

Machine Learning in Scientific Computing

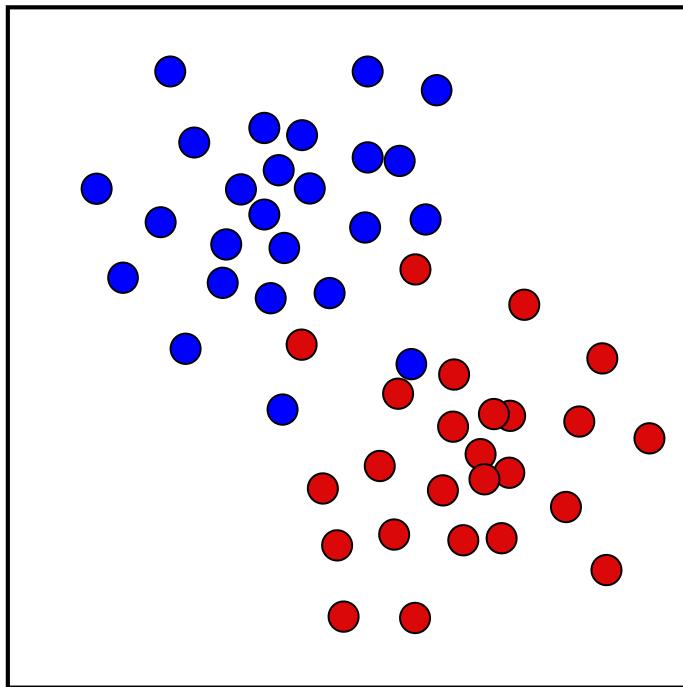
CECAM/CSM/IRTG SCHOOL 2018



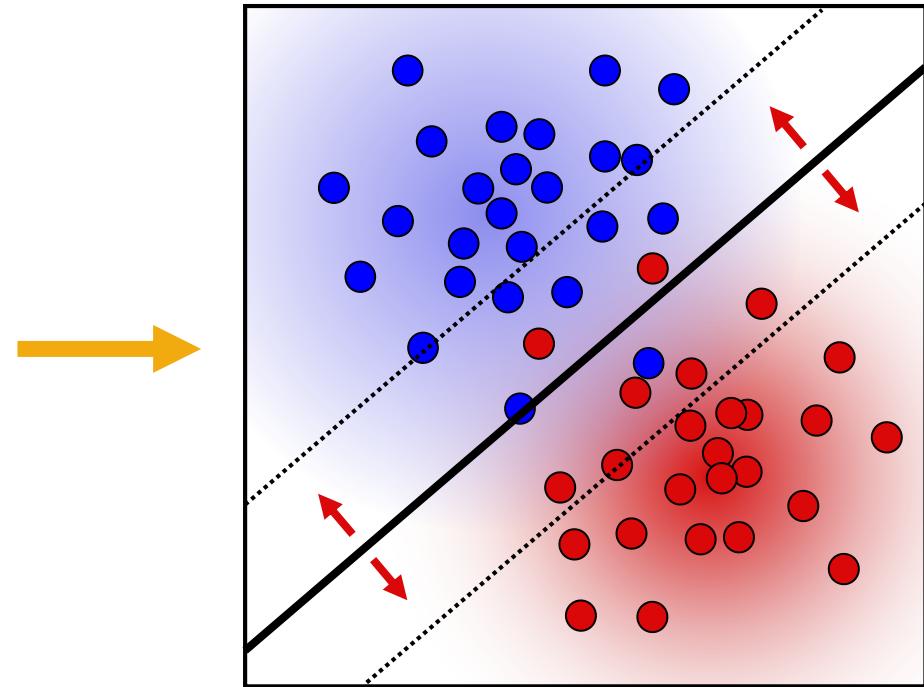
Lecture 3.2 Deep Learning

Neural Network Building Blocks

Support Vector Machines

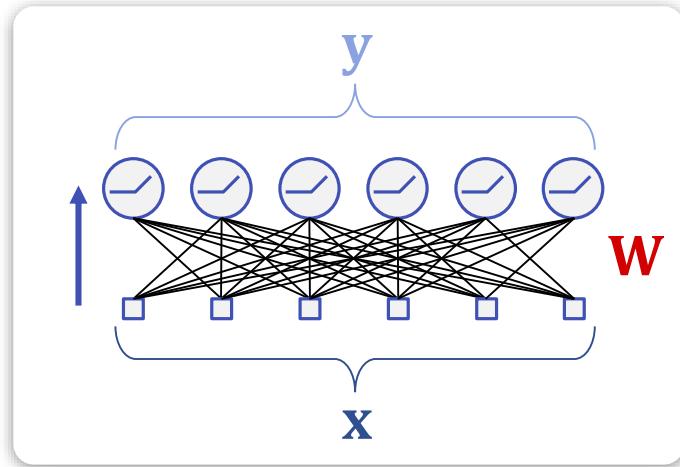


training set



separating hyperplane,
minimal penetration
of margin (L_1)

Architectural Building Blocks



Fully connected network layer

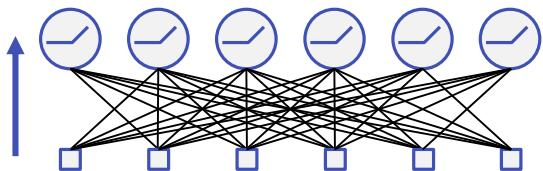
$$\textit{layer}: \mathbb{R}^n \rightarrow \mathbb{R}^m$$

