

# PhysH308

Energy

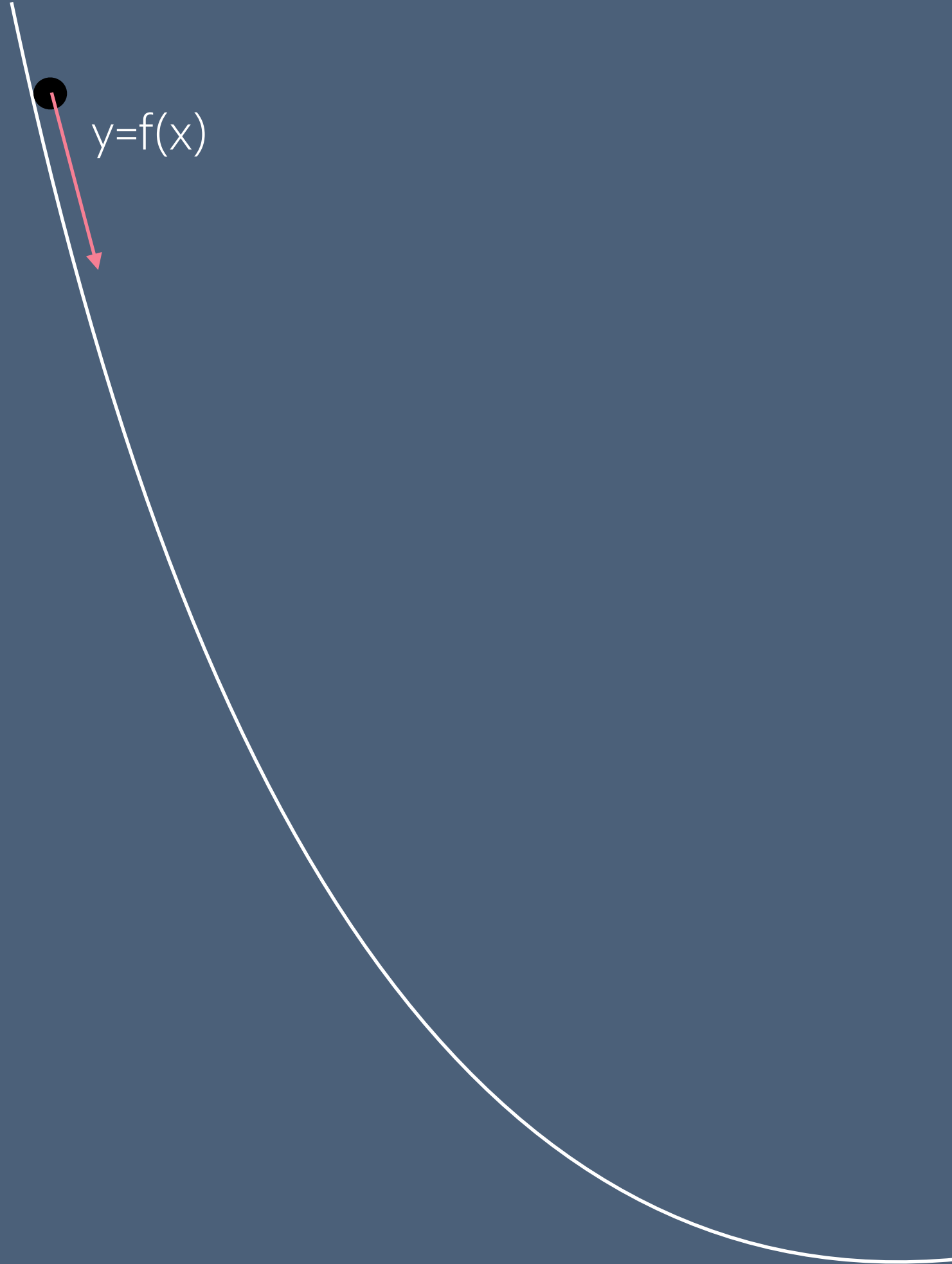
Ted Brzinski, Sept 24, 2024

# Curvilinear coordinates

Identify constraints  $\rightarrow$  reduce the dimensionality  $\rightarrow$  describe the motion *along the path*

