Polyalphabetic Ciphers

- A polyalphabetic cipher is any cipher based on substitution, using multiple substitution alphabets.
- polyalphabetic cipher techniques have the following features in common:
  - A set of related monoalphabetic substitution rules is used.
  - A key determines which particular rule is chosen for a given transformation.

Polyalphabetic Ciphers Encryption

- Assume

a	b	c	d	e	f	g	h	i	j	k	l	m
0	1	2	3	4	5	6	7	8	9	10	11	12

n	o	p	q	r	s	t	u	v	w	x	y	z
13	14	15	16	17	18	19	20	21	22	23	24	25

- Then We set these Rules:

Polyalphabetic Ciphers Encryption

- Then We set Key as Rules:

1) Shift the first letter three position to the right
2) Shift the second letter five position to the right
3) Shift the third letter seven position to the right

- Given Plaintext = security

Polyalphabetic Ciphers Encryption

- Given Plaintext = security

1) Divide Plaintext to three words

a	b	c	d	e	f	g	h	i	j	k	l	m
0	1	2	3	4	5	6	7	8	9	10	11	12

n	o	p	q	r	s	t	u	v	w	x	y	z
13	14	15	16	17	18	19	20	21	22	23	24	25

2) P= sec uri ty

3) C= VJJ XWP WD

Polyalphabetic Ciphers Decryption

- Then We set Key as Rules: (reverse)

1) Shift the first letter three position to the left
2) Shift the second letter five position to the left
3) Shift the third letter seven position to the left

- Given Ciphertext = VJJXWPWD

Polyalphabetic Ciphers Decryption

- Given C= VJJXWPWD

1) Divide Plaintext to three words as your rules number

a	b	c	d	e	f	g	h	i	j	k	l	m
0	1	2	3	4	5	6	7	8	9	10	11	12

n	o	p	q	r	s	t	u	v	w	x	y	z
13	14	15	16	17	18	19	20	21	22	23	24	25

2) C= VJJ XWP WD

3) C= SEC URI TY

Vigenère Cipher

- The Vigenère cipher, was invented by a Frenchman, Blaise de Vigenère in the 16th century.

- Vigenère cipher is a simple polyalphabetic cipher

Vigenère Cipher

- $C_i = (P_i + K) mod\ 26$
- $P_i = (C_i - K) mod\ 26$

- **Repeating key**

Vigenère Cipher Encryption

- K=deceptive
- P=we are discovered save yourself

```
key:          deceptivedeceptivedeceptive
plaintext:    wearediscoveredsaveyourself
```

a	b	c	d	e	f	g	h	i	j	k	l	m
0	1	2	3	4	5	6	7	8	9	10	11	12

n	o	p	q	r	s	t	u	v	w	x	y	z
13	14	15	16	17	18	19	20	21	22	23	24	25

Vigenère Cipher Encryption

```
key:          deceptivedeceptivedeceptive
plaintext:    wearediscoveredsaveyourself
```

key	3	4	2	4	15	19	8	21	4	3	4	2	4	15
plaintext	22	4	0	17	4	3	8	18	2	14	21	4	17	4
ciphertext	25	8	2	21	19	22	16	13	6	17	25	6	21	19

key	19	8	21	4	3	4	2	4	15	19	8	21	4
plaintext	3	18	0	21	4	24	14	20	17	18	4	11	5
ciphertext	22	0	21	25	7	2	16	24	6	11	12	6	9

Vigenère Cipher Encryption

- Result

```
key:          deceptivedeceptivedeceptive
plaintext:    wearediscoveredsaveyourself
ciphertext:   ZICVTWQNGRZGVTWAVZHCQYGLMGJ
```

Vigenère Cipher Encryption

- The strength of Vigenère Cipher is that there are multiple ciphertext letters for each plaintext letter

Vigenère Cipher Decryption

- decryption simply works in reverse
- $P_i = (C_i - K) mod\ 26$

```
ciphertext:     ZICVTWQNGRZGVTWAVZHCQYGLMGJ
key:            deceptivedeceptivedeceptive
plaintext:      wearediscoveredsaveyourself
```