$$\mathbf{y} = \textit{layer}(\mathbf{x}) = \textit{nonLinearity}(\mathbf{Wx})$$

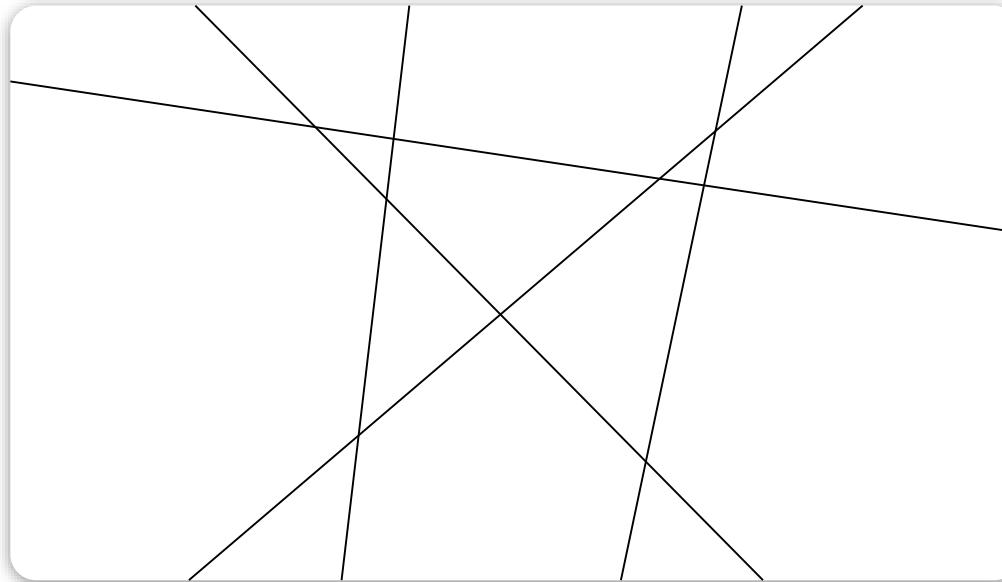
$$y_j = \textit{nonLinearity} \left(\sum_{i=1}^n w_{ij} x_i \right)$$

$$\textit{nonLinearity}(\mathbf{y}) = \begin{cases} \max(\mathbf{y}, 0) & \text{"relu"} \\ \tanh(\mathbf{y}) \\ \dots \end{cases}$$

Architectural Building Blocks

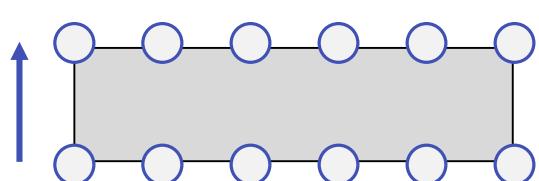


Fully connected network layer



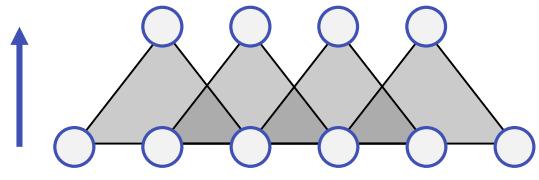
Interpretation: ReLu-Layer = Arrangement of Hyperplanes

Architectural Building Blocks



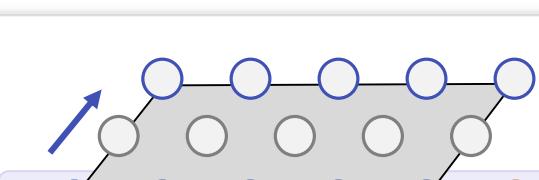
Fully connected network layer

global connection / global dependencies
e.g: feature classification



Convolutional neural network

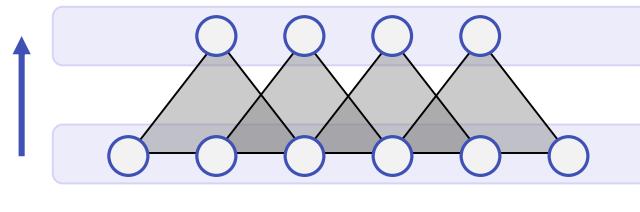
local connection / local correlations
e.g.: image/audio/text data



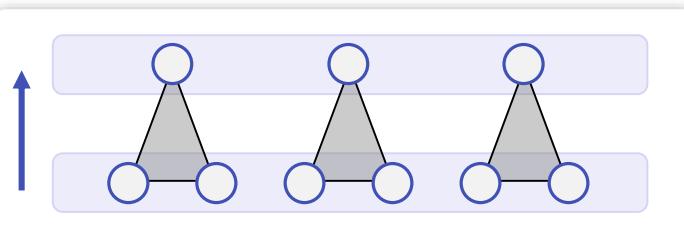
Recurrent neural networks

Markov-chain models with memory

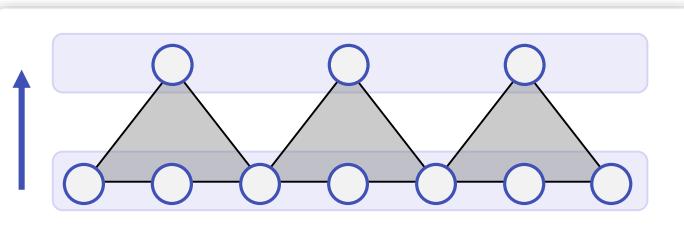
Convolutional Building Blocks



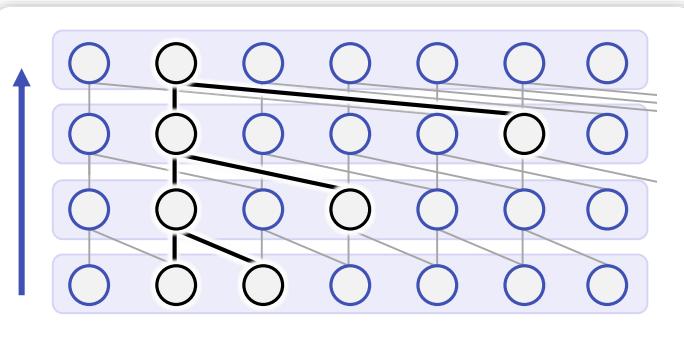
Convolutional neural network
local connection / local correlations



Pooling layer
reduce resolution (half, third, ...)