- $U = mgy = mgf(x)$

- $T = \frac{1}{2}m (\dot{x}^2 + \dot{y}^2)$

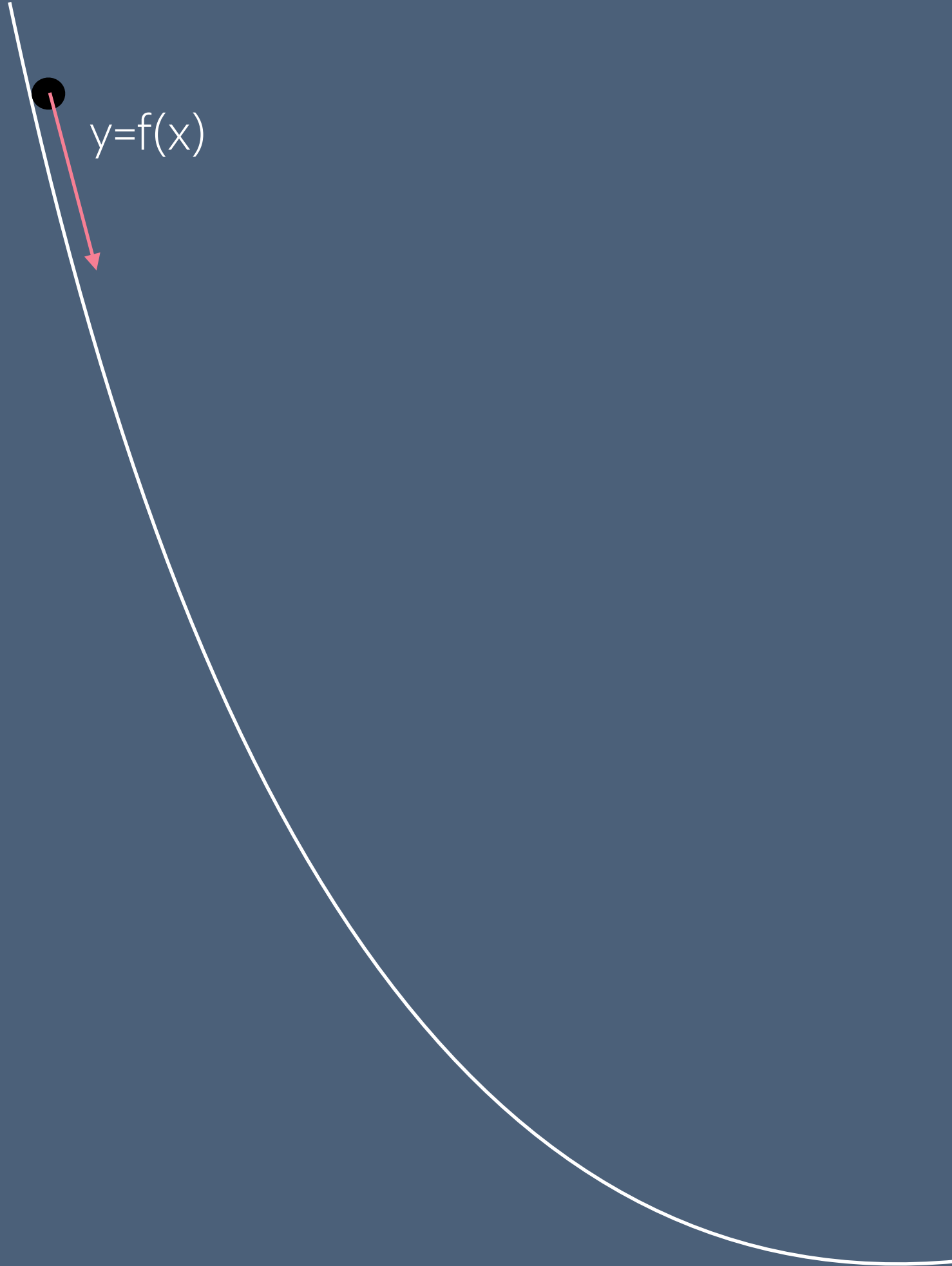


# Curvilinear coordinates

Identify constraints  $\rightarrow$  reduce the dimensionality  $\rightarrow$  describe the motion *along the path*

