

MASTER'S THESIS ON
SEMI-BLIND SOURCE SEPARATION VIA
SPARSE REPRESENTATIONS AND ONLINE
DICTIONARY LEARNING

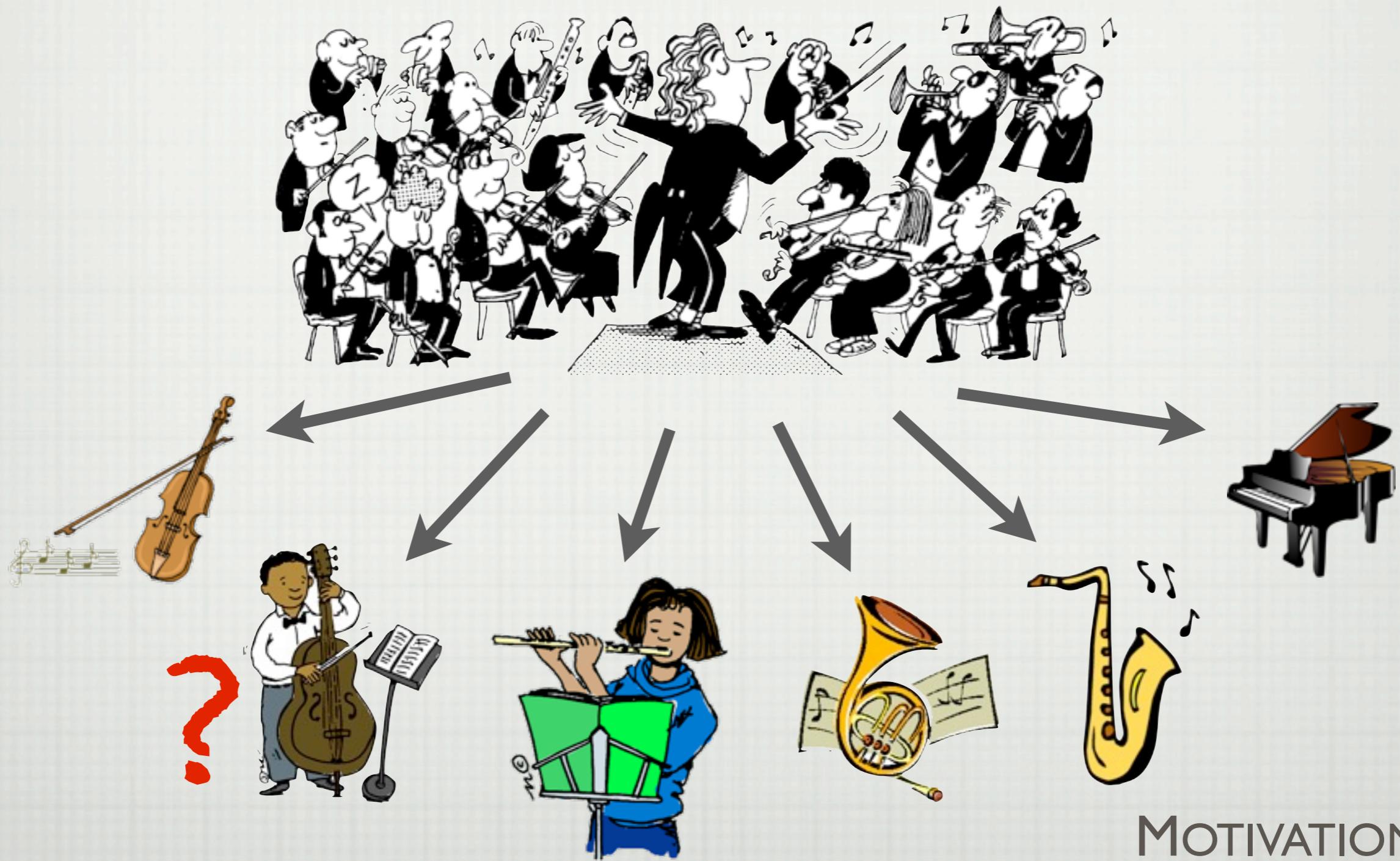
BY

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ADVISOR: PROF. JARVIS HAUPT



THE LAST TIME I WAS AT THE MINNESOTA ORCHESTRA..



How Do I IDENTIFY WHAT CELLO SOUNDS LIKE?



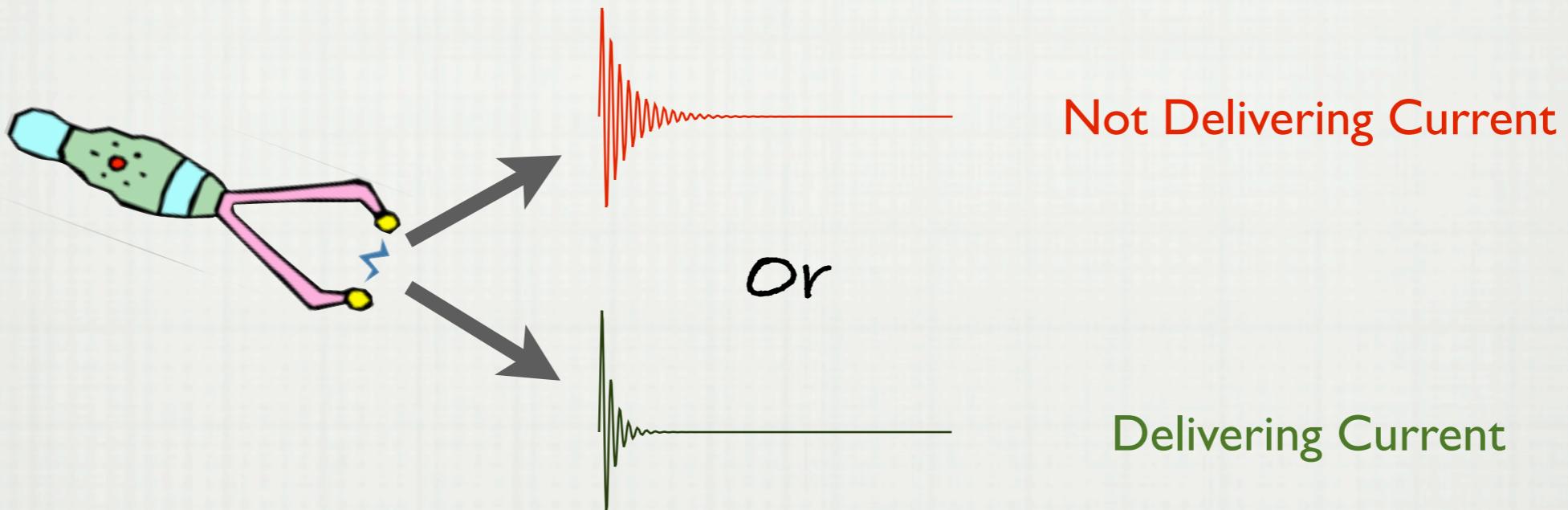
MOTIVATION

THE COCKTAIL PARTY PROBLEM : BLIND SOURCE SEPARATION



- Multiple speakers are simultaneously speaking
- The aim is to separately comprehend each speaker.
- None of the sources are known a-priori - ***Blind Source Separation Problem***

CONSIDER AN AUDIO FORENSICS APPLICATION



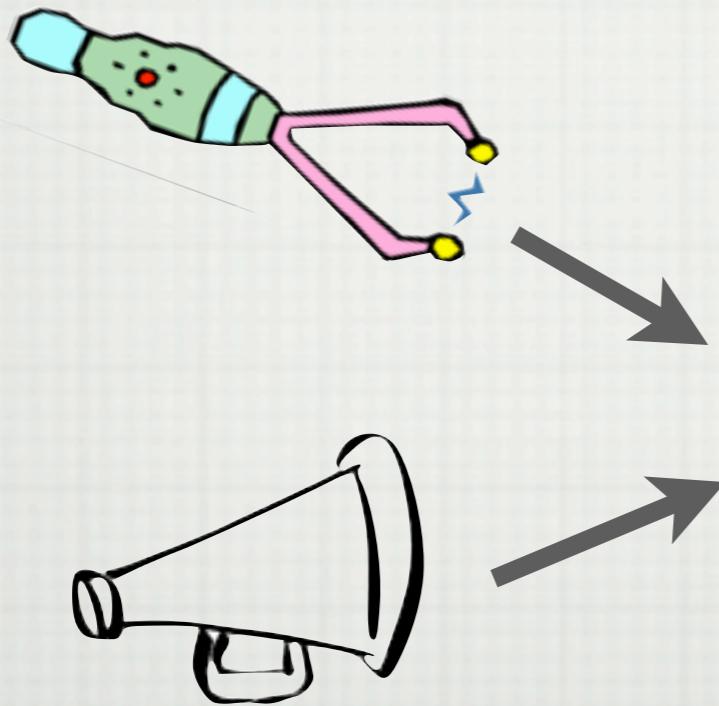
- Electro-shock Law enforcement devices generate characteristic **Nominally Periodic** signals, indicating discharge of current.
- These signals are often corrupted by background noise like speech, etc., not known *a-priori*.

MOTIVATION

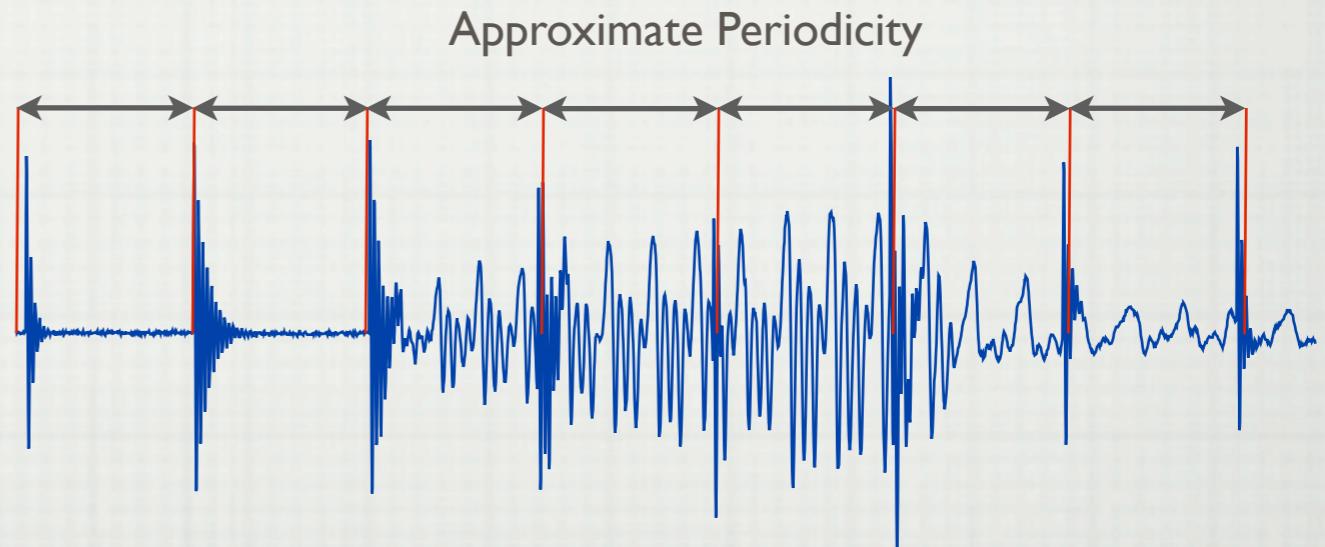
AUDIO FORENSICS APPLICATION: SINGLE CHANNEL SOURCE SEPARATION

- It is of interest to detect if the device is delivering current or not from a single mixture of the sources, referred to as **Single-Channel Source Separation**
- On the whole, **A Single Channel Semi-Blind Source Separation problem.**