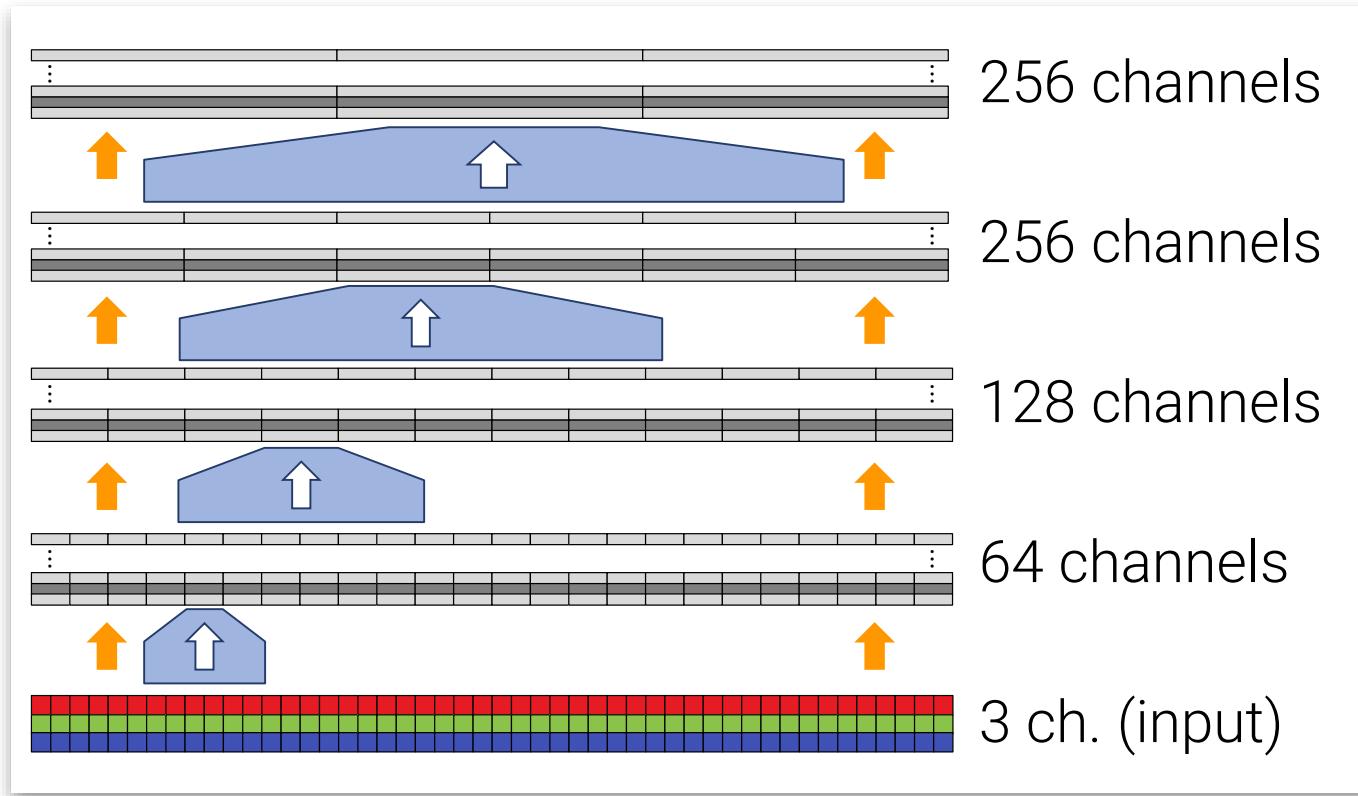


Convolution with stride
reduce resolution, learned filters



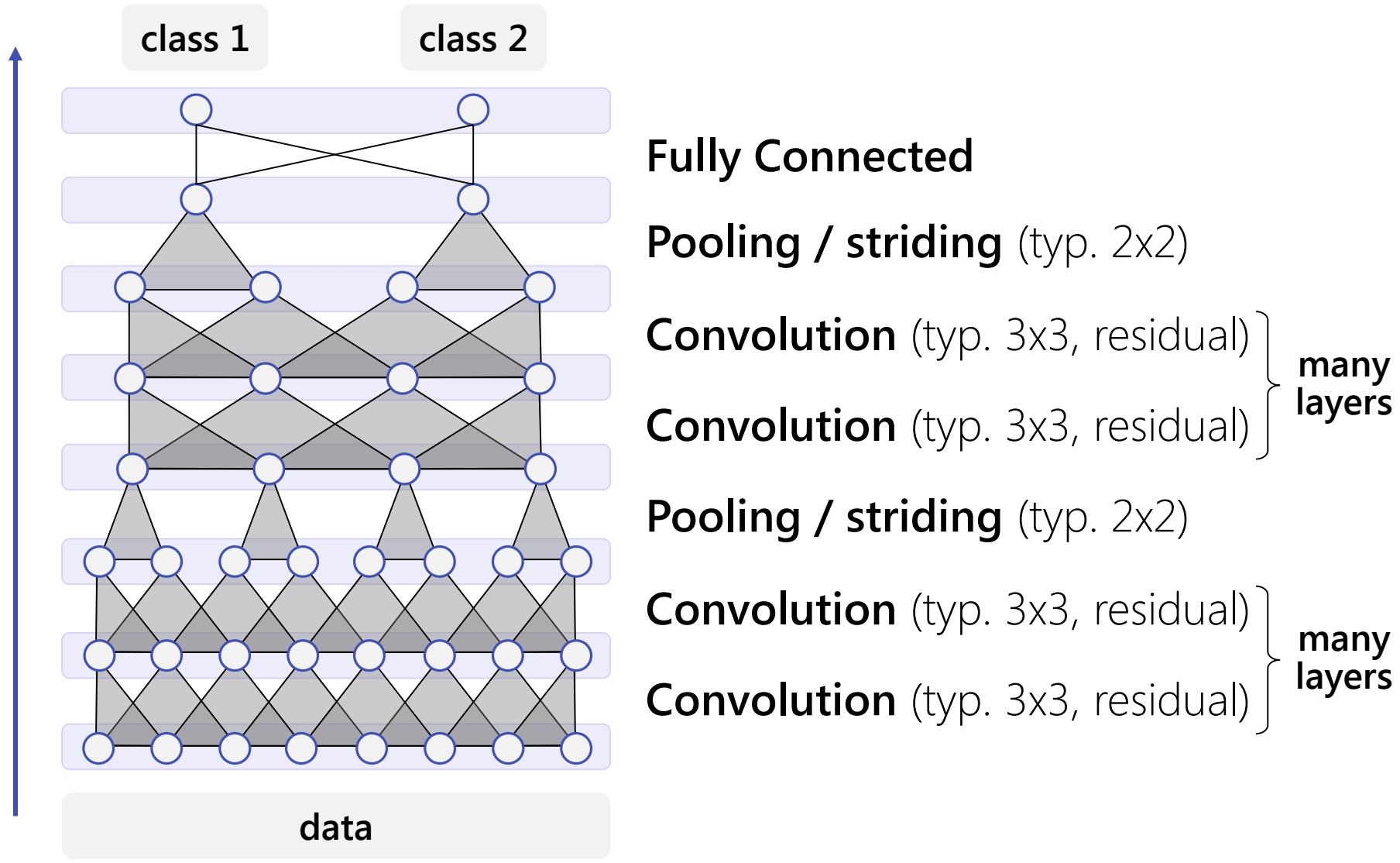
Dilated networks
aggregate context, same resolution

