# Scalability and Satisfiability of Quality-of-Information in Wireless Networks

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Abstract—Quality of Information (QoI) provides a contextdependent measure of the utility that a network delivers to its users by incorporating non-traditional information attributes. Quickly and easily predicting performance and limitations of a network using QoI metrics is a valuable tool for network design. Even more useful is an understanding of how network components like topology, bandwidth, protocols, etc. impact these limitations. In this paper, we develop a QoI-based framework that can provide accurate estimates for limitations on network size and achievable QoI requirements, focusing on completeness and timeliness. We extend this framework to model competing flows and data loads as random variables to capture the stochastic nature of real networks. We show that our framework can provide a characterization of delays for satisfied queries to further analyze performance when some late arrivals are acceptable. Analysis shows that large tradeoffs exist between network parameters, such as QoI requirements, topology, and network size. Simulation results also provide evidence that the developed framework can estimate network limits and delays with high accuracy. Finally, this work also introduces scalably feasible QoI regions, which provide upper bounds on QoI requirements that can be supported for certain network applications.

#### I. INTRODUCTION

Traditional approaches to studying network scalability and performance limitations have been focused on finding theoretical limits on throughput and delay. In many applications, however, the relationship between these metrics and the effectiveness of the network is highly non-linear. Therefore, having a framework to evaluate network scalability with respect to achievable *Quality of Information* (QoI) requirements is necessary.

Additionally, while theoretical, asymptotic analysis of individual network topologies, protocols, etc. is important, such analysis lacks the ability to quickly obtain an accurate estimate of a projected network's abilities when these individual components are pieced together. Often, extensive simulation or experimentation testbeds must be created to test proposed network setups, which is difficult and time-consuming.

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As an example, imagine being given the task of deploying a wireless sensor network for a particular application. Given a proposed network with a defined size, topology, parameters, and protocols, what is the level of QoI requirements it can support? Now, consider the converse: Given a certain QoI that is desired by users of a network, what is the maximum number of nodes that the network can support? Which has a bigger impact on this scalability, the imposed information requirements, or the strict timeliness requirements?

Our main contribution in this paper is a novel framework that can predict scalability and performance of a network with respect to QoI requirements for answering such questions. We explain this framework in detail in Section IV and provide example applications in Section V. As a second contribution we extend this framework in Section VI, capturing the stochastic nature of query sources and destinations as well as data requirements, and show that it can be used to characterize query delays. In both cases, we provide results from realistic implementations in the ns-3 network simulation environment.

We also present several pieces of supporting work. First we provide an example of an application that relies on QoI to highlight the difference in QoI and traditional metrics in Section III. We show in Section VII that our framework is also quite useful in quickly and easily understanding the impact of parameters and design choices, providing a secondary benefit to network designers of allowing them to compare networks and identify tradeoffs. Finally, we show how the framework can also provide bounds on QoI capacity in some applications in Section VIII.

#### II. RELATED WORK

The scalability model derived in this work is inspired by the symptotic scalability framework outlined in [2], which has been previously applied to content-agnostic static networks [3] and mobile networks [4]. Other works characterize the capacity of wireless networks, like [5], [6], but all do so by considering how networks scale asymptotically or by analyzing specific network instances instead of developing a general model. Experimental techniques, like Response Surface Methodology [7], for example, may be applied to solve the problem we do, but these require complex test beds instead of a compact mathematical framework.

A large number of works provide definitions for QoI and frameworks that utilize it. We will address only the most relevant ones here. Primarily, QoI has been considered from a number of angles including routing [8], scheduling/rate control [9], [10], and impact on usage of network resources [11]. Our focus is on a broader scale here, though, modeling scalability and limitations of an entire network.

A framework called Operational Information Content Capacity is outlined in [12], which describes the obtainable region of QoI, a notion similar to the *scalably feasible QoI region* developed here. This approach dose not provide any method for determining the possible size of the network or impact of network design choices like medium access protocols. We also note that a notion similar to QoI satisfiablility was considered in [13] which addresses resource allocation for long-term average QoI outage satisfaction. However, the focus of [13] is energy-efficient scheduling and power allocation in a single-hop three-node network rather than scalability.

In Section III, we use similarity-based image collection as an example of an application that is best evaluated using QoI. This application has previously been considered in [14] and [15]. Our scope is greater than that of [14], which does not consider attributes of timeliness, nor the consideration of transmission rates and network topology. We use the same similary-based image selection algorithm as in [15], but provide new methods of quantifying QoI.

#### III. QOI MODEL

QoI is a multi-dimensional metric that can be defined for an application to give a more meaningful measure of the value of information. It consists of attributes such as timeliness, freshness, completeness, accuracy, precision, etc. For example, information that contributes to a decision-making process may only be useful if it arrives before the decision must be made, or it may have varying usefulness based on how similar or dissimilar it is to other data already collected.

The specific details of which attributes are considered and how they contribute to QoI is application-dependent. Chosen QoI metrics are stored as a vector associated with a data item. Here, as in [16], we specify a vector of minimum values for each QoI metric, and information is evaluated based on whether it satisfies all of the QoI requirements or not. We use this approach to establish the edges of QoI satisfiability for the vector of metrics, which defines the boundaries of maximum achievable QoI regions in the metric space.

We choose to use two QoI attributes, one that is time-based and one that is information-content-based. The first attribute is timeliness, T, of data. For the second attribute, we present a notion of *completeness*, C, which we show can be defined multiple ways, depending on the application and context. Together, a QoI requirement of  $\mathbf{q} = \{C, T\}$  specifies a quantity of data that must be delivered as well as a deadline by which it must arrive to be useful. Since completeness is a rather new concept, we explain an example image selection algorithm and show how it can be evaluated with completeness.

#### A. Example Application: Similarity-based Image Retrieval

As a motivating example, we choose a network in which nodes store photographs that are to be exchanged or collected at one or more data sinks. This example covers surveillance missions of military tactical networks or camera sensor networks. In this model, nodes can act as both clients and servers, issuing queries and serving images in response. Therefore, as the network size increases, the amount of traffic is also likely to increase, but possibly disproportionately. This fact exemplifies why the problem of characterizing the scalability limits for an instance is not straightforward.

