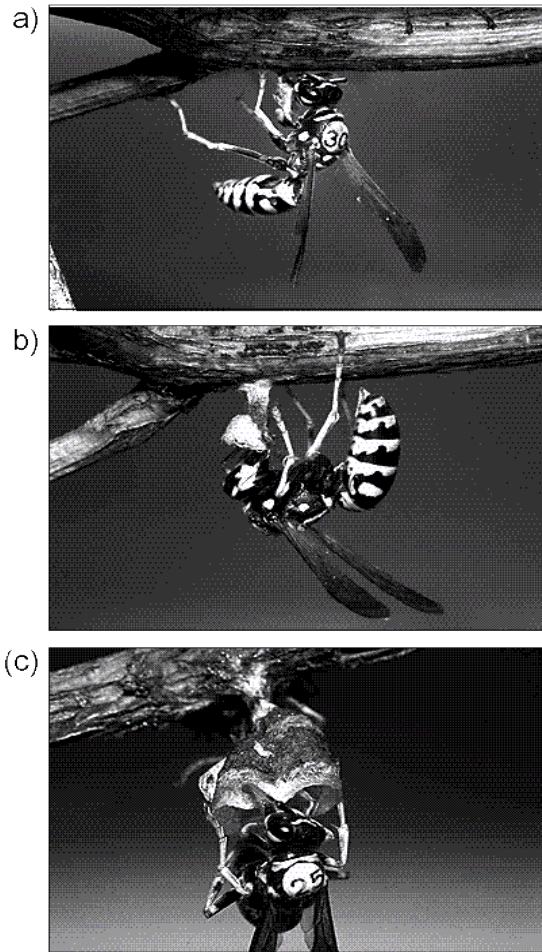


Termites



Wasps

# Wasps Building a Nest

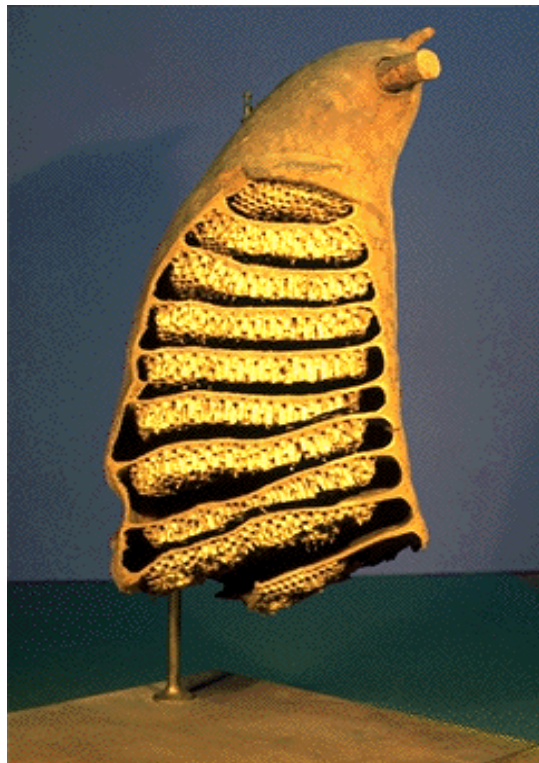


Video recordings by Guy Theraulaz



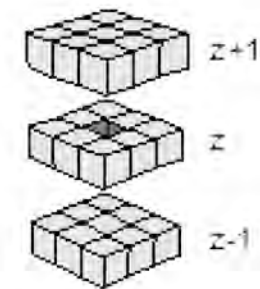
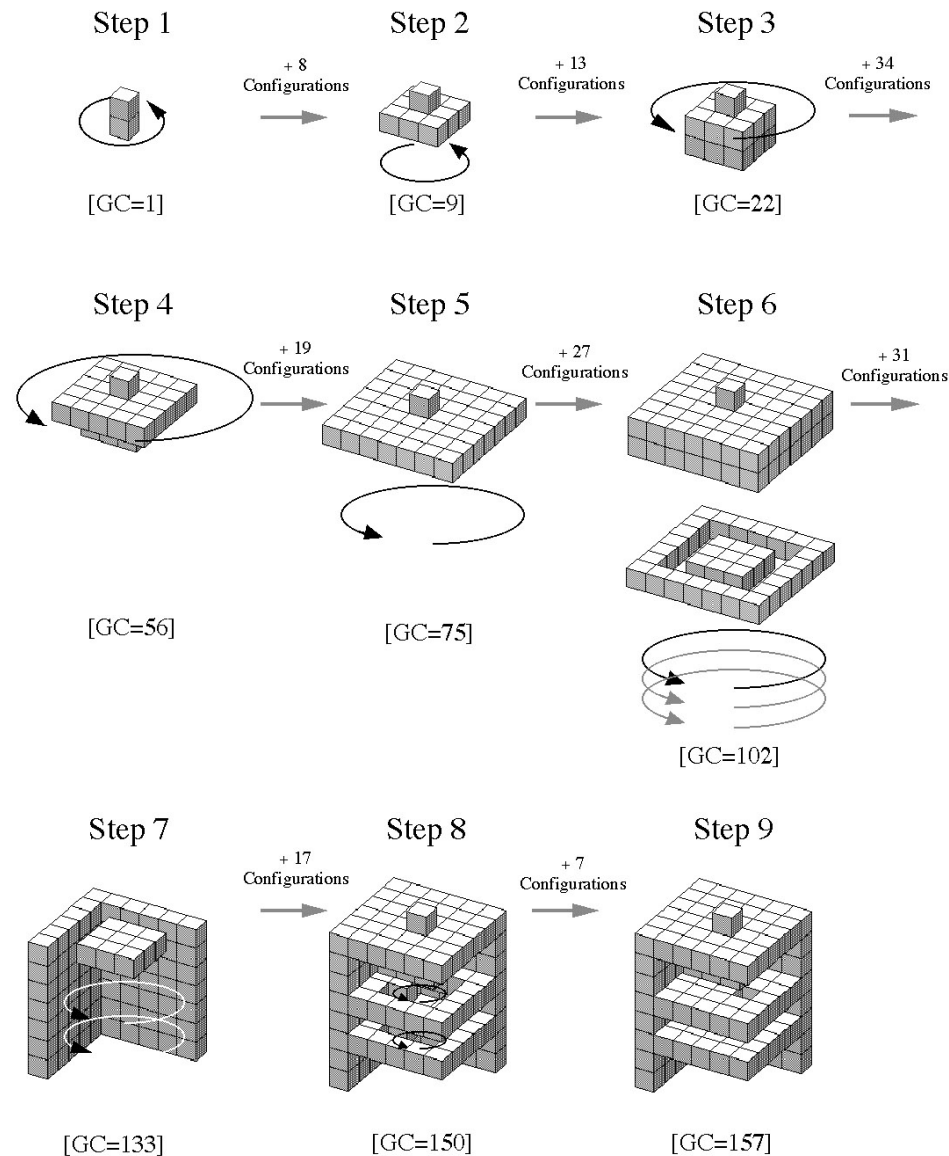
# Wasps' Nests

Photos by Guy Theraulaz



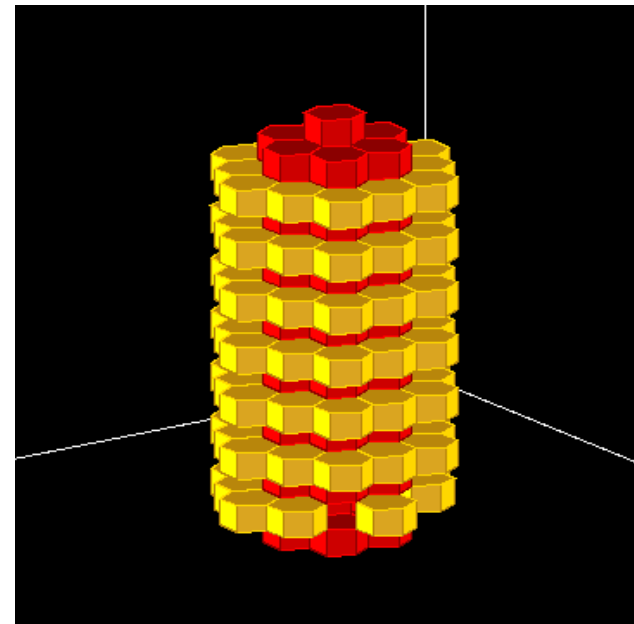
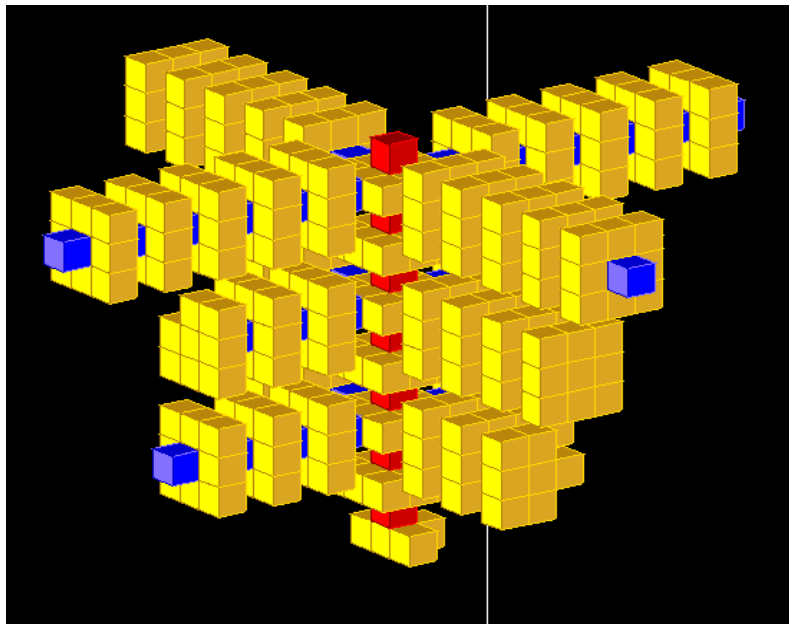
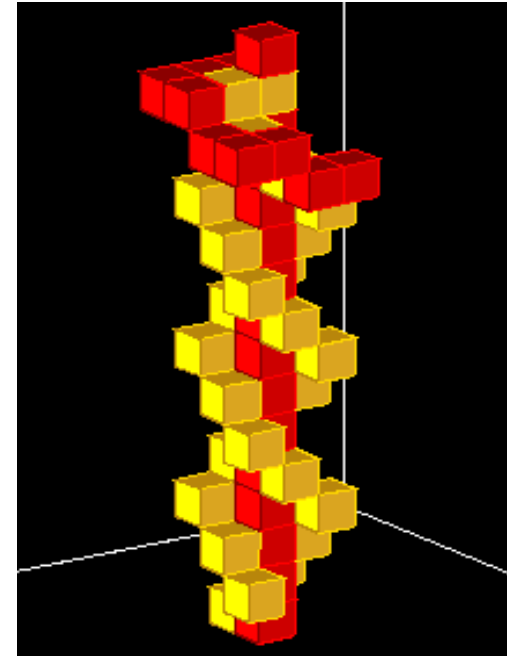
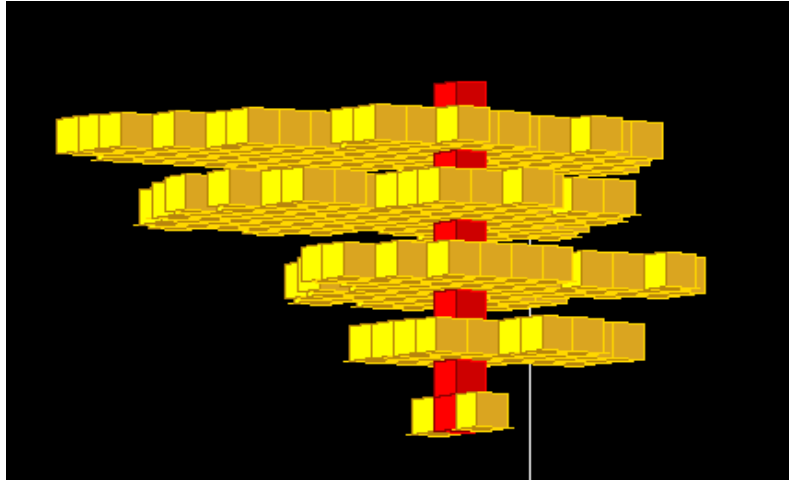
# Artificial Nest Building

Theraulaz & Bonabeau, 1995



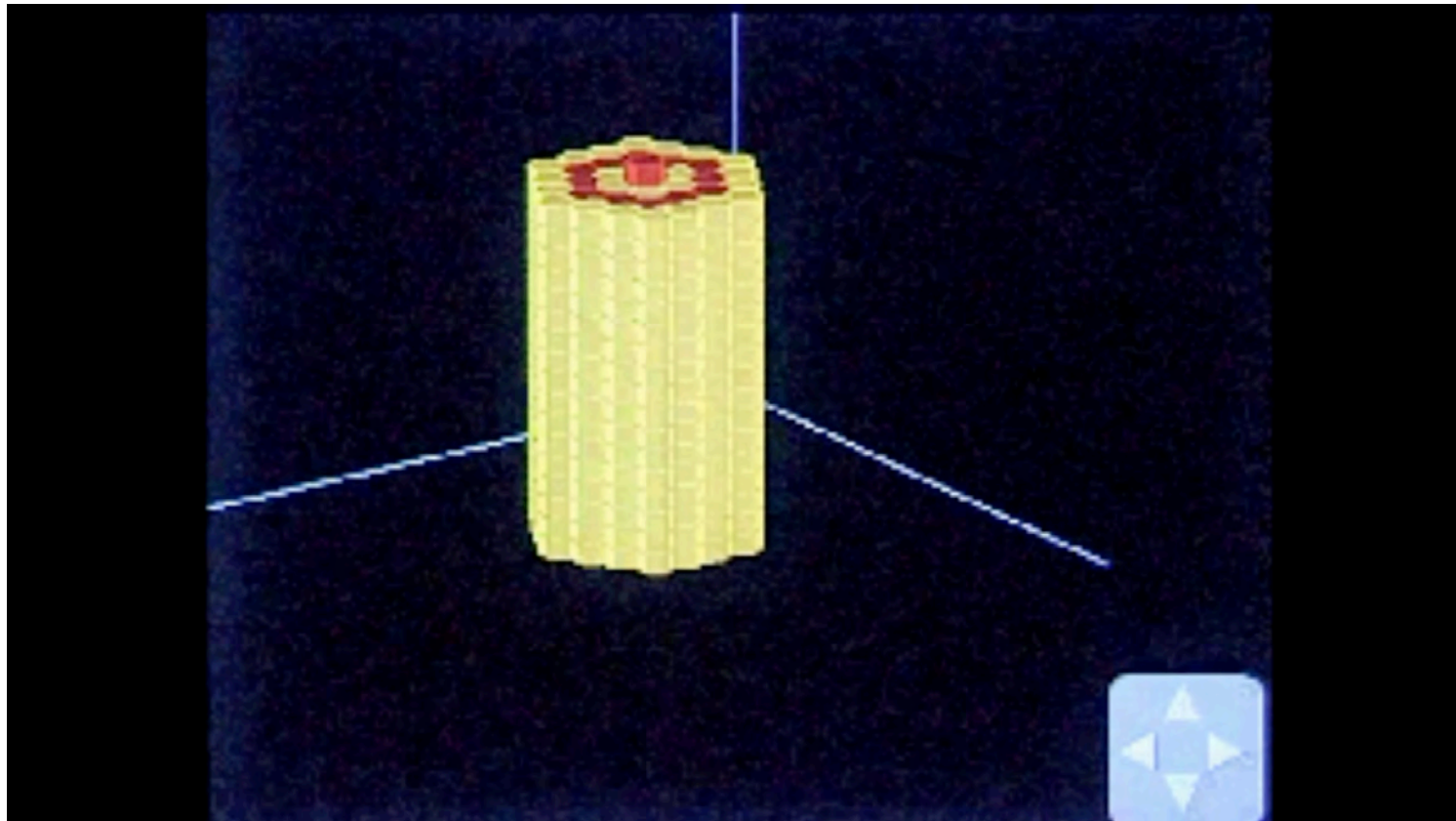
Sensory field

# Some Simulation Results



# More Simulation Results (1)

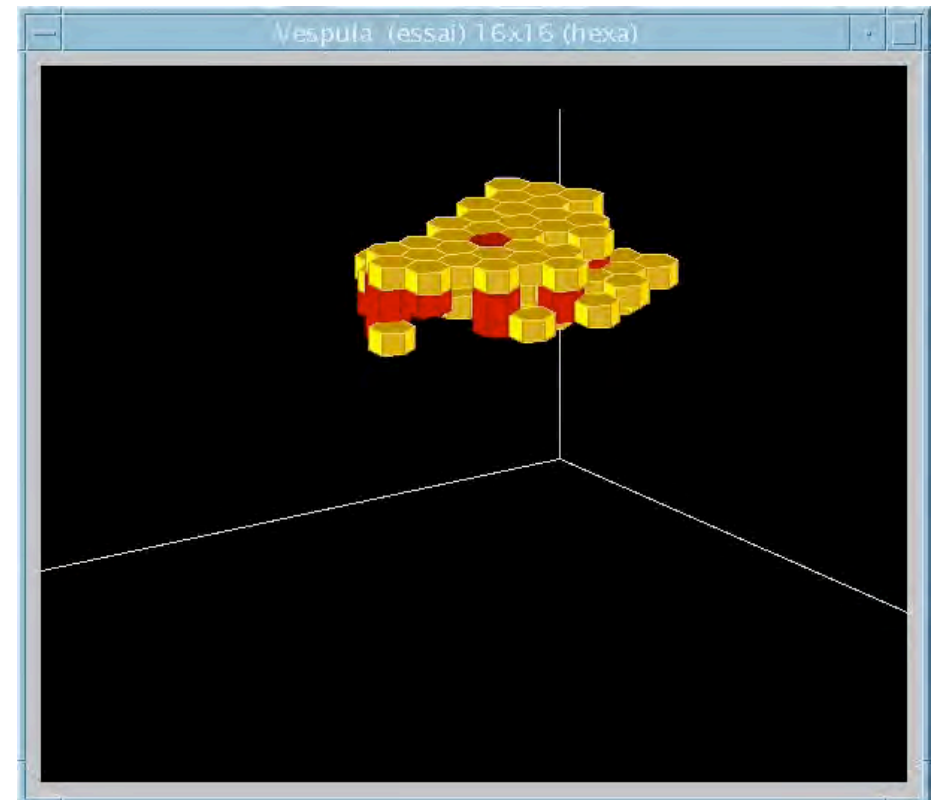
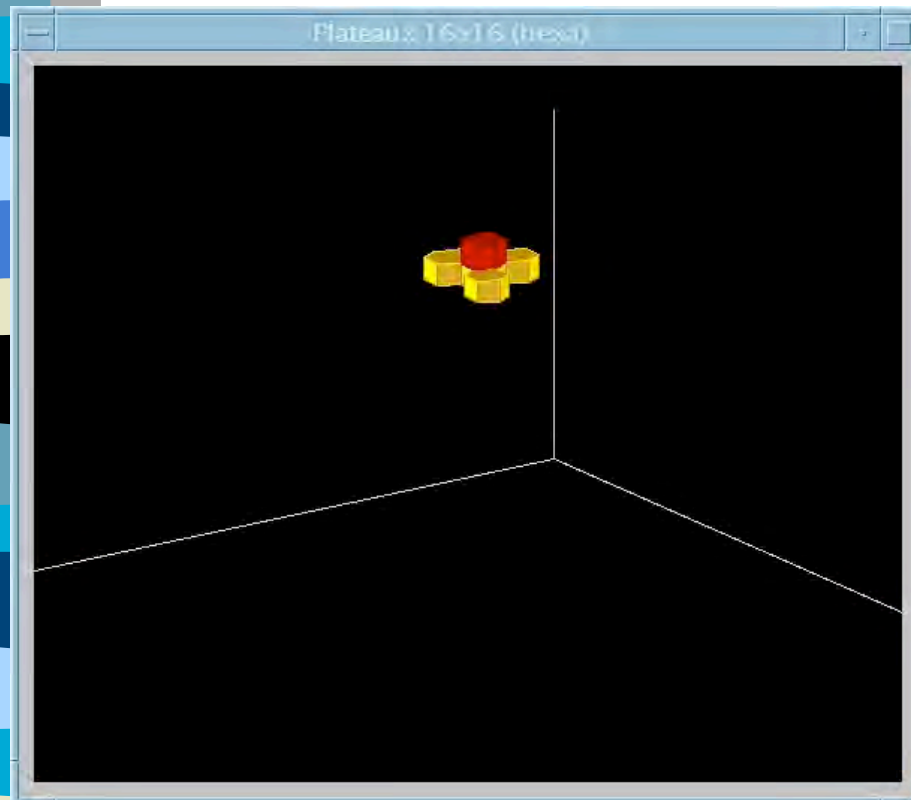
Theraulaz & Bonabeau, 1995





# More Simulation Results (2)

Theraulaz & Bonabeau, 1995





# Types of Stigmergy

- ***Sematectonics***  
E.g., termites nest building
- ***Sign-based***  
E.g., ants trail following behavior
- ***Quantitative***  
E.g., ants trail following behavior and termites nest building
- ***Qualitative***  
E.g., social wasps nest building





# “Artificial” Stigmergy

*Indirect communication mediated by modifications of environmental states which are only **locally accessible** by the communicating agents*

Dorigo & Di Caro, 1999

- **Characteristics of artificial stigmergy:**
  - **Indirect communication**
  - **Local accessibility**



# What is swarm intelligence?

**Swarm intelligence:** “Any attempt to design algorithms or distributed problem-solving devices inspired by the collective behavior of **social insect colonies** and other animal societies”

From “Bonabeau E., M. Dorigo & G. Theraulaz, *Swarm Intelligence: From Natural to Artificial Systems*, Oxford University Press, Oxford University Press, 1999, page 7”.