Nominally Periodic signal $x_p \in \mathbb{R}^n$



Background Noise $x_u \in \mathbb{R}^n$



Single Linear Mixture
 $x \in \mathbb{R}^n$

MOTIVATION

OUTLINE : BIRD'S EYE VIEW OF THE PRESENTATION

- Background: Setting the stage
- Semi-Blind Morphological Component Analysis (SBMCA)
- Evaluation of SBMCA : Simulation Specifics
- Conclusions and Future Work

BACKGROUND

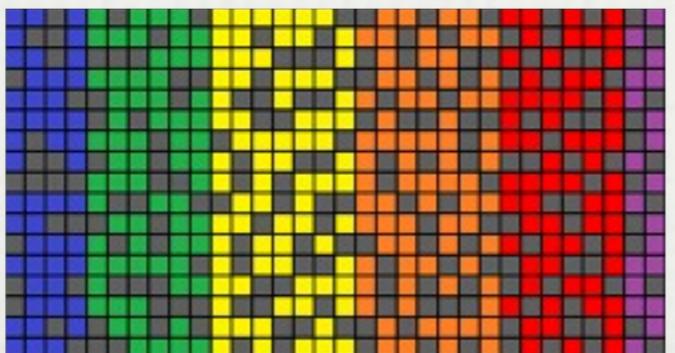
MODEL

- We suppose that, m is an integer which divides n into q equal parts
 - x is represented by matrix $X \in \mathbb{R}^{m \times q}$, and
- The aim is to separate X into its constituent matrices X_p and X_u

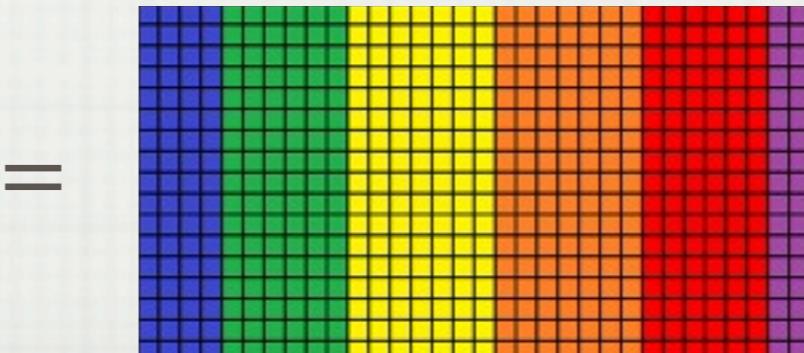
$$X = X_p + X_u$$

TRUNCATED-SINGULAR VALUE DECOMPOSITION(SVD)

- Let X_p be a rank- r matrix and X_u be random Gaussian noise.
- Estimating X_p is equivalent to finding a rank- r approximation of X



Noisy Data



Low-Rank
Approximation

BACKGROUND

ROBUST PCA^[1,2]

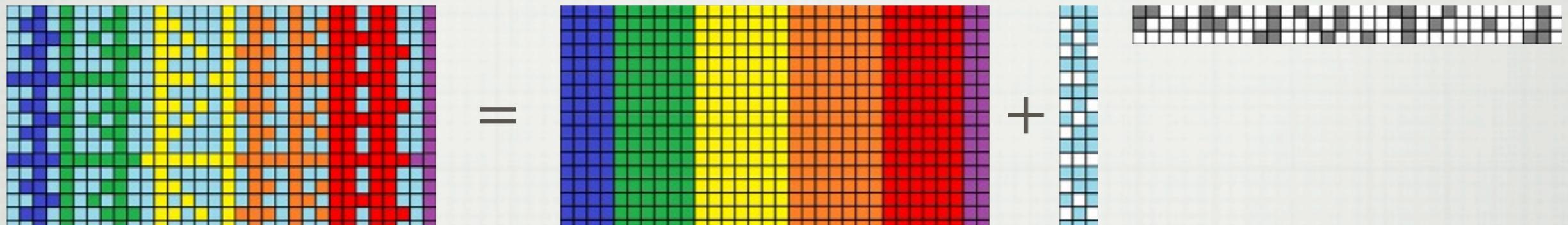
- Let X_u be comprised of impulsive noise, in such a case we adopt Robust PCA, leading to following decomposition :

$$\text{Data} = \text{Low-Rank} + \text{Sparse}$$

BACKGROUND

LOW-RANK PLUS SPARSE IN A KNOWN DICTIONARY^[3]

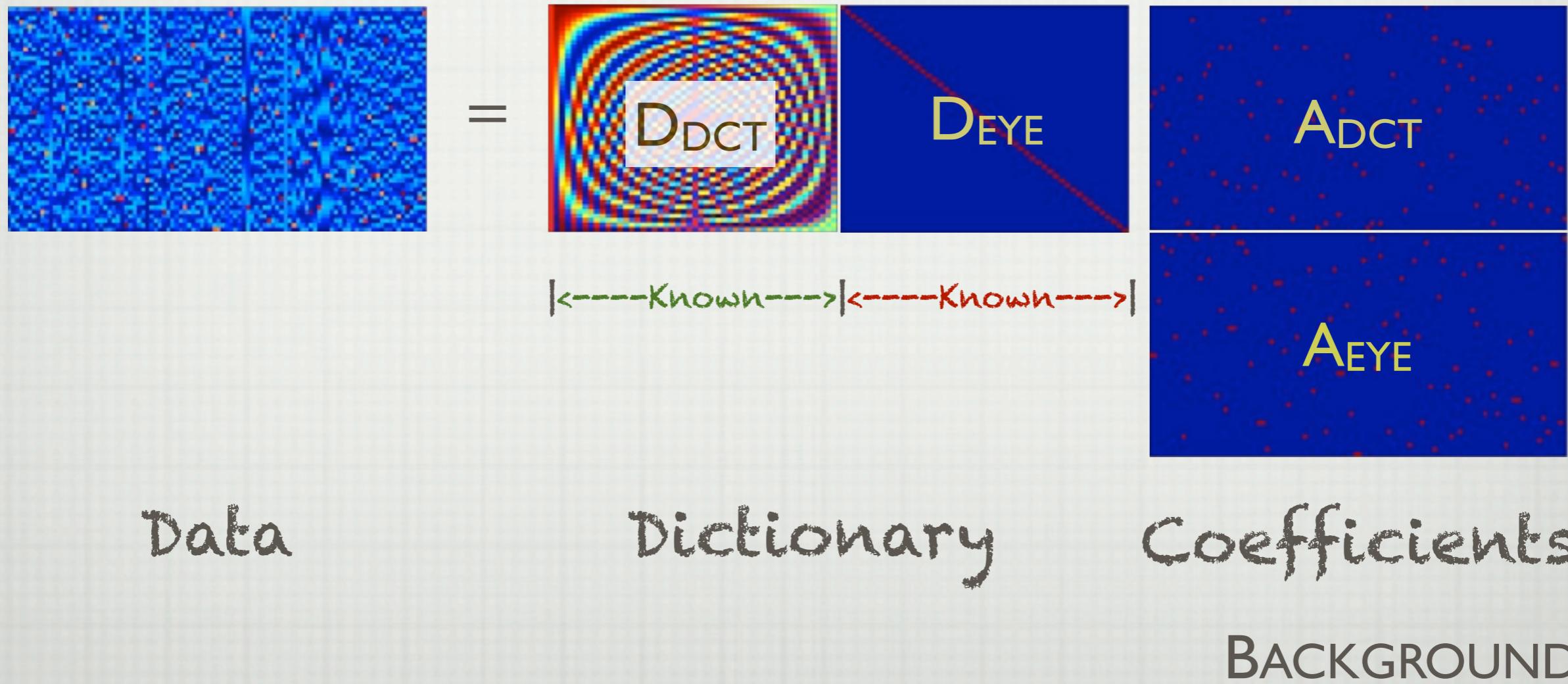
- In case X_u is sparse in some known dictionary,

$$\text{Data} = \text{Low-Rank} + \text{Dictionary Sparse}$$


BACKGROUND

MORPHOLOGICAL COMPONENT ANALYSIS^[4,5,6]

- Another extension: X_p and X_u are both sparse in some known dictionaries, represented as :



Data

Dictionary

Coefficients

BACKGROUND

REVISITING THE CELLIST: So, How Do I IDENTIFY WHAT CELLO Sounds LIKE?



- I can listen to a sample of Cello before the next act.
 - I **Train** my ears to Cello.
 - Training data required.
 - I know how other instruments sound.
 - I **Learn** the features of Cello by employing my prior **Experience** with other instruments.
 - An **Online** methodology.
- Or**

REVISITING THE CELLIST: How Do I IDENTIFY WHAT CELLO SOUNDS LIKE?



Motivation for our approach



I can listen to a sample of Cello before the next act.

Or

I **Train** my ears to Cello.

Training data required.

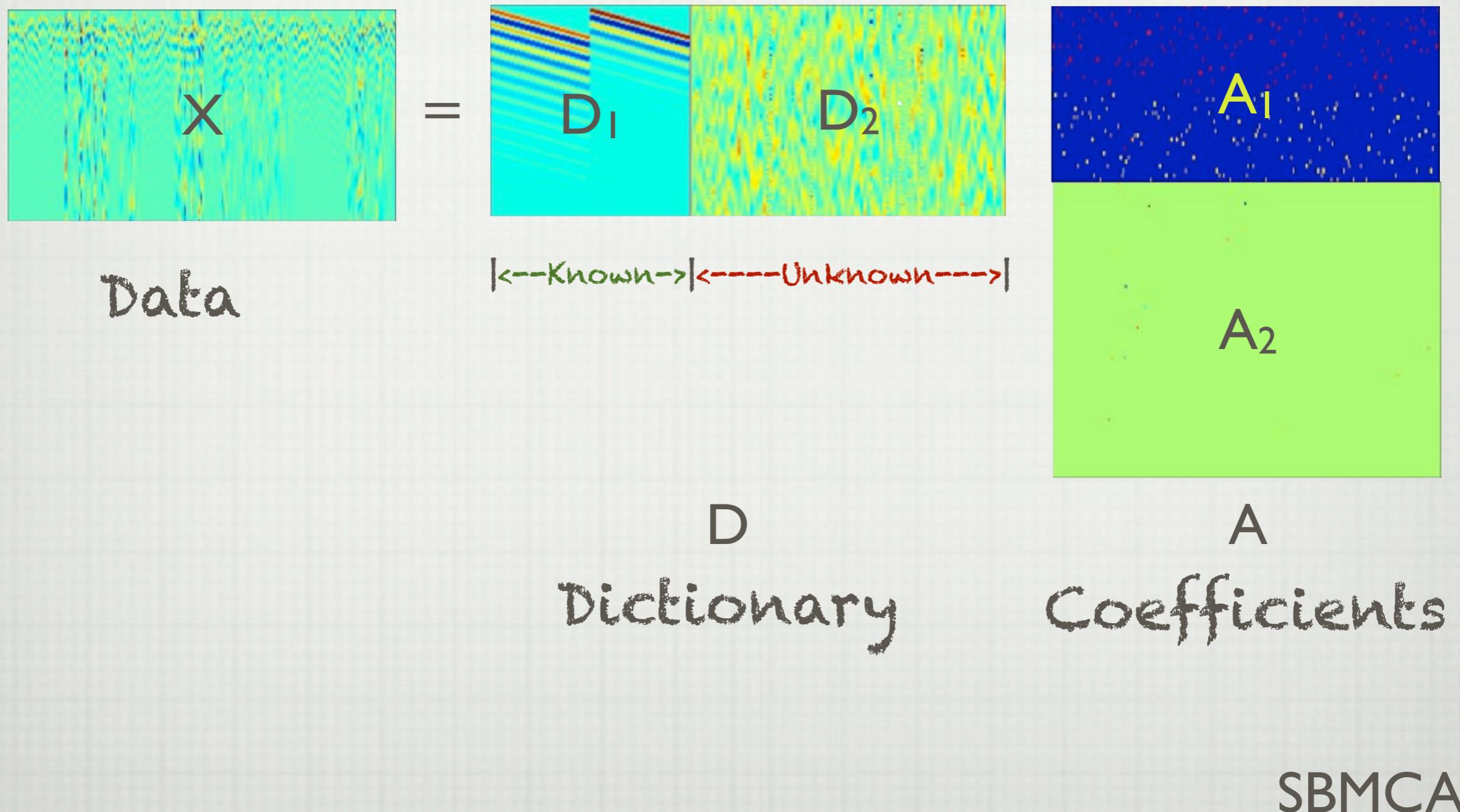
I know how other instruments sound.