To satisfy completeness of a query, we utilize measurements of the similarity or dissimilarity between pairs of images as explained in the rest of this section. To get a similarity measurement, we use the same choice as was shown to be effective in [15]. A technique called Color and Edge Directivity Descriptor (CEDD) [17] provides a 54-byte vector of qualities inherent to a photograph like lightness, contrast, and color. The similarity between two images can then be given as a scalar by calculating the *Tanimoto Similarity* [18] between their CEDD vectors. Dissimilarity is simply defined as 1 minus the similarity.

1) Selecting Similar Images: One possible query for data is to retrieve images from the network that are similar to an identified target image. The first type of query we introduce occurs when a user already has one image of a particular area or object of interest and would like to obtain similar images to get a more complete view of that specific scene or object. For example, if a user has a picture of an unknown suspicious person entering a building, but the person is not identifiable from that image, it would be useful to collect more images that are similar to that one with the possibility that another picture may have a better view of the person in question that can be used for identification or more context. Called **Top-K**, the query algorithm used for this application will choose the k images with the most similarity with respect to the target image.

We can evaluate the completeness of the result in one of two ways. First, we can use the similarity of the images as a value representing each image's effectiveness in providing a more complete view of the target scene. If we sum the similarity of all k images returned by the algorithm, we get a representation of completeness, which we naturally call *Sum Similarity*. While this measure of completeness is abstract, it can be refined in an actual implementation through testing and evaluating. This definition of completeness is useful, though, because it can be applied without any predetermined knowledge of the environment or pool of images.

Often, though, we can partition the environment in which the network operates into a number, n, of distinct settings or areas. In those cases, we can utilize a second method of quantifying completeness. Assume that each image belongs to one of these n sets, related to the setting it depicts. Naturally, then, when executing a Top-K query, the goal is for the algorithm to return images from the same set as the target

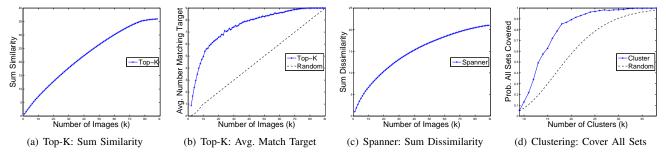


Fig. 1. Completeness metrics for the three image selection algorithms. Each exhibits a diminishing return as more images are added.

image. Completeness can then be given by the fraction of images returned that are in the same set as the target image.

2) Selecting Diverse Images: In contrast, given the set of all photographs available in the network, we might want to return the set of k images that exhibits the most diversity, ideally providing a user with a good sampling, or *complete view*, of available images. For instance, such a result would be quite useful in a surveillance mission. We present two query algorithms that can be used to achieve this goal.

One query that provides diverse images is known as the **Spanner** of the set of known photographs. For the Spanner algorithm, we employ a greedy algorithm similar to that in [15]. Here, the algorithm simply chooses images that provide the greatest minimum distance from all images already chosen. This minimum distance can be added to a running sum to provide a completeness metric of *Sum Dissimilarity*. This value represents a measure of completeness because a higher level of dissimilarity provides a more complete view of the feature space.

The other query that can achieve a complete view over all images is **Clustering**. In the Clustering algorithm, all images are separated into a k clusters based on their pairwise distances using any version of a k-means clustering algorithm, where k is given by the user. Then, the most central image from each cluster is returned. Here, assuming that the photographs of the same settings or objects of interest exhibit similar characteristics, Clustering also provides a complete view of the network's environment.

Both Spanner and Clustering algorithms can also be evaluated using a model assuming the environment is split into n sets. With this model, we can define completeness as either the number of sets represented by at least one of the k images returned or the probability of all n sets being represented by at least one image when k are returned. Here, though, we only show results for the second definition.

#### B. Experimental Results

To provide example values of these completeness metric definitions, experiments applying each query algorithm were run on a set of pictures taken at n=9 different settings around the Penn State campus. Each of these 9 settings is of a pictorially different area, e.g. a particular building, a downtown street, or a lawn setting, and over 20 images of each was taken. Then, for individual trials, 10 images from each set

were randomly selected to create an image pool of 90 pictures. The three algorithms were run over these 90 images, with the target image being randomly selected in the case of Top-K. Results for each of the different completeness metrics were averaged over 1,000 trials are shown in Figure 1.

Figure 1(a) shows the average sum similarity of images returned by the Top-K algorithm. Figure 1(b) provides the second definition of completeness for the Top-K algorithm, the number of images matching the set that the target image was randomly chosen from. Completeness results when dissimilarity is the objective are shown in Figures 1(c) and 1(d). Specifically, Figure 1(c) depicts the average Sum Dissimilarity returned by the Spanner algorithm, and Figure 1(d) represents the empirical probability of all 9 sets being represented in the k returned images. For reference, we also include expected values for the metrics in Figures 1(b) and 1(d) if the images were selected from the entire image pool at random, i.e., without regard for image similarity or dissimilarity. Details on these expected values given random selection are in Appendix A.

These figures exhibit the diminishing returns of completeness as more images are collected. This effect visually shows how QoI differs from throughput. As seen in these graphs, transmission of successive images does not result in a linear gain in completeness. For example, in Figure 1(b), it is evident that a value of only  $k \approx 10$  is needed to collect 5 images matching the target content, while collecting an additional 2 from the same set usually requires collecting over twice that number of pictures. Similarly, Figure 1(d) shows that jumping from k=10 to k=20, the likelihood of capturing at least one image of every setting grows substantially from just over 10% to approximately 90%. To approach probabilities close to gaining that final 10%, however, requires a jump to  $k\approx 30$ .