# What is swarm intelligence?

- **Swarm intelligence** is an artificial intelligence technique based around the study of **collective behavior in decentralized, self-organized** systems
- Swarm intelligence systems are typically made up of a **population of simple agents** interacting **locally** with one another and with their environment
- Although there is **normally no centralized control structure** dictating how individual agents should behave, **local interactions** between such agents often **lead to the emergence of global behavior**
- Examples of systems like this can be found in nature, including ant colonies, bird flocking, animal herding, and fish schooling



Swarm intelligence

# Swarm intelligence

Distinguish between

- **Scientific swarm intelligence**
- **Engineering swarm intelligence**

From “Scholarpedia, Swarm Intelligence”



Swarm intelligence

# Swarm intelligence

Distinguish between

- **Scientific swarm intelligence**  
is concerned with the understanding of natural swarm systems



Swarm intelligence

# Swarm intelligence

Distinguish between

- **Engineering swarm intelligence**  
is concerned with the design and implementation of artificial swarm systems



Swarm intelligence

# Swarm intelligence

**Engineering swarm intelligence**  
takes inspiration from  
**scientific swarm intelligence** studies  
to design problem-solving devices



Swarm intelligence

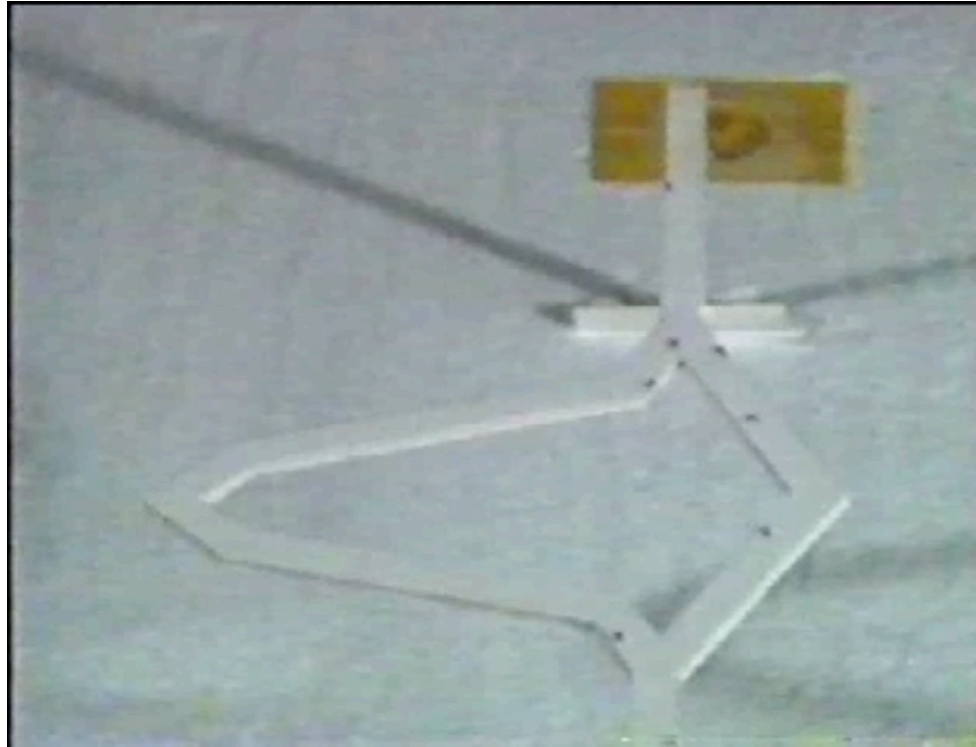
# Some examples of swarm intelligence systems

- Characteristics of swarm intelligence systems:
  - Multi-agent
  - Individuals are modeled as having stochastic behavior
  - Individuals use only local information
  - Self-organized and distributed control



Scientific swarm intelligence

# Example: Finding the shortest path



- Multi-agent
- Individuals use only local information
- Stochastic individuals
- Distributed control

Video by J.-L. Deneubourg

Scientific swarm intelligence

# Example: Cooperative transport



Multi-agent

Individuals use only local information

Stochastic individuals

Distributed control

Scientific swarm intelligence

# Example: Building a “bridge”



Video by A. Lioni

- Multi-agent
- Individuals use only local information
- Stochastic individuals
- Distributed control

Scientific swarm intelligence

# Example: Building a “bridge”



- Multi-agent
- Individuals use only local information
- Stochastic individuals
- Distributed control

Scientific swarm intelligence

# Example: Building a “bridge”



- Multi-agent
- Individuals use only local information
- Stochastic individuals
- Distributed control



BBC



Scientific swarm intelligence

# Example: Flocking birds



- Multi-agent
- Individuals use only local information
- Stochastic individuals
- Distributed control



40



Scientific swarm intelligence

# Example: Fish school



- Multi-agent
- Individuals use only local information
- Stochastic individuals
- Distributed control



# How to design swarm intelligence systems

- Essentially two ways:
  - researcher ingenuity
  - machine learning techniques



# How to design swarm intelligence systems

- Essentially two ways:
  - researcher ingenuity
    - examples:
      - **ant colony optimization, ant-based clustering**
  - machine learning techniques
    - (+ researcher ingenuity)
      - example: **swarm robotics**



Engineering swarm intelligence

# Research method

- Observe a social behavior
- Build a simple model to explain it
- Use the model of the social behavior as a source of inspiration for solving a practical problem that has some similarities with the observed social behavior

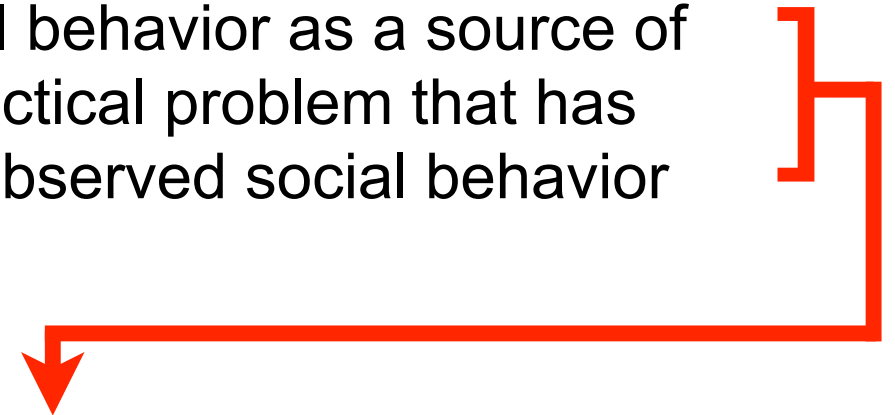
# Research method

- Observe a social behavior
- Build a simple model to explain it
- Use the model of the social behavior as a source of inspiration for solving a practical problem that has some similarities with the observed social behavior

] biologists

# Research method

- Observe a social behavior
- Build a simple model to explain it
- Use the model of the social behavior as a source of inspiration for solving a practical problem that has some similarities with the observed social behavior



Computer scientists, engineers,  
operation researchers, roboticists



From scientific to engineering swarm intelligence

# Examples

- Cemetery organization and brood sorting ➡ data clustering
- Birds flocking ➡ particle swarm optimization
- Foraging ➡ ant colony optimization
- Self-assembly and cooperative transport ➡ robotic implementations
- Division of labor ➡ adaptive task allocation





From scientific to engineering swarm intelligence

# Examples

- **Cemetery organization and brood sorting** ➡ data clustering
- Birds flocking ➡ particle swarm optimization
- Foraging ➡ ant colony optimization
- Self-assembly and cooperative transport ➡ robotic implementations
- Division of labor ➡ adaptive task allocation

# First example:

Ants' cemetery organization as an inspiration for a clustering algorithm



Methodology: observe social behavior

# Cemetery organization





Methodology: build simple model

# Cemetery organization

$$P = \left( \frac{k_1}{k_1 + f} \right)^2 \quad D = \left( \frac{f}{k_2 + f} \right)^2$$

Let:

- $P$  be the prob an unloaded ant picks up an item
- $D$  the prob a loaded ant drops an item
- $f$  the perceived fraction of items in the ant's neighborhood
- $k_1$  and  $k_2$  two threshold constants



Methodology: build simple model

# Cemetery organization

$$P = \left( \frac{k_1}{k_1 + f} \right)^2 \quad D = \left( \frac{f}{k_2 + f} \right)^2$$

$f$  is computed by keeping track of the # of items encountered by the ant in the last  $T$  time units divided by  $T$

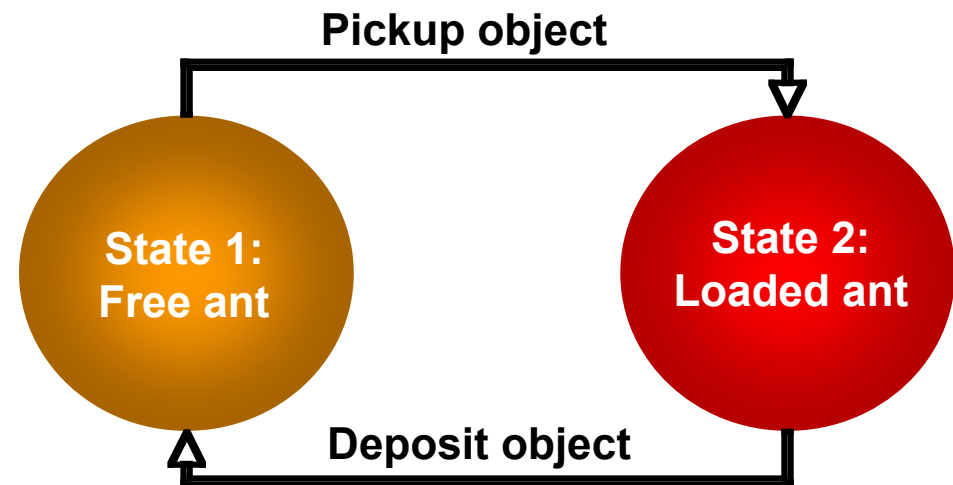
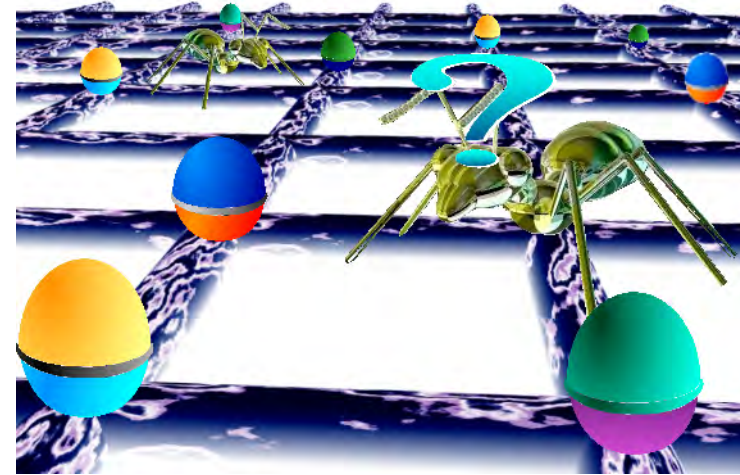
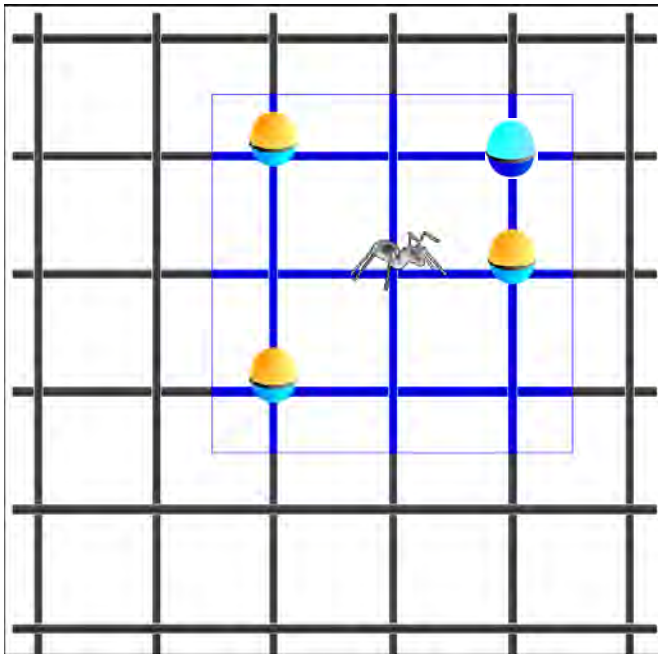
- $f \ll k_1 \rightarrow P \approx 1,$        $f \gg k_1 \rightarrow P \approx 0$
- $f \ll k_2 \rightarrow D \approx 0,$        $f \gg k_2 \rightarrow D \approx 1$

Methodology: identify and solve related practical problem

# Clustering and sorting data



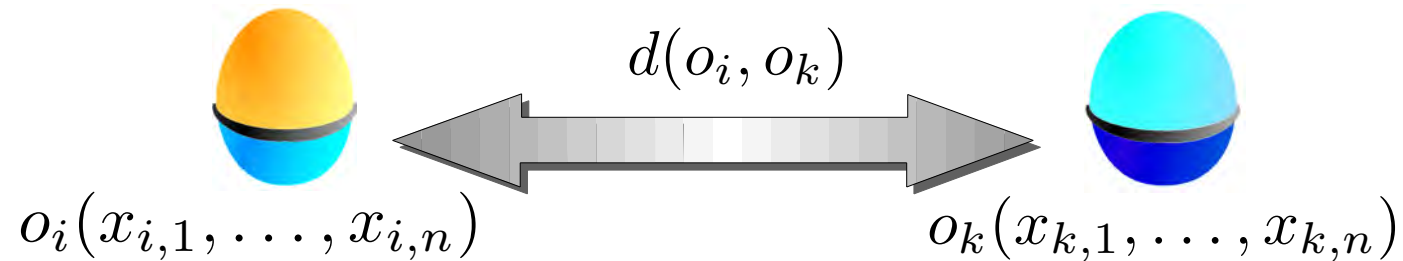
$$O_i(x_{i,1}, \dots, x_{i,n})$$





Methodology: identify and solve related practical problem

# Clustering and sorting data



$$d(o_i, o_k) = \frac{1}{n} \sum_{j=1}^n |x_{i,j} - x_{k,j}|$$

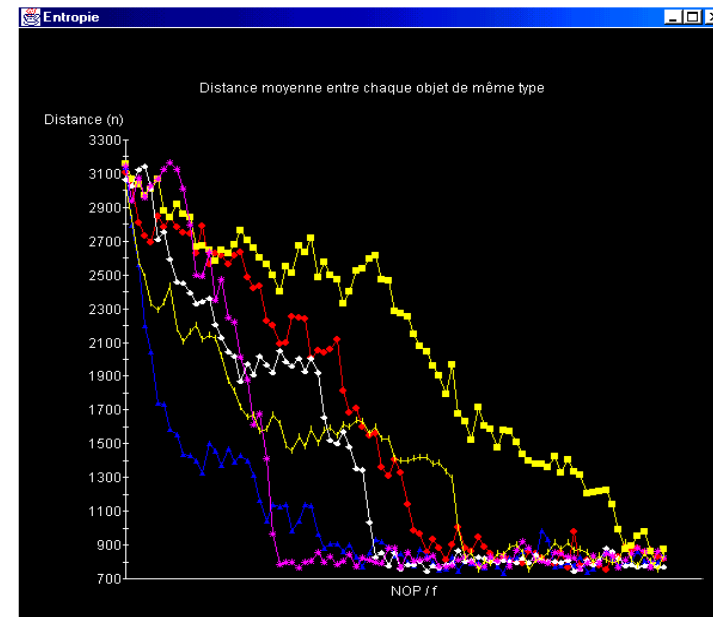
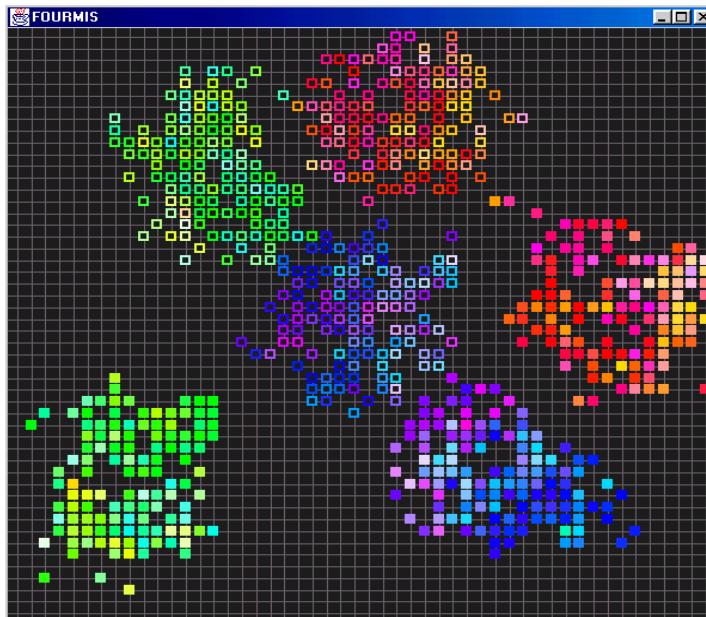
$$f(o_i) = \frac{\sum_{o_k \in J_{s \times s}(r)} (1 - d(o_i, o_k))}{Neigh}$$

$$P(o_i) = \left( \frac{k_1}{k_1 + f(o_i)} \right)^2, \quad D(o_i) = \left( \frac{f(o_i)}{k_2 + f(o_i)} \right)^2, \quad i \in objects\_set$$