I **Learn** the features of Cello by employing my prior **Experience** with other instruments.

An **Online** methodology.

SEMI-BLIND MORPHOLOGICAL COMPONENT ANALYSIS (SBMCA)

SEMI-BLIND MORPHOLOGICAL COMPONENT ANALYSIS^[7]



SEMI-BLIND MORPHOLOGICAL COMPONENT ANALYSIS: ALGORITHMIC CONSIDERATIONS

- Formally we set out to solve

$$\{\hat{A}_1, \hat{A}_2, \hat{D}_2\} = \arg \min_{A_1, A_2, D_2} \|X - D_1 A_1 - D_2 A_2\|_F^2 + \tilde{\lambda}_1 \|A_1\|_1 + \tilde{\lambda}_2 \|A_2\|_1$$

for $\tilde{\lambda}_1, \tilde{\lambda}_2 > 0$

- This optimization problem is

- Not jointly convex
 - Sensitive to initialization
- We adopt
 - Alternating Minimization based approach for Online Dictionary Learning^[8,9,10]

SBMCA

SEMI-BLIND MORPHOLOGICAL COMPONENT ANALYSIS ALGORITHMIC DETAILS

Algorithm 1: Semi-Blind MCA Algorithm

Input: Original Data $X \in \mathbb{R}^{m \times q}$, Known Dictionary $D_1 \in \mathbb{R}^{m \times d}$,

Regularization parameters $\lambda_1, \lambda_2, \lambda_3 > 0$,

Number of elements in unknown dictionary ℓ .

Initialize: $\tilde{A}_1 \leftarrow \arg \min_{A_1} \|X - D_1 A_1\|_F^2 + \lambda_1 \|A_1\|_1$

(or other suitable initialization depending on the problem.)

Iterate (repeat until convergence):

repeat

Dictionary Learning:

$$\{\tilde{D}_2, \tilde{A}_2\} \leftarrow \arg \min_{D_2, A_2} \|X - D_1 \tilde{A}_1 - D_2 A_2\|_F^2 + \lambda_2 \|A_2\|_1$$

Coefficient Update:

$$\tilde{D} = [D_1 \ \tilde{D}_2]$$

$$[\tilde{A}_1^T \ \tilde{A}_2^T]^T \triangleq \tilde{A} \leftarrow \arg \min_A \|X - \tilde{D} A\|_F^2 + \lambda_3 \|A\|_1$$

until convergence

Output: Learned dictionary $\hat{D}_2 \leftarrow \tilde{D}_2$,

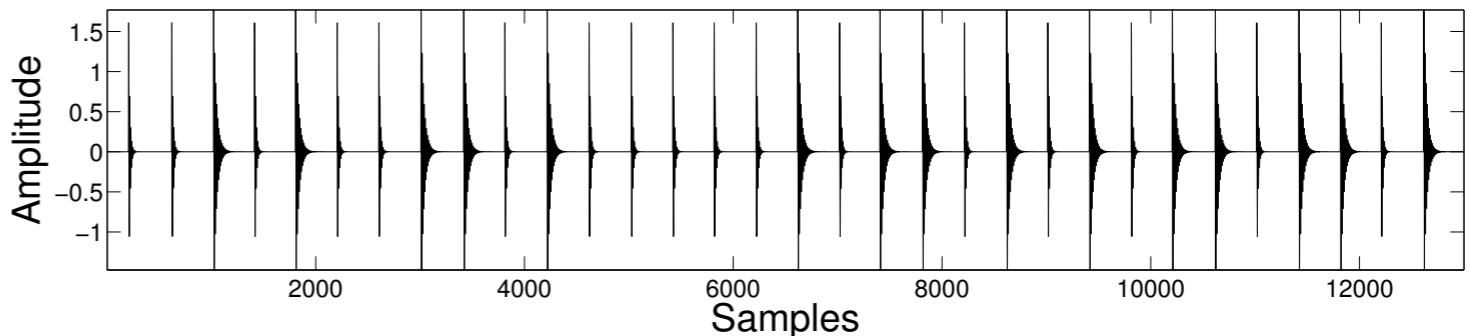
Coefficient estimates $\hat{A}_1 = \tilde{A}_1$, $\hat{A}_2 = \tilde{A}_2$.

SBMCA

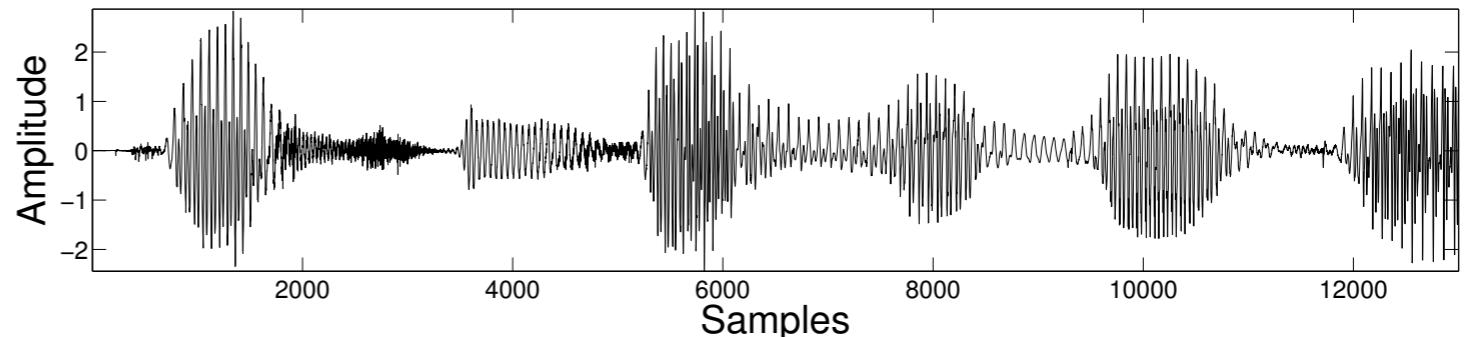
EVALUATION OF PERFORMANCE

SIGNAL CONFIGURATION

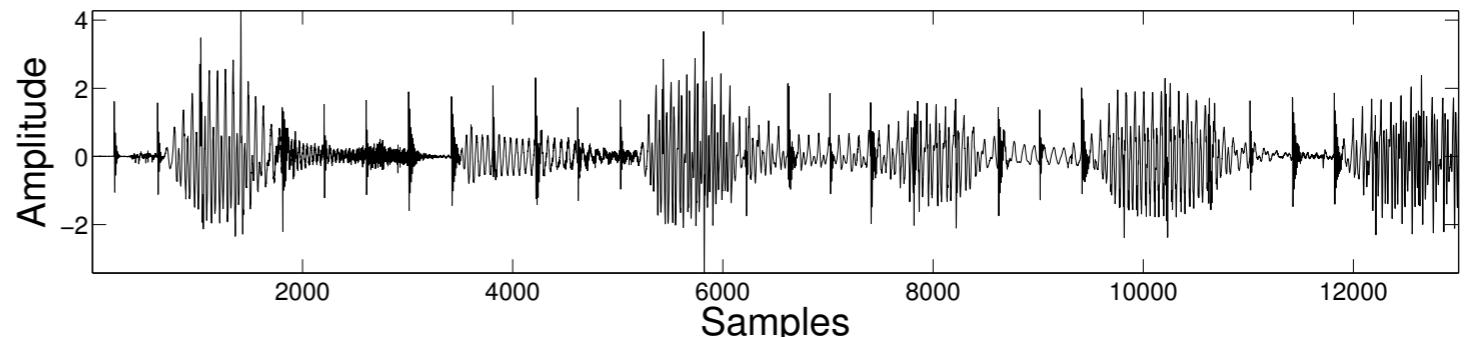
Nominally Periodic Signal



Unknown Background Signal



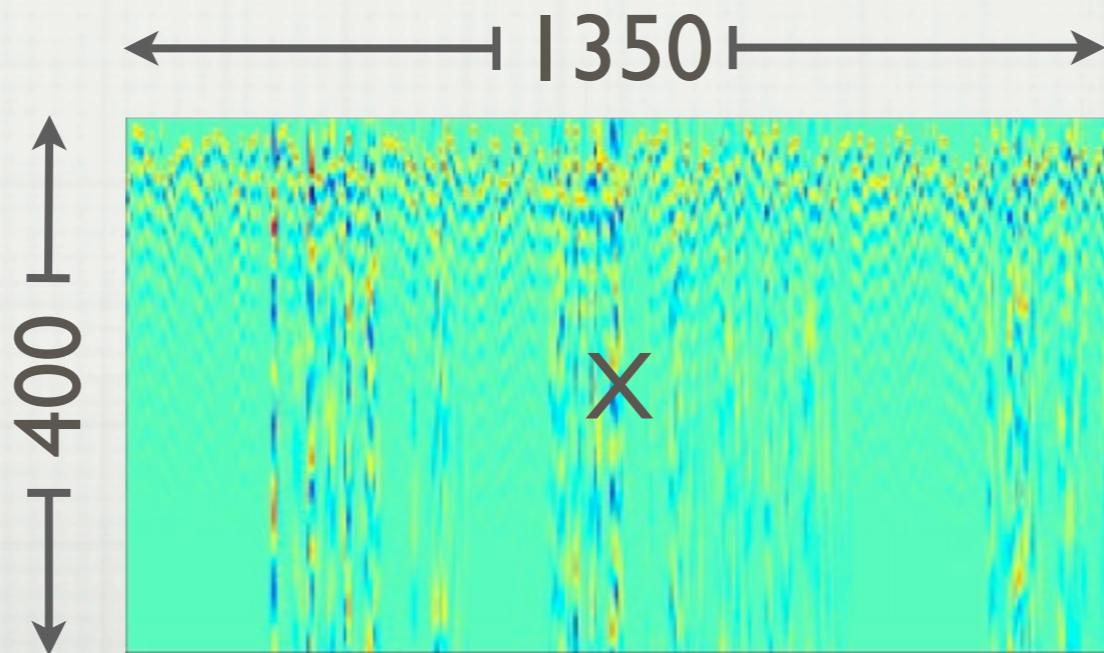
Linear Mixture



EVALUATION

DATA GENERATION

- Data formed from a mixture of Speech¹ (unknown) and nominally periodic signal (one per period)
- Data matrix looks like,