Autokey Cipher

- An autokey cipher (also known as the autoclave cipher) is a cipher which incorporates the message (the plaintext) into the key.
- $P = \{p_1, p_2, p_3, \dots, p_n\}$
- $K = \{k_1, p_1, p_2, p_3, \dots, p_{n-1}\}$
- $C = \{c_1, c_2, c_3, \dots, c_n\}$

Autokey Cipher

- $C_i = (P_i + K_i) mod\ 26$
- $P_i = (C_i - K_i) mod\ 26$

a	b	c	d	e	f	g	h	i	j	k	l	m
0	1	2	3	4	5	6	7	8	9	10	11	12

n	o	p	q	r	s	t	u	v	w	x	y	z
13	14	15	16	17	18	19	20	21	22	23	24	25

Autokey Cipher Encryption

- K=m
- P=attack is today

Plaintext	a	t	t	a	c	k	i	s	t	o	d	a	y
P Value	0	19	19	0	2	10	8	18	19	14	3	0	24
Key	12	0	19	19	0	2	10	8	18	19	14	3	0
C Value	12	19	12	19	2	12	18	0	11	7	17	3	24
Ciphertext	m	t	m	t	c	m	s	a	l	h	r	d	y

Autokey Cipher Decryption

- K=m
- C=mtmtcmsalhrdy

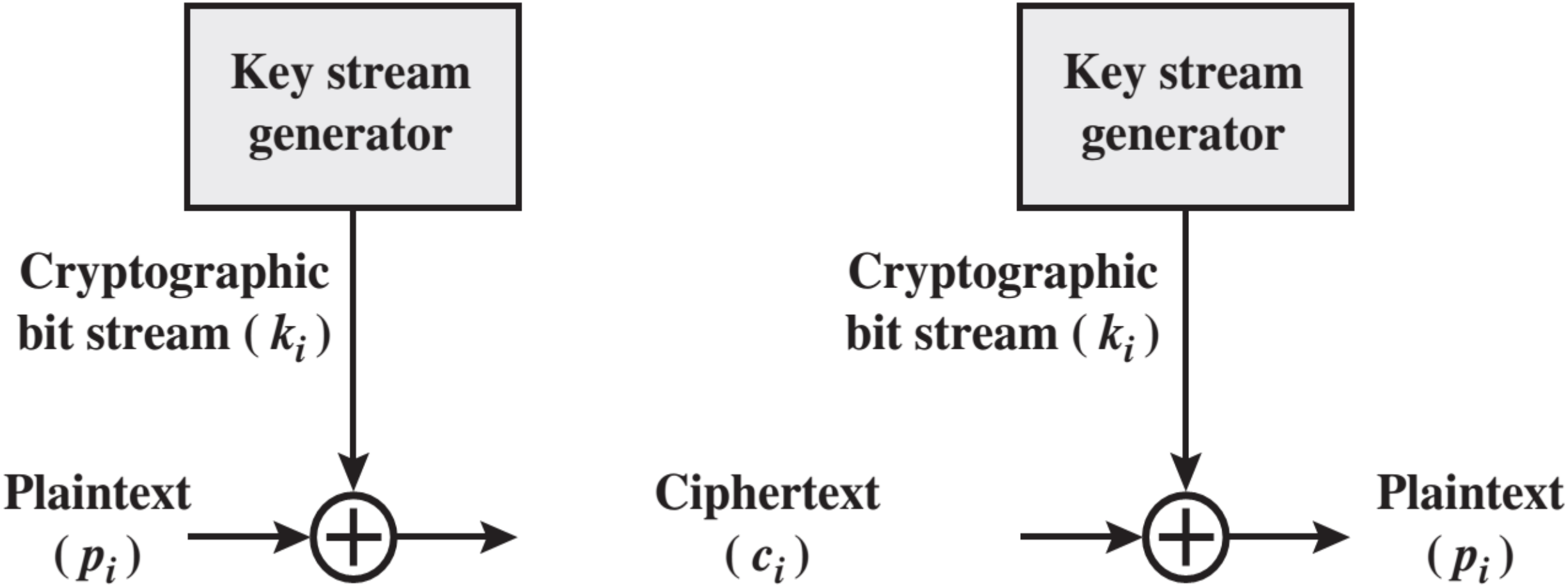
Ciphertext	m	t	m	t	c	m	s	a	l	h	r	d	y
C Value	12	19	12	19	2	12	18	0	11	7	17	3	24
Key	12	0	19	19	0	2	10	8	18	19	14	3	0
P Value	0	19	19	0	2	10	8	18	19	14	3	0	24
Plaintext	a	t	t	a	c	k	i	s	t	o	d	a	y