Methodology: identify and solve related practical problem

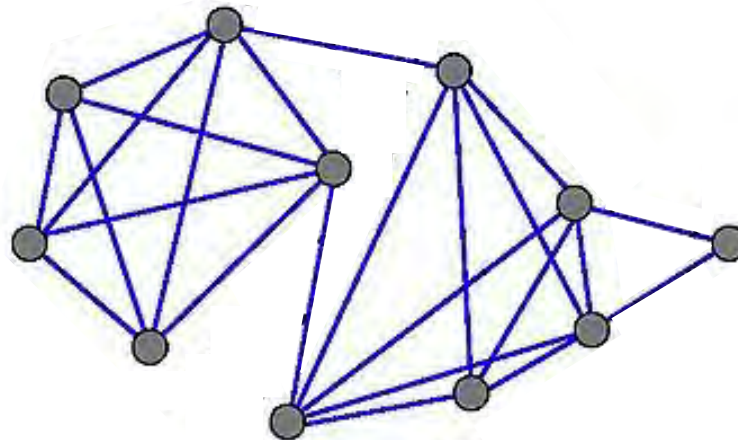
# Clustering and sorting data

- Attributes : 3 primary color components defining a color (R,G,B) and full/empty
- 726 objects with random attributes
- Objects randomly positioned at start, 20 ants, 50x50 grid



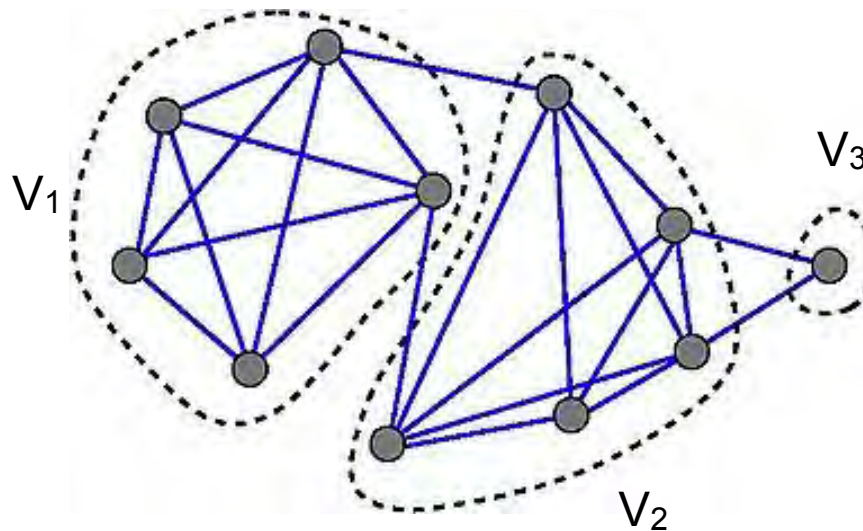
# Example of application: graph partitioning

Let  $G = (V, E)$  be a graph and  $P_k$  a partition of  $V$  in  $k$  non-empty classes  $V_1, \dots, V_k$



# Example of application: graph partitioning

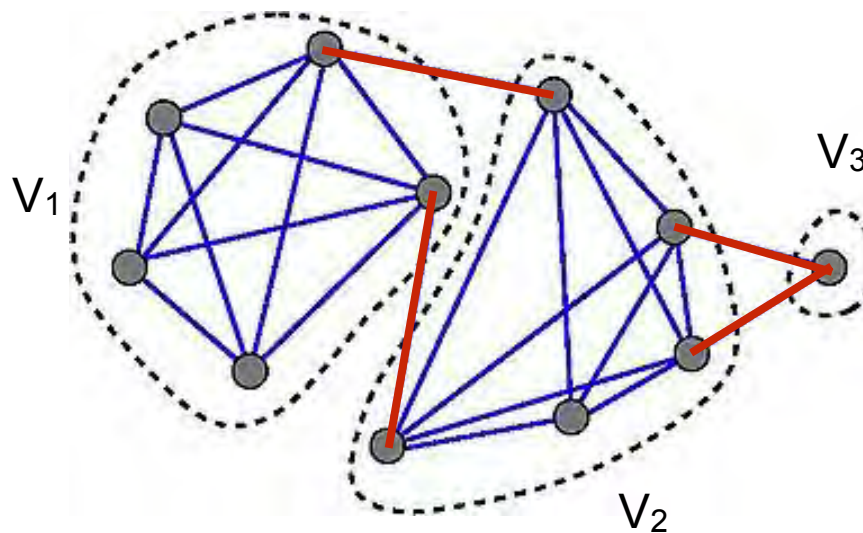
Let  $G = (V, E)$  be a graph and  $P_k$  a partition of  $V$  in  $k$  non-empty classes  $V_1, \dots, V_k$



# Example of application: graph partitioning

Let  $G = (V, E)$  be a graph and  $P_k$  a partition of  $V$  in  $k$  non-empty classes  $V_1, \dots, V_k$

Let  $E(V_h)$  be the set of edges with one extremity in  $V_h$  and the other in  $V_j$ ,  $V_j \neq V_h$



# Example of application: graph partitioning

Let  $G = (V, E)$  be a graph and  $P_k$  a partition of  $V$  in  $k$  non-empty classes  $V_1, \dots, V_k$

Let  $E(V_h)$  be the set of edges with one extremity in  $V_h$  and the other in  $V_j$ ,  $V_j \neq V_h$

The  $k$ -partitioning problem is to find a partition such that:

$$\min \sum_{h=1, k} |E(V_h)|$$

Graph partitioning is a difficult problem :

- If  $k$  is not fixed, then the problem is NP-hard
- If  $k$  is fixed, then complexity  $O(|V|^k)^2$



# Example of application: graph partitioning

- **Idea**

- attack  $k$ -partitioning (with  $k$  not fixed) as a clustering problem using artificial ants

- **Method**

- throw randomly  $v_i \in V$  on the plane
- let ants reorganize vertices so that graph nodes clusters appear in the 2D space

$$P_p(v_i) = \frac{\alpha_1}{\alpha_1 + f(v_i)} \quad P_d(v_i) = \frac{f(v_i)}{\alpha_2 + f(v_i)}$$

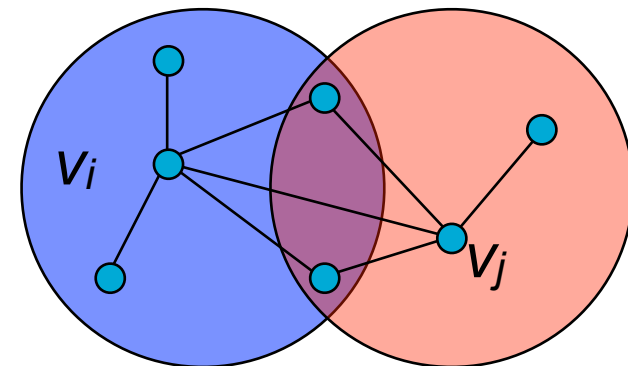
# Example of application: graph partitioning

- **Method**

- throw randomly  $v_i \in V$  on the plane
- let ants reorganize vertices so that graph clusters are located in the same portion of the 2D space

$$P_p(v_i) = \frac{\alpha_1}{\alpha_1 + f(v_i)}$$

$$P_d(v_i) = \frac{f(v_i)}{\alpha_2 + f(v_i)}$$



Vertices having many common neighbors and few distinct neighbors are considered “similar”



# Example of application: graph partitioning

- **Method**

- throw randomly  $v_i \in V$  on the plane
- let ants reorganize vertices so that graph clusters are located in the same portion of the 2D space

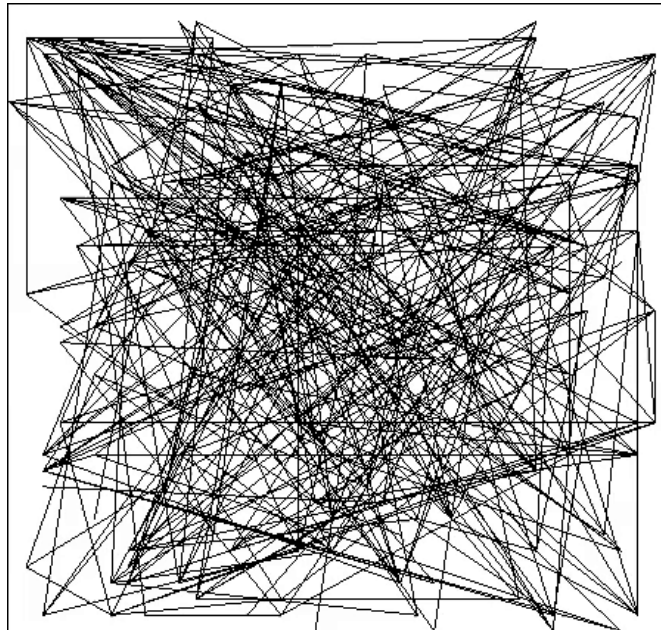
- **Results**

- the number of inter-cluster edges is greatly reduced
- different cluster are clearly separated

# Example of application: graph partitioning

- **Results**

- the number of inter-cluster edges is greatly reduced
- different cluster are clearly separated





From scientific to engineering swarm intelligence

# Examples

- Cemetery organization and brood sorting ➡ data clustering
- **Birds flocking** ➡ **particle swarm optimization**
- Foraging ➡ ant colony optimization
- Self-assembly and cooperative transport ➡ robotic implementations
- Division of labor ➡ adaptive task allocation

# Second example:

Flocking and schooling as an inspiration for continuous optimization algorithms (particle swarm optimization)

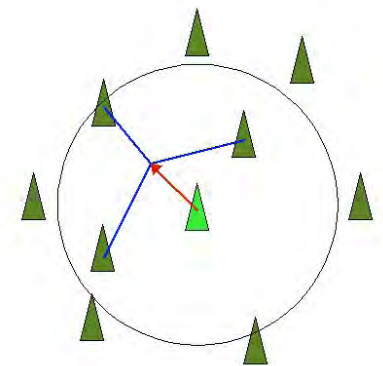
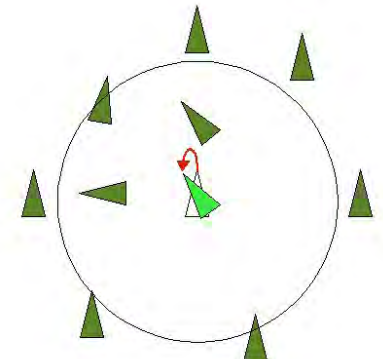
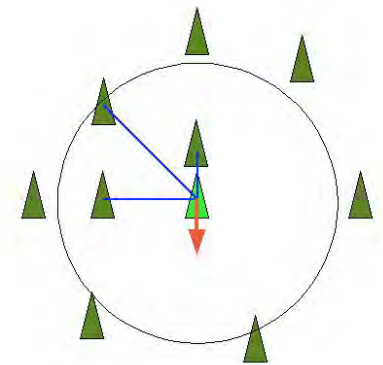




# Craig Reynold's boids simulation [Reynolds, 1987]

Reynolds [1987] proposed a behavioral model in which each agent follows three rules:

- **Separation:**
  - Each agent tries to move away from its neighbors if they are too close
- **Alignment:**
  - Each agent steers towards the average heading of its neighbors
- **Cohesion:**
  - Each agent tries to go towards the average position of its neighbors



**These simple rules yield surprisingly realistic swarm behavior**

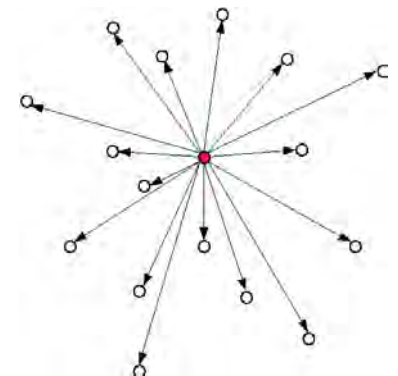
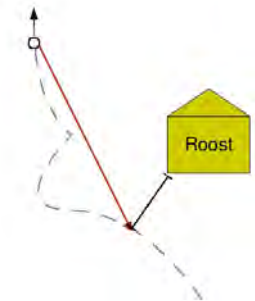
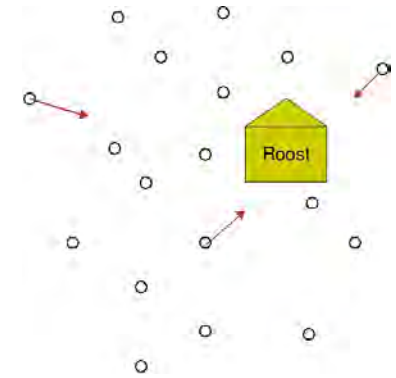
# Real versus computer generated flocking



# Origins of particle swarm optimization (PSO)

Kennedy & Eberhart [1995] included a 'roost' in a simplified Reynolds-like simulation so that each agent:

- is attracted to the location of the roost
- remembers the position it was closest to the roost
- shares information with its neighbors (originally, all other agents) about its closest position to the roost



# Origins of PSO

Eventually, all agents land on the roost

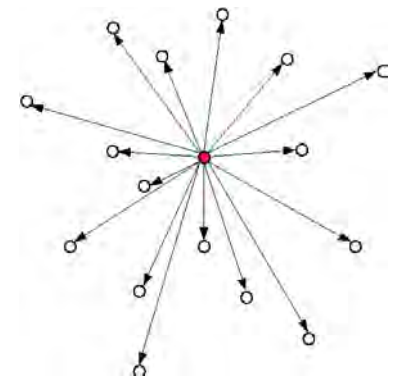
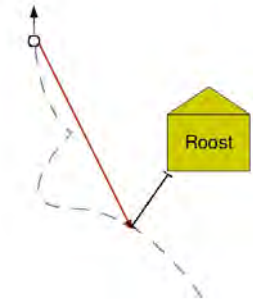
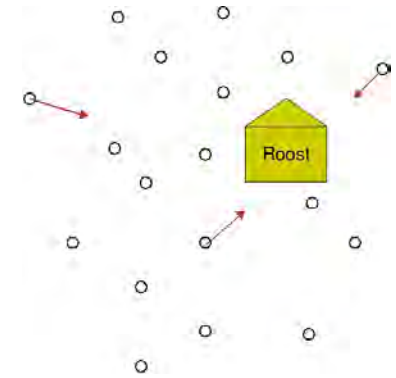
In other words, the agents minimized the distance that separated them from the roost

In two dimensions, the distance that separates a particle from the roost is

$$D_{roost}(x) = \sqrt{(roost_1 - x_1)^2 + (roost_2 - x_2)^2}$$

where  $x$  is the particle's position and roost is the position of the roost

**What if the notion of distance to the roost is changed by an unknown function?**





# Origins of PSO

If this function is changed, say with

$$F(x) = 20 + (x_1^2 - 10\cos(2\pi x_1)) + (x_2^2 - 10\cos(2\pi x_2))$$

would the agents find the value of  $x$  such that minimizes the function  $F(x)$ ?

This is how the idea of the particle swarm optimization algorithm was born



# PSO basic concepts

- PSO consists of a **swarm of particles**
- Each particle resides at a **position** in the search space
- The **fitness** of each particle represents the quality of its position
- The particles “fly” over the search space with a certain **velocity**
- The **velocity** (both direction and speed) of each particle is influenced by its own best position found so far and the best solution that was found so far by its **neighbors**
- Eventually the swarm **converges** to (locally-)**optimal** positions



# PSO basic algorithm

- A swarm is a set of particles, denoted by  $P$
- Each particle  $i$  has a neighborhood  $N_i \subset P$
- Particles move in the search space according to the following equations:

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t (pb_i^t - x_i^t) + \psi_2 U_2^t (lb^t - x_i^t)$$

$$x_i^{t+1} = x_i^t + v_i^{t+1}$$

- where  $v_i^t$  is particle  $i$ 's velocity
- $\psi_1$  and  $\psi_2$  are parameters called acceleration coefficients
- $U_1^t$  and  $U_2^t$  are diagonal matrices with random in-diagonal entries in the range  $[0, 1)$
- $pb_i^t$  is particle  $i$ 's personal best position
- $lb^t$  is the swarm's local best position
- $x_i^t$  is the particles current position



# PSO components

inertia

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t (pb_i^t - x_i^t) + \psi_2 U_2^t (lb_i^t - x_i^t)$$

# PSO components

personal influence

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t(pb_i^t - x_i^t) + \psi_2 U_2^t(lb_i^t - x_i^t)$$

# PSO components

social influence

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t(pb_i^t - x_i^t) + \psi_2 U_2^t(lb_i^t - x_i^t)$$



# PSO basic algorithm

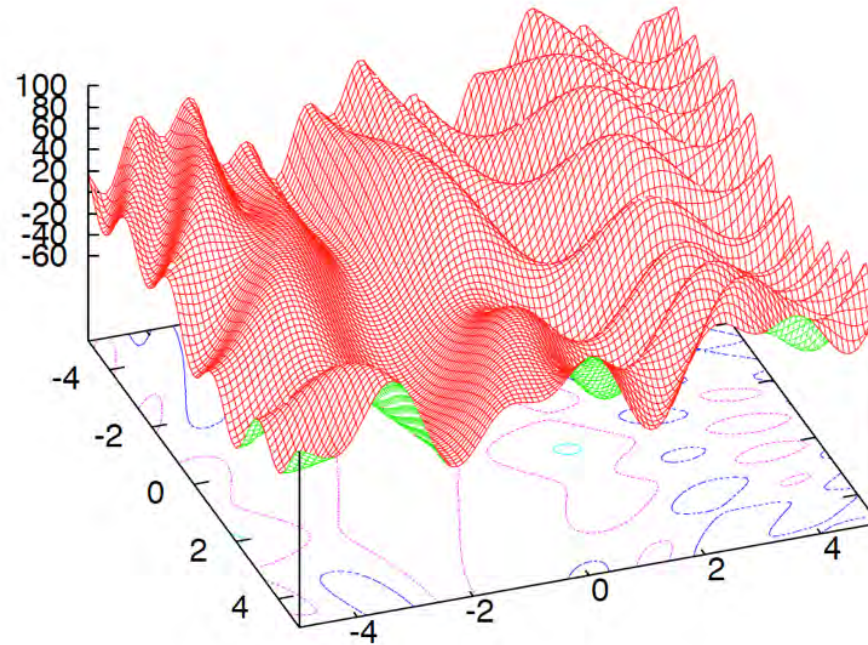
- Randomly initialize particle positions and velocities
- While not terminate
  - For each particle  $i$ :
    - Evaluate its quality  $p_i^t$  at its current position  $x_i^t$
    - If  $p_i^t$  is better than  $pb_i^t$  then update  $pb_i^t$
    - If  $p_i^t$  is better than  $lb^t$  then update  $lb^t$
  - For each particle
    - Update velocity and position using:

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t(pb_i^t - x_i^t) + \psi_2 U_2^t(lb^t - x_i^t)$$

$$x_i^{t+1} = x_i^t + v_i^{t+1}$$

# PSO basic algorithm

## Continuos optimization problem

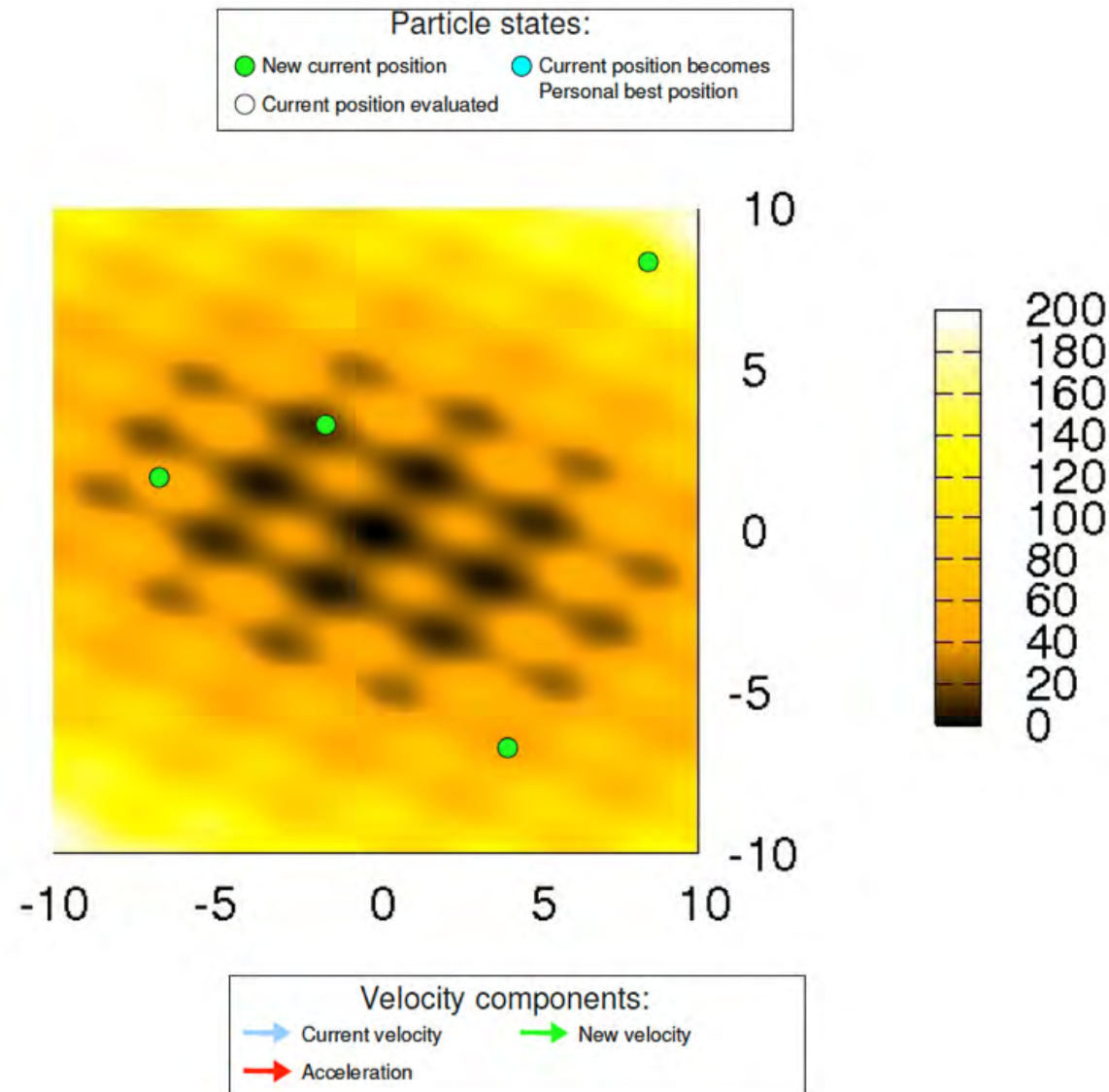


Find  $\mathcal{X}^* \subseteq \mathcal{X} \subseteq \mathcal{R}^n$  such that

$$\mathcal{X}^* = \operatorname{argmin}_{x \in \mathcal{X}} f(x) = \{x^* \in \mathcal{X} : f(x^*) \leq f(x) \ \forall x \in \mathcal{X}\}$$

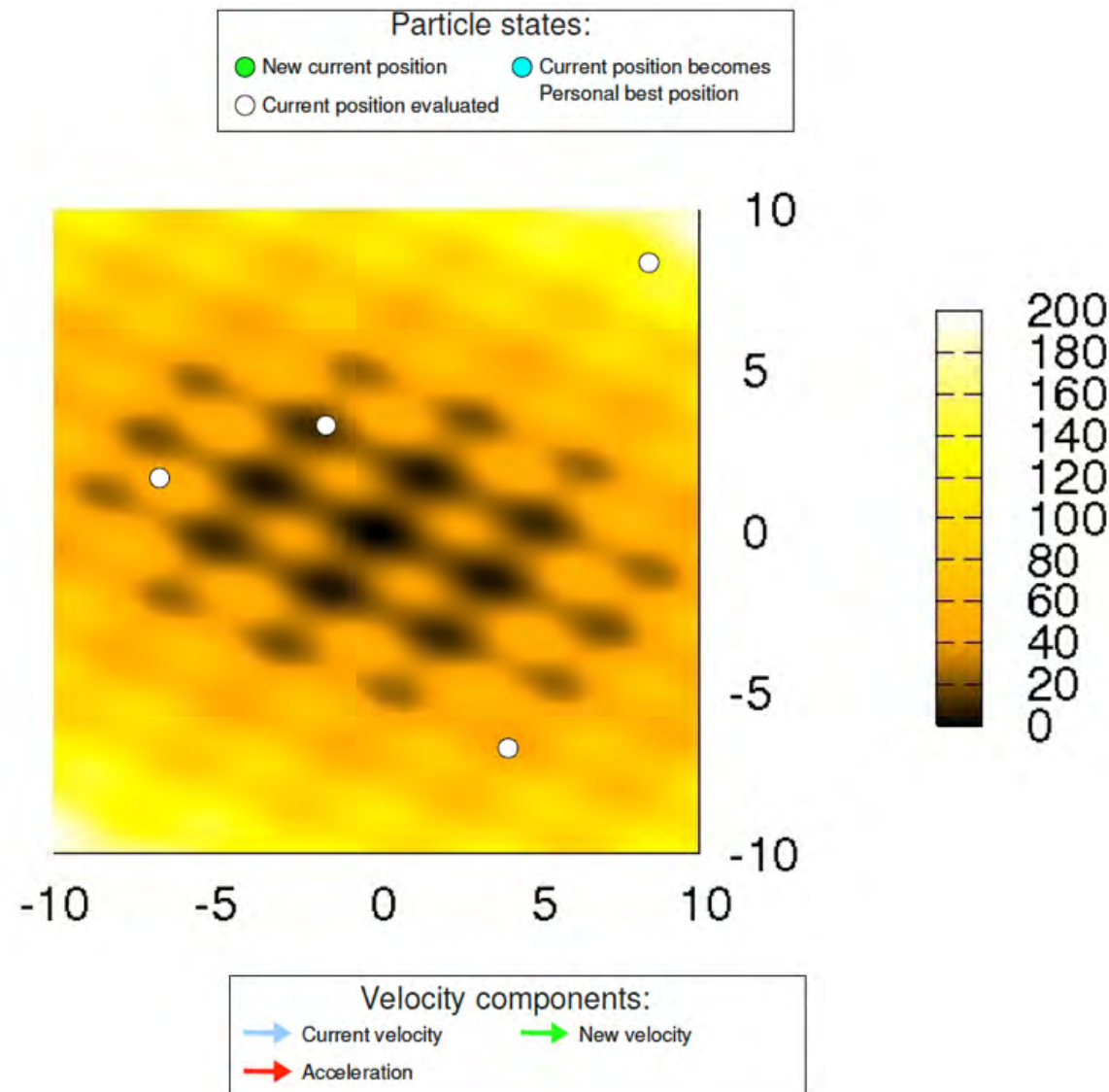
# PSO basic algorithm

1. Create a population of agents (called particles) uniformly distributed over X



# PSO basic algorithm

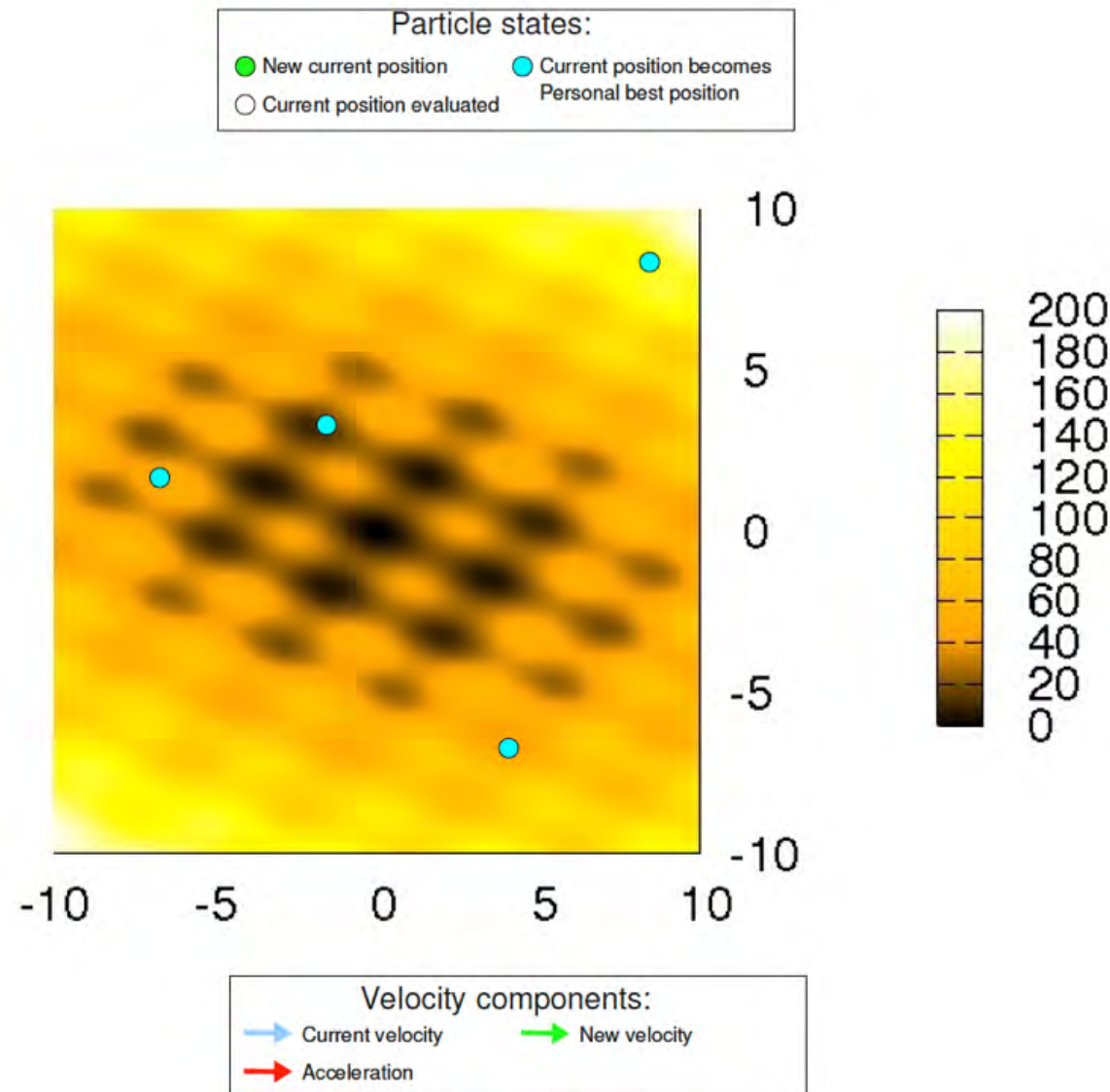
2. Evaluate each particle's position according to the objective function





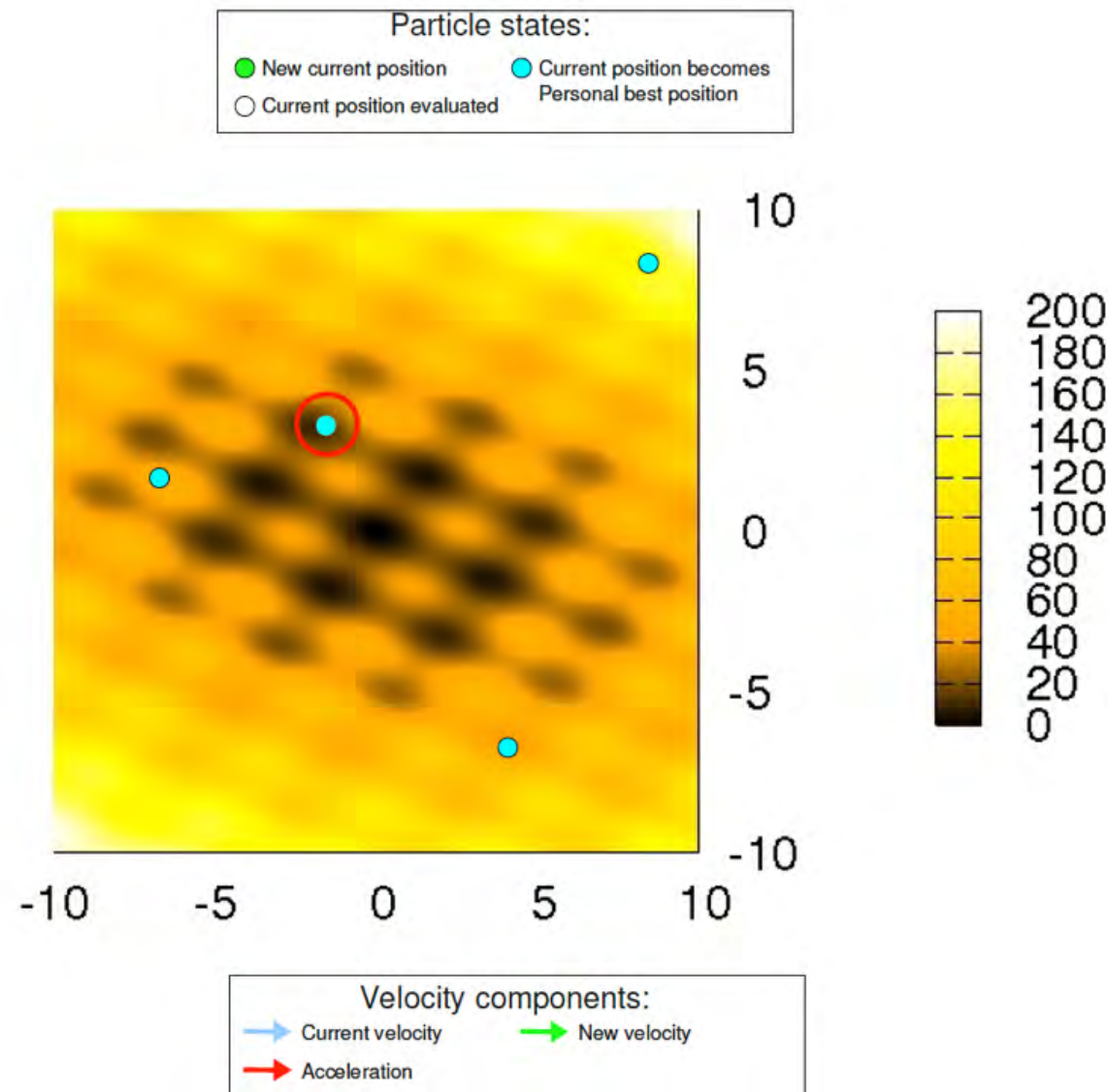
# PSO basic algorithm

3. A particle compares its current position with its personal best position. If there is improvement, the particle's current position becomes its new personal best position



# PSO basic algorithm

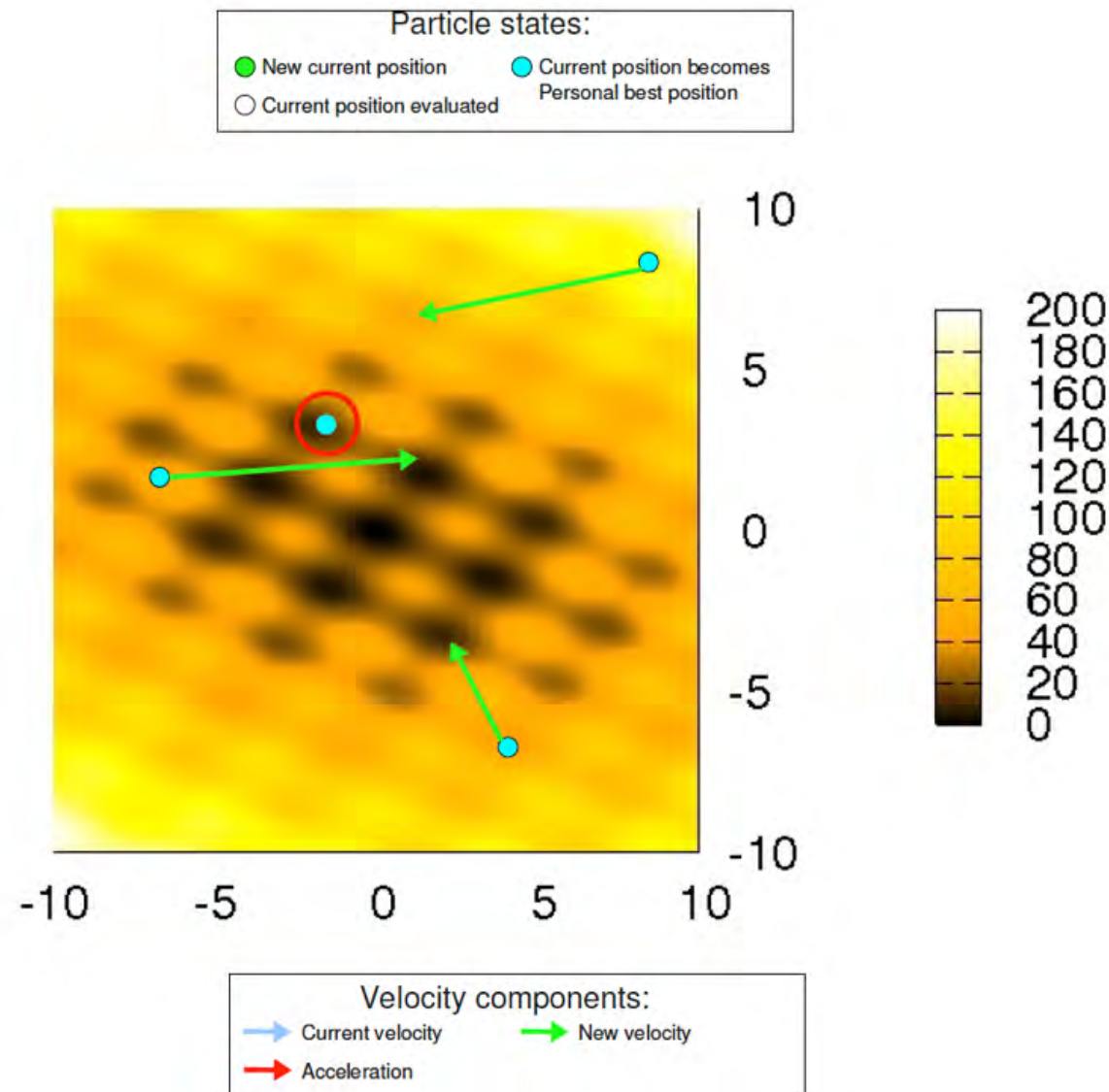
## 4. Determine the best particle



# PSO basic algorithm

5. Update particles' velocities according to

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t (pb_i^t - x_i^t) + \psi_2 U_2^t (lb_i^t - x_i^t)$$