¹ Speech Samples obtained from VoxForge Speech Corpus: www.voxforge.org/home

EVALUATION

FREQUENCY DOMAIN SOURCE SEPARATION

Method	D_1	D_2
SBMCA		 Unknown
MCA-DCT-Fourier		 $ \mathcal{F}\{DCT\} $
MCA-Identity-Fourier		 $ \mathcal{F}\{Identity\} $

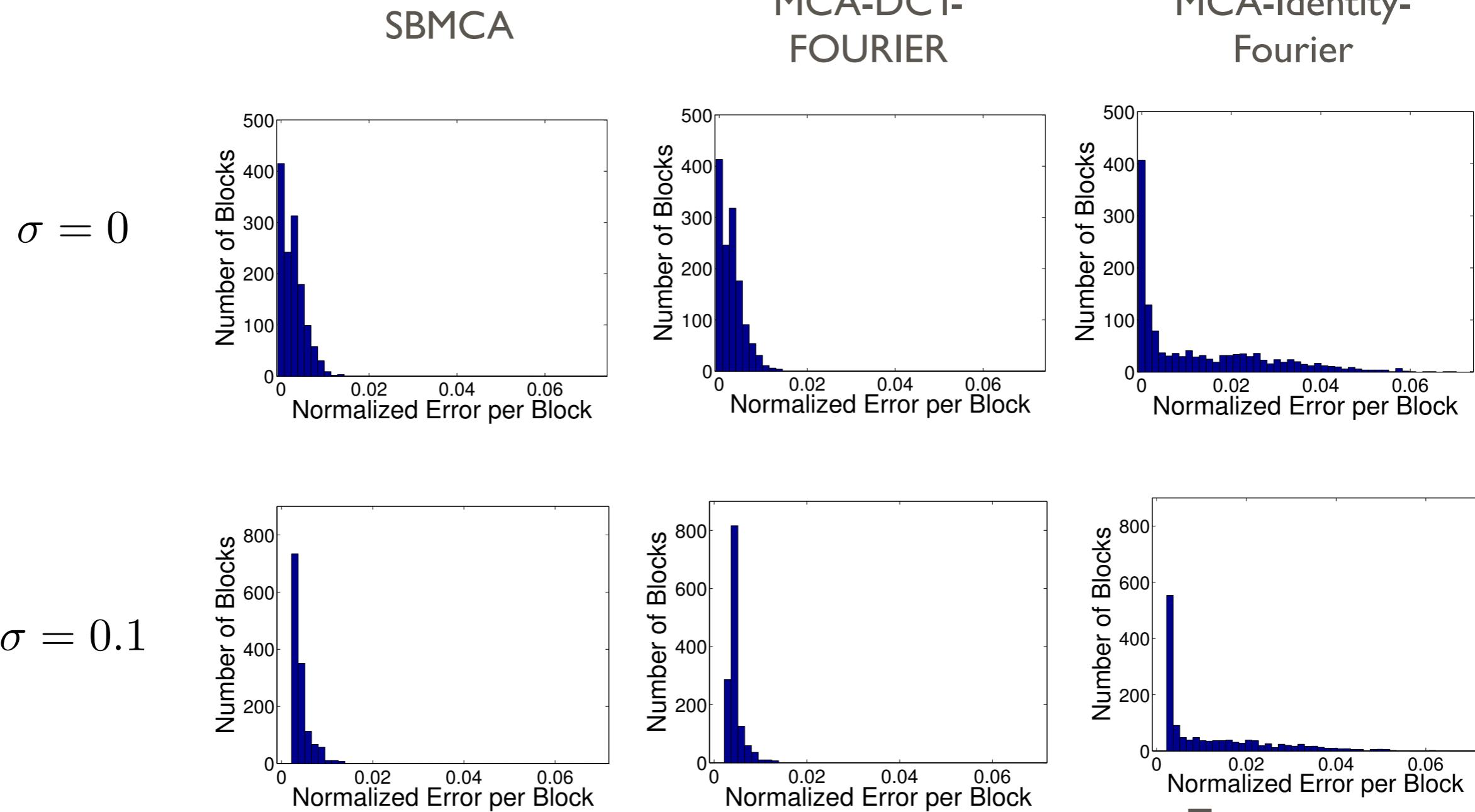
SOURCE SEPARATION IN FREQUENCY DOMAIN

Table 1: Analysis of reconstruction SNR(in dB): Frequency Domain Separation

Noise $\mathcal{N}(0, \sigma^2)$	$\sigma = 0$		$\sigma = 0.001$		$\sigma = 0.01$		$\sigma = 0.1$	
Method \ Signal	x_p	x_u	x_p	x_u	x_p	x_u	x_p	x_u
SBMCA	8.95	15.21	8.91	15.17	8.83	15.09	6.80	11.56
MCA-DCT-Fourier	8.81	15.16	8.81	15.16	8.88	15.19	6.82	12.50
MCA-Identity-Fourier	1.19	-19.07	1.19	-19.07	1.19	-18.90	1.34	-9.57