The relationship between the number of images and completeness in each of these graphs also shows that obtaining a certain value of QoI or completeness requires a different number of images depending on the set available and their similarities. We can denote the number of images required to achieve a level of completeness, C, as  $k_{req} = Q(C)$ . This relationship will be useful later in determining capacity and scalability limits.

#### C. Further Discussion of QoI

We have defined and provided examples for a number of ways that completeness can be defined and used to obtain a concrete data requirement from a contextual QoI requirement. Throughout the rest of the paper, we use sum similarity and the probability of covering all sets using clustering as completeness metrics, but we note that any of the definitions of completeness used here, or any other QoI requirement that can be translated into a data requirement, for that matter, can be used.

Also, while metadata associated with photographs may be useful in obtaining similar goals to those given in this section, relying on such information is problematic because metadata is not guaranteed to be available, and it is not as universally applicable as content-based retrieval. For example, tags describing the image contents would require users to participate by entering this information, which is time-consuming and unreliable. Location and time stamps may be automatically applied by the device allowing an application to filter images accordingly, but these tags often do not account for factors such as the direction of the camera or obstructed views. Content-based processing, though, can be applied to any set of images.

#### IV. QOI SCALABILITY

Given the nonlinear returns of completeness and importance of timeliness outlined in the previous section, we contend that establishing limits of throughput is insufficient. A non-QoI-aware approach ignores very useful information such as how changes in achievable data rates affect the actual utility of information at its destination as well as how changes in one QoI requirement can affect satisfiability of other requirements.

For these reasons, we set the goal of determining the capacity of a network, and relatedly, the scalability achievable with respect to QoI requirements. Previous methods that predict scalability do so by singling out a single bottleneck node and determining when it will be overloaded and drop packets. Here, we are forced to look at end to end flows and determine all contributors to delay, including MAC access, queuing delays, and multi-hop propagation to find the point at which timeliness requirements are violated or traffic load must be reduced thus adversely affecting completeness, leading to a more comprehensive analysis.

#### A. QoI Satisfiability Framework

In order to establish the framework, we examine an arbitrary flow,  $F_1$ , in the network that has a QoI requirement of  $\mathbf{q}=\{C,T\}$ , where C is the minimum required completeness metric of choice, such as sum similarity as explained above, and T is the required timeliness. This flow will have a data size requirement, which is given by a chosen QoI function Q(C). Using the example application from III, for example, Q(C) can return the number of images,  $k_{req}$ , required to achieve the requested completeness C. We use a fixed value the data size here for simplicity in developing the equations characterizing

delay, but we expand our consideration to use a distribution for data size in our applications in Section V.

Assuming each image has a size of  $I_S$ , then we can also use B to describe the total number of bits required by the flow,  $B = k_{req} * I_S$ . To match realistic network implications, we assume this data will be transmitted in a series of packets with size  $P_S$  bits each. The number of packets per flow, then, is simply  $P_N = \lceil B/P_S \rceil$ . We assume that each node in the network can transmit at W bits per second when it is allocated media access.

Our goal is to establish the limits at which this arbitrary flow can no longer be completed with the QoI requirements satisfied. We build and explain our model for achieving this goal by working through an example TDMA line network, a portion of which is shown in Figures 2 and 3. (We discuss addressing non-TDMA networks in Section IX.) In this network, we assume a simple 3-slot TDMA scheme, which allows each node equal time access to the medium and removes any potential interference or hidden terminal issues. The TDMA Slot assignments are labeled above each node. For simplicity, we will assume that one slot is appropriately sized to transmit a single packet, i.e.,  $T_{slot} = P_S/W$  and that packets use static routes calculated beforehand such that the overhead is not a consideration here.

Now, two factors,  $D_1$  and  $D_2$ , contribute to the total delay of completing flow  $F_1$ . The first contributor,  $D_1$ , is the end to end delay incurred by sending the B bits across the entire path. To quantify this delay, we must consider several factors beyond just the available bandwidth and number of packets. First, each node can only utilize its allotted channel time, creating a Channel Factor of  $CF = N_{frame}/N_i$ , where  $N_i$  is the number of slots allocated to node i and  $N_{frame}$  is the total number of slots in each frame. In this case,  $N_i = 1, \forall i$  and  $N_{frame} = 3$ .

The second factor to consider for  $D_1$  is the fraction of allocated slots that are utilized by the node to serve flows other than  $F_1$  that are either originating in or being routed through nodes on the path of flow  $F_1$ . We call the total number of flows competing at node i the Traffic Factor,  $TF_i$ , of that node. For any flow, the maximum contributor to delay is the node along the path with the maximum  $TF_i$ , which we will just call TF here. More detail about determining this TF will be outlined in Section V-A. Incorporating these considerations into a calculation for  $D_1$ , we achieve the following expression:

$$D_1 = T_{slot} \cdot P_N \cdot CF \cdot TF \tag{1}$$

Figure 2 depicts the delay of  $D_1$  in a simple case of only two flows,  $F_1$  and  $F_2$ , being present, in which case TF=2. In this example we use flows that consist of only 2  $(F_{i-j})$  is packet j in flow i) packets to portray the delay. In most real applications,  $P_N$  will be much larger, making  $D_1$  a good approximation of this delay component.

The second delay that exists is due to multi-hop propagation of packets. This delay is simply the time for a single packet to traverse the path length. Note that this delay is not necessarily just the path length multiplied by  $T_{slot}$ , because of possible

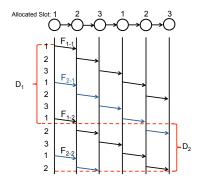


Fig. 2. Example of line network using TDMA highlighting source of delays,  $D_1$  and  $D_2$ . (Node labels are slot assignments.) Here,  $TF=2,\ CF=3,$  and DF=1.

