

# Message Authentication and Hash Functions



# Message Authentication

- Message authentication is concerned with:
  - Protecting the integrity of a message
  - Validating identity of originator
  - Non-repudiation of origin (dispute resolution)
- Will consider the security requirements
- Three alternative functions used:
  - **Message encryption**
  - **Message Authentication Code (MAC)**
  - **Hash functions**

# Message Authentication Requirements

In communications across a network, the following attacks could be identified:

- **Disclosure:** Release of message contents
- **Traffic analysis:** Discovery of the pattern of traffic between parties
- **Masquerade:** Insertion of messages into the network from a fraudulent source
- **Content modification:** Modification of the contents of a message

# Message Authentication Requirements

- **Sequence modification:** Modification to a sequence of messages between parties
- **Timing modification:** Delay or replay of messages
- **Source repudiation:** Denial of transmission of message by source
- **Destination repudiation:** Denial of receipt of message by destination

# Authentication Function

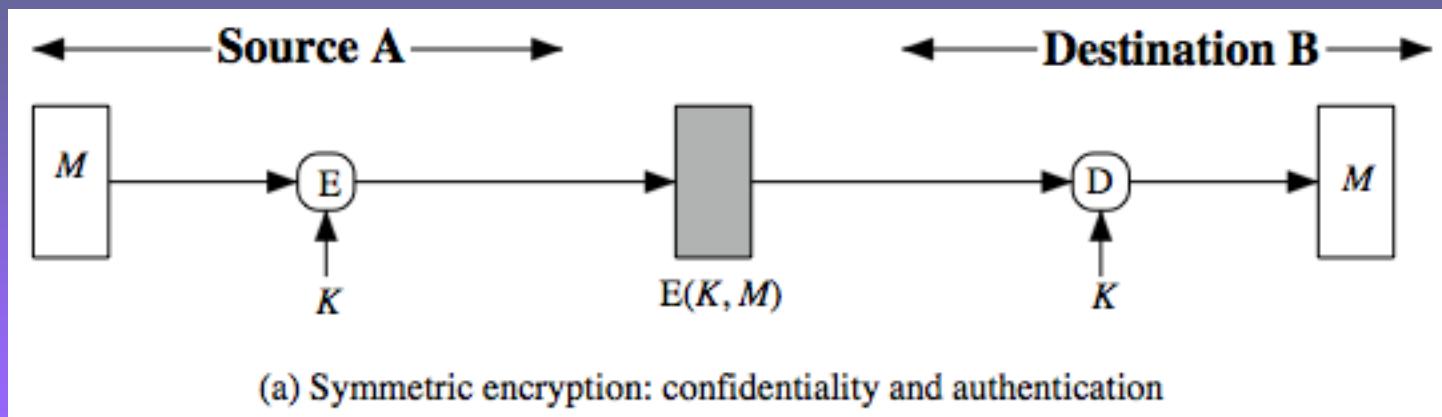
- Message Encryption
- Message Authentication Code (MAC)
- Hash Function

# Message Encryption

- Message encryption by itself also provides a measure of authentication
- The analysis differs for symmetric and public key encryption schemes.

# Symmetric Message Encryption

- Encryption can also provides authentication
- If symmetric encryption is used then:
  - Receiver know sender must have created it
  - Since only sender and receiver use key
  - If message has suitable structure, redundancy or a checksum to detect any changes