EVALUATION

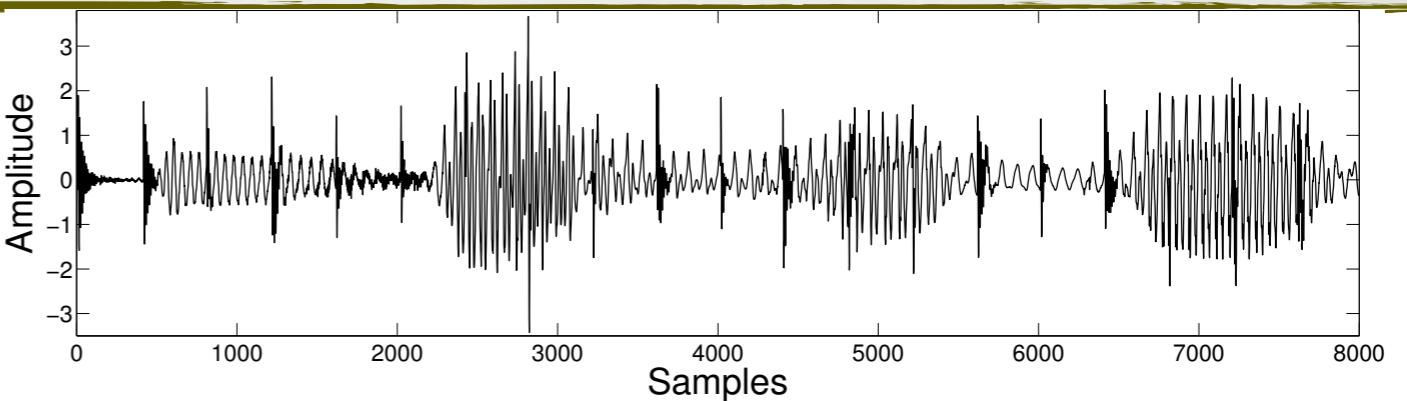
SOURCE SEPARATION IN FREQUENCY DOMAIN: NOMINALLY PERIODIC SIGNAL



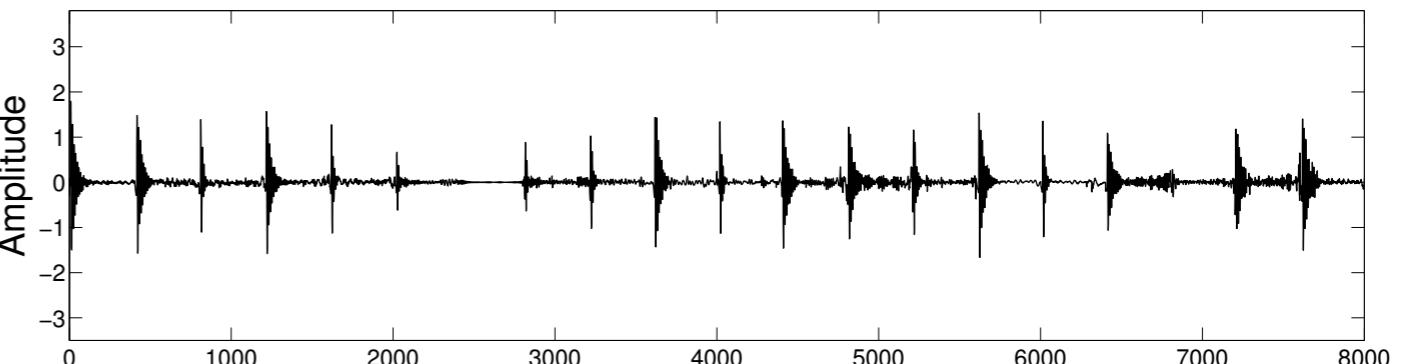
SOURCE SEPARATION IN FREQUENCY DOMAIN: NOMINALLY PERIODIC SIGNAL

$$\sigma = 0$$

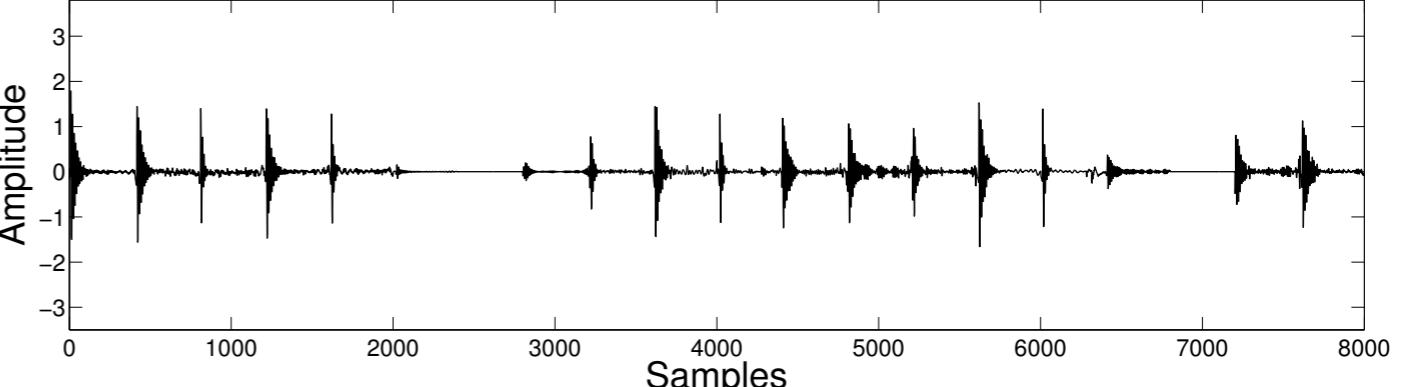
Original Mixture



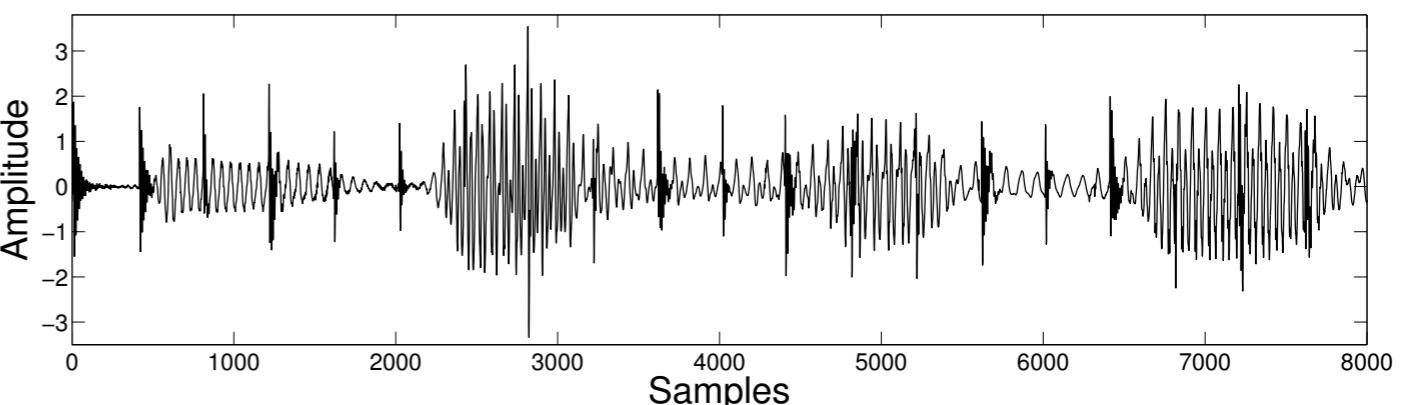
SBMCA



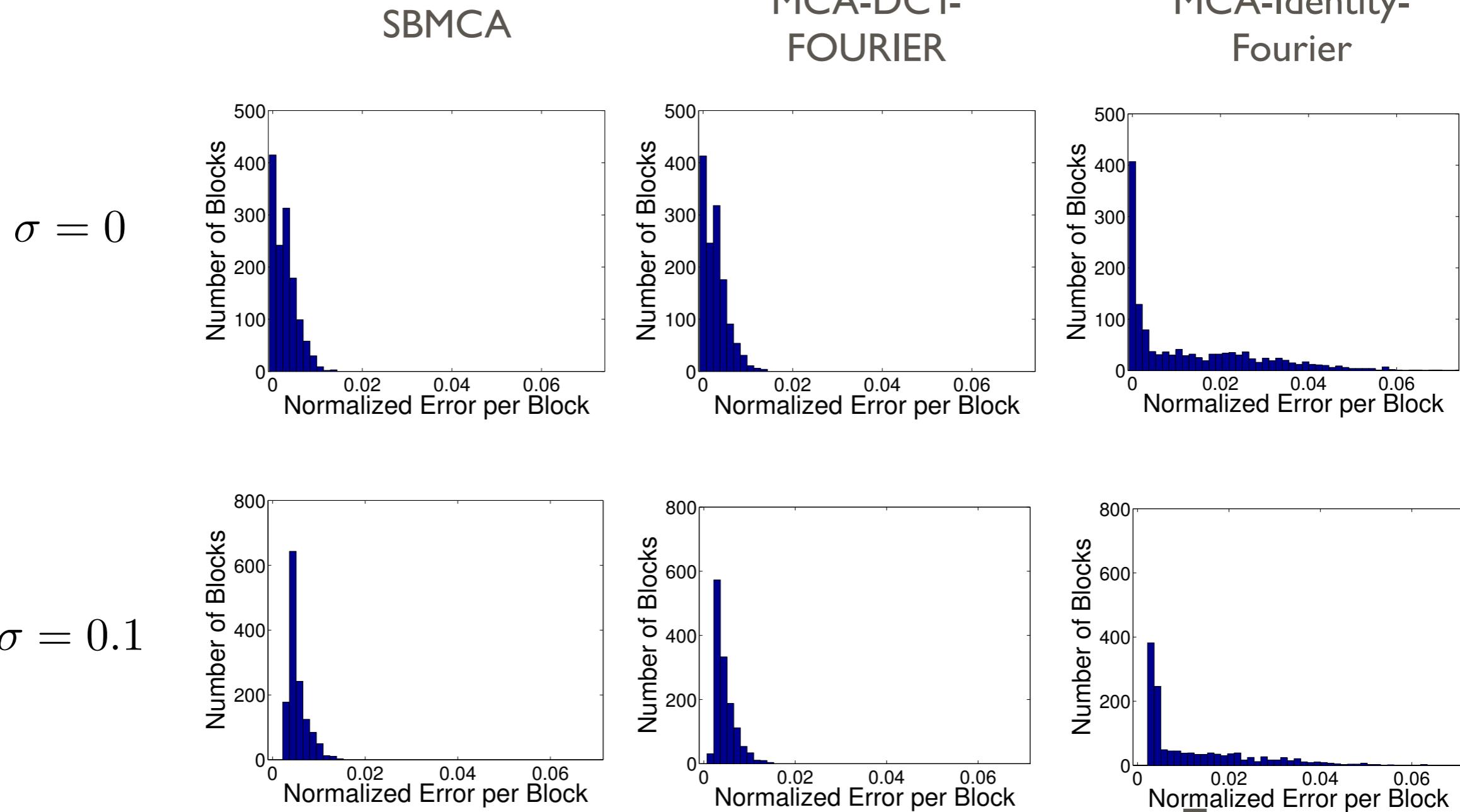
MCA-DCT-Fourier



MCA-Identity-Fourier



SOURCE SEPARATION IN FREQUENCY DOMAIN: BACKGROUND SIGNAL

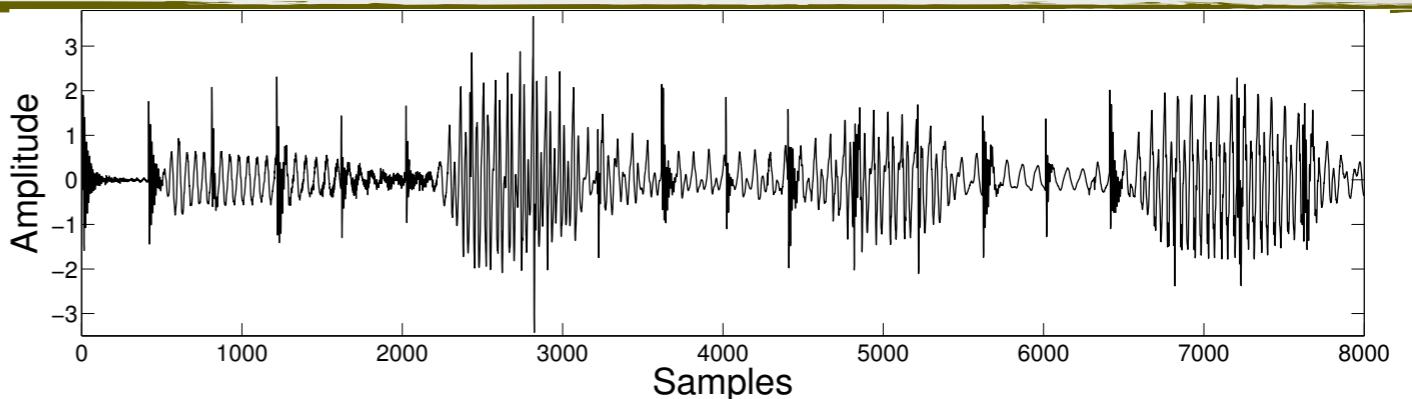


EVALUATION

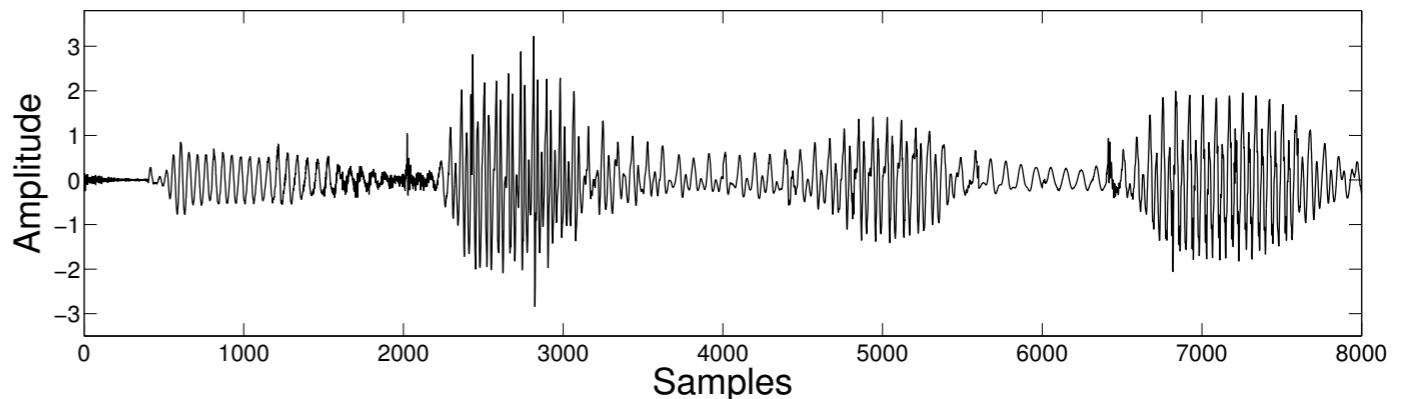
SOURCE SEPARATION IN FREQUENCY DOMAIN: BACKGROUND SIGNAL

$$\sigma = 0$$

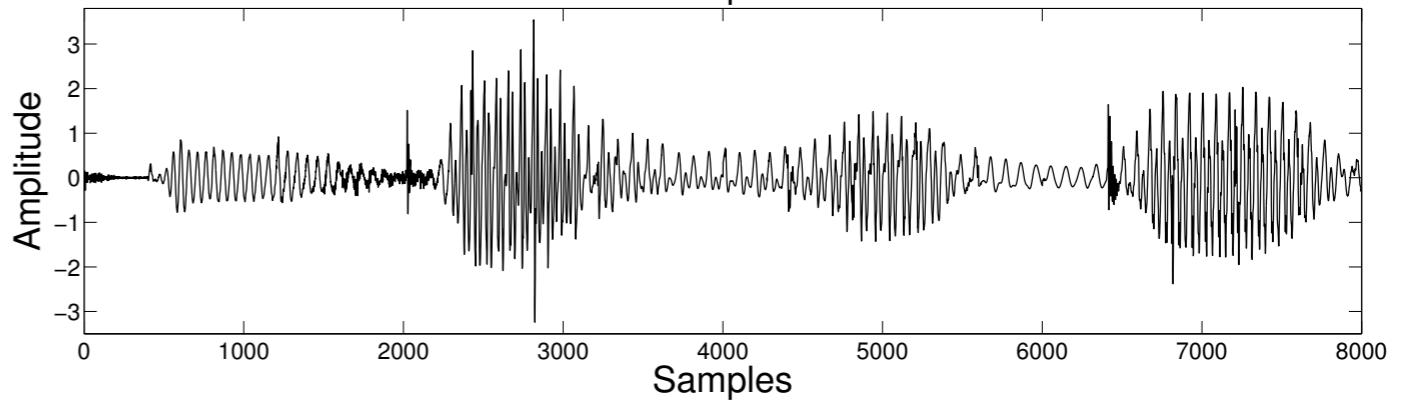
Original Mixture



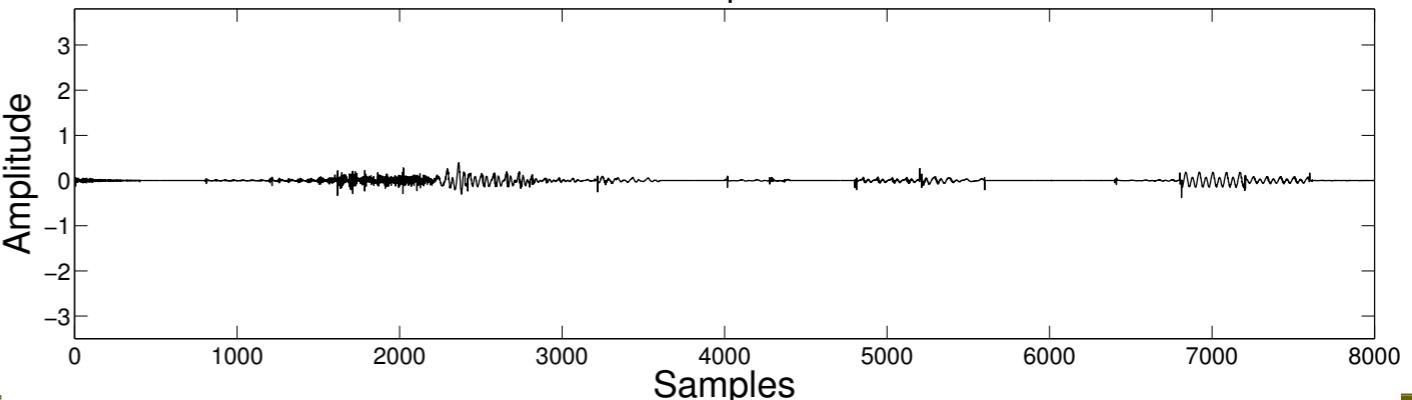
SBMCA



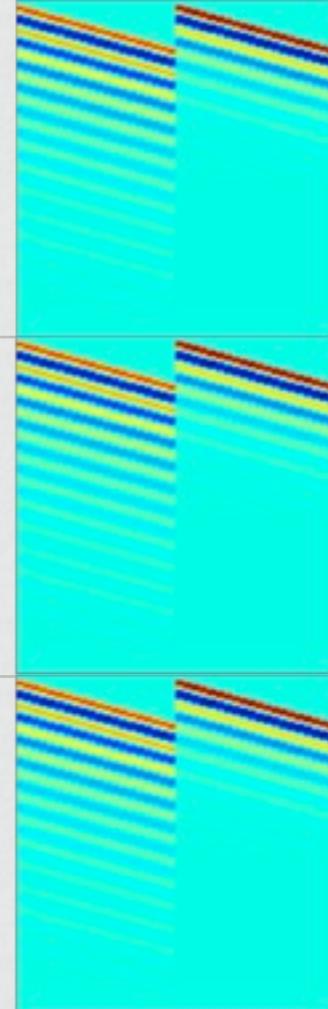
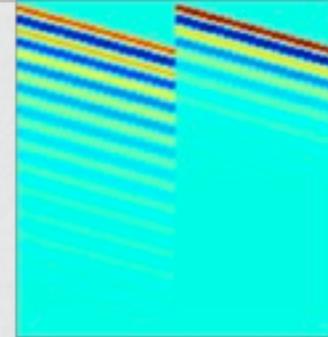
