# Robust Hyperproperty Preservation for Secure Compilation

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# Special Thanks to:









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Robust Compilation Criteria

**Proof Techniques** 

Where is FAC?

 many criteria imply secure compilation preserving memory safety, CFI, non interference, program equivalence

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Is that all?

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Goal: study criteria that

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#### Goal: study criteria that

- are security-driven and preserve security properties formally
- are robust (hold for all adversarial context)

 many criteria imply secure compilation preserving memory safety, CFI, non interference, program equivalence

Relate backtranslation techniques and property preservation

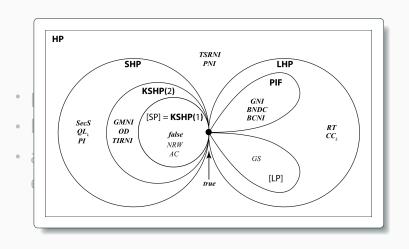
#### Goal

- are security-driven and preserve security properties formally
- are robust (hold for all adversarial context)

• properties = sets of traces

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- hyperproperties = sets of sets of traces

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- hyperproperties = sets of sets of traces
- are organised in subclasses for expressiveness



# Robust Compilation Criteria

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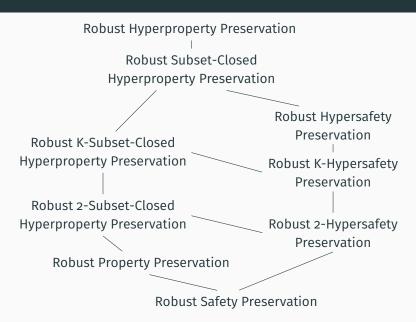
#### In the partial order:

- higher notions are stronger
  - and trickier to achieve
- each notion comes in two flavours
  - one with clear HP correspondence
  - one for simpler proofs

#### **Notation**

- P<sub>s</sub>, P<sub>t</sub>: components of S and T
- $\mathbb{C}_{s}$ ,  $\mathbb{C}_{t}$ : contexts
- $\mathbb{C}_{s}[P_{s}], \mathbb{C}_{t}[P_{t}]$ : whole programs
- $\llbracket \cdot \rrbracket : \mathsf{P}_{\mathsf{s}} \to \mathsf{P}_{\mathsf{t}} : \mathsf{compiler} \; \mathsf{from} \; \mathsf{S} \; \mathsf{to} \; \mathsf{T}$
- β: traces (possibly infinite), I/O with an environment
- Behav  $(P_s)$ : set of traces of  $P_s$
- $\pi$ : prefix (finite)
- < : prefixing</p>

#### **Robust Compilation Criteria**



#### RPP: Robust Property Preservation

#### **Definition (RPP)**

```
\begin{split} \llbracket \cdot \rrbracket \in \mathsf{RPP} &\stackrel{\text{def}}{=} \forall \mathsf{P}_{\mathsf{s}}, \mathsf{P}. \\ & \quad \text{if } \left( \forall \mathbb{C}_{\mathsf{s}}.\mathsf{Behav}\left( \mathbb{C}_{\mathsf{s}}\left[\mathsf{P}_{\mathsf{s}}\right] \right) \subseteq \mathsf{P} \right) \\ & \quad \text{then } \left( \forall \mathbb{C}_{\mathsf{t}}.\mathsf{Behav}\left( \mathbb{C}_{\mathsf{t}}\left[ \llbracket \mathsf{P}_{\mathsf{s}} \rrbracket \right] \right) \subseteq \mathsf{P} \right) \end{split}
```