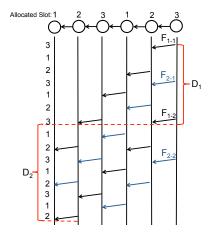


Fig. 3. In the opposite direction, DF=2. (TF and CF are unchanged here.)

queuing delays and/or ordering constraints. We show here how ordering constraints impact this TDMA network. A node cannot forward a packet from the flow until it receives that packet from the previous hop. In our line network example, when the direction of the flow matches the nodes' schedule of slots 1-2-3-1-2-3, as in Figure 2, each successive node receives a packet on the time slot before it is scheduled, resulting in no extra delay. For a flow in the opposite direction, though, where nodes are scheduled 3-2-1-3-2-1, as in Figure 3, the first slot 1 is not utilized, because the first node scheduled in time slot 1 has not yet received a packet in the flow. Every other slot is wasted, on average, for the initialization of the flow, resulting in approximately twice the delay. We will use a term that we call the Delay Factor, or DF, to account for this effect where it exists. The multi-hop propagation delay, then, is modeled by

$$D_2 = T_{slot} \cdot DF \cdot (PL - 1) \tag{2}$$

where PL is the average path length.

We note several points about this delay factor. First, in a loaded network, the nodes can and will serve other flows while awaiting the arrival of packets in this flow of focus. That utilized bandwidth does not, however, preclude this DF

impact on delay for the flow of interest,  $F_1$ . Any node cannot serve  $F_1$  until a packet from that flow has been received. Second, this delay is only accounted for once per flow because all other packets are pipelined. All other packets' delay is captured by the end to end delay,  $D_1$ . This effect is best illustrated by examining the difference between  $D_2$  in Figures 2 and 3. Here, we see the multi-hop propagation requires twice the number of slots because every other slot is unused in  $F_1$ 's propagation. To calculate a DF for an entire network, we can calculate a DF for each possible sample path and find the average of these values.

By adding the two components of delay, we can give a relation for a network that will successfully achieve an average flow's data and timeliness requirements:

$$T_{slot} \cdot P_N \cdot CF \cdot TF + T_{slot} \cdot DF \cdot (PL - 1) \le T$$

Recalling that the time of a slot is determined by  $T_{slot} = P_S/W$  and that the total number of bits required for a flow  $P_S \cdot P_N = k_{req} \cdot I_S$  (where  $k_{req}$  is given by a function of required QoI), we can get the following expression:

$$W \cdot T - k_{reg} \cdot I_S \cdot CF \cdot TF - P_S \cdot DF \cdot (PL - 1) \ge 0$$
 (3)

Every network will have its own set of parameters that can be substituted into this general formula, providing a tool to approximate limitations and sensitivity to changes in specific parameters. To show this usefulness concretely, we provide derived values for a TDMA-based wireless network with several basic topologies.

### V. EXAMPLE OF APPLYING FRAMEWORK

We illustrate the application of Equation (3) using an Nnode TDMA network with three different topologies: clique, line, and grid, also known as a "Manhattan grid." Discussion of other network control protocols and topologies are addressed in Section IX. We adopt a traffic model that uses Top-K queries as an example application. We assume that all nodes have a set of collected images that are used to respond to Top-K queries. Each node produces queries according to a Poisson process with exponential interarrival times with parameter  $\lambda$ , each with a target image and target QoI,  $q = \{C, T\}$ , describing the required completeness (here, we use sum similarity) and timeliness, and sends it to another node chosen at random. Here, the actual size of the response fulfilling the query can be given by a distribution that incorporates the number of images required,  $k_{req}$ , and the size of each image. The details of this distribution can be given from empirical observations of experiments like those in Section III.

#### A. Defining Traffic Factor

The Traffic Factor will depend on the traffic pattern and routing scheme used in the network, but here we outline a general formula for modeling it with a random variable based on the traffic model described above.

Let  $\rho(x)$  be the number of shortest paths of all other nodes that include node x. Let  $\chi_{ij}$  represent the existence of a flow from node i to node j. We assume that  $\chi_{ij}$  is equal to 1

with probability  $p_f$  and 0 otherwise. Then, the traffic factor of a node x,  $TF_x$ , is given by the sum of  $\chi_{ij}$  for all  $\rho(x)$  pairs (i,j) in which x is along the shortest path. If  $\chi_{ij}$  is i.i.d for all pairs (i,j), then  $TF_x$  is a Binomial random variable with n=N and  $p=p_f$ . Depending on the traffic pattern of the application(s) in the network, the conditions for using an approximation for  $TF_x$  are likely to be satisfied as we show in the next section where we approximate it with a Poisson distribution.

With a goal of determining maximum scalability and QoI-satisfiability limits, we choose to focus on the bottleneck node, b, which is the node that results in the largest mean  $\mu_{TF_x}$  value. While some non-uniform topologies may require some processing or calculation to determine this bottleneck node, in the topologies we explore in depth here, finding the bottleneck is intuitive. Next, we derive the TF expression for the bottleneck node in line and grid topologies.

1) Line Network Traffic Factor: First, let us look at the number of paths that go through the bottleneck node, which is the center node for a line network. We will assume that N is odd here, for simplicity of notation, but the logic is the same for even values of N. Since there are  $\frac{N-1}{2}$  nodes on each side the center node, the total number of paths that go through it is

$$\rho(b) = 2(\frac{N-1}{2})^2$$

Then, since there are N flows and N\*(N-1) total paths in the network, we can approximate the probability of each path containing a flow as  $p_f = \frac{1}{N-1}$ . Then,  $TF_x$  will be a Binomial random variable with  $n = \rho(b)$  and  $p = \frac{1}{N-1}$ . Therefore, since np remains fixed and p approaches zero for a given network size N, we can use a Poisson approximation for  $TF_x$  in this case, giving the following distribution:

$$f_{TF_b}(t) = e^{-(\frac{N-1}{2})} \frac{(\frac{N-1}{2})^t}{t!}$$

While a Poisson approximation is appropriate here, in other applications,  $TF_x$  may be approximated using a Normal distribution instead, especially when p does not approach zero or one for a given network size.