Typical ConvNet

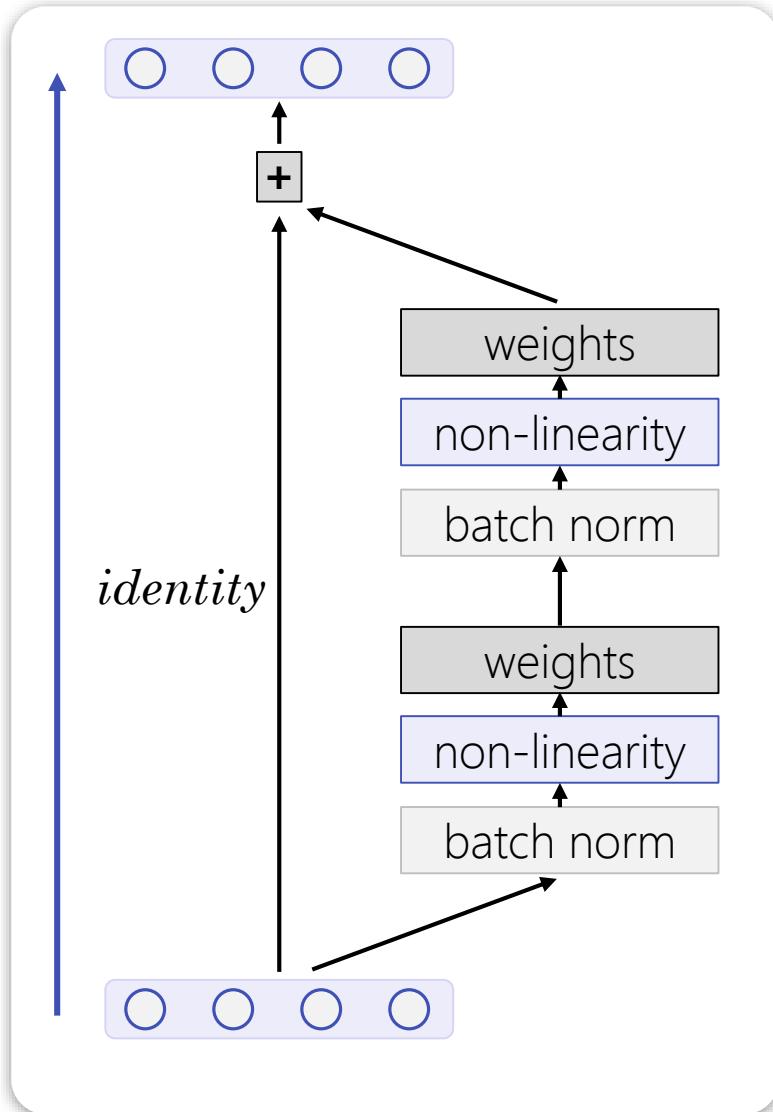


Coarse Graining
(model correlations at different scales)

Image Classification



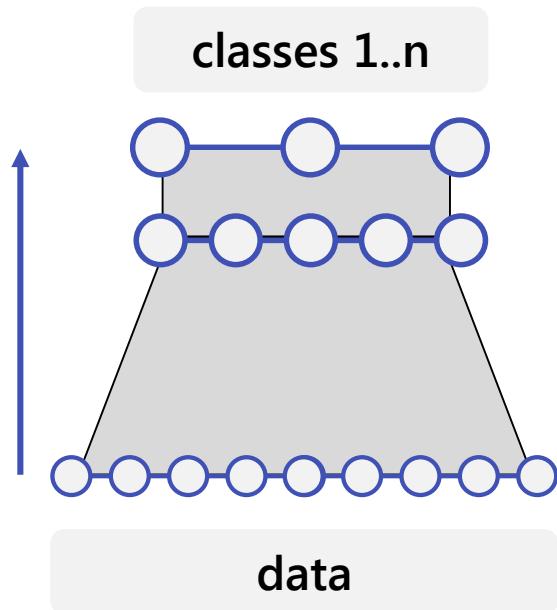
Architectural Building Blocks



Residual networks

Allows very deep networks
Identity mapping as default

Image Classification



Fully connected

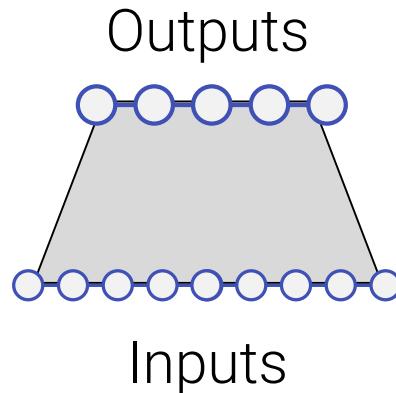
(typ. global av. pooling + 1 layer)

Convolution + pooling or striding

(typ. 20-100 layers)