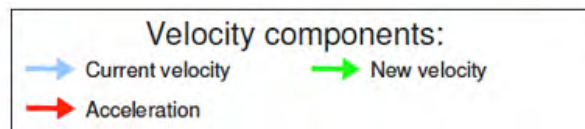
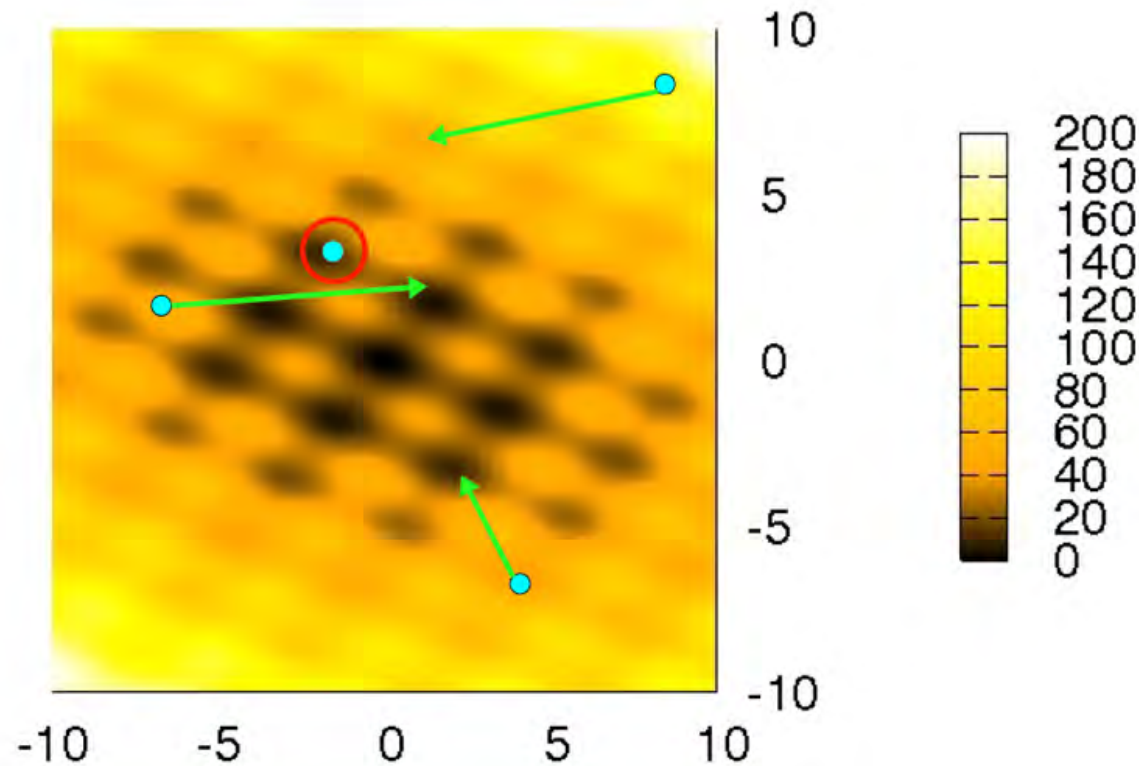
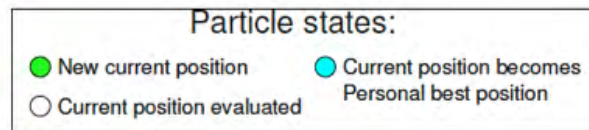


# PSO basic algorithm

5. Update particles' velocities according to

$$v_i^{t+1} = \cancel{v_i^t} + \psi_1 U_1^t (pb_i^t - x_i^t) + \psi_2 U_2^t (lb_i^t - x_i^t)$$

II  
0

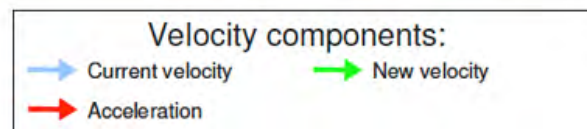
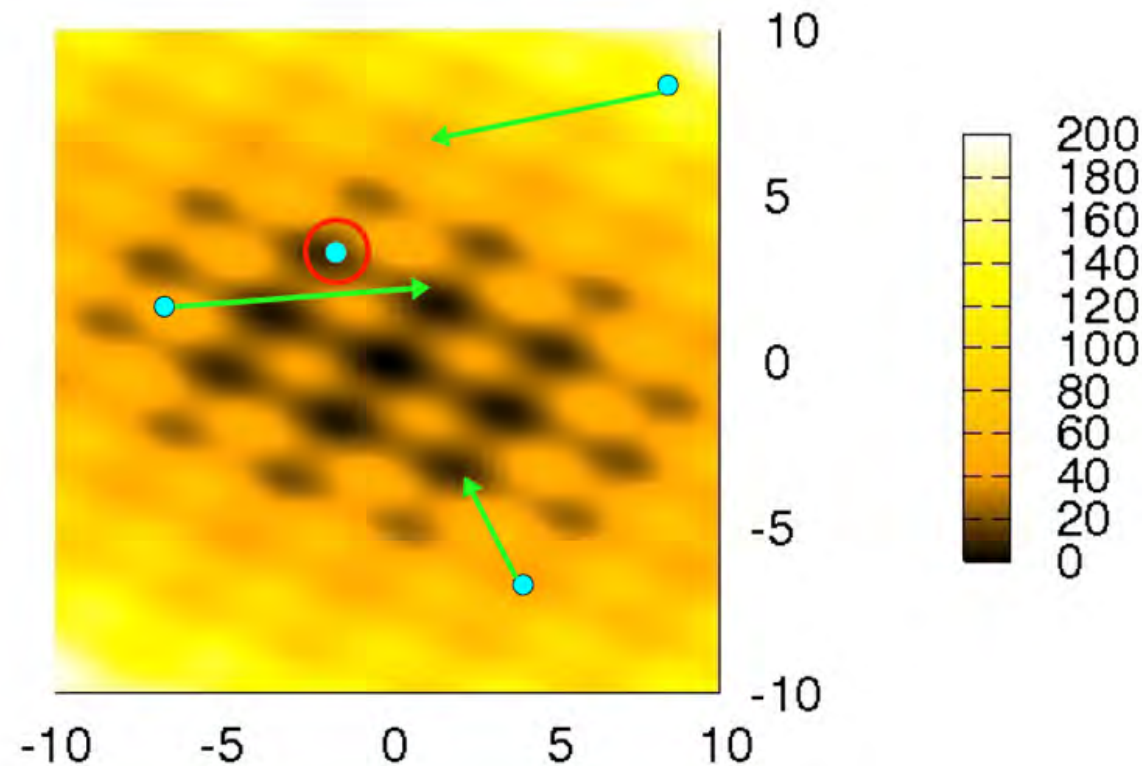
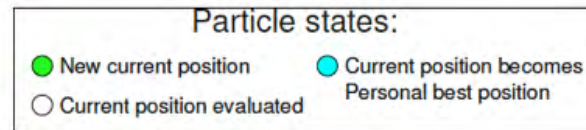


# PSO basic algorithm

5. Update particles' velocities according to

$$v_i^{t+1} = \cancel{v_i^t} + \psi_1 \cancel{U_1^t(p b_i^t - x_i^t)} + \psi_2 U_2^t(l b_i^t - x_i^t)$$

||  
0 ||  
0

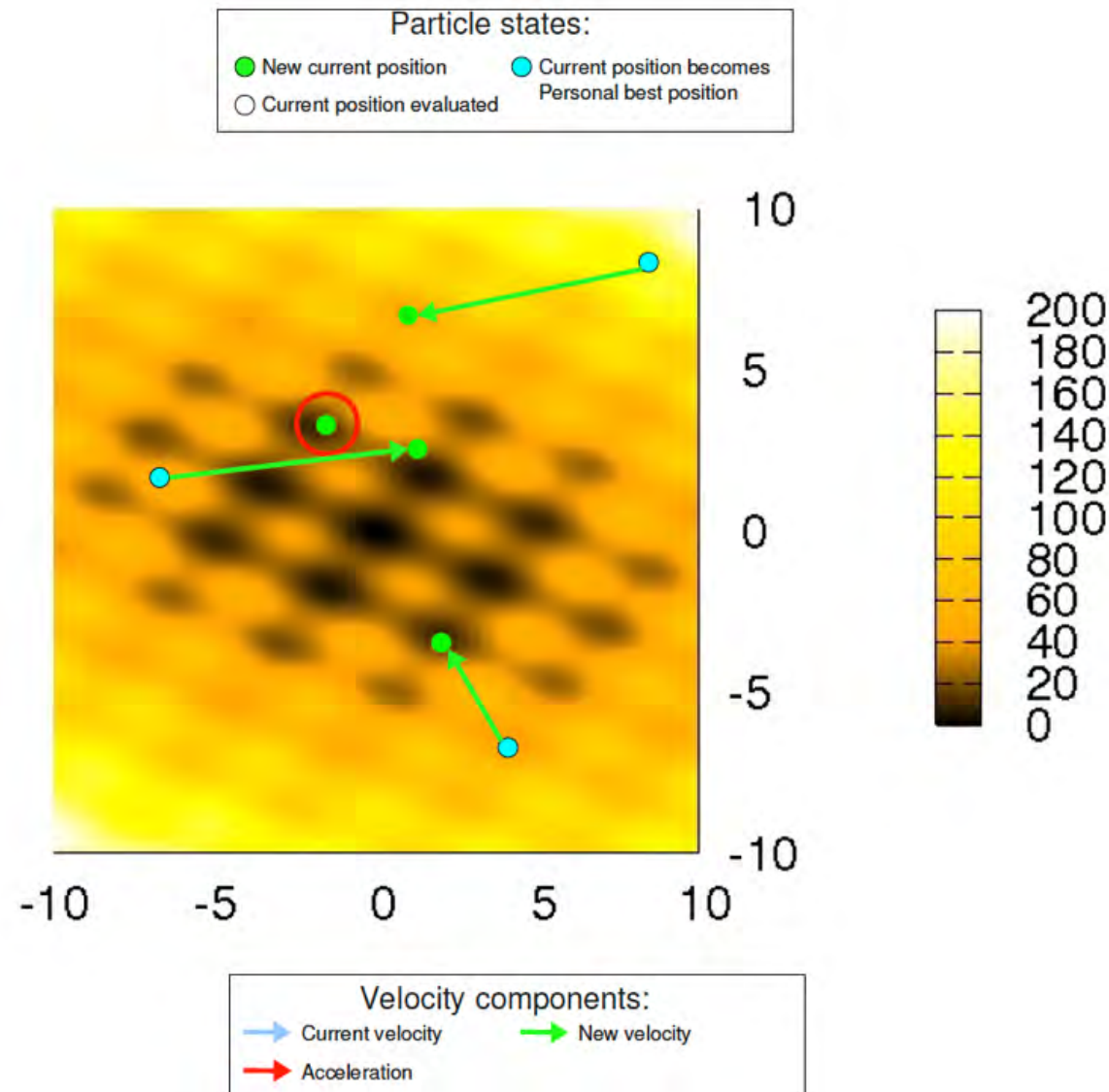




# PSO basic algorithm

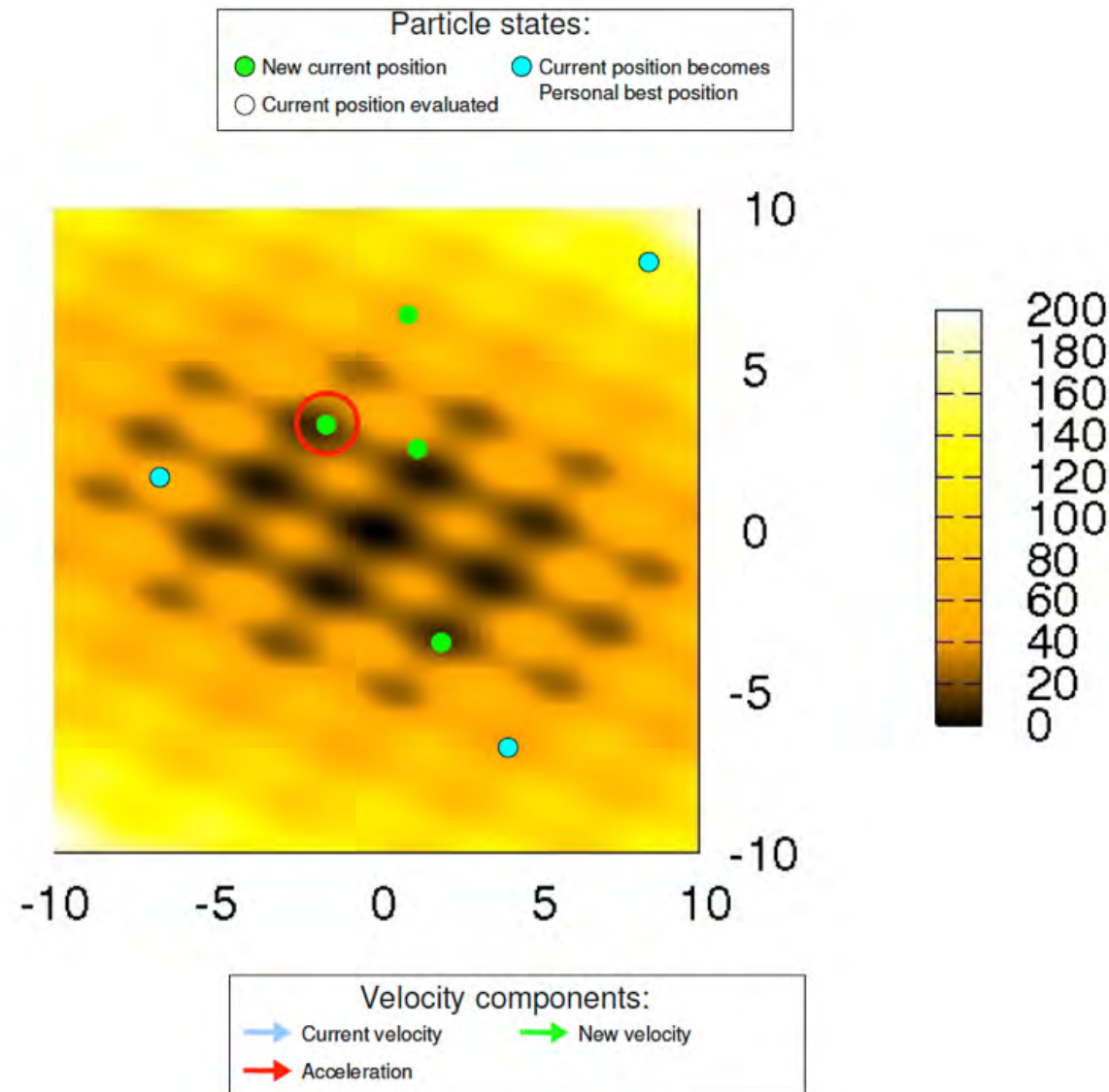
6. Move particles to their new positions according to

$$x_i^{t+1} = x_i^t + v_i^{t+1}$$



# PSO basic algorithm

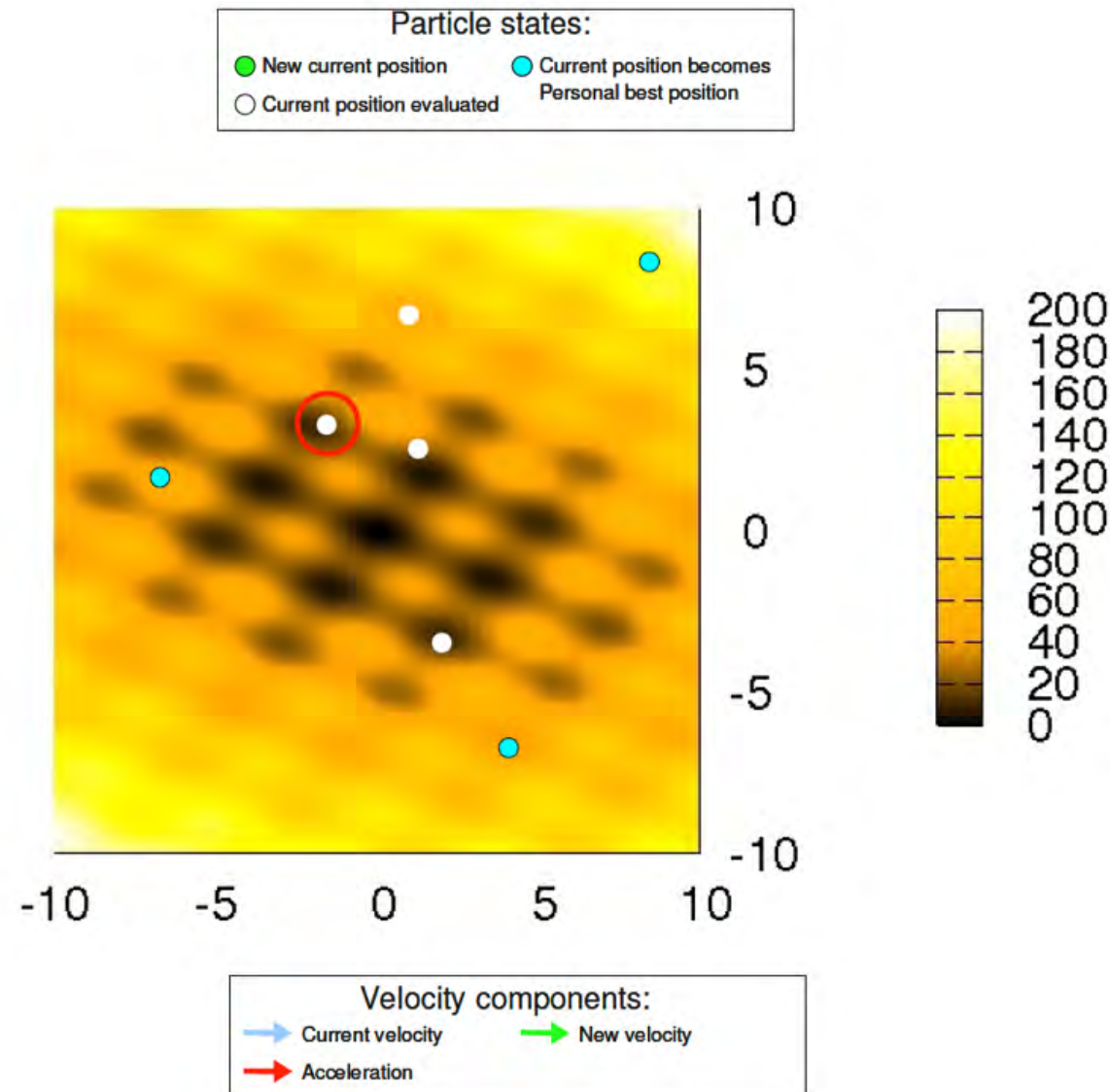
7. Go to step 2 until stopping criteria are satisfied