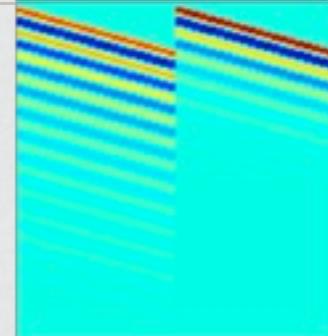
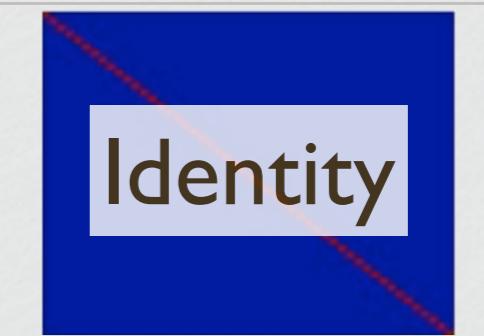
MCA-DCT-Fourier



MCA-Identity-Fourier



TIME DOMAIN SOURCE SEPARATION

Method	D_1	D_2
SBMCA		
MCA-DCT		
MCA-Identity		

SOURCE SEPARATION IN TIME DOMAIN

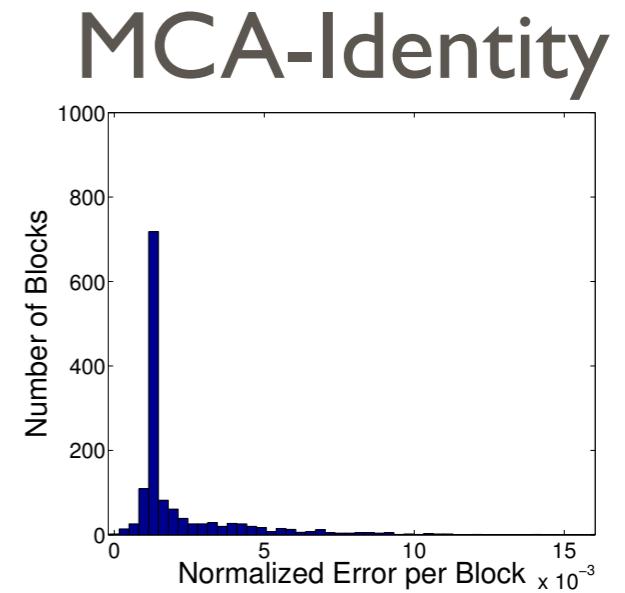
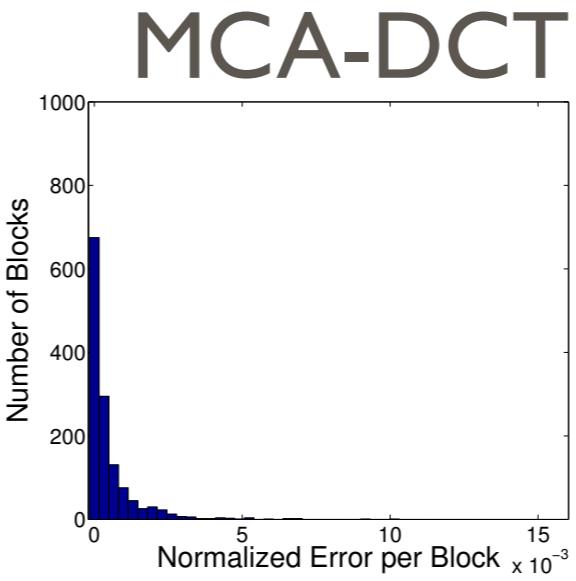
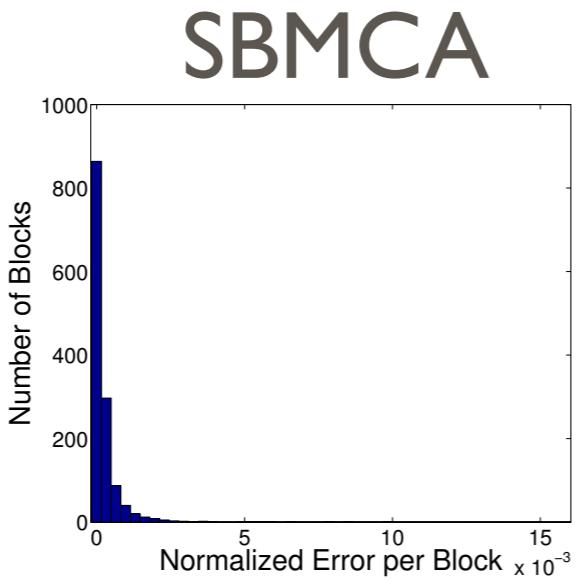
Table 2: Analysis of reconstruction SNR(in dB): Time Domain Separation

Noise $\mathcal{N}(0, \sigma^2)$	$\sigma = 0$		$\sigma = 0.001$		$\sigma = 0.01$		$\sigma = 0.1$	
Method \ Signal	x_p	x_u	x_p	x_u	x_p	x_u	x_p	x_u
SBMCA	23.72	29.32	23.73	29.32	23.08	27.40	19.72	16.84
MCA-DCT	20.44	26.02	20.46	26.02	20.19	24.96	18.09	16.72
MCA-Identity	10.90	16.06	10.90	16.44	10.90	16.33	10.78	11.44

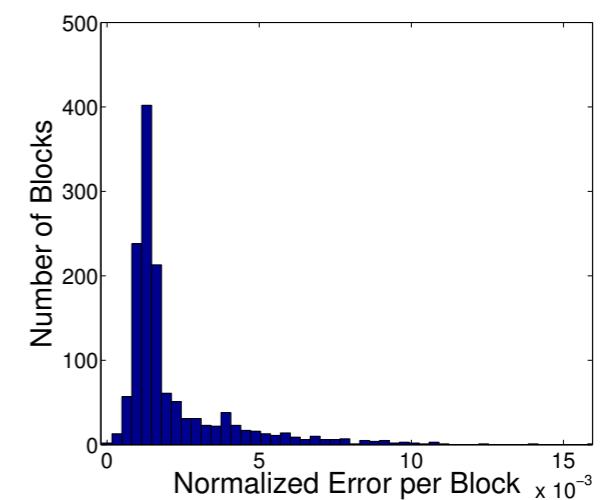
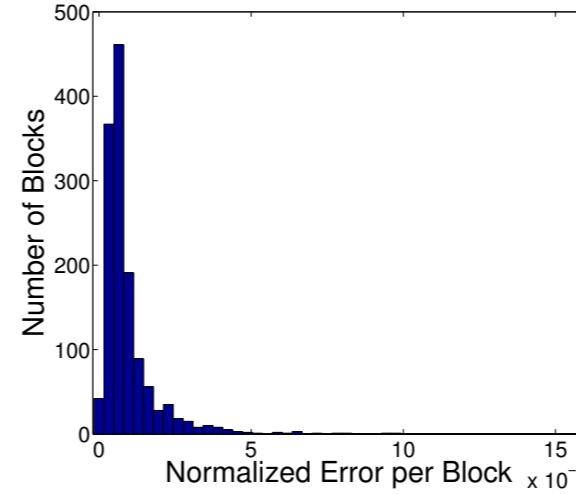
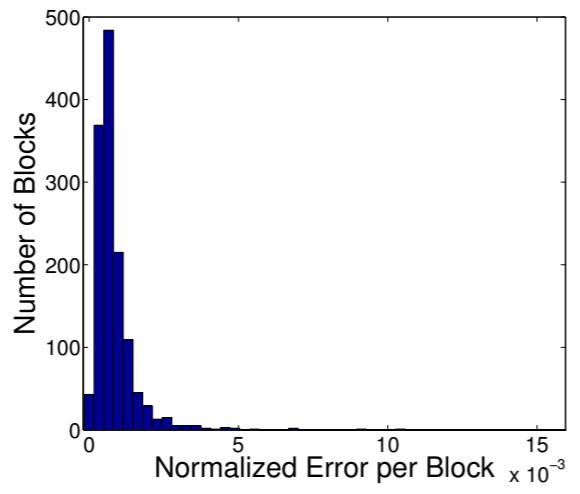
EVALUATION