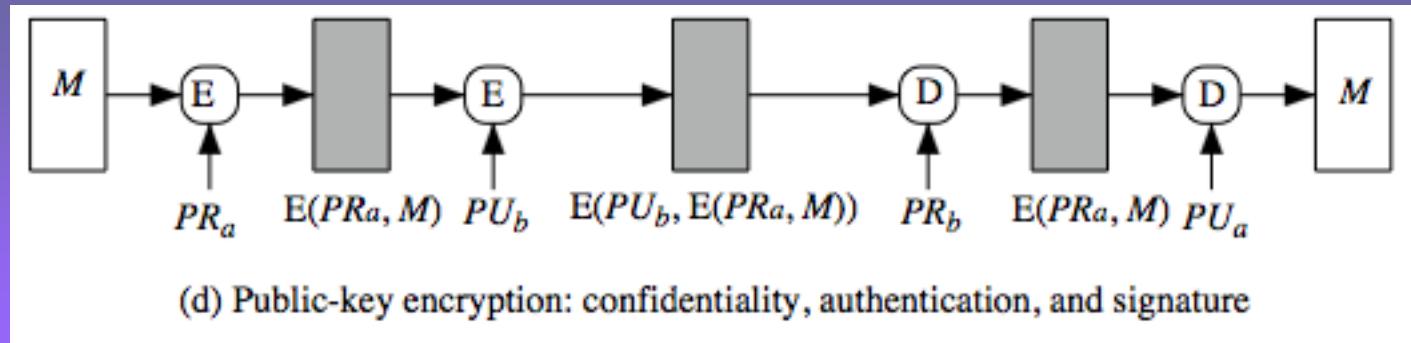
# Public-key Message Encryption

➤ If public-key encryption is used:

- Anyone potentially knows public-key

However if

- Sender signs message using their private-key
- Then encrypts with recipients public key
- Have both secrecy and authentication
- Again need to recognize corrupted messages
- But at cost of two public-key uses on message



# Message Authentication Codes (MAC)

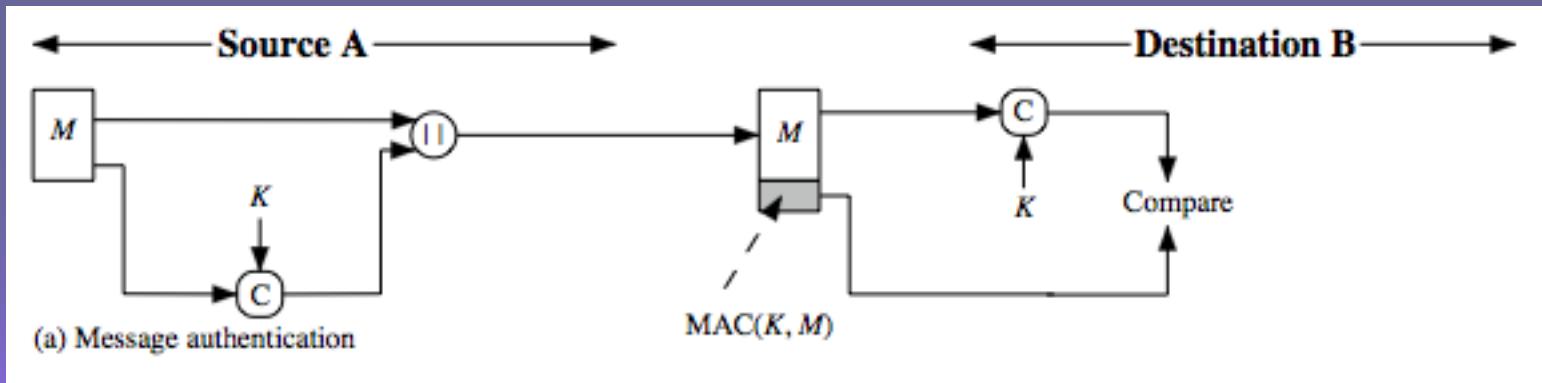
- Why use a MAC?
  - sometimes only authentication is needed
  - sometimes need authentication to persist longer than the encryption (eg. archival use)
- provides authentication
- Can combine use of MAC with encryption for secrecy
  - generally use separate keys for each
  - can compute MAC either before or after encryption
  - is generally regarded as better done before
- MAC is not a digital signature

# Message Authentication Code (MAC)

- Generated by an algorithm that creates a small fixed-sized block
  - depends on both message and some key
  - like encryption though need not be reversible
- Appended to message as a **signature**
- Receiver performs same computation on message and checks it matches the MAC
- Provides assurance that message is unaltered and comes from sender