2) Grid Network Traffic Factor: Again, the bottleneck node, i.e., the node with the highest number of paths going through it is the center node, and we give the derivation for when  $\sqrt{N}$  is odd, but the logic follows similarly for even values. As proved in [19], the most optimal routing scheme for maximum capacity is "Row-First, Column-Second" routing, so we assume paths follow this approach. Again, we adopt a traffic pattern in which each node is the source of exactly one flow and that the destination is uniformly chosen from all other N-1 nodes. For each source node, we can determine the number of destinations that route through the center. We separate nodes into two categories for this counting.

First, we consider the nodes circled in set A in Figure 4, of which there are  $\sqrt{N} \cdot \frac{\sqrt{N}-1}{2}$ . Through manual inspection, one can deduce that the only destination nodes in the figure that result in a path that is relayed by the center node are the

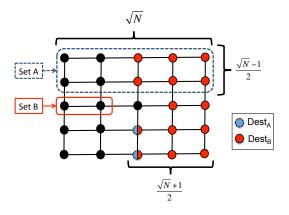


Fig. 4. Sources and destinations used in proving TF for grid networks

two bottom nodes in the center column in the figure, marked with blue. There are  $\frac{\sqrt{N}-1}{2}$  of these destination nodes for the nodes in set A, so the total number of paths from the nodes in set A is  $\sqrt{N}\cdot(\frac{\sqrt{N}-1}{2})^2.$  Now, if we also consider the reverse, i.e. imagine the figure rotated vertically, then we can give the total number of paths from nodes not in the same row as the center node as  $2\cdot\sqrt{N}\cdot(\frac{\sqrt{N}-1}{2})^2.$ 

Next, we consider the nodes in the same row as the center node, which we call set B. Here, all destinations on the "opposite" side of the center as well as those in the same column of the center require being routed through the center node when originating from any nodes in set B. Just as above, we can count the number of paths from the nodes in set B that route through the center and double it to count the reverse. The resulting number of paths is  $2 \cdot (\sqrt{N} \cdot \frac{\sqrt{N}+1}{2} - 1) \cdot (\frac{\sqrt{N}-1}{2})$ .

Adding together these paths and simplifying gives us the following expression for the total number of paths that go through the center node:

$$\rho(b) = \sqrt{N} \cdot (N-2) + 1 \tag{4}$$

Just as with line networks, the probability of each path containing a flow is  $p_f=\frac{1}{N-1}$ , so the traffic factor for the center node of a grid network is approximated with a Poisson distribution:

$$f_{TF_b}(t) = e^{-(\frac{\sqrt{N} \cdot (N-2)+1}{N-1})} \frac{(\frac{\sqrt{N} \cdot (N-2)+1}{N-1})^t}{t!}$$

which can be approximated by the following for large values of N.

$$f_{TF_b}(t) = e^{-(\sqrt{N})} \frac{(\sqrt{N})^t}{t!}$$

#### B. Scalability Equations

Once an expression for the Traffic Factor (TF) is derived, we can use it along with expressions for the Channel Factor (CF), Delay Factor (DF), and Path Length (PL) for the network to create specific instances of Equation (3) that estimate the scalability and QoI-satisfiability limits of the particular network of interest. Since our goal is to determine the point at which the system is unable to support the offered traffic load within the timeliness constraints, we use maximum

values for these factors where applicable, specifically  $TF_{max}$  and  $PL_{max}$ .

The  $PL_{max}$  is usually quickly determined by an examination of the topology, such as  $PL_{max} = N-1$  for a line network and  $PL_{max} = 2 \cdot \sqrt{N}$  for a grid network. To get a good estimate of  $TF_{max}$ , we can simply utilize the mean and standard deviation of the distribution derived above to create the following:  $TF_{max} = \mu_{TF} + \eta \cdot \sigma_{TF}$  where  $\eta$  is a factor that can adjust how conservative the estimates should be. This notion of  $\eta$  is analogous to the z-score of a standard normal distribution, and is applicable here since  $TF_x$  approaches a Normal distribution as the network size, N, grows. As an example, we use  $\eta = 3.5$  in the validation results below, which captures approximately 99.7% of the maximum of the TF distribution.

Table I shows expressions for clique, line, and grid networks as derived above and in [2]. Then, substituting the factors into equation 3, we achieve the scalability equations for each topology in Table II.

To find the limitation of a particular parameter or QoI component, the scalability equation can be solved for the variable of interest. Then all known values can be substituted to get the limit of the variable of interest. For example, given a network size and completeness requirement, we can determine a clique network's minimum sustainable timeliness with the equation  $T \geq \frac{I_S \cdot k_{req} \cdot (N-1)}{W}$ , where  $k_{req}$  is given by the completeness function Q(C). In practice, solutions for these equations will most likely need to be made numerically, but doing so is rather straightforward using any number of commonly available tools. As we will show in Section VII, these equations can also be easily used to determine the impact of other network parameters on this timeliness limit.

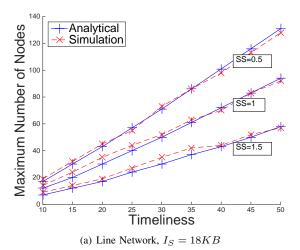
#### C. Minimum Timeliness/Maximum Query Rate

Solving the Scalability equations for T reveals the minimum satisfiable timeliness value for which all queries are expected to complete within the deadline constraint, which we will call  $T_{min}$ . Consequently, this minimum satisfiable timeliness value also correlates to the maximum traffic rate that can be served by the network,  $\lambda_{max} = \frac{1}{T_{min}}$ . If the average rate of queries,  $\lambda$ , is greater than  $\frac{1}{T_{min}}$ , then the traffic will exceed the network capacity and the number of active queries in the system will grow without bound, causing packets to be dropped and/or delays to grow without bound. Therefore, the maximum query rate is  $\lambda_{max} = \frac{1}{T_{min}}$ , and, consequently, the minimum timeliness for which all flows can be expected to complete before the deadline is  $T_{min}$ .

In some applications, having a certain amount of queries not complete by the timeliness requirement may be acceptable. As we show in Section VI, we can develop a more detailed characterization of the delay equation than the Scalability Equations here for these applications.