# **RC: Robust Compilation**

#### **Definition: (RC)**

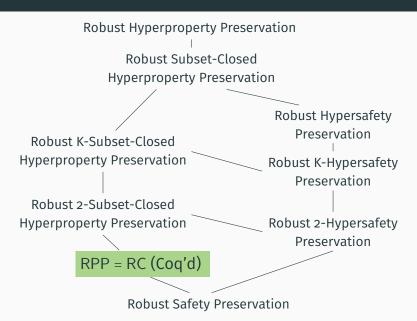
```
[\![\cdot]\!] \in \mathsf{RC} \stackrel{\mathsf{def}}{=} \forall \mathbb{C}_{\mathsf{t}}, \mathsf{P}_{\mathsf{s}}, \beta. \exists \mathbb{C}_{\mathsf{s}}.
\mathsf{if} \ \beta \in \mathsf{Behav} \left(\mathbb{C}_{\mathsf{t}} \left[[\![\mathsf{P}_{\mathsf{s}}]\!]\right]\right)
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# **Robust Compilation Criteria**



#### **Robust Safety Property Preservation**

#### **Definition (RSPP)**

```
\begin{split} \llbracket \cdot \rrbracket \in \mathsf{RSPP} &\stackrel{\scriptscriptstyle\mathsf{def}}{=} \forall \mathsf{P}_\mathsf{s}, \mathsf{P} \in SP \\ & \mathsf{if} \quad (\forall \mathbb{C}_\mathsf{s}.\mathsf{Behav} \left( \mathbb{C}_\mathsf{s} \left[ \mathsf{P}_\mathsf{s} \right] \right) \subseteq \mathsf{P} \right) \\ & \mathsf{then} \quad (\forall \mathbb{C}_\mathsf{t}.\mathsf{Behav} \left( \mathbb{C}_\mathsf{t} \left[ \llbracket \mathsf{P}_\mathsf{s} \rrbracket \right] \right) \subseteq \mathsf{P} \right) \end{split}
```

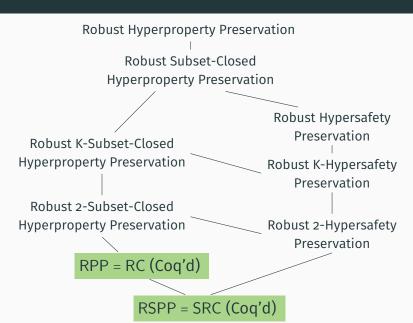
# **Robust Safety Compilation**

#### **Definition: (RC)**

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#### **Definition: (SRC)**

# **Robust Compilation Criteria**



# RSHP: Robust Hypersafery Preservation

#### **Definition (RPP)**

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\begin{split} \llbracket \cdot \rrbracket \in \mathsf{RPP} &\stackrel{\scriptscriptstyle\mathsf{def}}{=} \forall \mathsf{P}_\mathsf{s}, \mathsf{P}. \\ &\quad \mathsf{if} \ \left( \forall \mathbb{C}_\mathsf{s}.\mathsf{Behav} \left( \mathbb{C}_\mathsf{s} \left[ \mathsf{P}_\mathsf{s} \right] \right) \subseteq \mathsf{P} \right) \\ &\quad \mathsf{then} \ \left( \forall \mathbb{C}_\mathsf{t}.\mathsf{Behav} \left( \mathbb{C}_\mathsf{t} \left[ \llbracket \mathsf{P}_\mathsf{s} \rrbracket \right] \right) \subseteq \mathsf{P} \right) \end{split}
```

#### RSHP: Robust Hypersafery Preservation

#### **Definition (RSHP)**

```
\begin{split} \llbracket \cdot \rrbracket \in \mathsf{RSHP} &\stackrel{\mathsf{def}}{=} \forall \mathsf{P}_\mathsf{s}, \ \mathsf{H} \in \mathit{SHP} \ . \\ & \quad \mathsf{if} \ \left( \forall \mathbb{C}_\mathsf{s}. \mathsf{Behav} \left( \mathbb{C}_\mathsf{s} \left[ \mathsf{P}_\mathsf{s} \right] \right) \in \mathsf{H} \right) \\ & \quad \mathsf{then} \ \left( \forall \mathbb{C}_\mathsf{t}. \mathsf{Behav} \left( \mathbb{C}_\mathsf{t} \left[ \llbracket \mathsf{P}_\mathsf{s} \rrbracket \right] \right) \in \mathsf{H} \right) \end{split}
```