Central Building Block: Regression

Trained with Examples



$\text{Prediction} \in \mathbb{R}^m$

General Regressor

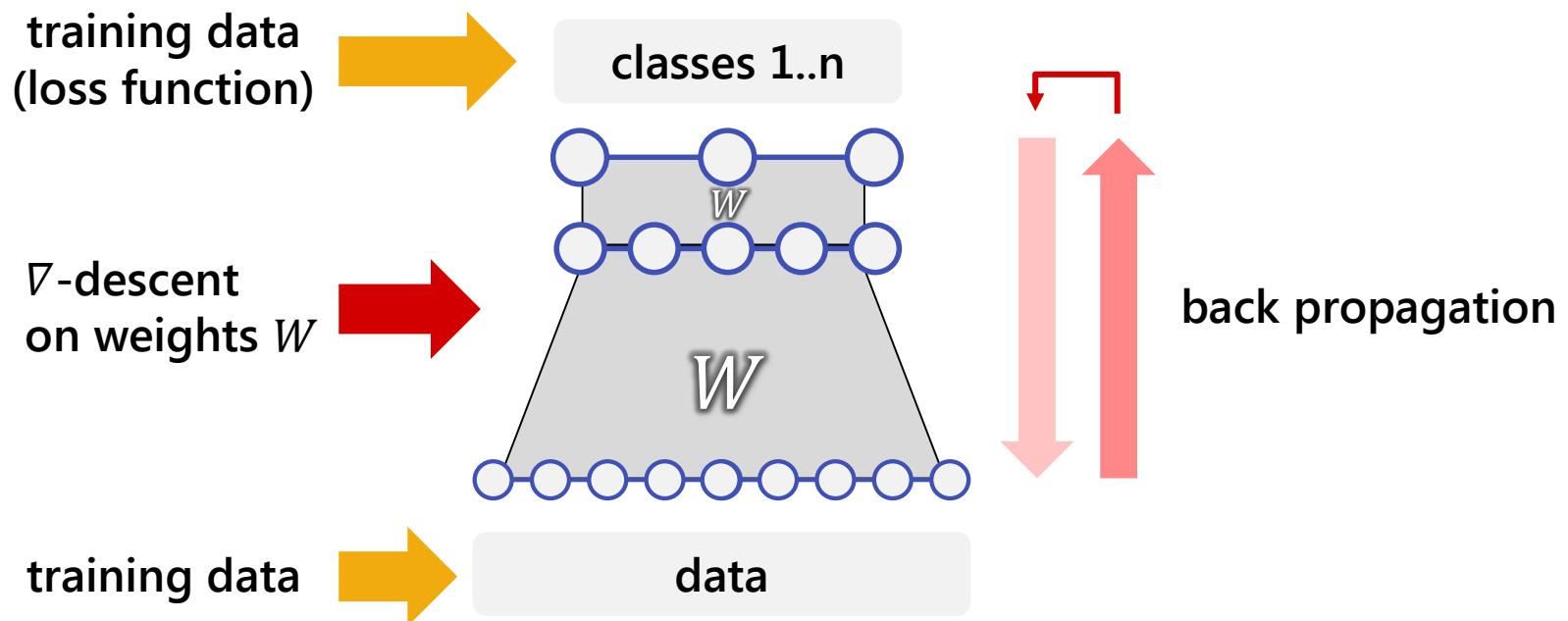
$\text{Data} \in \mathbb{R}^n$

maps
data to data

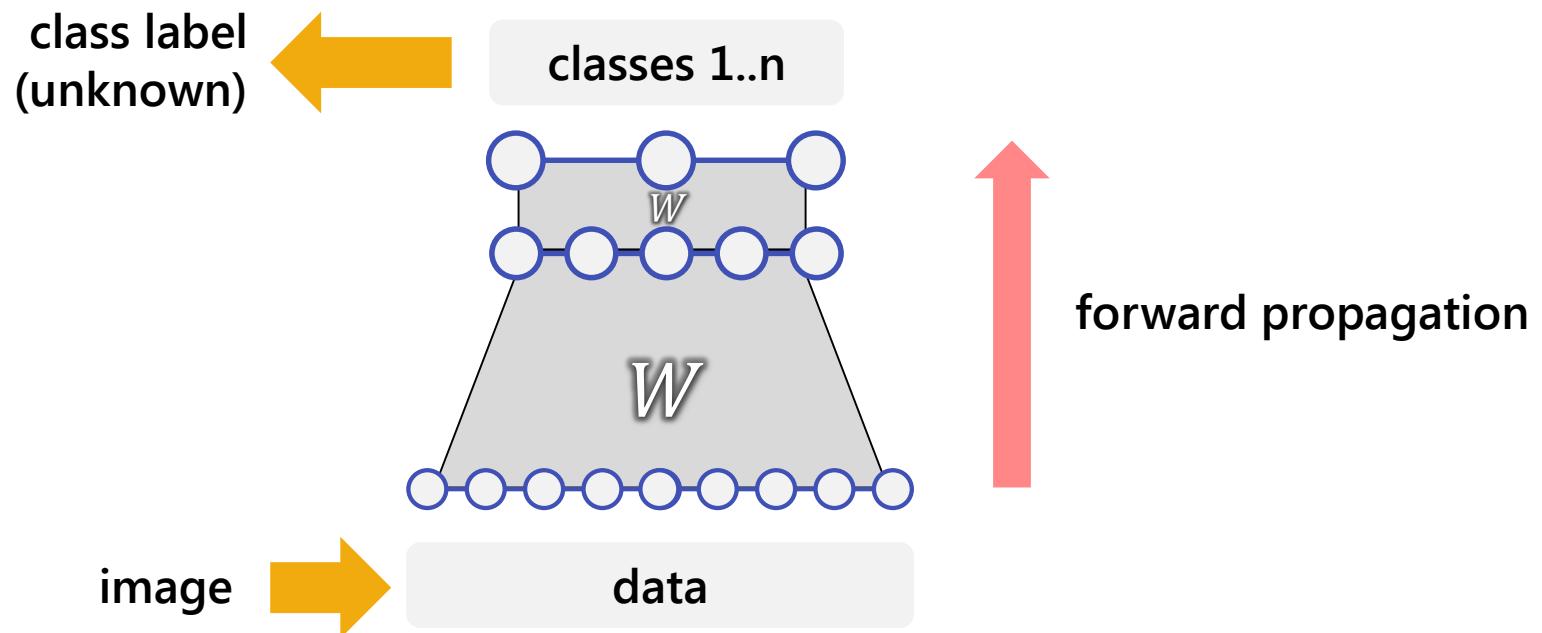
usually
excellent generalization
(not clear why)

Training & Inference

Discriminative Training



Inference



Loss Function

Notation

- Neural network f , weights \mathcal{W} , input \mathbf{x} , output \mathbf{y}
- Supervised, training data: $(\mathbf{x}_i, \mathbf{y}_i)_{i=1..n}$
- $f_{\mathcal{W}}(\mathbf{x}) = \mathbf{y}$

Different Loss Functions

Regression:

- Least squares $(f_W(\mathbf{x}_i) - \mathbf{y}_i)^2$

Classification

- One-Hot-Vectors \mathbf{y}_i
- Cross Entropy:

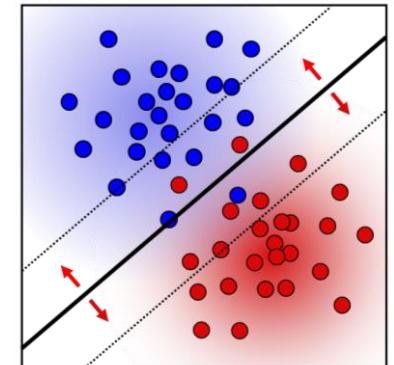
$$H(\text{softmax}(f_W(\mathbf{x}_i)), \mathbf{y}_i)$$

Softmax:

$$\text{softmax}(\mathbf{y}) = \begin{pmatrix} \frac{e^{-\mathbf{y}_1}}{\sum_{i=1}^n e^{-\mathbf{y}_i}} \\ \vdots \\ \frac{e^{-\mathbf{y}_n}}{\sum_{i=1}^n e^{-\mathbf{y}_i}} \end{pmatrix}$$

