IE531: Algorithms for Data Analytics Spring, 2016

Programming Assignment 1: Listing the n-th Lexicographic Permutation of a Symbol-Set with m Symbols

Due Date: February 29, 2016

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This assignment is a generalization of Problem 24 of Project Euler. The objective is to retrieve (or, reconstruct) a cataloged-object from a (large) collection of such objects that are ordered lexicographically (i.e. in "dictionary-order"). We will restrict attention to the case where the "alphabet" (over which the lexicographic/dictionary-order is maintained) is the numbers $\{0,1,\ldots,m\}(m \leq 9)$, where 0 is the first-member, 1 is second-member, 2 is the third-member etc. of the "alphabet." The objective is to generate the n-th member of the lexicographic list.

You are going to write a C++ program that will take the numbers n and m are command-line variables. A sample output is shown in figure 1. I have uploaded a hint.cpp file on Compass, in case you need help. Before you attempt this problem make sure you view the flipped-classroom video on this assignment, and the video that covers the Academic Integrity issues that are important to this course.

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Ramavarapus-Air:Debug sreenivas$ ./nth\ lexicographic\ permutation 1000000 10
Adopted Lexicographic Order is: 0123456789
Factorial-Number-System-Expansion of 1000000 is given below
1000000 = (0*1!) + (2*2!) + (2*3!) + (1*4!) + (5*5!) + (2*6!) + (6*7!) + (6*8!) + (2*9!)
Therefore, the 1000000-th lexicographic permutation is: 2783915460
Ramavarapus-Air:Debug sreenivas$ ./nth\ lexicographic\ permutation 2000003 10
Adopted Lexicographic Order is: 0123456789
Factorial-Number-System-Expansion of 2000003 is given below
2000003 = (1*1!) + (2*2!) + (1*3!) + (3*4!) + (4*5!) + (5*6!) + (4*7!) + (4*8!) + (5*9!)
Therefore, the 2000003-th lexicographic permutation is: 5468731902
Ramavarapus-Air:Debug sreenivas$ ./nth\ lexicographic\ permutation 3000007 10
Adopted Lexicographic Order is: 0123456789
Factorial-Number-System-Expansion of 3000007 is given below
3000007 = (1*1!) + (0*2!) + (1*3!) + (0*4!) + (4*5!) + (1*6!) + (3*7!) + (2*8!) + (8*9!)
Therefore, the 3000007-th lexicographic permutation is: 8241705369
Ramavarapus-Air:Debug sreenivas$
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Figure 1: Sample output for this assignment. In all of these illustrative examples m=10 (i.e. the "alphabet" is $\{0,2,\ldots,8\}$. I have presented the results for three cases here (viz. n=1000000, n=2000003 and n=3000007)