# SHRC: Hypersafety Robust Compilation

#### **Definition: (RC)**

```
 \begin{split} \llbracket \cdot \rrbracket \in \mathsf{RC} &\stackrel{\scriptscriptstyle\mathsf{def}}{=} \forall \mathsf{P}_\mathsf{s}, \mathbb{C}_\mathsf{t}, \pi. \exists \mathbb{C}_\mathsf{s}. \\ & \mathsf{if} \ \pi \mathsf{<} \mathsf{Behav} \left( \mathbb{C}_\mathsf{t} \left[ \llbracket \mathsf{P}_\mathsf{s} \rrbracket \right] \right) \\ & \mathsf{then} \ \pi \mathsf{<} \mathsf{Behav} \left( \mathbb{C}_\mathsf{s} \left[ \mathsf{P}_\mathsf{s} \right] \right) \end{split}
```

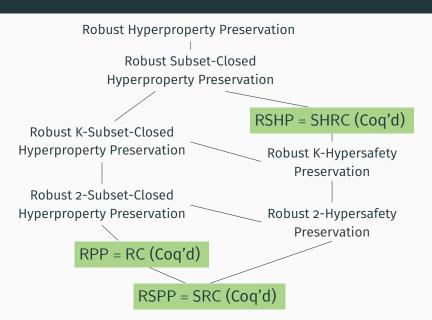
#### SHRC: Hypersafety Robust Compilation

#### **Definition: (SHRC)**

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\begin{split} \llbracket \cdot \rrbracket \in & \mathsf{SHRC} \stackrel{\mathsf{def}}{=} \forall \mathsf{P}_{\mathsf{s}}, \mathbb{C}_{\mathsf{t}}, \frac{\hat{\pi}}{\hat{\pi}}. \exists \mathbb{C}_{\mathsf{s}}. \\ & \mathsf{if} \ \hat{\pi} \underset{\mathsf{<}}{\lessdot} \mathsf{Behav} \left( \mathbb{C}_{\mathsf{t}} \left[ \llbracket \mathsf{P}_{\mathsf{s}} \rrbracket \right] \right) \\ & \mathsf{then} \ \hat{\pi} \underset{\mathsf{<}}{\lessdot} \mathsf{Behav} \left( \mathbb{C}_{\mathsf{s}} \left[ \mathsf{P}_{\mathsf{s}} \right] \right) \end{split}
```

 $\hat{\pi}$ : finite set of prefixes

#### **Robust Compilation Criteria**



# **Robust Hyperproperty Preservation**

#### **Definition (RHP)**