- Max-Margin:

$$\text{margin}(f_W(\mathbf{x}_i), \mathbf{y}_i)$$



Cross Entropy as Maximum-Likelihood

$$\arg \min_W KL(\mathbf{y}_i \parallel f_{\mathcal{W}}(\mathbf{x}_i)) \quad \xleftarrow{\text{Cross-Entropy Loss}}$$

$$= \arg \min_W \sum_{k=1}^{n_l} [\mathbf{y}_i]_k \log_2 \frac{[\mathbf{y}_i]_k}{[f_{\mathcal{W}}(\mathbf{x}_i)]_k}$$

$$= \arg \min_W \left(H(\mathbf{y}_i, f_{\mathcal{W}}(\mathbf{x}_i)) - H(\mathbf{y}_i) \right)$$

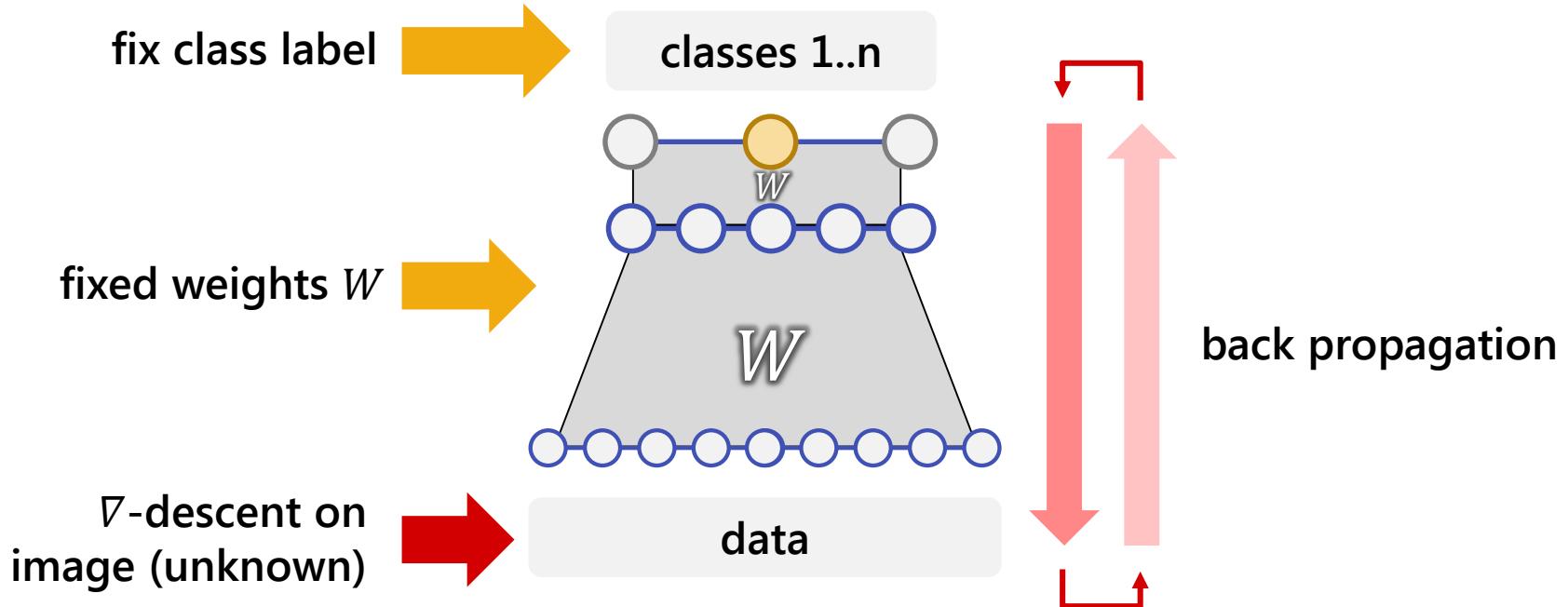
$$= \arg \min_W \left(H(\mathbf{y}_i, f_{\mathcal{W}}(\mathbf{x}_i)) \right)$$

$$= \arg \min_W \sum_{k=1}^{n_l} [\mathbf{y}_i]_k \log_2 [f_{\mathcal{W}}(\mathbf{x}_i)]_k$$

$$= \arg \min_W \log_2 [f_{\mathcal{W}}(\mathbf{x}_i)]_{k=l_i} \quad \xleftarrow{\text{Class likelihood (maximization)}}$$

Variational Inversion

Variational Inversion





Google's „Deep Dream (Inceptionism)“ Algorithms

Image: Daniel Strecker



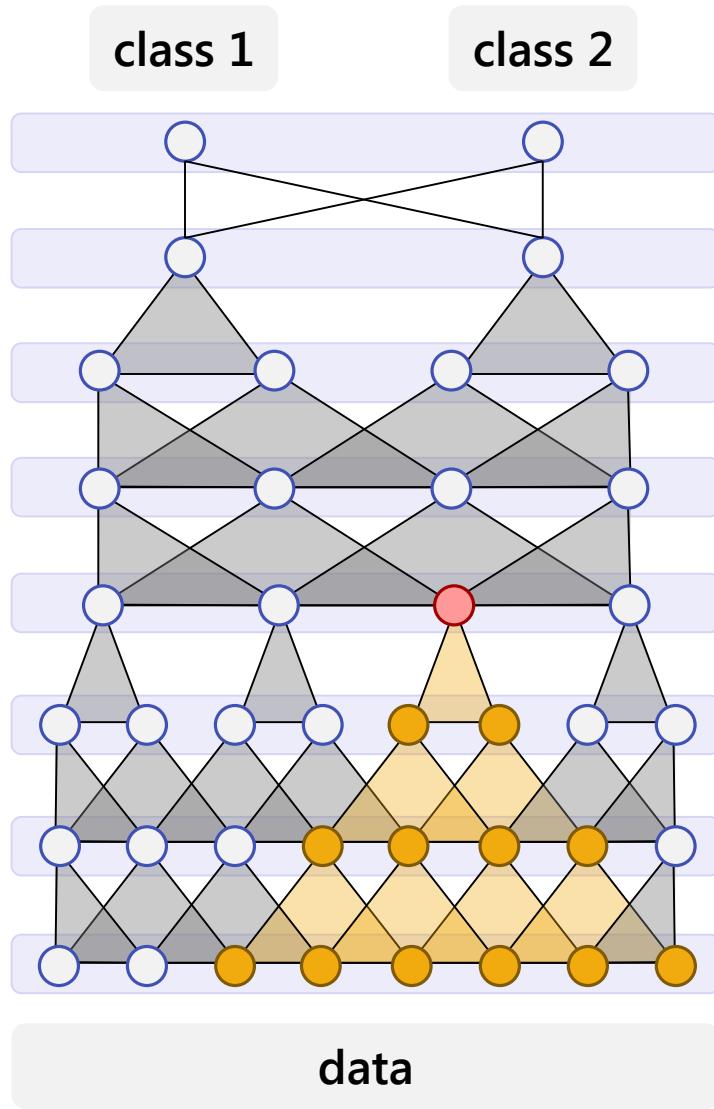
Google's „Deep Dream (Inceptionism)“ Algorithms