- $U = mgy = mgf(x)$

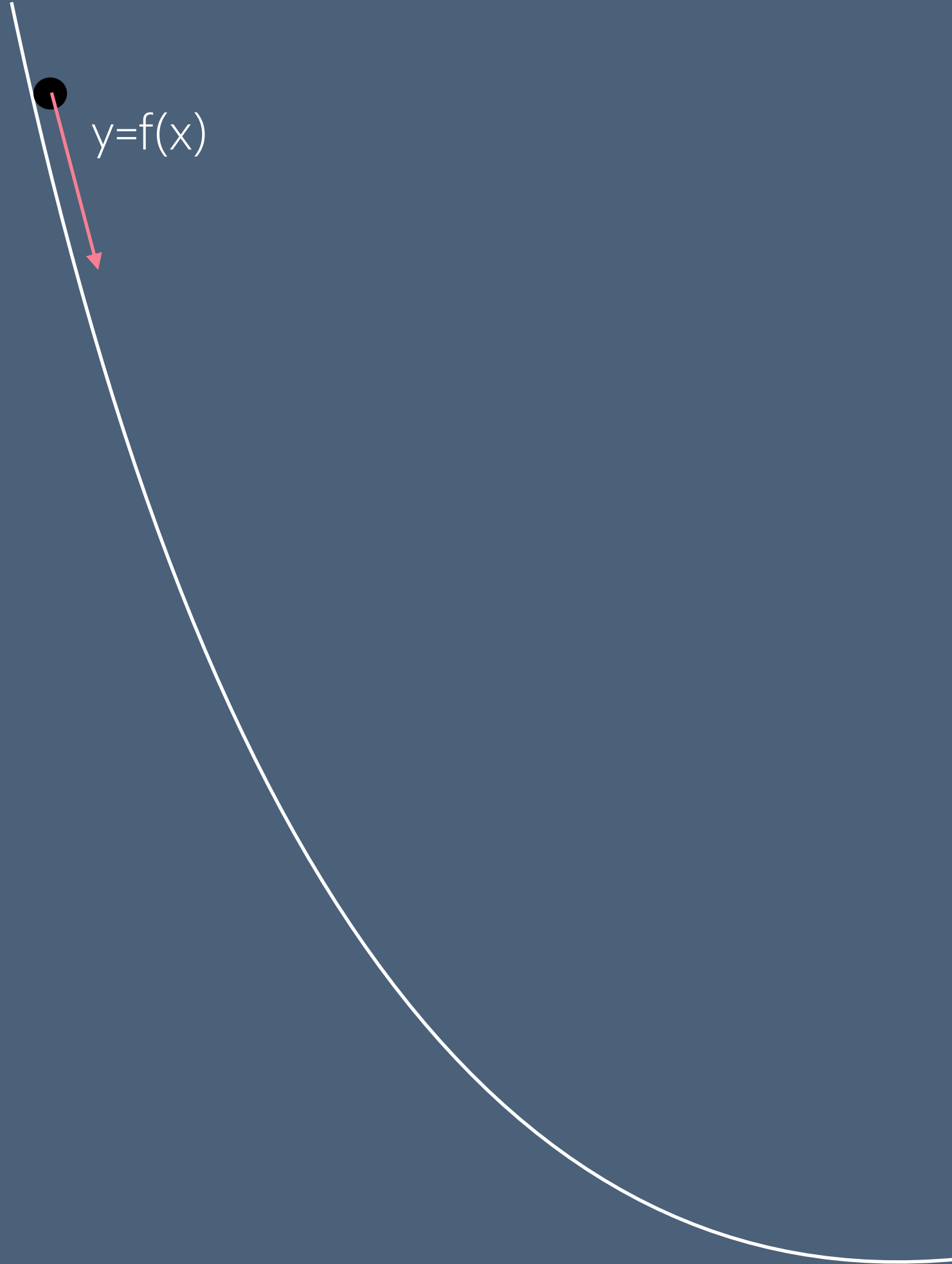
- $T = \frac{1}{2}m \left( \dot{x}^2 + \left( \frac{dy}{dx} \right)^2 \dot{x}^2 \right)$



# Curvilinear coordinates

Identify constraints  $\rightarrow$  reduce the dimensionality  $\rightarrow$  describe the motion *along the path*