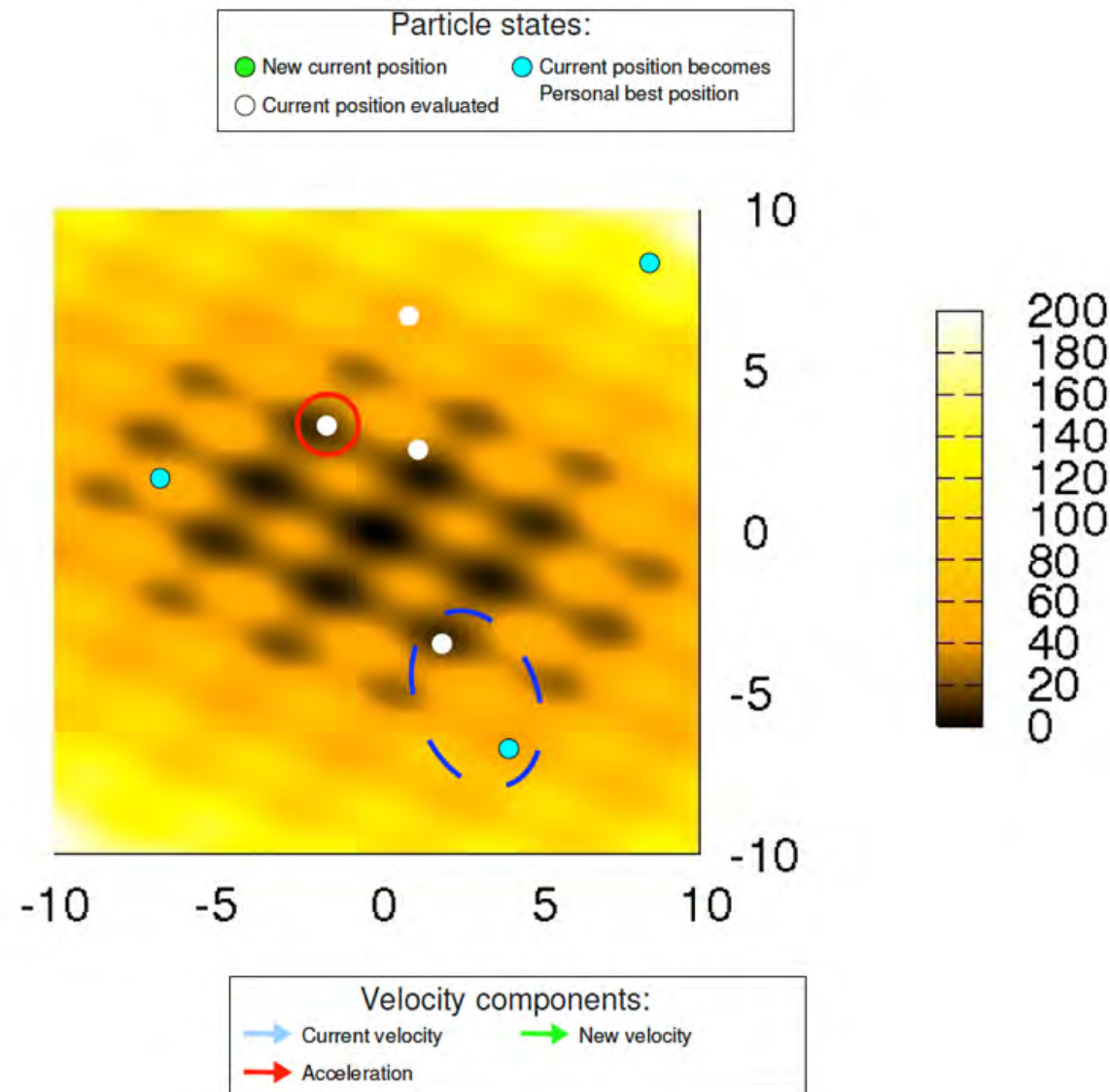
# PSO basic algorithm

2. Evaluate each particle's position according to the objective function



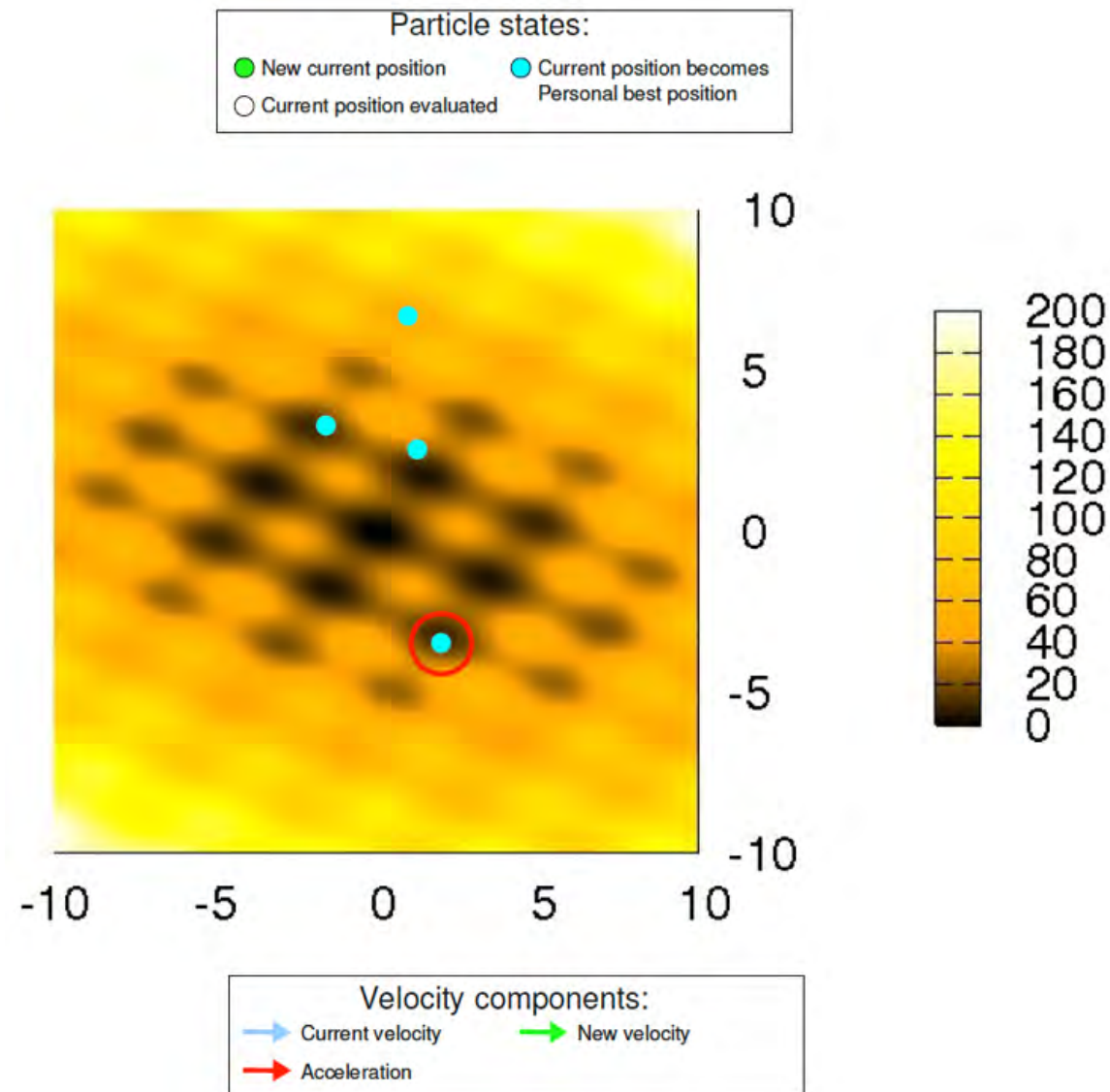
# PSO basic algorithm

3. A particle compares its current position with its personal best position. If there is improvement, the particle's current position becomes its new personal best position



# PSO basic algorithm

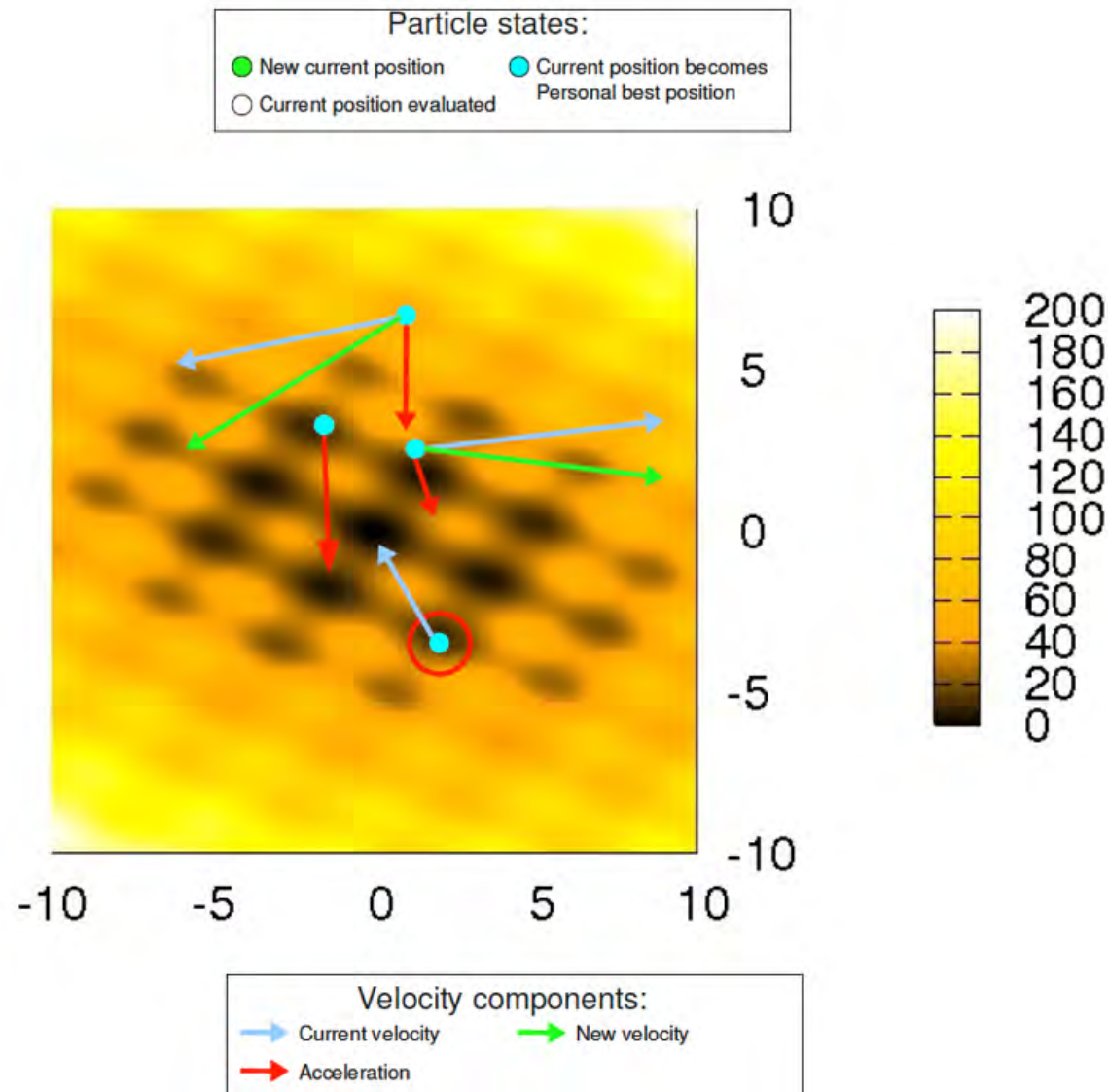
## 4. Determine the best particle



# PSO basic algorithm

5. Update particles' velocities according to

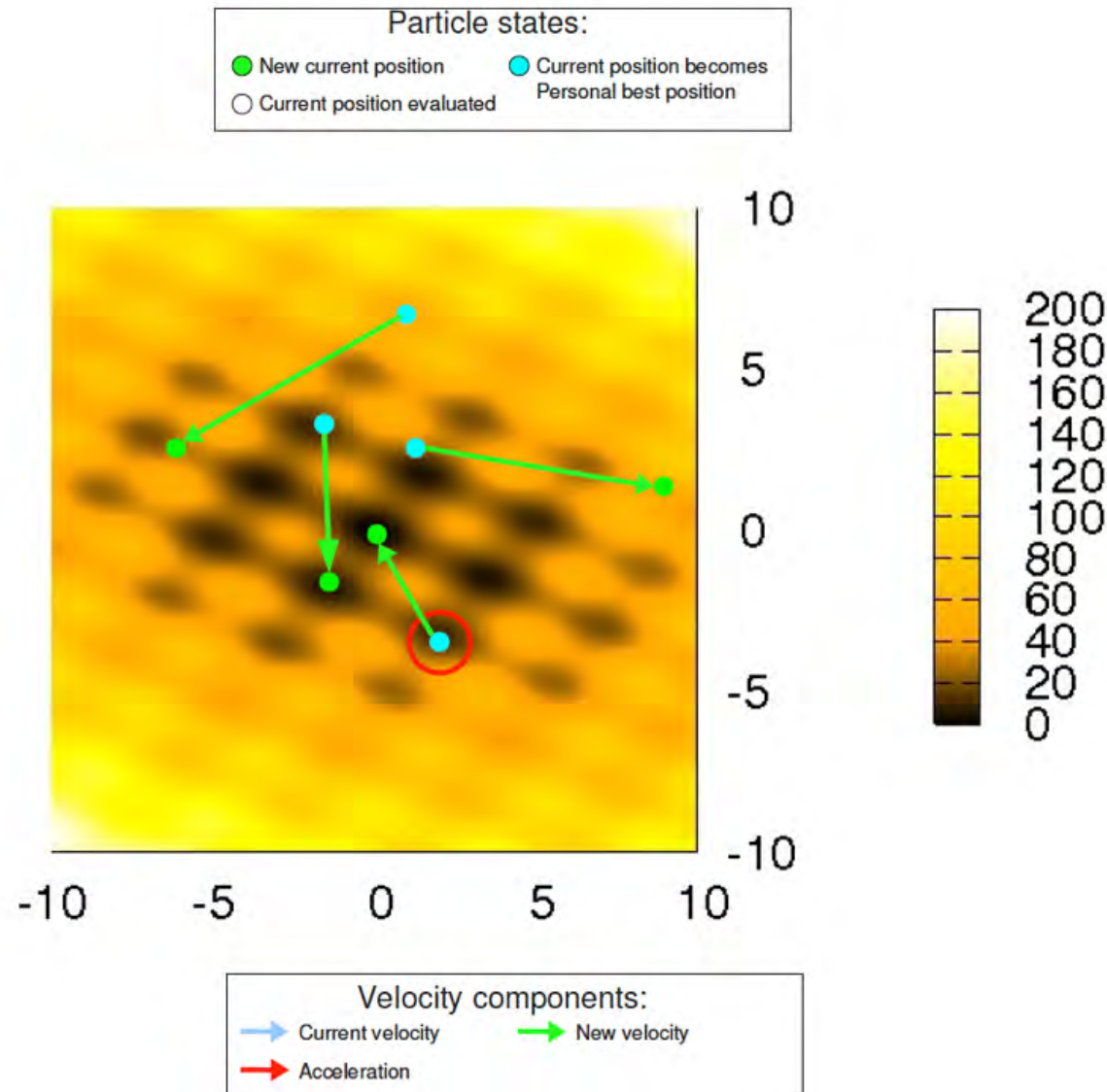
$$v_i^{t+1} = v_i^t + \psi_1 U_1^t (pb_i^t - x_i^t) + \psi_2 U_2^t (lb_i^t - x_i^t)$$