#### D. Validation of Scalability Equations

To show how effective estimates using this framework can be, we simulated the network topologies and traffic described



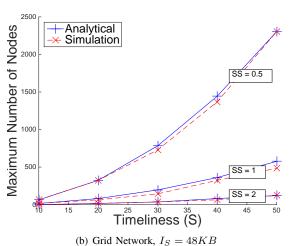


Fig. 5. Empirical results match analytical results closely for all tests.

above in Section V in the ns3 network simulator, comparing empirical results to those generated analytically with this framework, labeled Analytical. We use a channel rate of W=2Mbps, packet sizes of  $P_s=1500$  bytes, and image sizes of 18 and 48 Kbytes. As above, the correlation between Sum Similarity and  $k_{req}$  is taken from the actual observed relation in Figure 1(a). All values of parameters  $(SS,\,T,\,I_S,\,$ etc.) were chosen to test a variety of network sizes and QoI requirements while remaining within realistic network sizes, both with respect to real-world deployments and simulations with feasible run-times.

#### VI. FINDING LIMITS AND CHARACTERIZING DELAY

As explained in Section III, delay of a flow can be expressed as

$$D = \frac{k_{req} \cdot I_S \cdot CF \cdot TF}{W} + \frac{P_S \cdot DF \cdot (PL - 1)}{W}$$
 (6)

Let PL() be a function that provides the path length between i and j, and let  $TF_i^j$  be a random variable of the Traffic Factor for the bottleneck node between i and j, i.e. the node along the path from i to j with the highest  $u_x$ . Finally, let  $P_N$  be

	CF	$\mu_{TF}$	$\sigma_{TF}$	DF	$PL_{max}$	
Clique	N-1	1	1	1	1	
Line	3	$\frac{N-1}{2}$	$\sqrt{\frac{N-1}{2}}$	1.5	N-1	
Grid	5	$\sqrt{N}$	$N^{\frac{1}{4}}$	2.5	$2 \cdot \sqrt{N}$	
TABLE I						

CF, TF, DF, AND PL VALUES FOR EXAMPLE TOPOLOGIES

	Equation
Clique	$W \cdot T - I_S \cdot k_{req} \cdot (N-1) \ge 0$
Line	$W \cdot T - 3 \cdot I_S \cdot k_{req} \cdot (\frac{N-1}{2} + \eta \cdot \sqrt{\frac{N-1}{2}}) - 1.5 \cdot P_S \cdot (N-1) \ge 0$
Grid	$W \cdot T - 5 \cdot I_S \cdot k_{req} \cdot (\sqrt{N} + \eta \cdot N^{\frac{1}{4}}) - 2.5 \cdot P_S \cdot (2 \cdot \sqrt{N} - 1) \ge 0$
	TARLE II

SCALABILITY EQUATIONS

$$F_D(d) = \frac{1}{N} \cdot \sum_{i=1}^{N} \sum_{j \neq i} \sum_{tf=1}^{tf_{max}} F_{P_N}(\frac{d - C_2 \cdot PL(i, j)}{C_1 \cdot p_N}) \cdot f_{TF_{i|j}}(tf) \cdot p(j)$$
(10)

a random variable that describes the number of packets in a given request, capturing both the possible randomness of  $k_{req}$ and  $I_S$ . Then, building on the equation for delay above and making some substitutions, we can get the following equation to describe the delay from a node i given a destination of j:

$$D_i^j = \frac{P_S \cdot CF \cdot P_N \cdot TF_i^j}{W} + \frac{P_S \cdot DF \cdot (PL(i,j) - 1)}{W} \quad (7)$$

Defining two constants to simplify the expression,

$$C_1 = \frac{P_S \cdot CF}{W}$$
$$C_2 = \frac{P_S \cdot DF}{W}$$

we can express the delay as

$$D_{i}^{j} = C_{1} \cdot P_{N} \cdot TF_{i}^{j} + C_{2} \cdot PL(i, j) \tag{8}$$

We can develop an expression for a distribution of delay as follows. First, we define the cumulative distribution of a source-destination pair (i, j):

$$P(D_i^j \le d) = P(C_1 \cdot P_N \cdot TF_i^j + C_2 \cdot PL(i, j) \le d)$$
$$= P(P_N \cdot TF_i^j \le \frac{d - C_2 \cdot PL(i, j)}{C_1})$$

Next, conditioning over all possible values of TF, we get

$$P(D_i^j \leq d) = \sum_{\tau=1}^{\tau_{max}} P(P_N \cdot TF \leq \frac{d - C_2 \cdot PL(i,j)}{C_1} | TF = \tau) \cdot f_{TF_i^j}^{j}(\tau)$$
 quality estimates to answer these question  $P(D_i^j \leq d) = \sum_{\tau=1}^{\tau_{max}} P(P_N \cdot TF \leq \frac{d - C_2 \cdot PL(i,j)}{C_1} | TF = \tau) \cdot f_{TF_i^j}^{j}(\tau)$   $P(D_i^j \leq d) = \sum_{\tau=1}^{\tau_{max}} P(P_N \cdot TF \leq \frac{d - C_2 \cdot PL(i,j)}{C_1} | TF = \tau) \cdot f_{TF_i^j}^{j}(\tau)$ 

$$= \sum_{\tau=1}^{\tau_{max}} P(P_N \le \frac{d - C_2 \cdot PL(i, j)}{C_1 \cdot \tau}) \cdot f_{TF_i^j}(\tau)$$

Substituting the cumulative distribution representing the data load,  $F_{P_N}$ :

$$F_{D_i^j}(d) = \sum_{\tau=1}^{\tau_{max}} F_{P_N}(\frac{d - C_2 \cdot PL(i, j)}{C_1 \cdot \tau}) \cdot f_{TF_i^j}(\tau)$$

Then, we can generalize the expression to give a distribution for a flow originating in node i with an unknown destination by conditioning over all possible destinations, j.

$$F_{D_i} = \sum_{j \neq i} \left[ \sum_{\tau=1}^{\tau_{max}} F_{P_N} \left( \frac{d - C_2 \cdot PL(i, j)}{C_1 \cdot \tau} \right) \cdot f_{TF_i^j}(\tau) \right] \cdot p(j)$$
 (9)

Finally, we can get an average distribution of all flows' delays by summing over all sources and dividing by the the number of sources. This average delay distribution is in Equation (10).