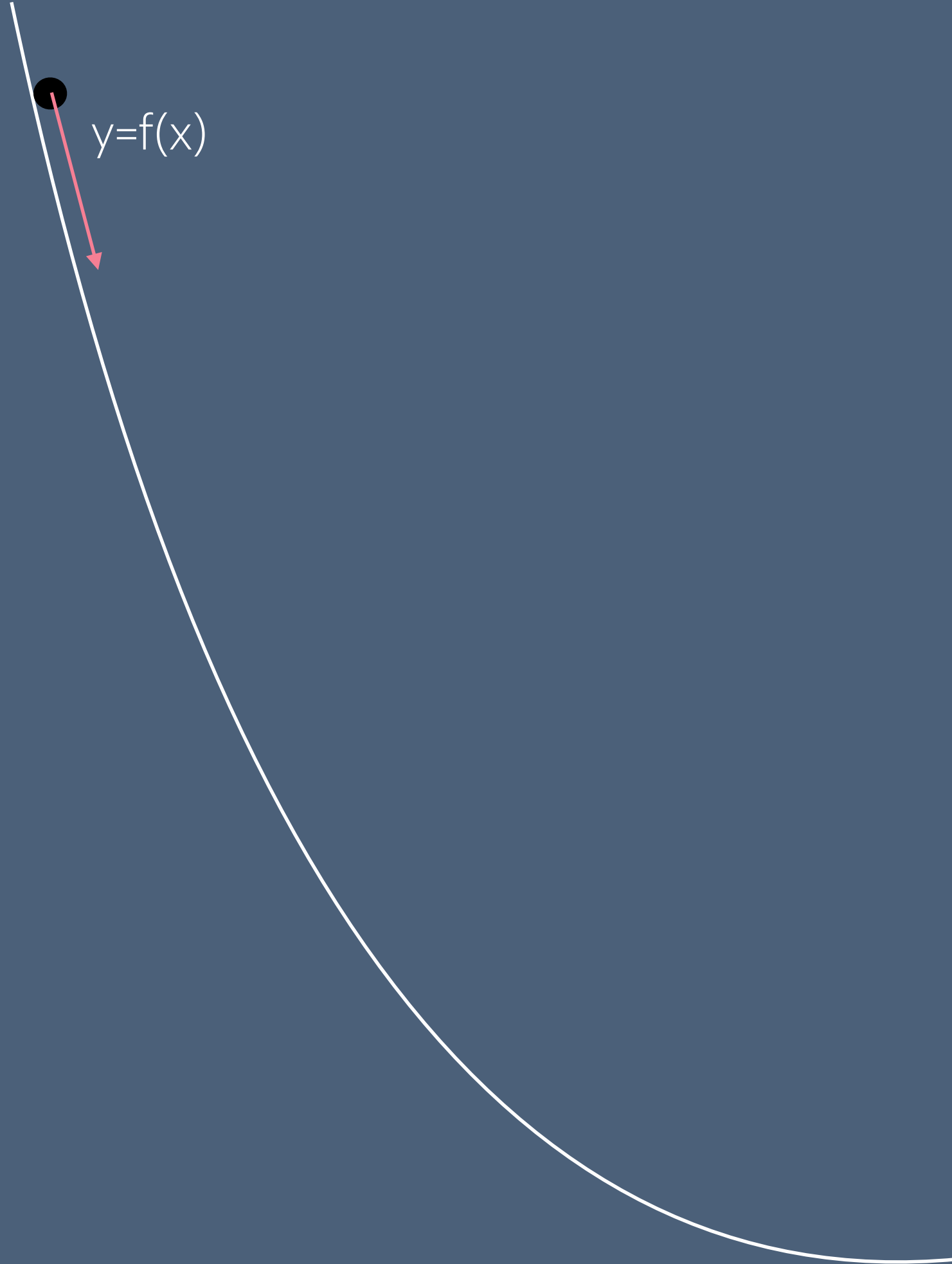
- $U = mgy = mgf(x)$
- $T = \frac{1}{2}m (\dot{x}^2 + f'^2(x)\dot{x}^2)$



# Curvilinear coordinates

Identify constraints  $\rightarrow$  reduce the dimensionality  $\rightarrow$  describe the motion *along the path*

