

→ Maximize PROFIT
↳ Revenue - Cost.

At $y_1, 2$ — will go till 20.

ACTIONS and associated aspects.
↳ $x_1 \rightarrow$ Barrel extracted + processed

↳ COST $\rightarrow x_1^2$

20 Sell x_1 at price p_1 .

30 Exploration \rightarrow will lead to discovery
↳ y_1 Revenue value, Discount factor = d .

* STATE VARS:

1. Barrel of Oil \rightarrow 'oil-qt'
2. Year of exploration $\rightarrow y_1$

$\rightarrow y_1$ will go from 0 to 1 to 10 both inclusive.

\rightarrow Initial oil-qt is 100 barrels.
↳ And should not go below 0.

* STOP CRITERION

No matter how much we extract we cannot perform actions.
 $\therefore \text{Profit (Year 1)} = 0$

→ We cannot perform selling actions if available oil-qt is 0

⇒ But we dont need to phrase this as a STOP CRITERION

⇒ This 0 can be included in the choices too at each state from the combination map.

⇒ ⇒ At all combinations of the state variable, we need to EVALUATE profit (+ change in state variables) generated from all possible choices.
↳ PROFIT is generated by performing sequence of actions.

** Input state = oil-qt, T

↳ choice → Extract x + quantity from the oil-qt
↳ $x_t \leq 20$
↳ $x_t \leq \text{oil-qt}$

* DYNAMICS.

\Rightarrow Cost associated with extraction of
 $x_t \rightarrow x_t^2$

Revenue $\rightarrow x_t \times p_t$

PROFIT $\rightarrow -x_t^2 + x_t \times p_t$

Discounted Profit $\rightarrow \sum_{t=0}^T \delta^t \text{Profit}$
 $\hookrightarrow \frac{1}{d}$

● Oath ut \rightarrow barrel \rightarrow left \rightarrow oil-qt - $x_t + j_t$
 \Rightarrow time $\rightarrow T+1$ Explored.

\Rightarrow From stop criterion we know
 x_t is 0 for $\forall t \geq 11$.

\rightarrow For $\forall t \leq 10$ let oil-qt = oil-qt.
 Then x_t will be in range 0 to oil-qt
 of $\{$ both inclusive $\}$ CHOICES

for all possible values of x_t
 \hookrightarrow At any x_t .
 Profit = $-x_t^2 + x_t \times p_t + \delta \times \text{Profit}$

$$\text{Profit}_t = -x_t^2 + x_t p_t + \frac{1}{d} (p_{t+1} - p_t) + \text{Profit}_{t+1}$$

↳ We will have series of x_t

↳ We need to compute max (statistic) of this series, as well as state-value (x_t) that is generating this max value

↳ And cache them for future (back-time) calculation.

Dynamic (Pseudo Bellman) Equation

$$\text{Profit}(0_t, t) = \max_{x_t} \left[x_t p_t - x_t^2 + \frac{1}{d} [p_{t+1} - p_t] + \text{Profit}(0_{t+1}, t+1) \right]$$

→ We know $\text{Profit}(0_t, t=11) = 0$

↳ This can help compute by pivoting $\text{Profit}(0_t, t=10)$.

Iterate till $x_t = 1$ ↩