# PSO basic algorithm

6. Move particles to their new positions according to

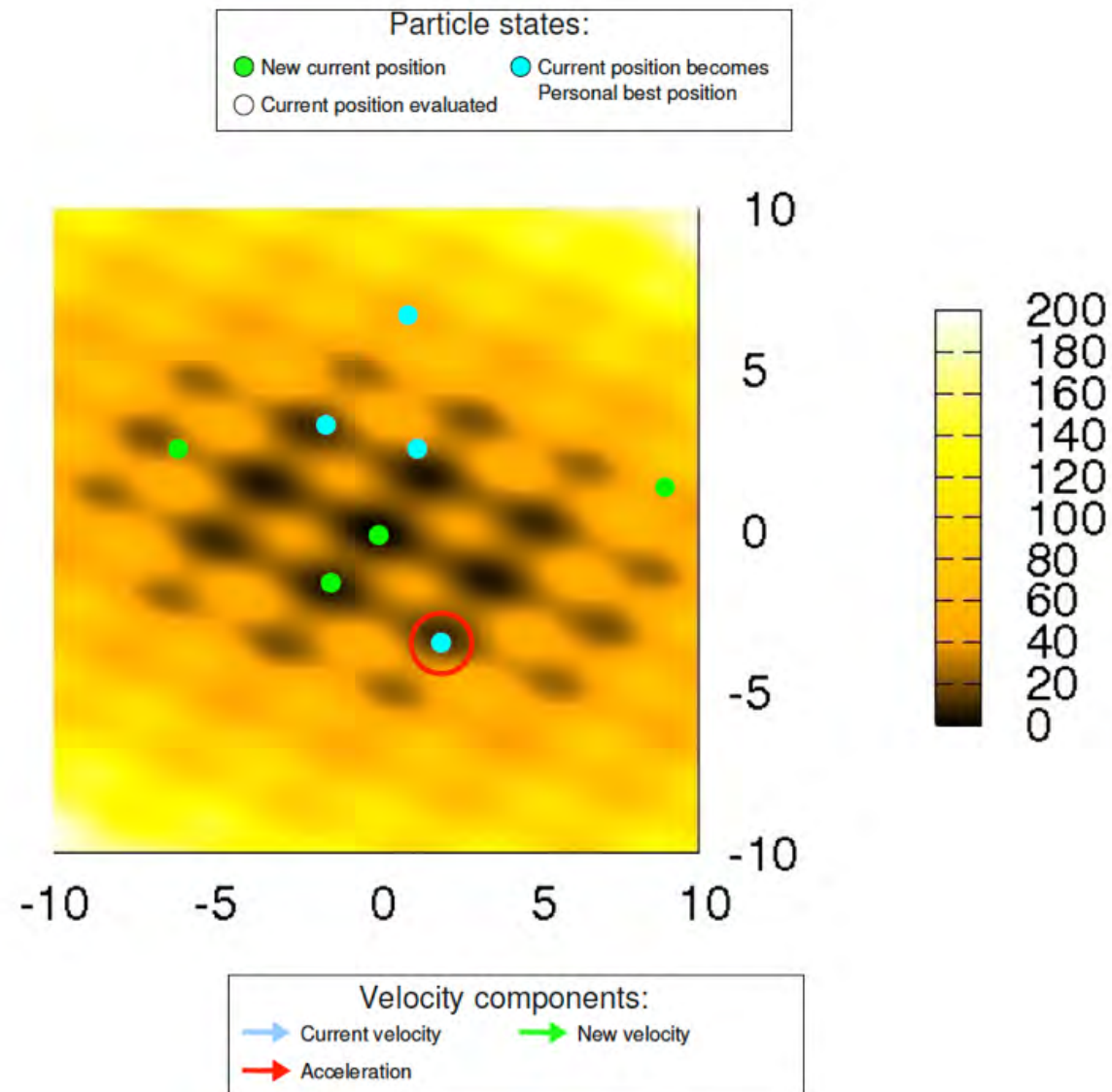
$$x_i^{t+1} = x_i^t + v_i^{t+1}$$





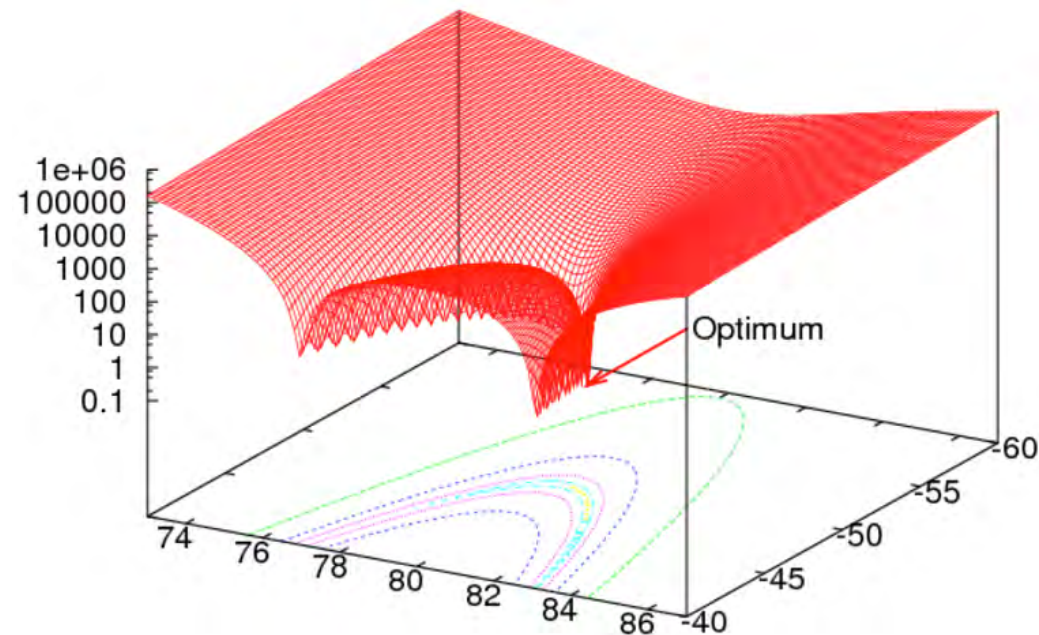
# PSO basic algorithm

7. Go to step 2 until stopping criteria are satisfied



# Example

Rosenbrock function (2D):  $100(x_2 - x_1^2)^2 + (x_1 - 1)^2$

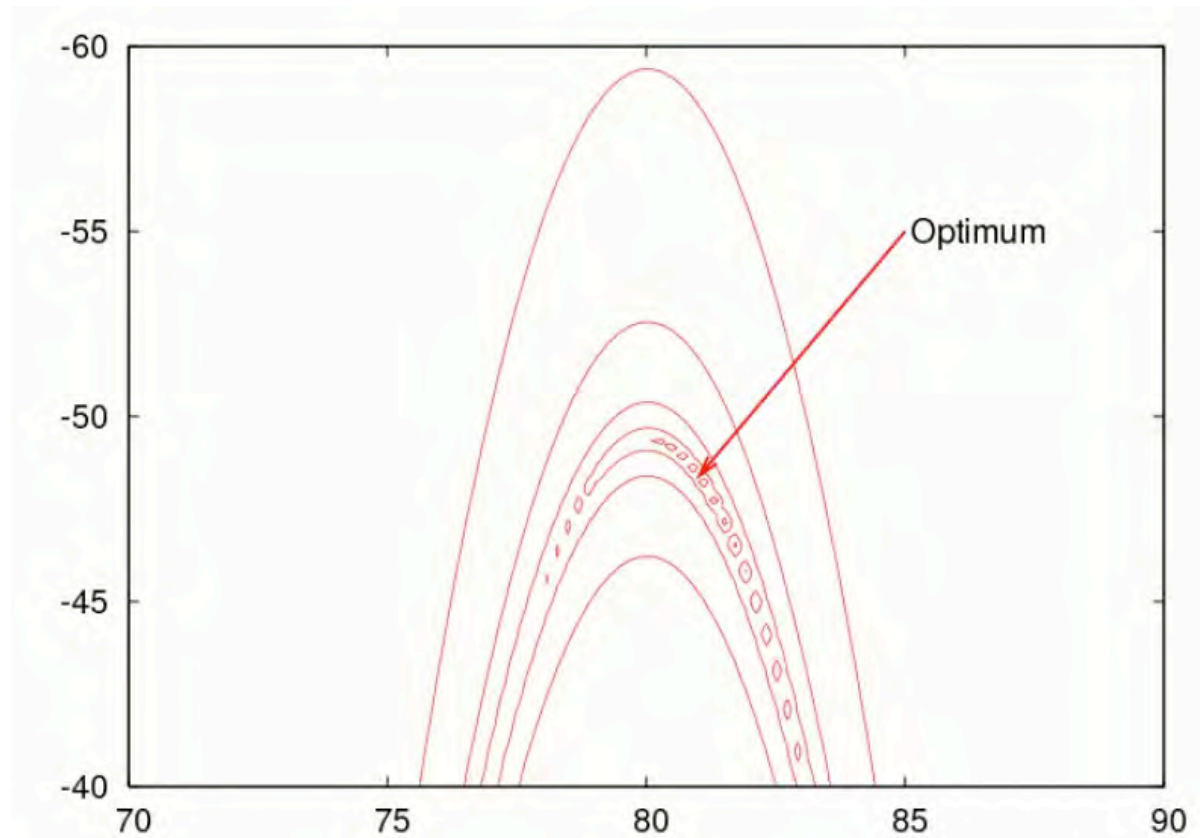


Difficult benchmark function:  
optimum is located at the bottom of a narrow curved valley



# Example

Rosenbrock function (2D):  $100(x_2 - x_1^2)^2 + (x_1 - 1)^2$



The black dots are the particles' current positions.  
The blue dots are the particles' personal best positions



# PSO variants

Almost all modifications vary in some way the velocity-update rule:

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t(pb_i^t - x_i^t) + \psi_2 U_2^t(gb^t - x_i^t)$$



# PSO variants

Almost all modifications vary in some way the velocity-update rule:

inertia

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t(pb_i^t - x_i^t) + \psi_2 U_2^t(gb^t - x_i^t)$$



# PSO variants

Almost all modifications vary in some way the velocity-update rule:

personal influence

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t(pb_i^t - x_i^t) + \psi_2 U_2^t(gb^t - x_i^t)$$



# PSO variants

Almost all modifications vary in some way the velocity-update rule:

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t(pb_i^t - x_i^t) + \overset{\text{social influence}}{\psi_2 U_2^t(lb_i^t - x_i^t)}$$

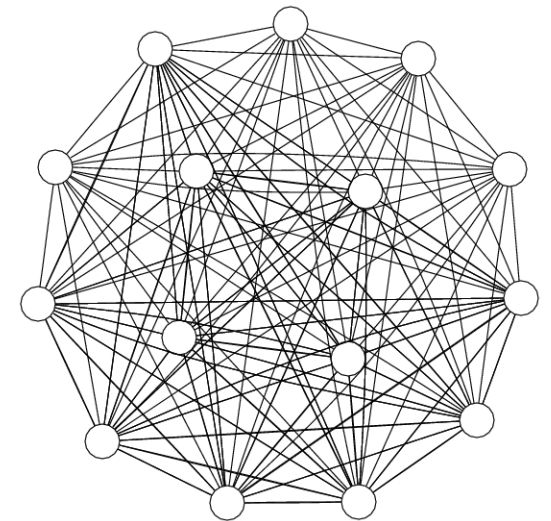
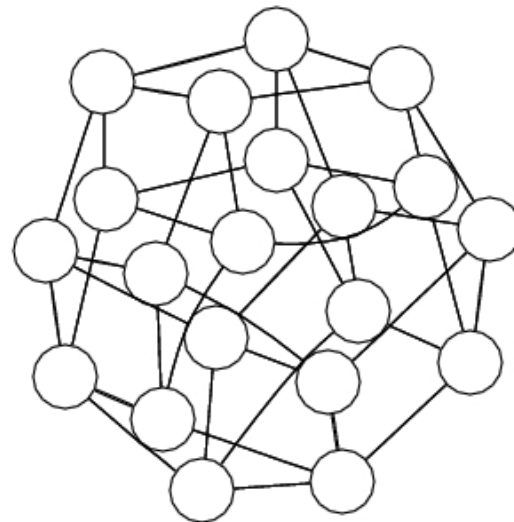
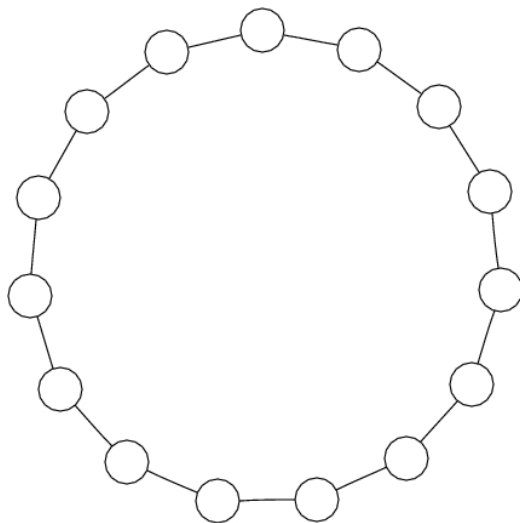
# PSO: neighborhood topology

Particles' neighborhoods create a population topology

For each particle, the social influence term depends on its best neighbor

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t(pb_i^t - x_i^t) + \psi_2 U_2^t(lb_i^t - x_i^t)$$

$$v_i^{t+1} = v_i^t + \psi_1 U_1^t(pb_i^t - x_i^t) + \psi_2 U_2^t(gb^t - x_i^t)$$





# Inertia weight

A parameter called inertia weight can be used to control the particles' speed of convergence

A large inertia weight favors the diversification of the search process while a small inertia weight favors its intensification

The modified rule is:



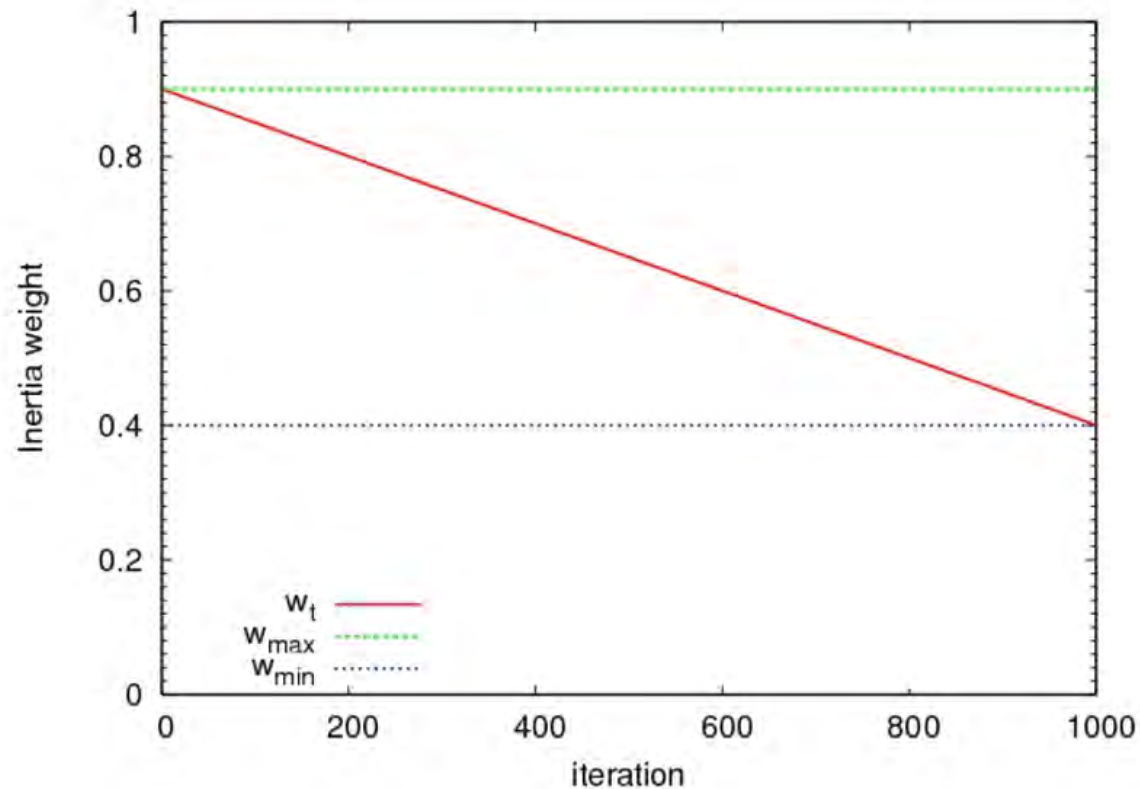
$$v_i^{t+1} = w \cdot v_i^t + \psi_1 U_1^t(pb_i^t - x_i^t) + \psi_2 U_2^t(lb_i^t - x_i^t)$$

with  $0.0 < w \leq 1.0$



# Inertia weight

The value of the inertia weight can be decreased during a run to favor diversification during the first iterations of the algorithm and intensification during the last ones





# Other variants

There are many other variants reported in the literature. Among others:

- with dynamic neighborhood topologies (e.g., Suganthan [1999], Mohais et al. [2005])
- with different velocity update rules (e.g., Poli et al. [2005], Liu et al. [2005] )
- with components from other approaches (e.g., Angeline [1998], Iqbal & Montes de Oca [2006] )
- for discrete optimization problems (e.g., Kennedy & Eberhart [1997], Wang et al. [2003] )
- ...

Thousands of papers deal with PSO algorithms and its applications

# Scholarpedia articles

- [http://www.scholarpedia.org/article/Swarm\\_intelligence](http://www.scholarpedia.org/article/Swarm_intelligence)
- [http://www.scholarpedia.org/article/Particle\\_swarm\\_optimization](http://www.scholarpedia.org/article/Particle_swarm_optimization)
- [http://www.scholarpedia.org/article/Ant\\_colony\\_optimization](http://www.scholarpedia.org/article/Ant_colony_optimization)
- [http://www.scholarpedia.org/article/Swarm\\_robotics](http://www.scholarpedia.org/article/Swarm_robotics)



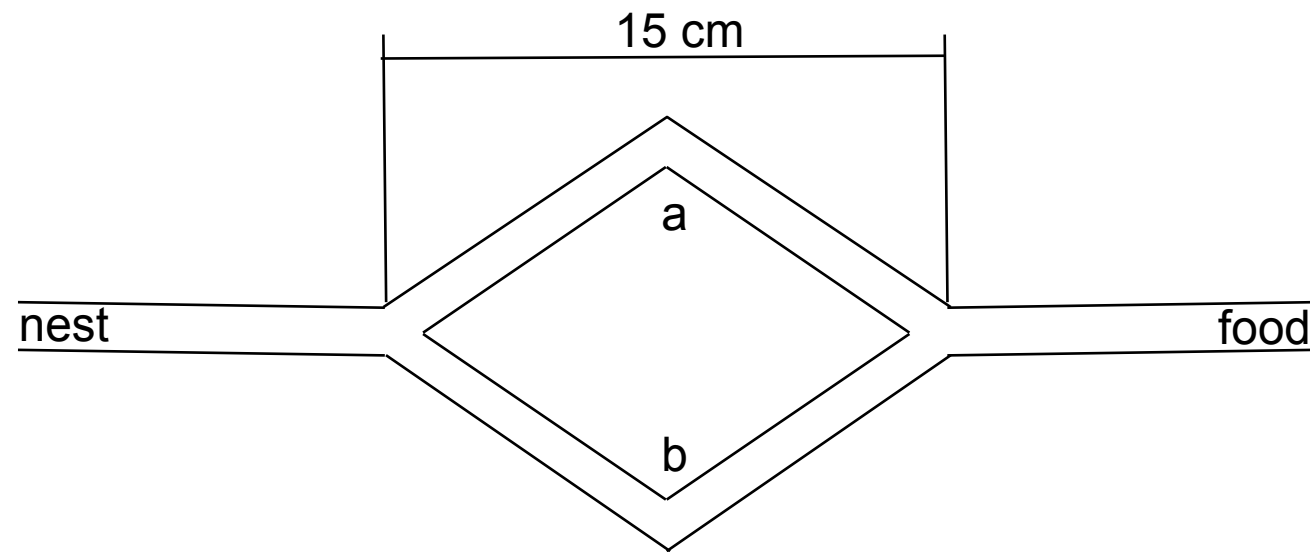
From scientific to engineering swarm intelligence

# Examples

- Cemetery organization and brood sorting ➡ data clustering
- Birds flocking ➡ particle swarm optimization
- **Foraging** ➡ **ant colony optimization**
- Self-assembly and cooperative transport ➡ robotic implementations
- Division of labor ➡ adaptive task allocation