- $U = mgy = mgf(x)$
- $T = \frac{1}{2}m\dot{x}^2 (1 + f'^2(x))$



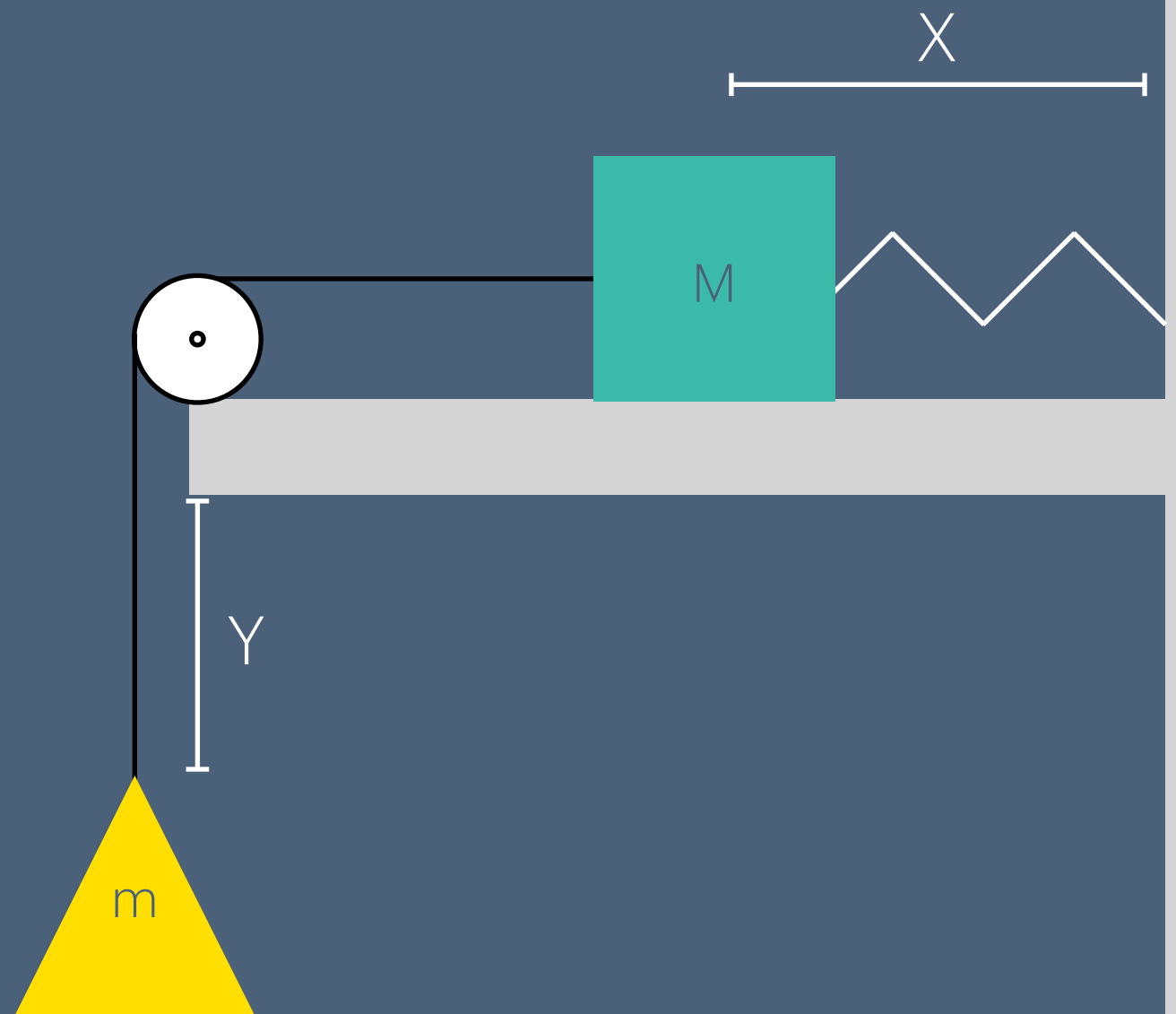
# Curvilinear coordinates

- $U_M = \frac{1}{2}kx^2$

- $U_m = -mgy$

- $T_M = \frac{1}{2}m\dot{x}^2$