#### A. Probability of Timeliness Satisfiability

While the minimum timeliness at which all flows are expected to complete before their deadlines can be determined by the scalability equations in Section V, some applications may benefit from an understanding of what the probability of completing within the timeliness constraints for those below the minimum fully satisfiable timeliness. For example, if a mission issues a number of queries for information to support decision-making, receiving 80% or 90% of the responses may be sufficient for making the decision. The question of importance, then, is "How far can we reduce the timeliness constraint and still expect to receive x% of the queries in time?" Or, equivalently, we may pose the question, "When the network is operating at the edge of capacity, what is the expected delay for x% of queries to be completed?" Since equation 10 provides the distribution of delays, it provides quality estimates to answer these questions.

Figure 6 shows expected delay distributions from 10 alongside distributions of delays recorded in ns3 simulations of the same networks. We argue that minimum QoI requirements for most applications tend to be over 50%, and therefore focus on the top half of the delay distribution. In all cases here, analytical predictions of satisfying the timeliness requirement are within about 10% of empirical results for probabilities above 0.5.

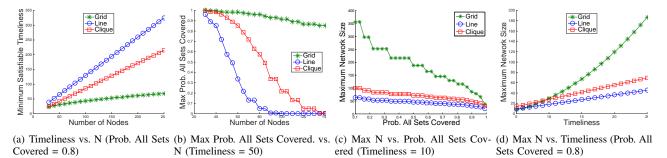


Fig. 7. Varying design parameters provide immediate limitations as well as evident trends and comparisons.

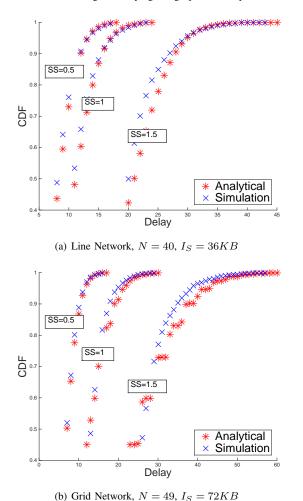


Fig. 6. Characterization of delay using framework follows distribution of empirical results in most cases.

#### VII. IMPACT ON NETWORK DESIGN

Now that we have established a model for QoI satisfiability and scalability and shown its accuracy in predicting estimated limits, we show how it can also provide quick, but useful intuition about the impact of various network parameters. Once an equation for a network's limitations is formulated as was done for equations in Table II, it can be solved for a single parameter to gain an understanding of its reliance on the other

factors. This analysis can be done very quickly and easily by approximating when appropriate, or by using symbolic and/or numerical solvers. To exemplify this application in network design, we have applied this process to the equations in Table II using the probability of covering all available images sets using the clustering algorithm in Section III as the completeness metric and created several figures that provide insight into network limitations and tradeoffs.

Figure 7(a) shows minimum satisfiable timeliness values for different topologies of increasing size. While it may be intuitive that a grid network should be able to serve flows with lower timeliness constraints than a line network since it will have shorter average path lengths, what is not intuitive is how much lower of a timeliness constraint is satisfiable. Here, we see that a grid network can scale up to over 250 nodes while supporting flows with T=50. A line network, on the other hand, can only scale to only approximately 20% of that network size for the same timeliness value. Additionally, it is useful to know how a clique network's timeliness satisfiability scales in comparison to either a grid or line network since its operation is quite different.

Figure 7(b) visualizes the maximum expected probability of collecting images that cover all sets of image settings for network instances with timeliness fixed. Here, again, limits and trends are quickly evident. In addition, the nonlinearity of completeness requirements are manifested here as the data requirements for the highest completeness requirements are only sustainable for small networks, and achievable completeness diminishes quickly as the network size grows for line and clique networks.

Finally, given a topology and application with predetermined requirements of **q**, we may be simply interested in how large our network can grow before its capacity to deliver the desired QoI is no longer possible. Values that answer this question are in Figures 7(c) and 7(d). Once again, the graphs show the major impact completeness and timeliness requirements can have on network size. Figure 7(c) especially shows the impact of using completeness instead of simply throughput as the non-linear relationship of completeness to data rate pointed out in Section III is evident in the scalability of grid networks here.

#### VIII. SCALABLY FEASIBLE QOI REGIONS

In some applications, the data requirements to achieve a certain level of QoI may include a minimum number of nodes or sources in addition to the size of the data load that must be served. For example, a system may require that each image must come from a different node, perhaps because each node only has one image or maybe by design to provide increased credibility through corroboration, another contextual metric of interest in QoI-aware networks. We will use this example to illustrate an interesting observation that arises in such scenarios.

Let us assume that we are designing a surveillance network with nodes arranged in a grid and one data sink in the corner of the network. This data sink node issues queries with a set of QoI requirements that include completeness and timeliness,  $\mathbf{q} = \{C, T\}$ , but this completeness must be met while only allowing one image per source node. With this traffic model, we can derive a maximum traffic factor and create a scalability equation for this particular scenario.

Here, the data sink node will have two neighbors through which all queries will be forwarded, so clearly we can choose either of these to consider as the bottleneck node. Even if the network balances traffic evenly over both of these nodes, each must forward at least  $\frac{N-1}{2}-1$  since there are N-1 sources, half of which must be forwarded through each of the data sink's two neighbors, excluding the 1 image from each of these neighbors themselves. If we assume these queries may be simultaneously served in the worst case, then we can simply use this expression for the maximum Traffic Factor. Then, using the same values derived for a grid network in Table I in place of the other factors in Equation (3), we get the following scalability equation:

$$W \cdot T - 5 \cdot I_s \cdot (\frac{N-1}{2} - 1) - 2.5 \cdot P_s \cdot 2\sqrt{N}$$
 (10)

From this equation, we can determine the maximum network size, which we will call  $N_{max}$  here. However, the specified restriction that each node can contribute only one image to  $k_{req}$  implies a minimum network size of  $N \geq k_{req}$  in order to achieve the completeness outlined in the QoI requirements.