Vernam Cipher

- Vernam Cipher was introduced by an AT&T engineer named Gilbert Vernam in 1918.

- The ultimate defense against such a cryptanalysis is to choose a keyword that is as long as the plaintext and has no statistical relationship to it.

Vernam Cipher



Vernam Cipher

- Encryption
  - $C = P\ XOR\ K$
- Decryption
  - $P = C\ XOR\ K$

Vernam Cipher Encryption

- P=111000111010101101101
- K=1001010101

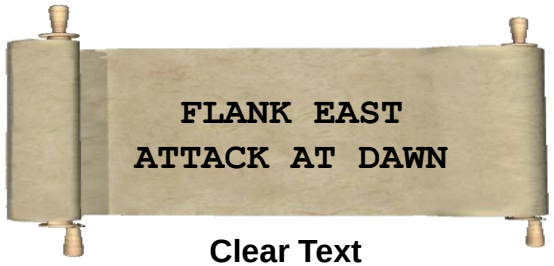
- P=111000111010101101101
- K=1001010101**1001010101**
- C=011101101100111111000

Vernam Cipher Decryption

- C=011101101100111111000
- K=1001010101**1001010101**
- P=1110001110101010101101

Transposition Ciphers

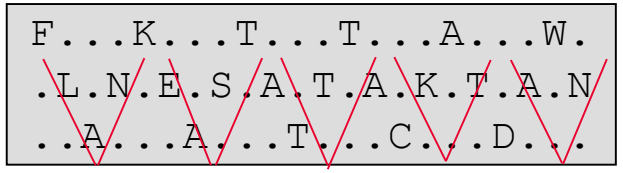
1



Clear Text

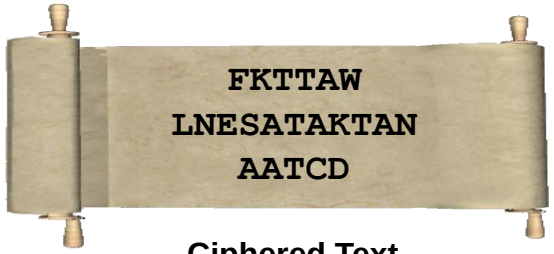
The clear text message would be encoded using a key of 3.

2



Use a rail fence cipher and a key of 3.

3



Ciphered Text

The clear text message would appear as follows.

Transposition Techniques

- Transposition Techniques performing some sort of permutation on the plaintext letters (reorder the position of letters in plaintext).

- Types:
  - Rail Fence Cipher
  - Row Transposition Cipher

Rail Fence Cipher Encryption

- P= meet me after the toga party
- K=2

$$1)\ p = \begin{bmatrix} m & e & m\,a & t & r & h & t & g\,p & r & y \\ e & t & e\,f & e & t & e & o & a\,a & t & \end{bmatrix}$$

2) C=mematrhtgpryetefeteoaat

Rail Fence Cipher Decryption

- C=mematrhtgpryetefeteoaat
- K=2

1) $C = \begin{bmatrix} m & e & m & a & t & r & h & t & g & p & r & y \\ e & t & e & f & e & t & e & o & a & a & t & \end{bmatrix}$ ↓