```
\begin{split} \llbracket \cdot \rrbracket \in \mathsf{RHP} &\stackrel{\text{\tiny def}}{=} \forall \mathsf{P}_\mathsf{s}, \mathsf{H}. \\ & \text{if } (\forall \mathbb{C}_\mathsf{s}.\mathsf{Behav} (\mathbb{C}_\mathsf{s} \left[\mathsf{P}_\mathsf{s}\right]) \in \mathsf{H}) \\ & \text{then } (\forall \mathbb{C}_\mathsf{t}.\mathsf{Behav} (\mathbb{C}_\mathsf{t} \left[\llbracket \mathsf{P}_\mathsf{s} \rrbracket \right]) \in \mathsf{H}) \end{split}
```

# **Hyperproperty Robust Compilation**

#### **Definition: (RC)**

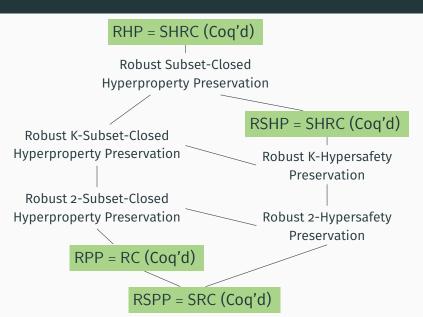
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[\![\cdot]\!] \in \mathsf{RC} \stackrel{\mathsf{def}}{=} \forall \mathbb{C}_{\mathsf{t}}, \mathsf{P}_{\mathsf{s}}, \beta. \exists \mathbb{C}_{\mathsf{s}}.
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# **Hyperproperty Robust Compilation**

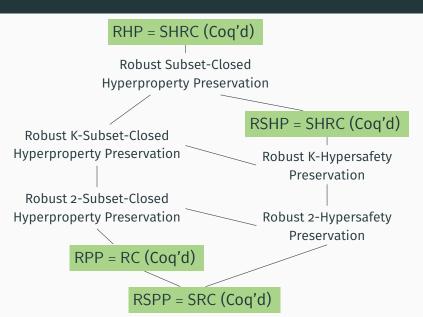
#### **Definition: (HRC)**

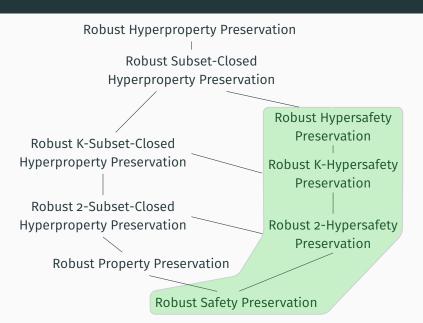
$$\label{eq:bounds} \begin{split} \llbracket \cdot \rrbracket \in \mathsf{HRC} &\stackrel{\scriptscriptstyle\mathsf{def}}{=} \forall \mathbb{C}_{\mathbf{t}}, \mathsf{P}_{\mathsf{s}}, \; \exists \mathbb{C}_{\mathsf{s}}. \; \forall \beta. \\ & \beta \in \mathsf{Behav}\left(\mathbb{C}_{\mathbf{t}}\left[\llbracket \mathsf{P}_{\mathsf{s}} \rrbracket\right]\right) \\ & \iff \beta \in \mathsf{Behav}\left(\mathbb{C}_{\mathsf{s}}\left[\mathsf{P}_{\mathsf{s}}\right]\right) \end{split}$$

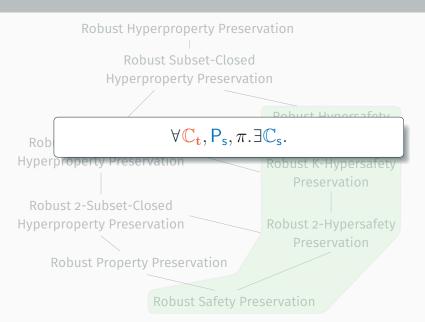
### **Robust Compilation Criteria**

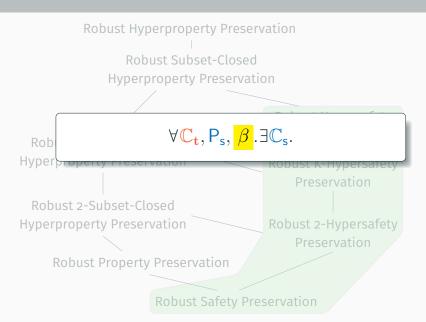


### **Robust Compilation Criteria**

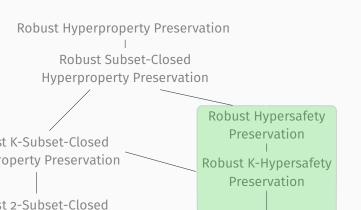




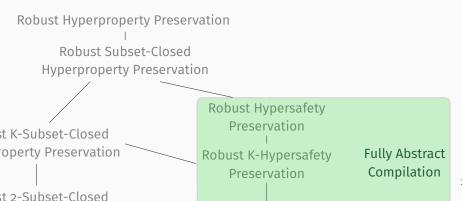


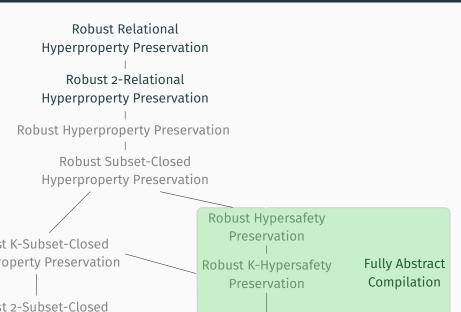


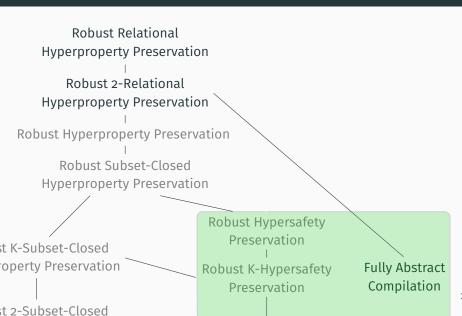
# Where is FAC?



Fully Abstract Compilation