# Message Authentication Code

- A small fixed-sized block of data
- Generated from message + secret key
- $\text{MAC} = \text{C}(K, M)$
- Appended to message when sent



# MAC Properties

- A MAC is a cryptographic checksum

$$\text{MAC} = C(K, M)$$

- condenses a variable-length message  $M$
- using a secret key  $K$
- to a fixed-sized authenticator

- Is a many-to-one function

- potentially many messages have same MAC
- but finding these needs to be very difficult

# Requirements for MACs

- Taking into account the types of attacks
- Need the MAC to satisfy the following:
  1. knowing a message and MAC, is infeasible to find another message with same MAC
  2. MACs should be uniformly distributed
  3. MAC should depend equally on all bits of the message

# Using Symmetric Ciphers for MACs

- Can use any block cipher chaining mode and use final block as a MAC
- **Data Authentication Algorithm (DAA)** is a widely used MAC based on DES-CBC
  - using  $IV=0$  and zero-pad of final block
  - encrypt message using DES in CBC mode
  - and send just the final block as the MAC
    - or the leftmost  $M$  bits ( $16 \leq M \leq 64$ ) of final block
- But final MAC is now too small for security

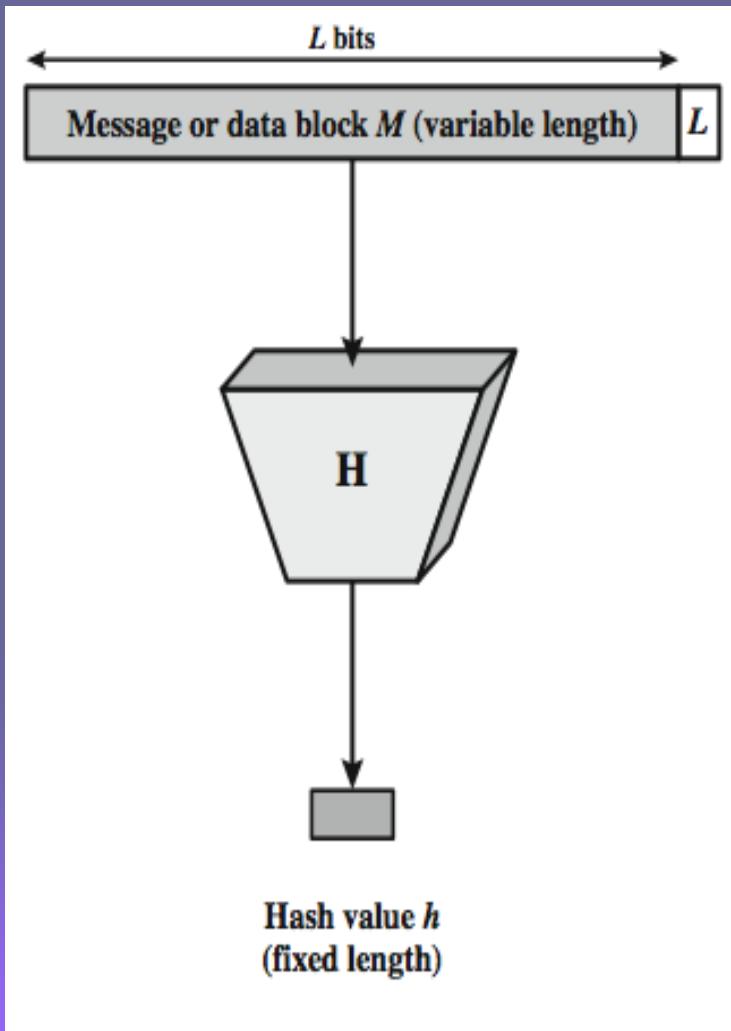
# Hash Functions

- Want a cryptographic hash function
  - Computationally infeasible to find data mapping to specific hash (one-way property)
  - Computationally infeasible to find two data to same hash (collision-free property)