Image: Daniel Strecke

Better Generative Image Models

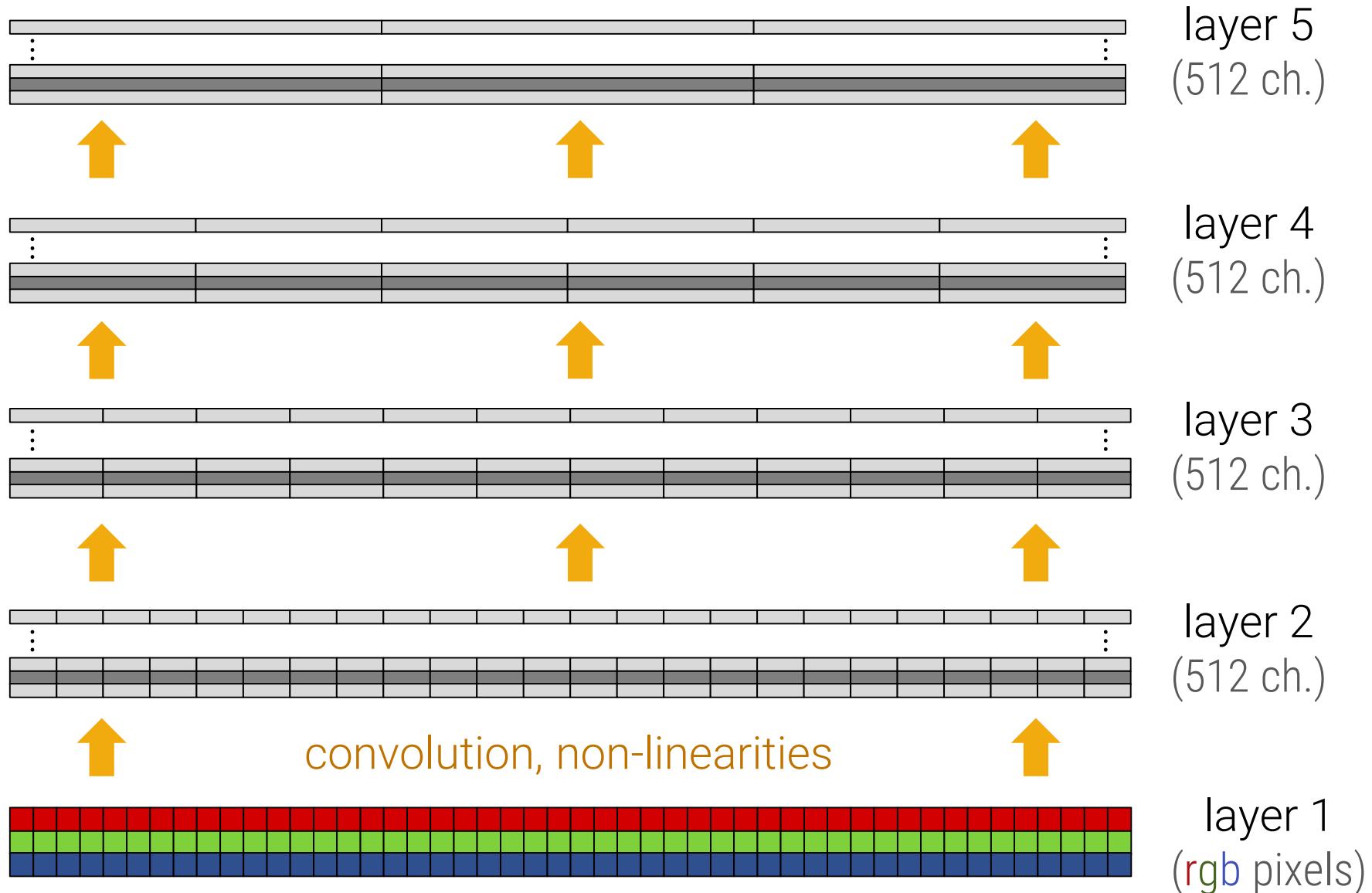
Convnets?