#### Conclusion

- motivated the Robust Compilation Partial Order
- · discussed some of these criteria
- analysed proof techniques for some criteria

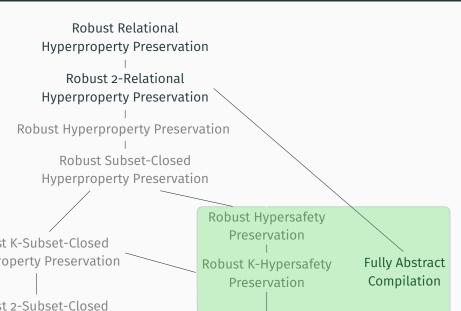
#### Conclusion

- motivated the Robust Compilation Partial Order
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# Conclusion



# **Robust Compilation Criteria**



# Robust Relational Hyperproperty Preservation

#### Definition: (HRC)

# Robust Relational Hyperproperty Preservation

#### **Definition: (RRHP)**

$$\begin{split} \llbracket \cdot \rrbracket \in & \mathsf{RRHP} \stackrel{\mathsf{def}}{=} \forall \mathbb{C}_{\mathbf{t}}, \; \exists \mathbb{C}_{\mathtt{s}}. \; \forall \mathsf{P}_{\mathtt{s}}, \beta \\ & \beta \in \mathsf{Behav} \left( \mathbb{C}_{\mathbf{t}} \left[ \llbracket \mathsf{P}_{\mathtt{s}} \rrbracket \right] \right) \\ & \iff \beta \in \mathsf{Behav} \left( \mathbb{C}_{\mathtt{s}} \left[ \mathsf{P}_{\mathtt{s}} \right] \right) \end{split}$$

# Robust 2-Relational Hyperproperty Preservation

#### **Definition: (RRHP)**

# Robust 2-Relational Hyperproperty Preservation

#### **Definition: (R2RHP)**

$$\begin{split} \llbracket \cdot \rrbracket \in \mathsf{R2RHP} &\stackrel{\text{\tiny def}}{=} \forall \mathbb{C}_t, \exists \mathbb{C}_s. \forall \begin{array}{c} \mathsf{P}_s, \mathsf{P}_s'. \beta \\ \\ & \beta \in \mathsf{Behav} \left( \mathbb{C}_t \left[ \llbracket \mathsf{P}_s \rrbracket \right] \right) \\ \\ \iff \beta \in \mathsf{Behav} \left( \mathbb{C}_s \left[ \mathsf{P}_s \right] \right) \\ \\ \mathsf{and} & \begin{pmatrix} \beta \in \mathsf{Behav} \left( \mathbb{C}_t \left[ \llbracket \mathsf{P}_s' \rrbracket \right] \right) \\ \\ \iff \beta \in \mathsf{Behav} \left( \mathbb{C}_s \left[ \mathsf{P}_s' \right] \right) \\ \end{pmatrix} \end{split}$$