# Hash Functions

- Condenses arbitrary message to fixed size  
$$h = H(M)$$
- Usually assume that the hash function is public and not keyed
  - cf. MAC which is keyed
- Hash used to detect changes to message
- Can use in various ways with message
- Most often to create a digital signature

# Cryptographic Hash Function

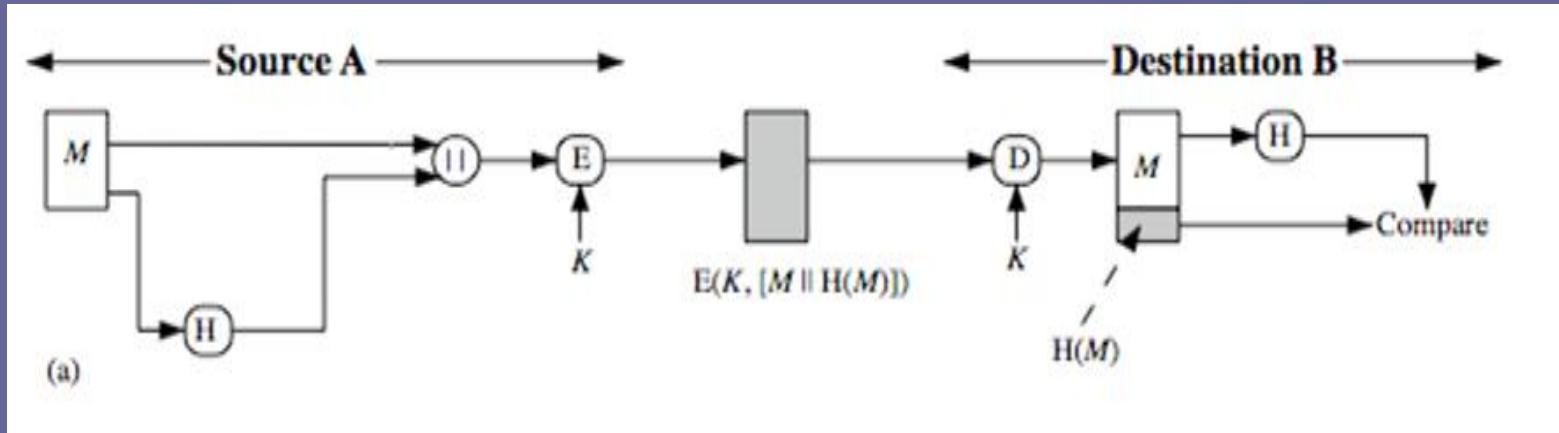


- Figure depicts the general operation of a cryptographic hash function.
- The input is padded out to an integer multiple of some fixed length (e.g., 1024 bits) and **the padding includes the value of the length of the original message in bits**.
- The length field is a security measure to increase the difficulty for an attacker to produce an alternative message with the same hash value.

# Hash Functions & Message Authentication

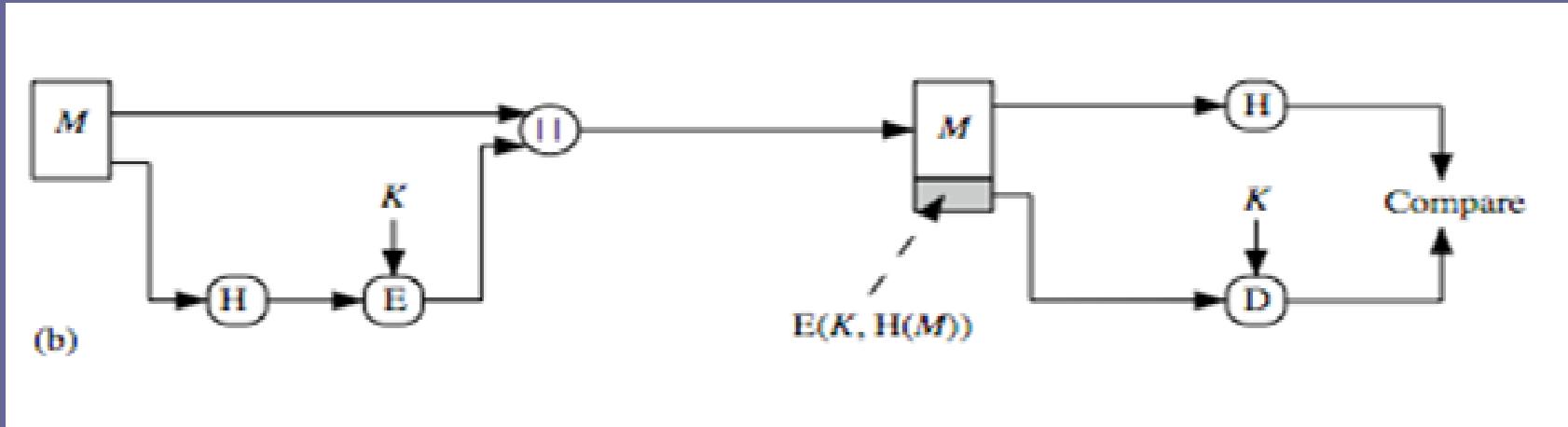
- Message authentication is a mechanism or service used to verify the integrity of a message, by assuring that the data received are exactly as sent.
- Figure A, B, C and D illustrates a variety of ways in which a hash code can be used to provide message authentication, as follows:

# A



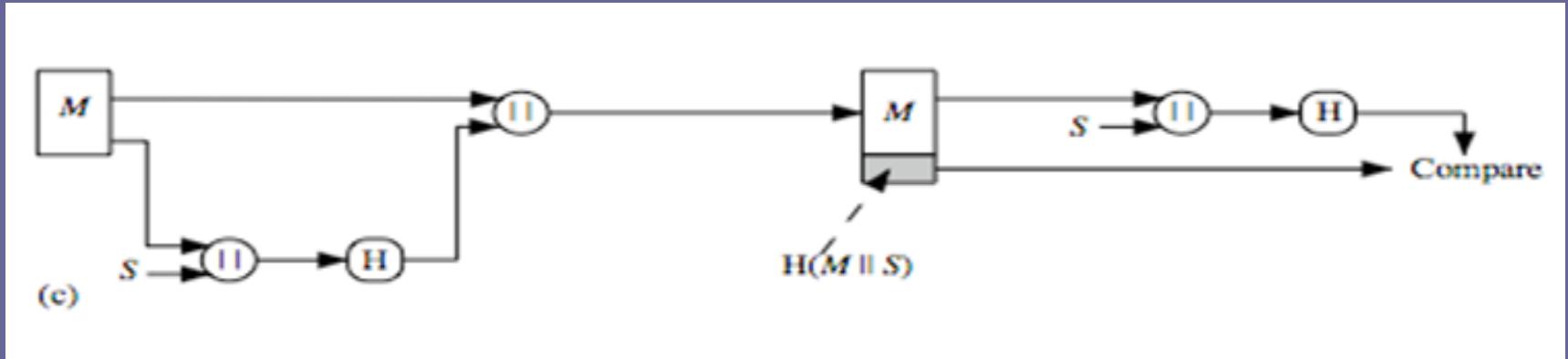
- The message plus concatenated hash code is encrypted using symmetric encryption. Since only A and B share the secret key, the message must have come from A and has not been altered.
- The hash code provides the structure or redundancy required to achieve authentication.