# Third example:

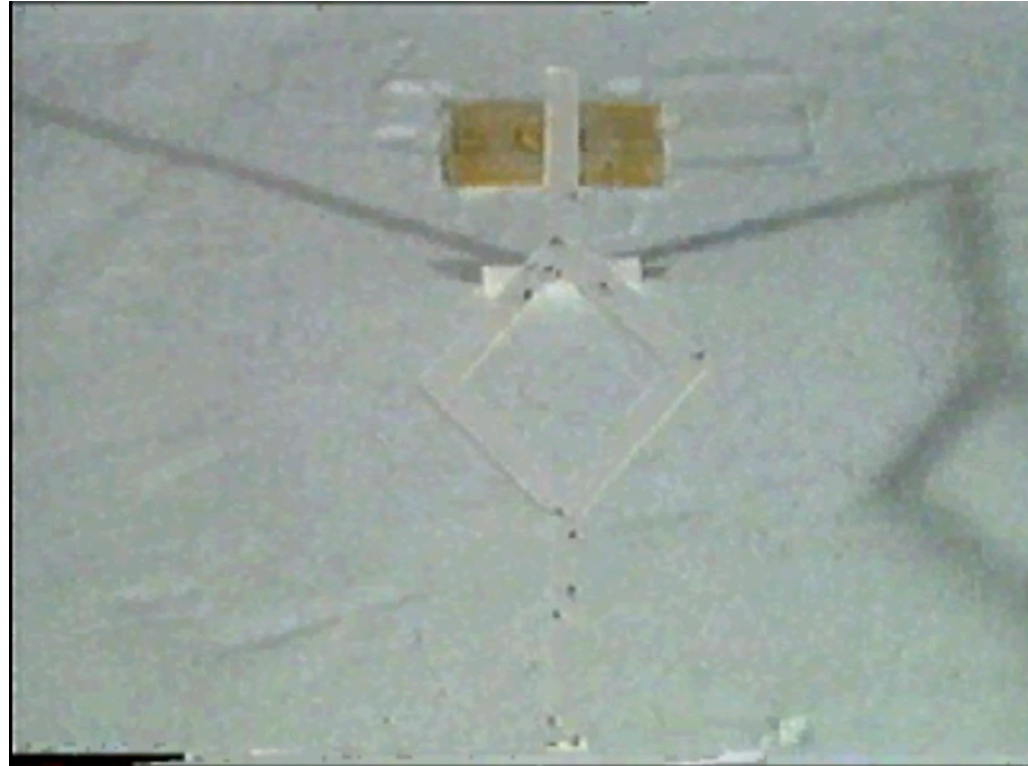
Ants' foraging behavior as an inspiration for shortest path algorithms (ant colony optimization)



The symmetric double bridge experiment  
(Deneubourg et al. 1989)

Ant colony optimization: the inspiration

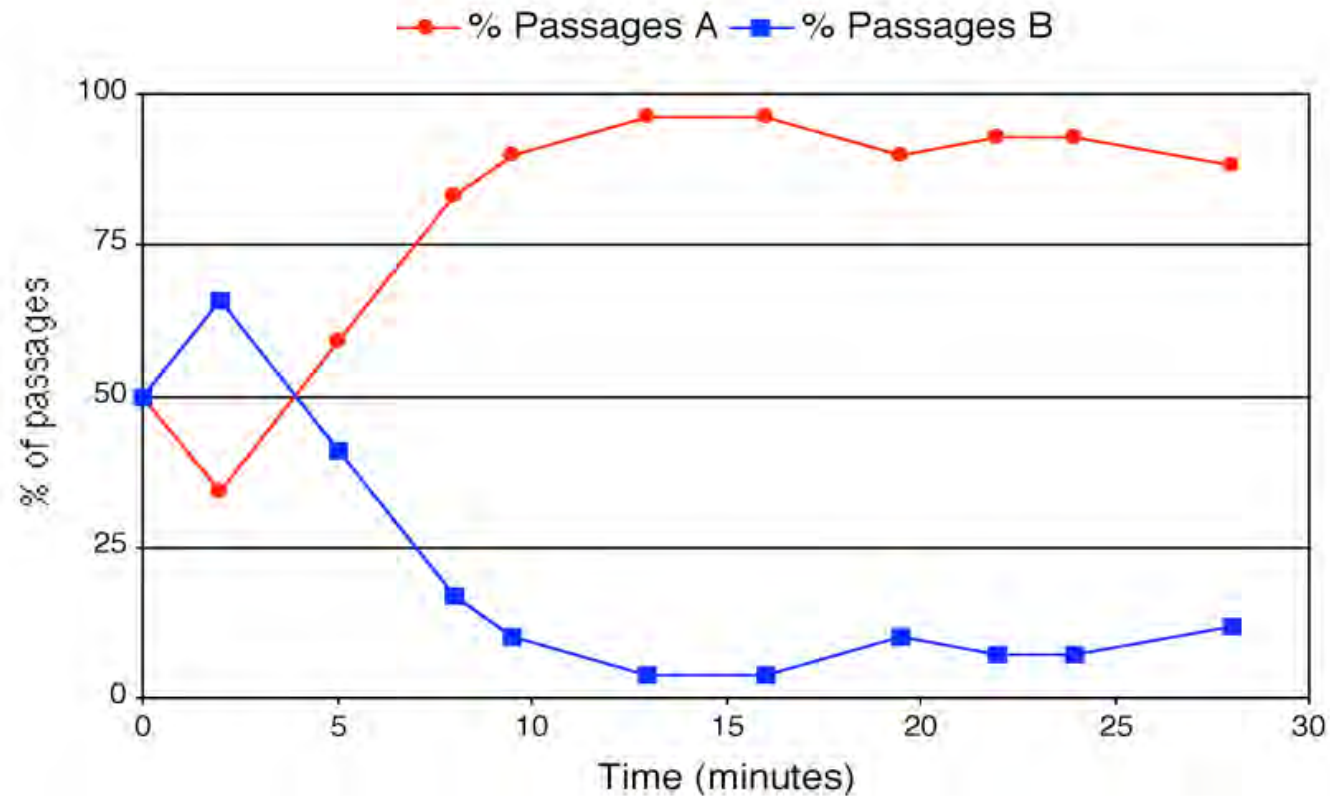
# Ants' foraging behavior



The symmetric double bridge experiment  
(Deneubourg et al. 1989)

Ant colony optimization: the inspiration

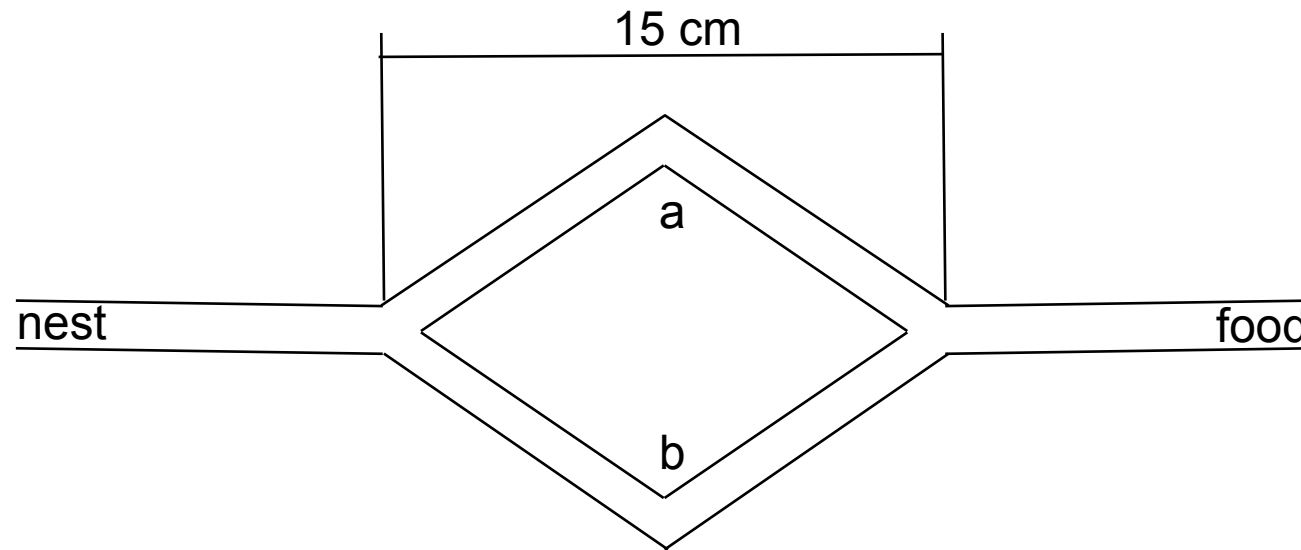
# Ants' foraging behavior





Ant colony optimization: the inspiration

# Ants' foraging behavior

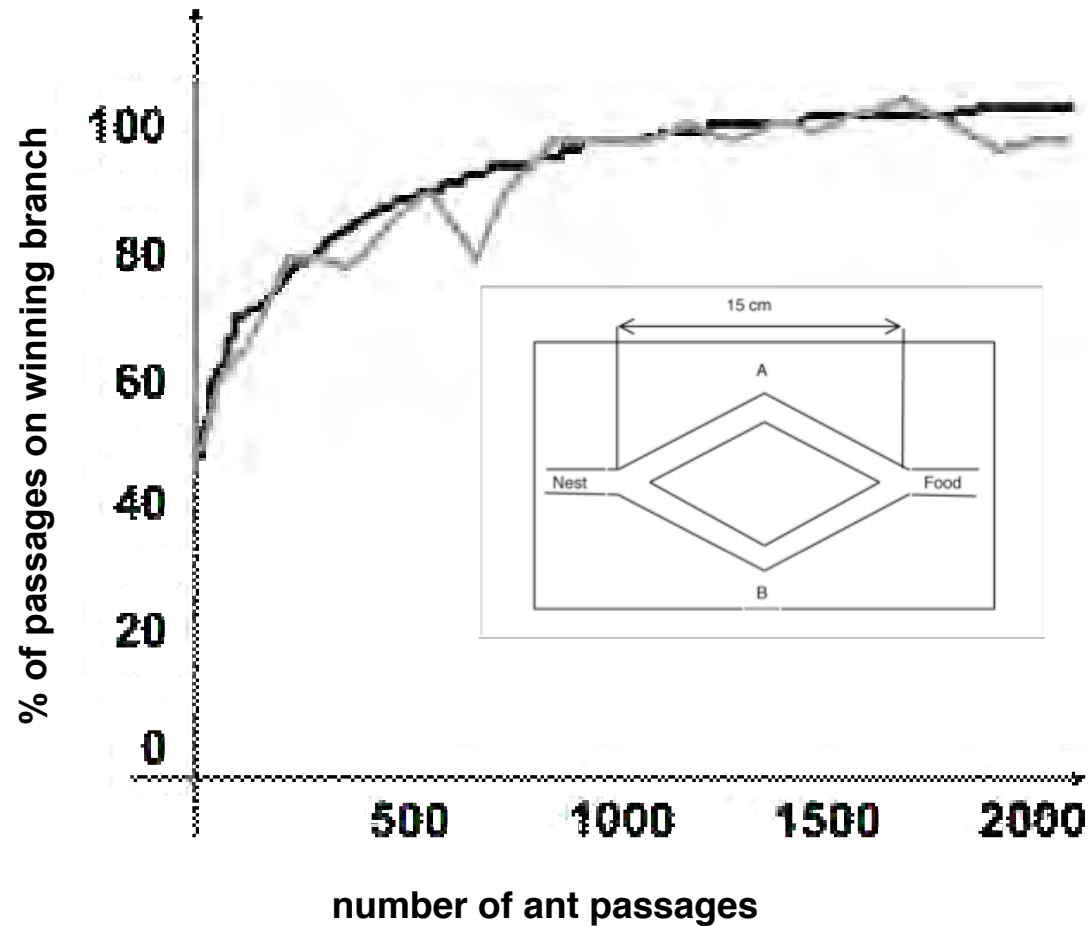


$$P_a = \frac{(c + a_i)^2}{(c + a_i)^2 + (c + b_i)^2} = 1 - P_b \quad a_{i+1} = \begin{cases} a_{i+1} & \text{if } \delta \leq P_a \\ a_i & \text{if } \delta > P_a \end{cases}$$

- $a_i$  = number of ants which chose a after  $i$  ants have made a choice
- $a_i + b_i = i$
- $\delta$  is randomly uniform in  $[0,1]$

Ant colony optimization: the inspiration

# Ants' foraging behavior

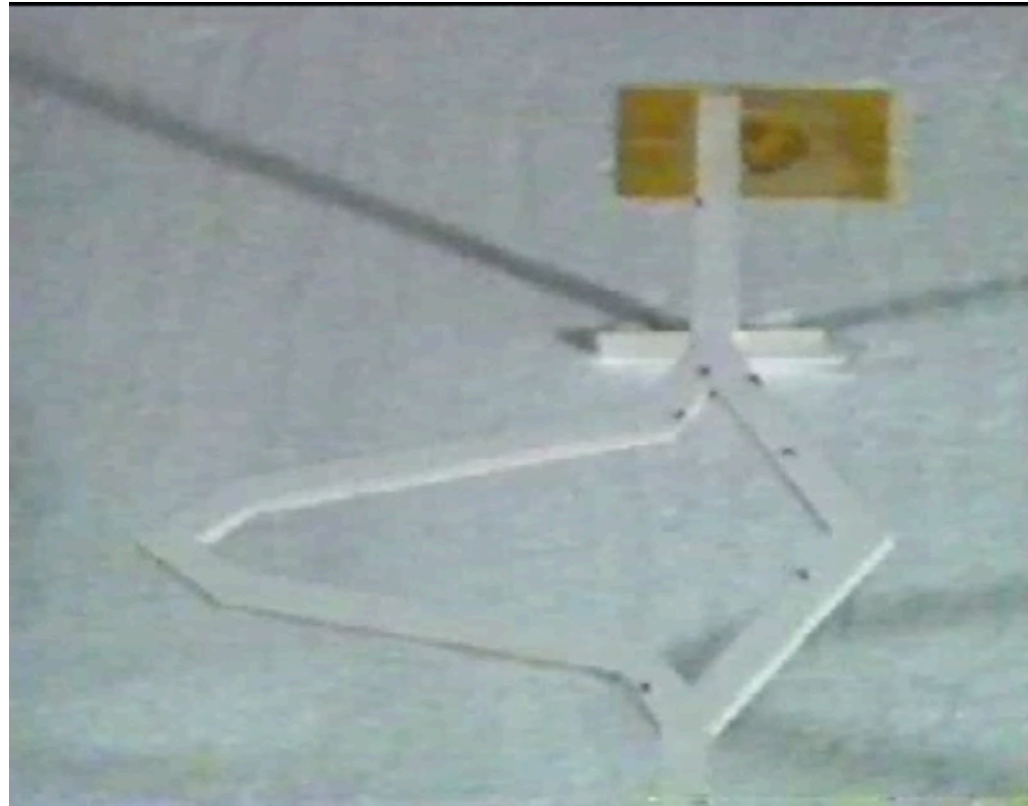


$$P_A = \frac{(c + A_i)^2}{(c + A_i)^2 + (c + B_i)^2} = 1 - P_B$$

$$A_{i+1} = \begin{cases} A_i + 1 & \text{if } \delta \leq P_A \\ A_i & \text{if } \delta > P_A \end{cases}$$

Ant colony optimization: the inspiration

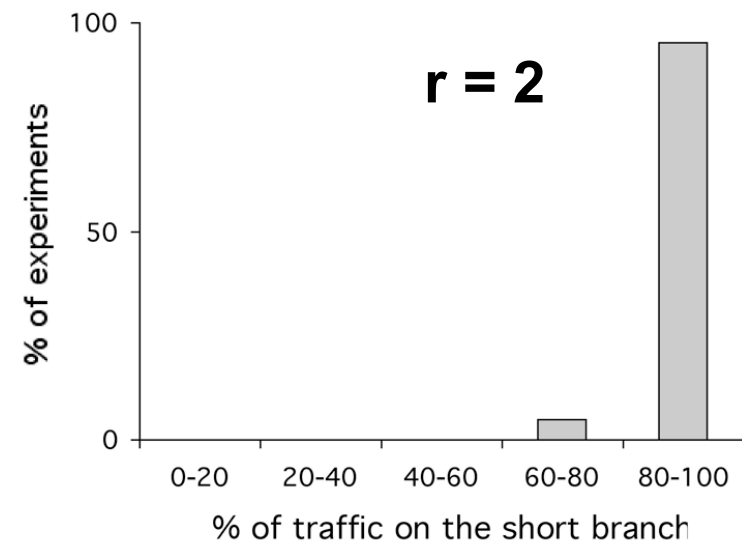
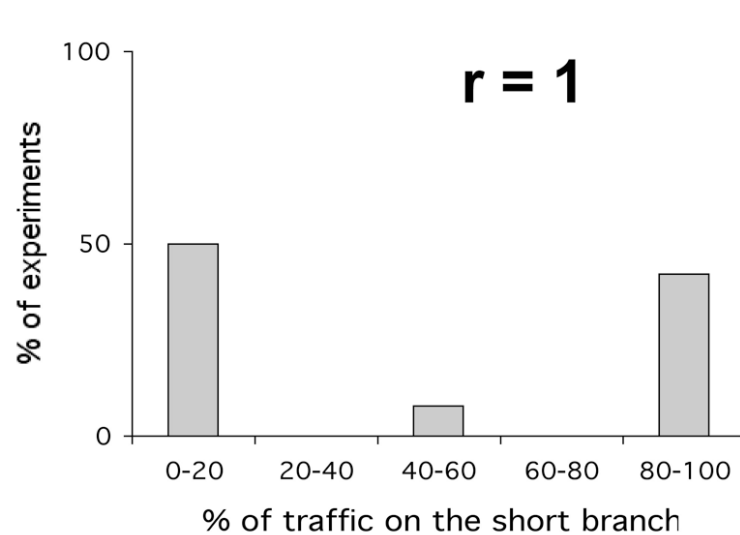
# Ants' foraging behavior



The asymmetric double bridge experiment  
(Deneubourg et al. 1989)

Ant colony optimization: the inspiration

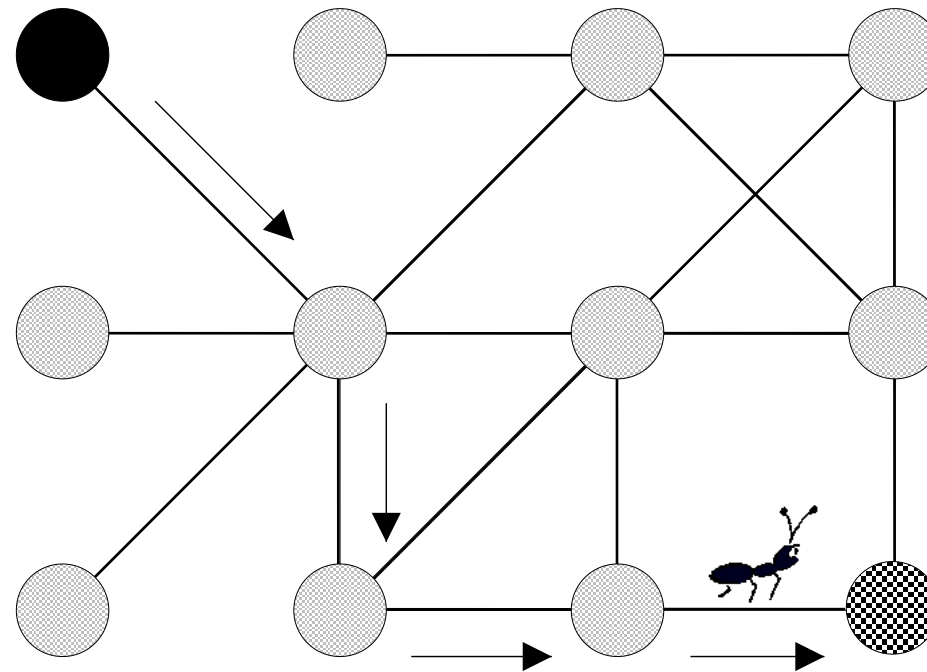
# Ants' foraging behavior



Ant colony optimization: the application

# From real to artificial ants

Source



Destination