SOURCE SEPARATION IN TIME DOMAIN: NOMINALLY PERIODIC SIGNAL

$\sigma = 0$



$\sigma = 0.1$

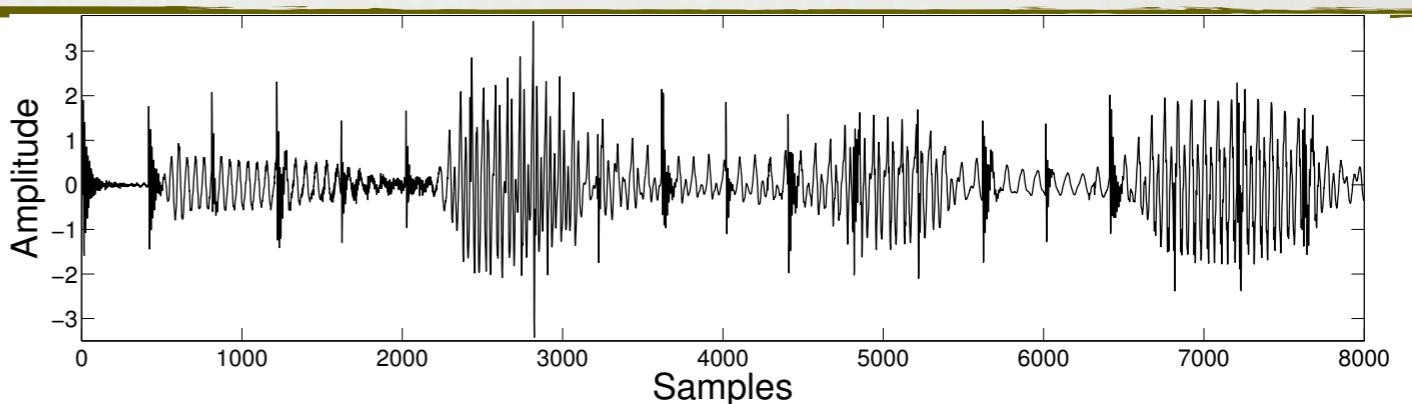


EVALUATION

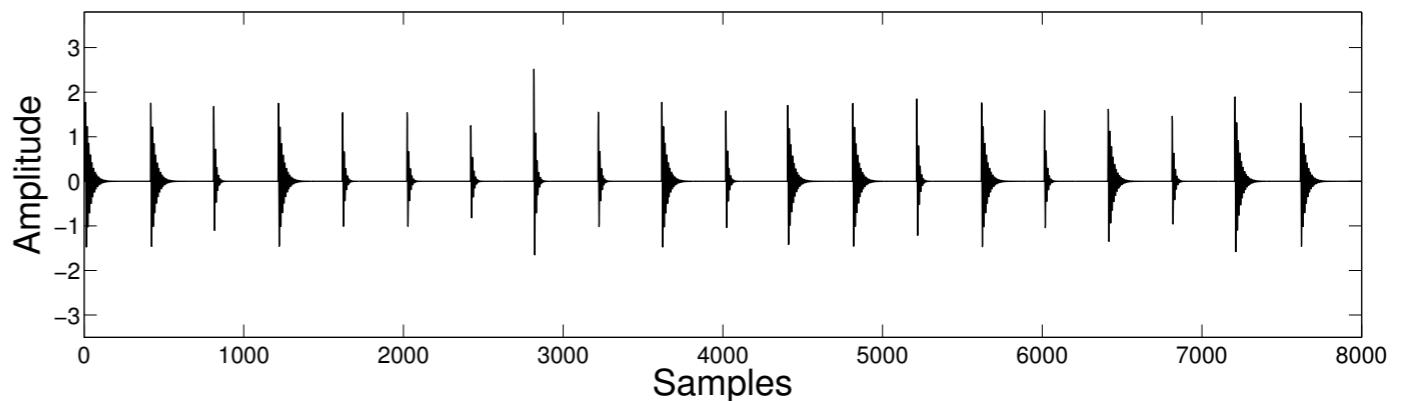
SOURCE SEPARATION IN TIME DOMAIN: NOMINALLY PERIODIC SIGNAL

$$\sigma = 0$$

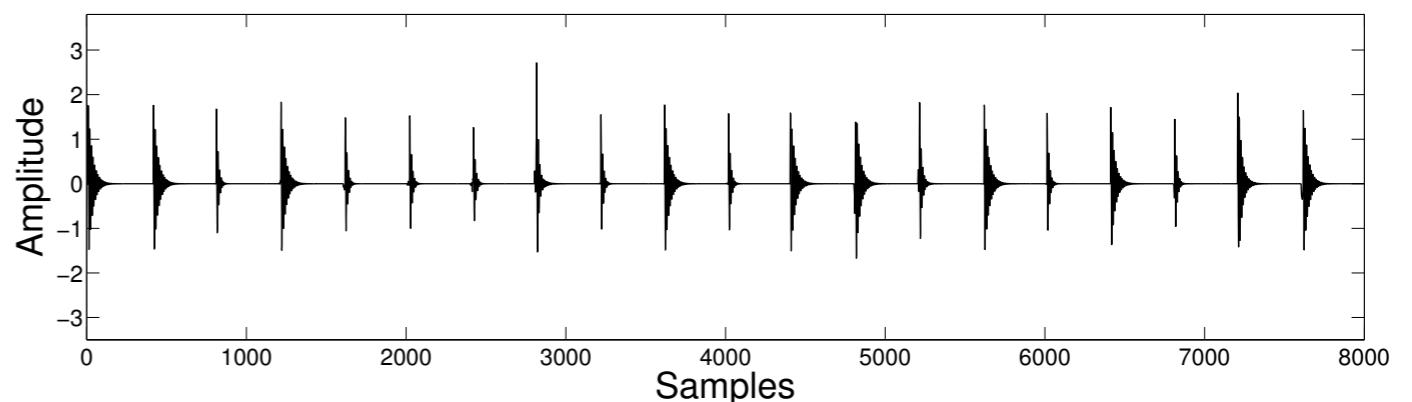
Original Mixture



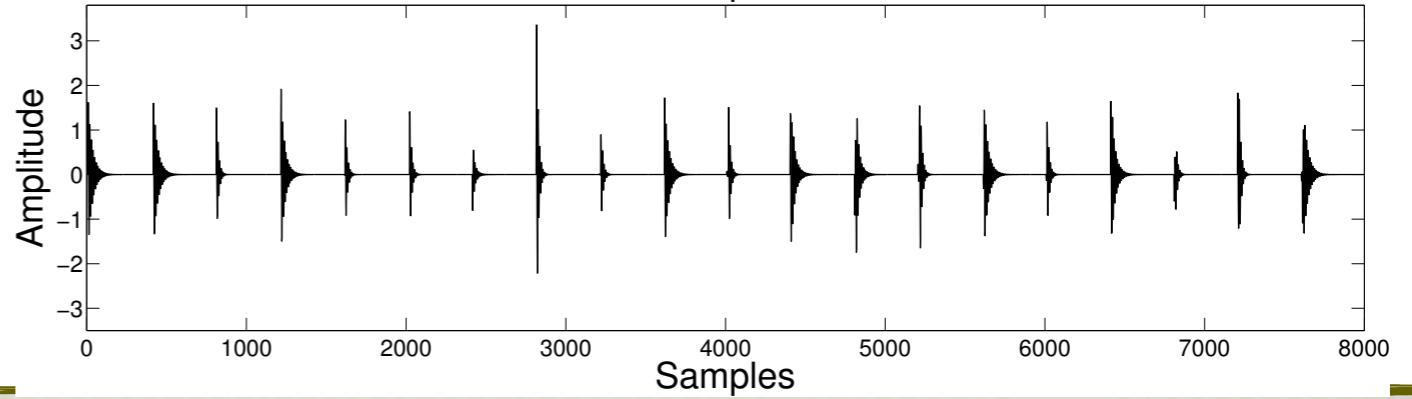
SBMCA



MCA-DCT

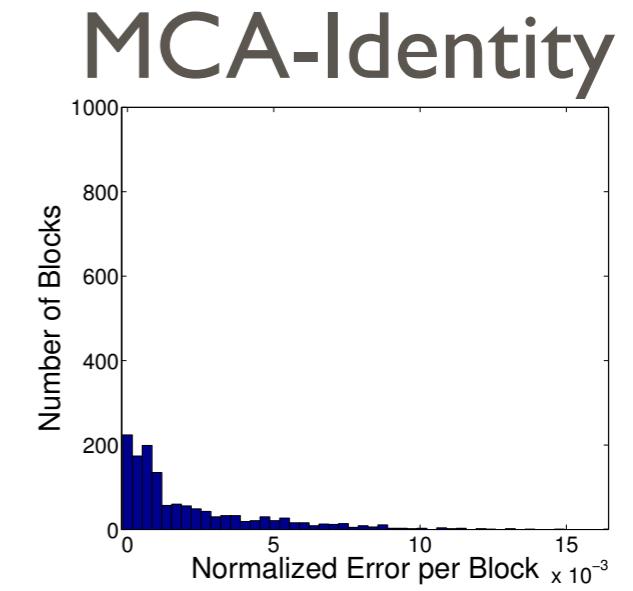
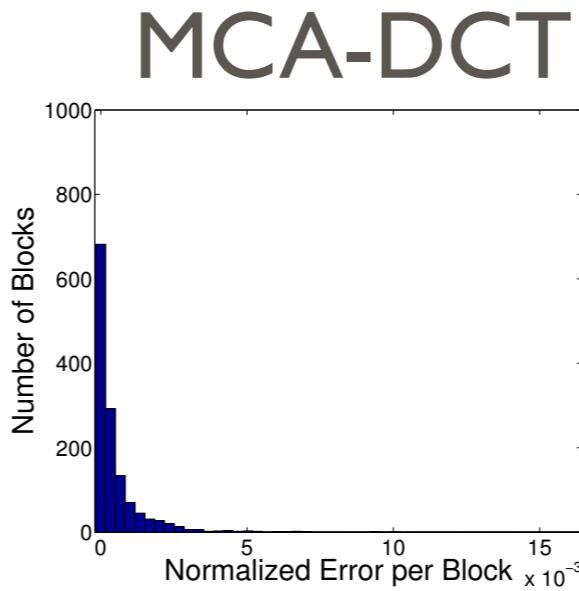
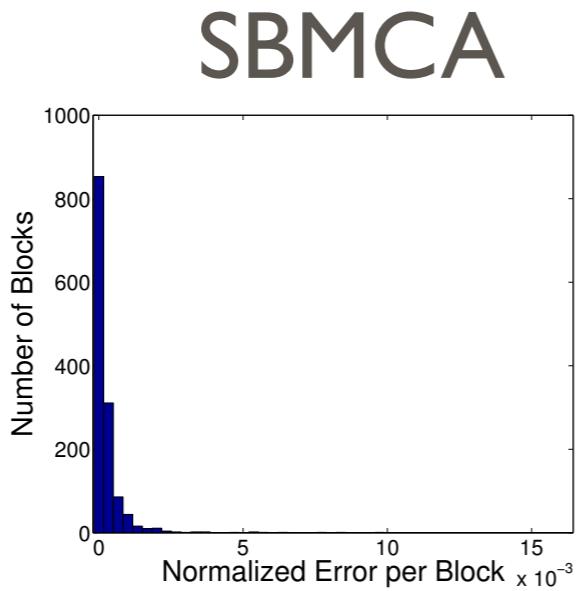