# B



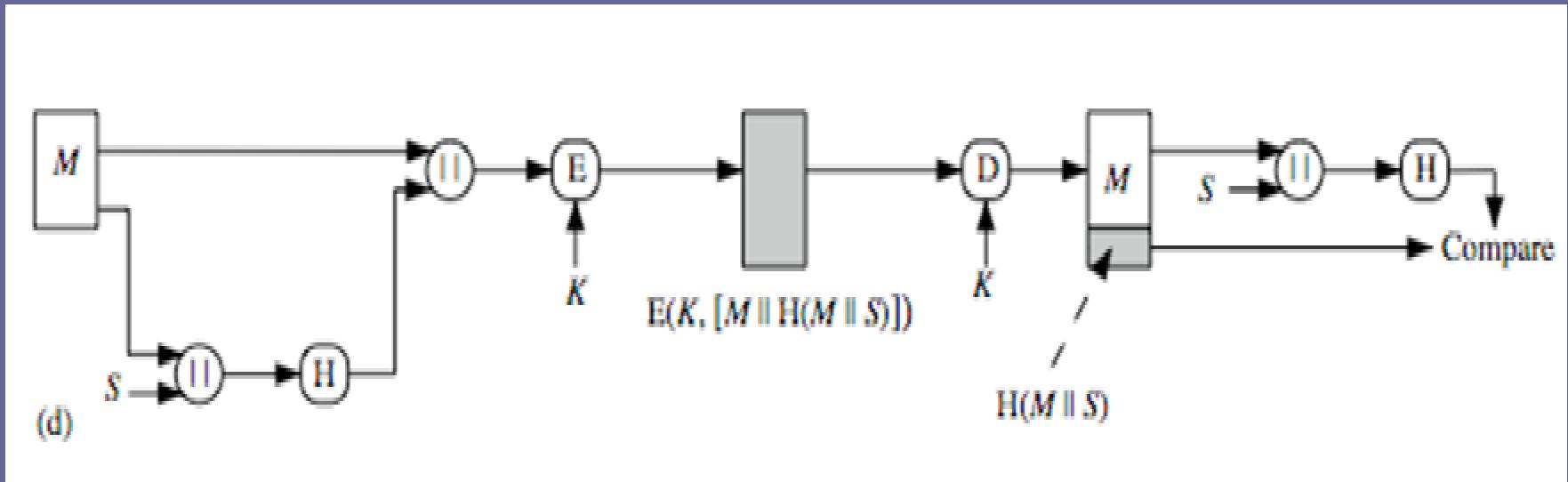
- Only the hash code is encrypted, using symmetric encryption. This reduces the processing burden for those applications not requiring confidentiality.

# C



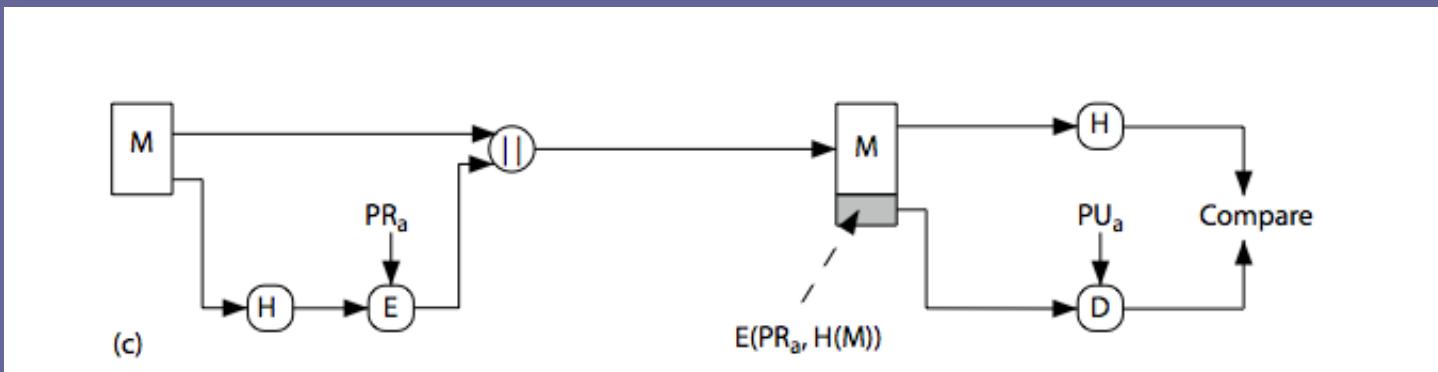
- Shows the use of a hash function but no encryption for message authentication.
- The technique assumes that the two communicating parties share a common secret value  $S$ .
- A computes the hash value over the concatenation of  $M$  and  $S$  and appends the resulting hash value to  $M$ .
- Because B possesses  $S$ , it can re-compute the hash value to verify.
- Because the secret value itself is not sent, an opponent cannot modify an intercepted message and cannot generate a false message.