- $T_m = \frac{1}{2}m\dot{y}^2$



# Curvilinear coordinates

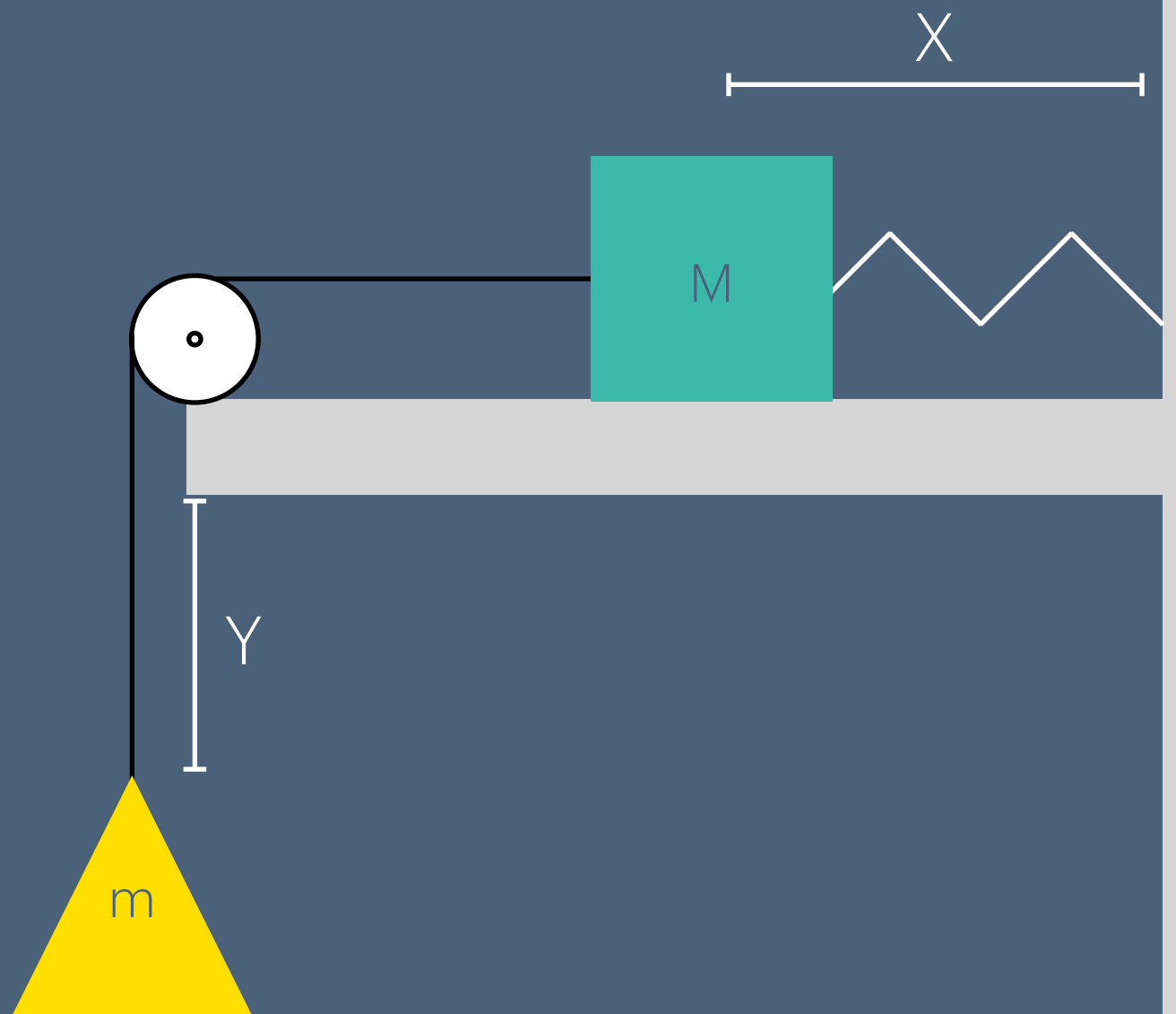
- $U_M = \frac{1}{2}kx^2$

- $U_m = -mgy$

- $T_M = \frac{1}{2}m\dot{x}^2$

- $T_m = \frac{1}{2}m\dot{y}^2$