MCA-Identity

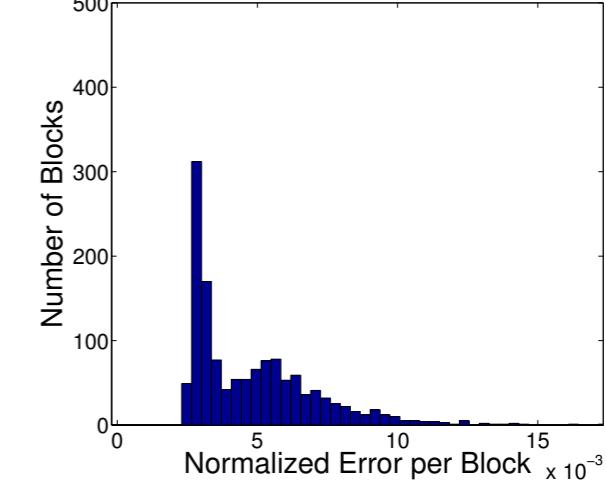
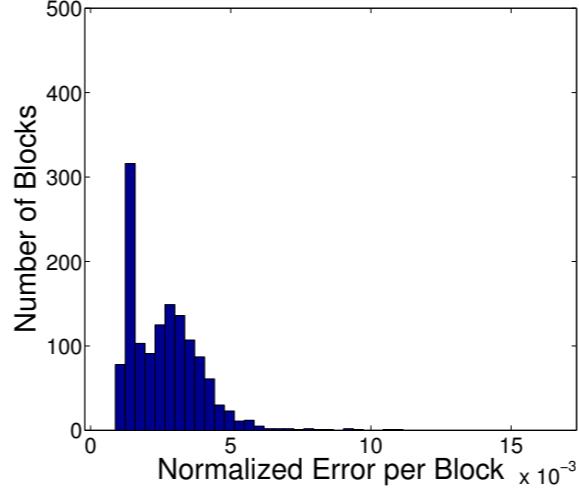
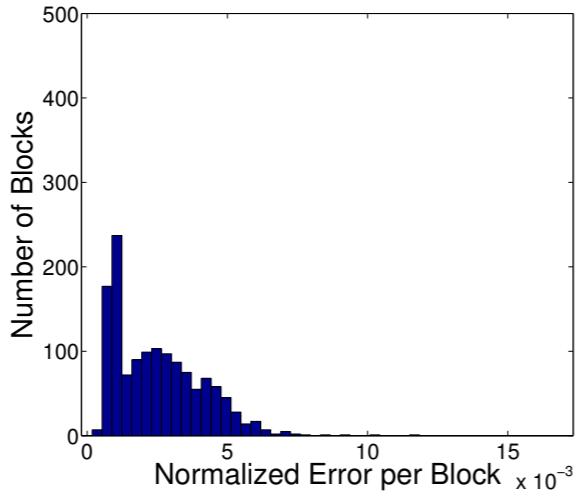


SOURCE SEPARATION IN TIME DOMAIN: BACKGROUND SIGNAL

$\sigma = 0$



$\sigma = 0.1$

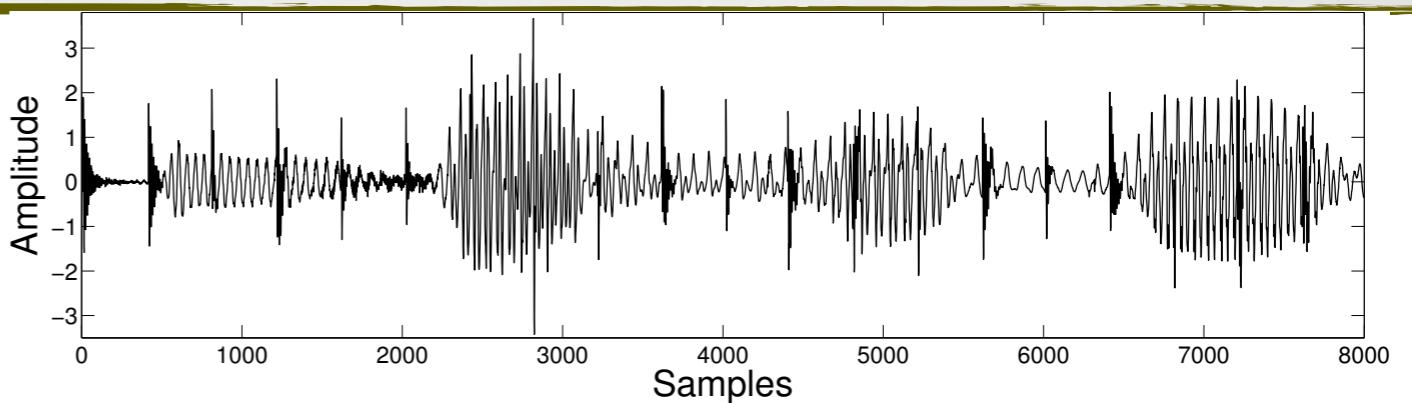


EVALUATION

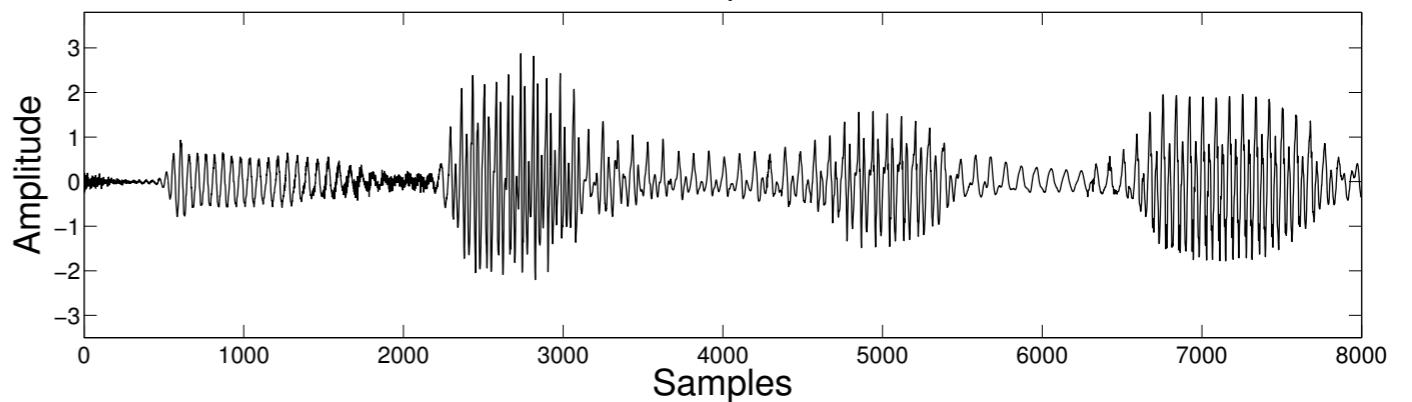
SOURCE SEPARATION IN TIME DOMAIN: BACKGROUND SIGNAL

$$\sigma = 0$$

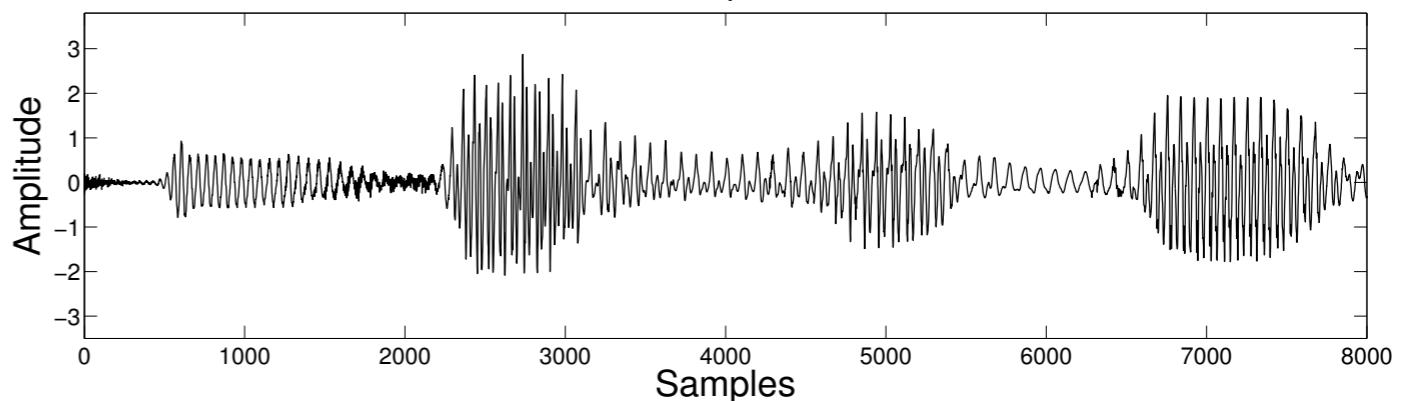
Original Mixture



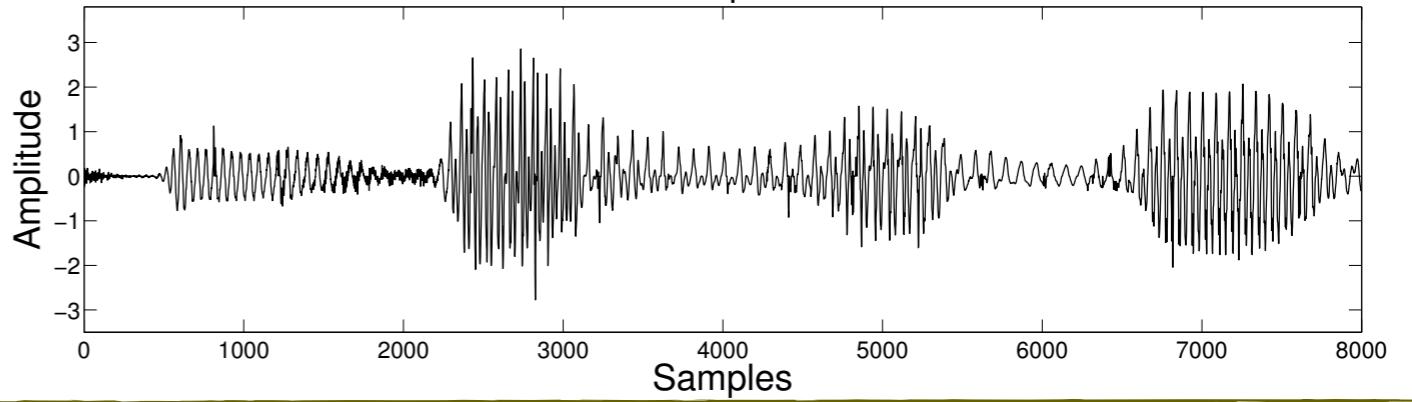
SBMCA



MCA-DCT



MCA-Identity



CONCLUSIONS

- Our approach exploits partial prior knowledge of one of the sources, in the form of a dictionary which sparsely represents local segments of one of the sources. A key feature being online learning of a dictionary (from the mixed source data itself) for representing the unknown background source.
- The timing uncertainty inherent in our application suggests that our approach may be combined with other existing alignment techniques [11, 12, 13].
- More recently [14] proposed a robust alignment procedure that can be viewed as an extension of robust PCA.
- We defer these extensions, as well as the investigation of our approach to other applications (e.g., in image or video processing) to future efforts.



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THANK YOU!