D



- Confidentiality can be added to the approach of (c) by encrypting the entire message plus the hash code.

# Hash Functions & Digital Signatures



# Requirements for Hash Functions

1. Can be applied to any sized message  $M$
2. Produces fixed-length output  $h$
3. Is easy to compute  $h=H(M)$  for any message  $M$
4. Given  $h$  is infeasible to find  $x$

$$H(x) = h$$

- one-way property

1. Given  $x$  is infeasible to find  $y$

$$H(y) = H(x)$$

- weak collision resistance

1. Is infeasible to find any  $x, y$

$$H(y) = H(x)$$

- strong collision resistance

# Simple Hash Functions

- Are several proposals for simple functions
- Based on XOR of message blocks
- Not secure since can manipulate any Message and either not change hash or change hash also
- Need a stronger cryptographic function (next chapter)

# Birthday Attacks

- Might think a 64-bit hash is secure
- But by **Birthday Paradox** is not
- **Birthday attack** works thus:
  - opponent generates  $2^{m/2}$  variations of a valid message all with essentially the same meaning
  - opponent also generates  $2^{m/2}$  variations of a desired fraudulent message
  - two sets of messages are compared to find pair with same hash (probability > 0.5 by birthday paradox)
  - have user sign the valid message, then substitute the forgery which will have a valid signature
- Conclusion is that need to use larger MAC/hash

Dear Anthony,

{This letter is} to introduce {you to} {Mr.} Alfred {P.}  
{ I am writing } {to you } {-- } {the}

Barton, the {newly appointed} {chief} jewellery buyer for {our}  
Northern {European} {area} . He {will take} over {the}  
responsibility for {the whole of} our interests in {watches and jewellery}  
in the {area} . Please {afford} him {every} help he {may need}  
to {seek out} the most {modern} lines for the {top} end of the  
market. He is {empowered} to receive on our behalf {samples}  
{authorized} {specimens} of the  
{latest} {watch and jewellery} products, {up} {subject} to a {limit}  
{newest} {jewellery and watch} of ten thousand dollars. He will {carry}  
{hold} a signed copy of this {letter}  
as proof of identity. An order with his signature, which is {appended}  
{attached}  
{authorizes} {allows} you to charge the cost to this company at the {above}  
address. We {fully} expect that our {level} {volume} of orders will increase in  
the {following} {next} year and {trust} {hope} that the new appointment will {be}  
{prove}  
{advantageous} {an advantage} to both our companies.

Figure 11.9 A Letter in 2<sup>3</sup> Variations [DAVI89]

# Block Ciphers as Hash Functions

- Can use block ciphers as hash functions
  - using  $H_0=0$  and zero-pad of final block
  - compute:  $H_i = E_{M_i}[H_{i-1}]$
  - and use final block as the hash value
  - similar to CBC but without a key
- Resulting hash is too small (64-bit)
  - both due to direct birthday attack
  - and to “meet-in-the-middle” attack
- Other variants also susceptible to attack

# Hash Functions & MAC Security

- Bike block ciphers have:
- **Brute-force** attacks exploiting
  - strong collision resistance hash have cost  $2^{m/2}$ 
    - have proposal for h/w MD5 cracker
    - 128-bit hash looks vulnerable, 160-bits better
  - MACs with known message-MAC pairs
    - can either attack keyspace (cf key search) or MAC
    - at least 128-bit MAC is needed for security

# Hash Functions & MAC Security

- **Cryptanalytic attacks** exploit structure
  - like block ciphers want brute-force attacks to be the best alternative
- Have a number of analytic attacks on iterated hash functions
  - $CV_i = f[CV_{i-1}, M_i]; H(M)=CV_N$
  - typically focus on collisions in function  $f$
  - like block ciphers is often composed of rounds
  - attacks exploit properties of round functions