- $y = x$



# Curvilinear coordinates

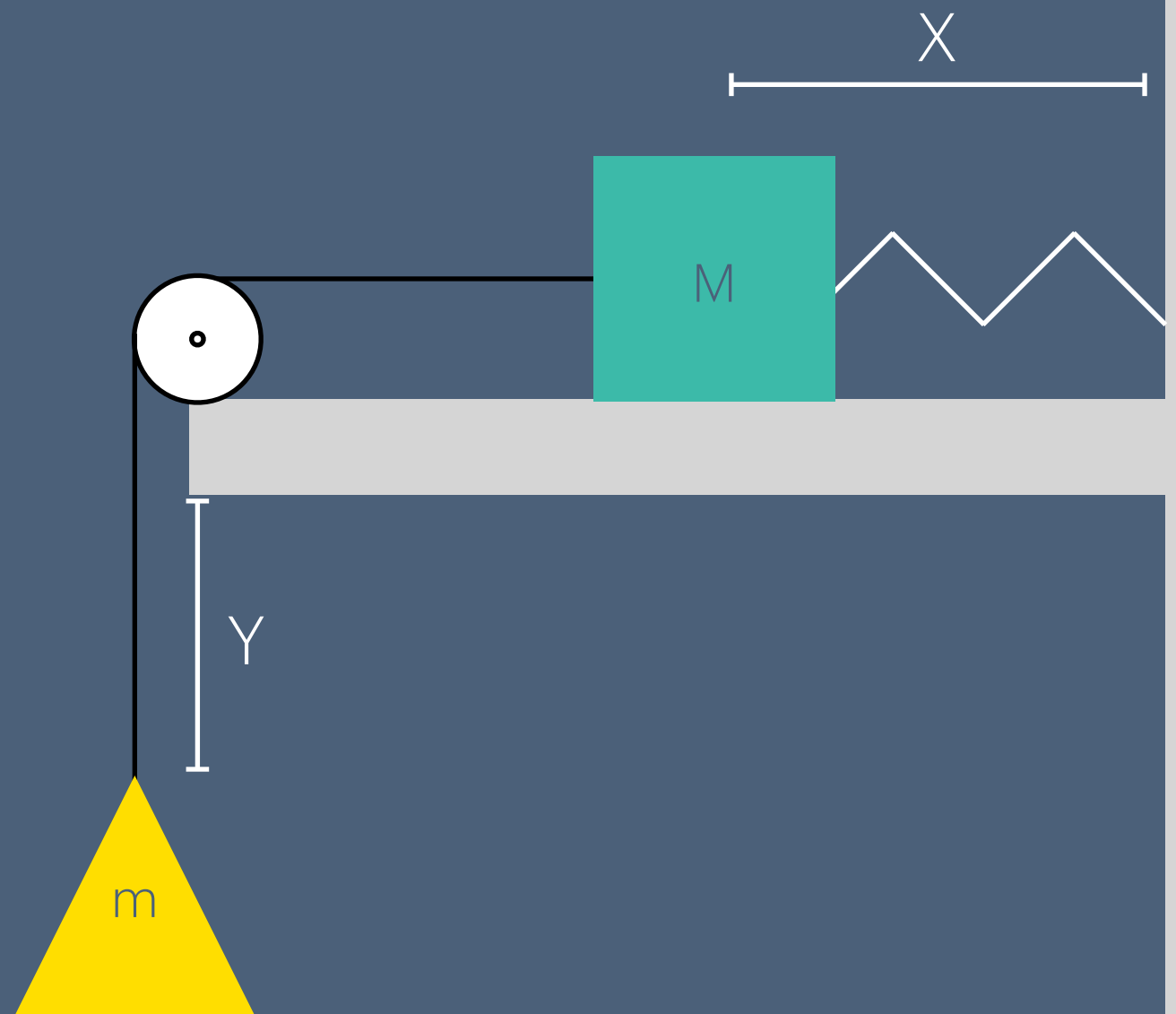
- $U_M = \frac{1}{2}kx^2$

- $U_m = -mgx$

- $T_M = \frac{1}{2}m\dot{x}^2$

- $T_m = \frac{1}{2}m\dot{x}^2$

- $y = x$

