

↳ Dynamic Programming

↳ State - vars

↳ Decision - vars.

↳ Objective fn \rightarrow A dynamic fn that associates current rewards with other rewards.

\Rightarrow The complication is we need to evaluate all the decision-variables for all combination of STATE - VARIABLES

\Rightarrow Decision variables + State variables are interdependent for majority of times.

For t^{th} day till T Days

↳ For i^{th} piece of cake.

↳ Evaluate for all choices.

Take statistic of all those evaluations.

Max value. \leftarrow

$$V(s, t) = \max \sum \text{Profit across all choices} + \text{Profit}(At t+1)$$

Because our stop criterion is at $(T+1)^{\text{th}}$ day.

KNAPSACK in a looping manner.

- ⇒ 0/1 → choice. (हो या न हो)
- ⇒ States → number of elements left in the choice bag + weight of knapsack left.
- ⇒ Objective → Maximize value (Reward)
- ⇒ Stop criterion → If Wt of knapsack ≤ 0 or If elements in choice bag = 0.

⇒ Procedure Flow :-
For all combination of states

of items. \times Integral wts

Maximize Value of choices! Reward Over choices.

⇒ Choices + Reward fn follows a dynamic behaviour

Reward at a particular state - Wt = w_i and element checked = $\#j$
↳ depends on the previous states.

$k = \begin{bmatrix} 0 & \text{for } x \text{ in range}(wt+1) \end{bmatrix}$
 $\text{for } x \text{ in range}(n+1)$

$k = \text{np.zeros}(\text{shape} = (n+1, wt+1))$

↳ used for caching.

$\text{for } i \text{ in range}(n+1)$
 $\text{for } j \text{ in range}(wt+1)$

start $i=0$

$j=0 \rightarrow 1, 2, \dots$

$i=0, j=0 \rightarrow$ stop criterion pivot
↳ $i=0$ or $j=0$.

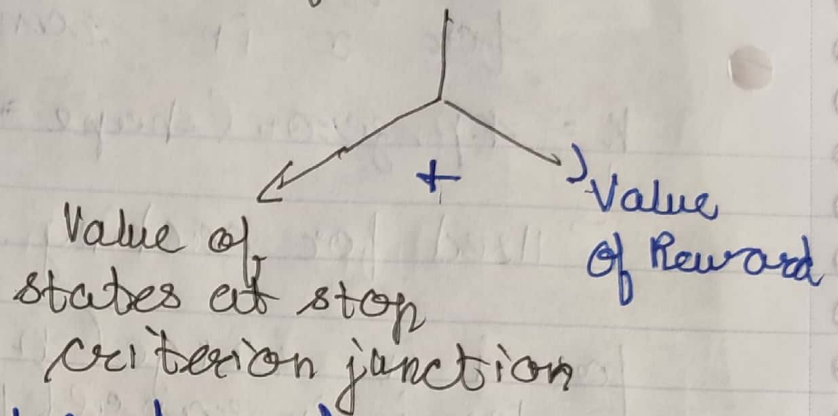
proc. \rightarrow Choice based procedure

proc(0,0) \rightarrow store in $k(0,0)$
proc(0,1)

\therefore proc(1,1) \rightarrow will use previous values of proc

Believing that \swarrow distribution
if the state never changes
why the value at i^{th} j^{th} wt
will always remain the same.

∴ Determination of STOP criterion



IS important.

→ Then we can build a top-down or Bottom-up approach for all combination of state variables.

→ Cache them and use it for future analysis.