2) P= meetmeafterthetogaparty

Row Transposition Cipher Encryption

- P= attack postponed until two am
- K= 4312567
- $C = \begin{pmatrix} 4 & 3 & 1 & 2 & 5 & 6 & 7 \\ a & t & t & a & c & k & p \\ o & s & t & p & o & n & e \\ d & u & n & t & i & l & t \\ w & o & a & m & x & x & x \end{pmatrix} = ttnaaptmtsuoaodwcoixknlxpetx$

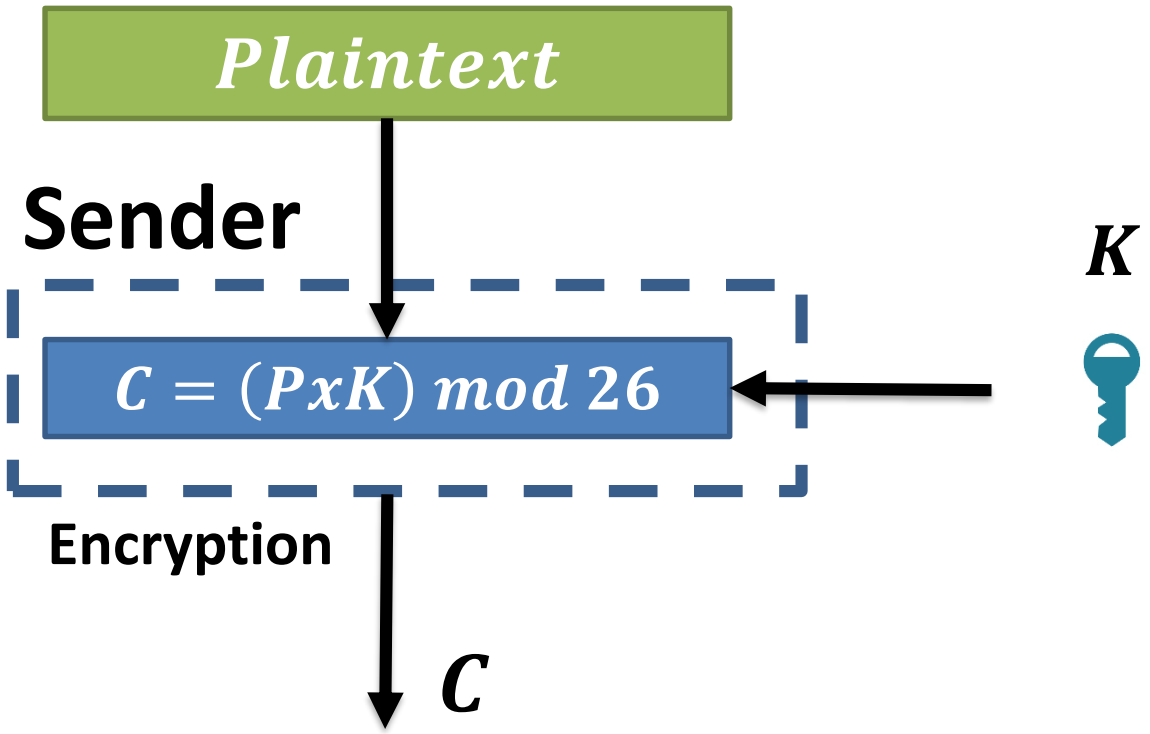
Row Transposition Cipher Decryption

- C= $ttnaaptmtsuoaodwcoixknlxpetx$ = Len(C)=28
- K= 4312567
- Each Column have 28/7= 4 letter

- $P = \begin{pmatrix} 4 & 3 & 1 & 2 & 5 & 6 & 7 \\ a & t & t & a & c & k & p \\ o & s & t & p & o & n & e \\ d & u & n & t & i & l & t \\ w & o & a & m & x & x & x \end{pmatrix} = attackpostponeduntiltwoamxxx$

Task1

- As shown in Figure below, use Multiplicative Cipher to encrypt "enemy attack tonight" with key = 4.



Task2

- As shown in Figure below, use Affine Cipher to encrypt "enemy attack tonight" with key pair (4,3).