Assignment #4

Name:	ID:
	This assignment has ${\bf 6}$ questions, for a total of ${\bf 25}$ marks.
Question 1: Polymorphic behaviour 5 marks	
Given a closed term	at t of type $\forall \alpha. \alpha \to \alpha \to \alpha \to \alpha$, and three closed values v_1, v_2, v_3 of type τ , define
and prove that t on	ly reduces to any of its supplied inputs.

- $\Gamma \vDash t_1 : \tau_1$
- $\Gamma \vDash t_2 : \tau_2$

Prove:

• $\Gamma \vDash \langle t_1, t_2 \rangle : \tau_1 \times \tau_2$

• $\Gamma \vDash t_1 : \tau_1 \times \tau_2$

Prove:

• $\Gamma \vDash t_1.1 : \tau_1$

• $\Gamma \vDash t_1 : \tau_1$

Prove:

• $\Gamma \vDash inl \ t_1 : \tau_1 \uplus \tau_2$

- $\Gamma \vDash t_0 : \tau_1 \uplus \tau_2$
- $\Gamma, x_1 : \tau_1 \vDash t_1 : \tau$
- $\Gamma, x_2 : \tau_2 \vDash t_2 : \tau$

Prove:

• $\Gamma \vDash case \ t_0 \ of \ inl \ x_1 \mapsto t_1 \mid inr \ x_2 \mapsto t_2 : \tau$

- $\bullet \ \Delta \vdash \tau'$
- $\Delta, \Gamma \vDash t : \exists \alpha. \tau$
- $\bullet \ \Delta; \alpha, \Gamma; x : \tau \vDash t' : \tau'$

Prove:

 $\bullet \ \Delta, \Gamma \vDash \mathsf{unpack} \ t \ \mathsf{as} \ \langle \alpha, x \rangle \ \mathsf{in} \ t' : \tau'$