These two facts are important, because when  $N_{max} < k_{req}$ , then it is not possible to provide the QoI level q. Hence, this set of QoI requirements is infeasible, or *scalably infeasible*. This phenomenon defines the concept of a *Scalably Feasible QoI Region*, which refers to the region in which sets of QoI pairs can be supported with the given network signature.

Figure 8 provides a visual representation of this region for a line network that institutes the given traffic model. Here,  $N_{max}$ , calculated for QoI requirements of Sum Similarity over the range [1,15] and Timeliness over the range [10,50], is shown in the graph by the blue surface. On the same graph is the number of images required,  $k_{req}$ , for each Sum Similarity requirement, shown with the yellow surface on the graph. The intersection of these two surfaces, displayed with a red line,

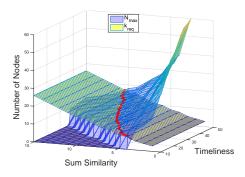


Fig. 8. The curved plane represents maximum scalability, and the flat plane represents minimum required images. Therefore, all (Sum Sim., Timeliness) pairs to the right of the intersecting red line are within the scalably feasible QoI region.

provides the edge of the scalably feasible QoI region. In this example, only QoI pairs to the right of this line, i.e. the region where  $N_{max} > k_{req}$ , are scalably feasible.

In general, regardless of how many images a node has, it is possible to analyze the trade-off between different QoI attributes for a fixed value of maximum network size,  $N_{max}$ . Specifically, by fixing N in Table II, one can obtain T and  $k_{req}$  (and, hence, C) resulting in the set of supportable  $\{C, T\}$  pairs defining a feasible region for QoI. This region can be visualized by intersecting the blue scalability curved plane with a flat surface fixed at  $N_{max}$  instead of the yellow surface in Figure 8. The scenario given in this section goes one step further and also takes into account the network size actually required to generate/support a given QoI requirement (using the non-flat yellow surface derived from experimental results in Figure 8).

#### IX. DISCUSSION

We note that although TDMA is primarily used in this work, the same approach can be taken to derive QoI-based relations in networks that use other MAC layer protocols. In these cases, the appropriate Delay Factor would need to be derived for each protocol. To examine an 802.11 network, for example, the DF would capture queuing delays and could be determined by extending a delay model such as in [20], and the CF could be estimated through studies of channel utilization like [21].

Similarly, although we only address the regular topologies of clique, line, and grid networks here, we believe the framework can be applied to more complex, irregular network topologies. In fact, some of the simple models presented here may already be quite useful for some of the topologies addressed. As shown in [22], for example, a dense random network may be closely approximated by a clique network, or random networks' capabilities can be approximately bounded by the limits of clique and grid networks, since these networks can be viewed of as examples of dense and sparse random networks, respectively.

#### X. CONCLUSION

This work provides several contributions to the field of QoI-aware wireless networks. First, we motivated the use of completeness and timeliness as QoI attributes, providing an example application and several different ways to measure completeness. Next, we developed a framework that can be used to predict QoI and network size limits for a specific network as well as predict expected probabilities of satisfying timeliness constraints beyond the point in which all queries are satisfied. We validated these models' accuracy by comparing analytical results with simulations performed in the ns3 network simulator in both cases. Examples of the impact of different network parameters were shown, providing concrete examples of the framework's usefulness in real-world applications. In addition, the concept of scalably feasible QoI regions was introduced. For future work, we plan to make generalizations of factors that will allow for easy application of this framework to any non-regular network topology and expand this framework to include consideration of more complex network control actions, such as caching and/or data compression or fusion, which are all of interest in QoI-aware networking.

## APPENDIX A EXPLANATION OF EXPECTED QOI WITH RANDOM IMAGE SELECTION

#### A. Top-K

First, we explain the expected number of images that are from the same set as the target image in the Top-K algorithm when images are selected from the entire image pool at random. We define the following:

- n = total number of images (summed over all sets)
- S = number of sets
- $S_k$  = set of target image
- k = number of images selected
- N<sub>S</sub> = number of images in each set (for simplicity, assumed to be the same for all sets)
- x = number of images returned from set  $S_k$

$$P(X = x | k) = \begin{cases} \frac{\binom{k}{x} * \binom{n-k}{k-x}}{\binom{n}{k}} & \text{if } k \le N_S, \\ \frac{\binom{N_S}{x} * \binom{n-N_S}{k-x}}{\binom{n}{k}} & \text{if } N_S < k \le n - N_S \end{cases}$$
(11)

Equation 11 provides the probability that x of the k selected images will be from the target set. When  $k \leq N_S$ , the total number of possible combinations of choosing x from the target set and k-x from the  $n-N_{S_k}$  remaining images over the entire sample space (n choose k). When  $N_S < k < n-N_S$ , then we consider the possible combinations of choosing x images from the target set and k-x images from the remaining  $n-N_S$  images. This probability formula can then be used to derive the expected values of x displayed in Figure 1(b).

#### B. Clustering

For Clustering, we want to determine the probability that we will cover each of the S sets with at least one of the k

chosen images if we had chosen them randomly. We will call  $X_i$  the random variable that represents the number of images from set i in the results. We use the following expression:

$$P(X_i > 0, \forall i | k) = (1 - P(X_i = 0))^S$$
 (12)

where  $X_i$  is given by a multivariate hypergeometric distribution, which gives us the following:

$$P(X_i = 0|k) = \frac{\binom{n - N_s}{k}}{\binom{n}{k}} \tag{13}$$

This probability expression is plotted directly against the percentage of trials in which all sets were covered in experiments using the Clustering algorithm in Figure 1(d).

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