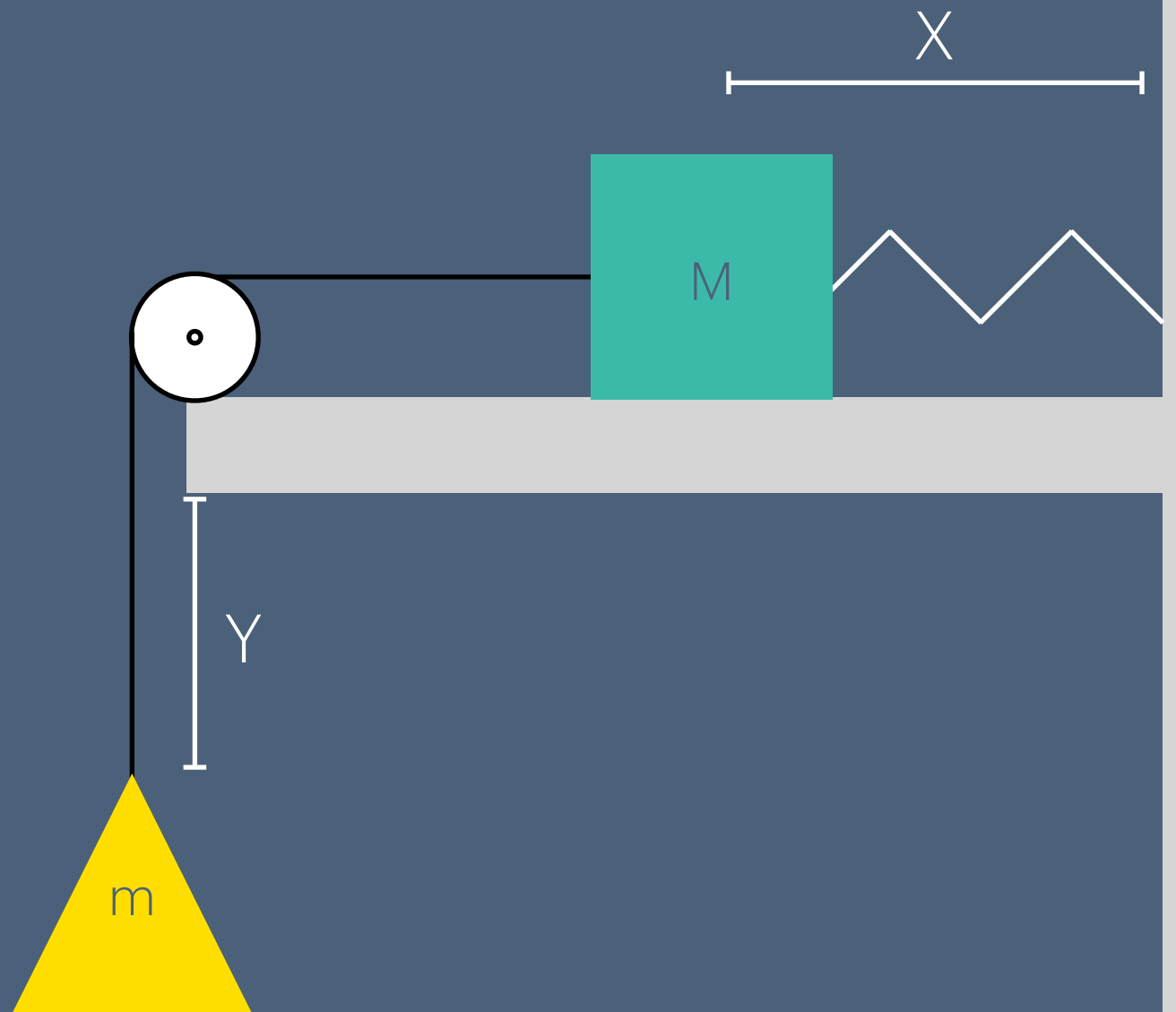




# Curvilinear coordinates

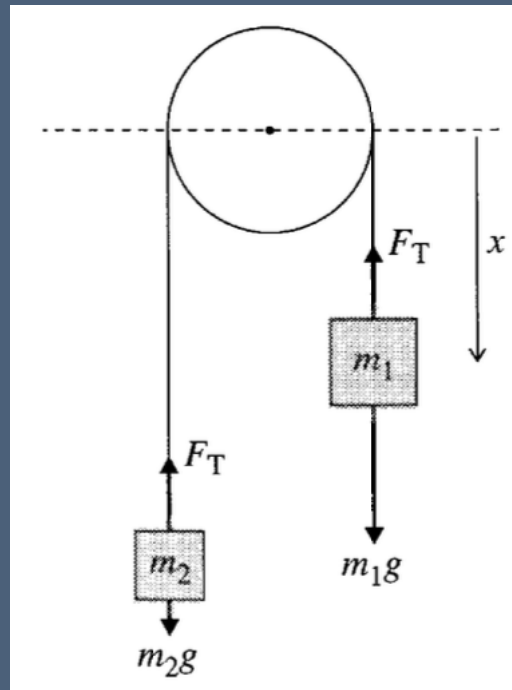
- $U = \frac{1}{2}kx^2 - mgx$

- $T_M = m\dot{x}^2$



# Today's problems

- 4.31



- 4.32