MRF Model is Build-In

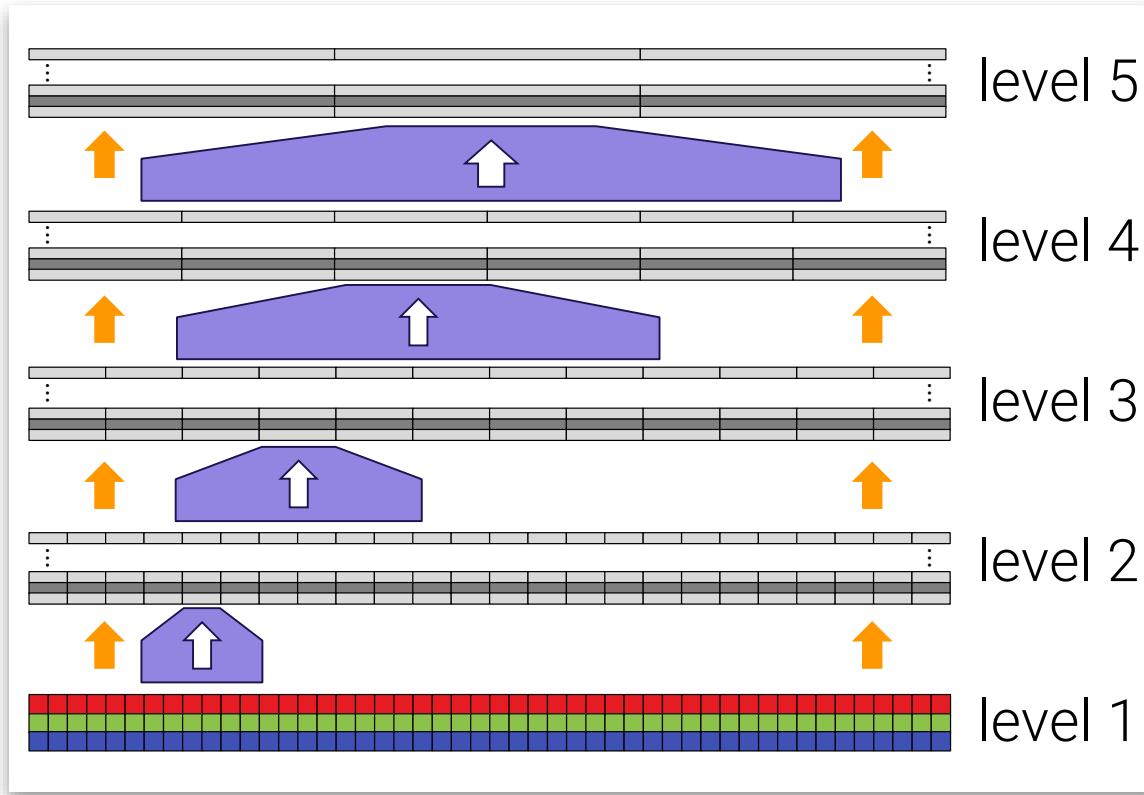


← **ConvNets** are
Markovian

VGG-Network (Discriminative!)

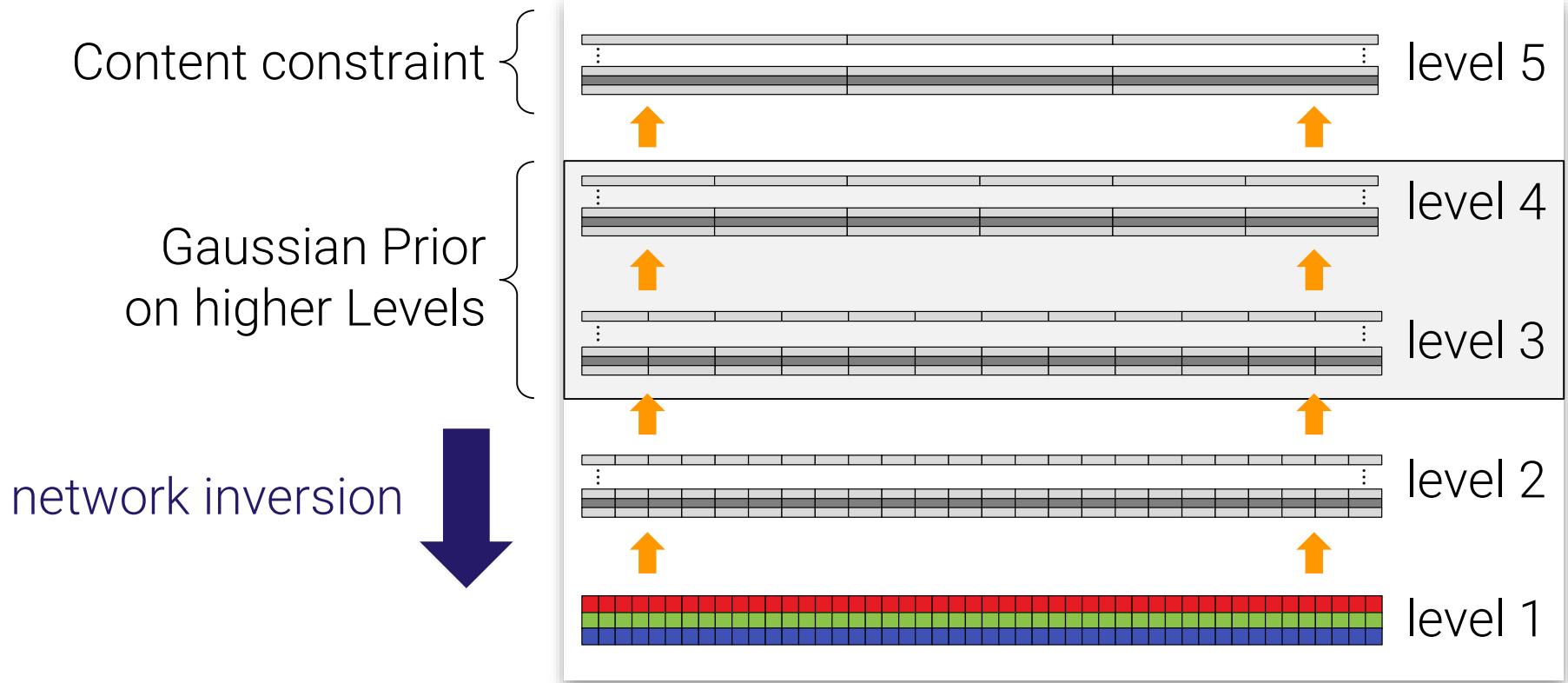


Discriminative Network



Coarse Graining
(model correlations at different scales)

High-Level Content Control



Picasso

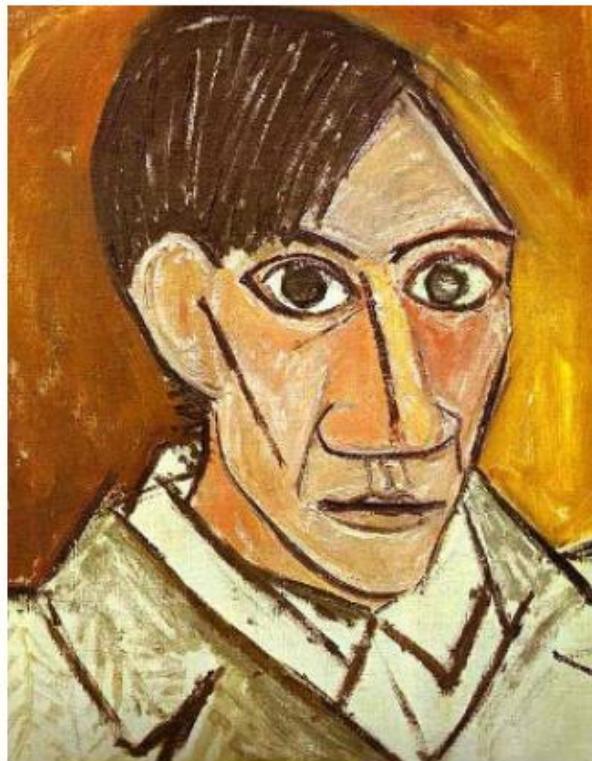


image sources: flickr user Christopher Michel, Pablo Picasso (self-portrait 1907)

Picasso



That was cute.
How do we get it right?

Learning generative models

Wishlist

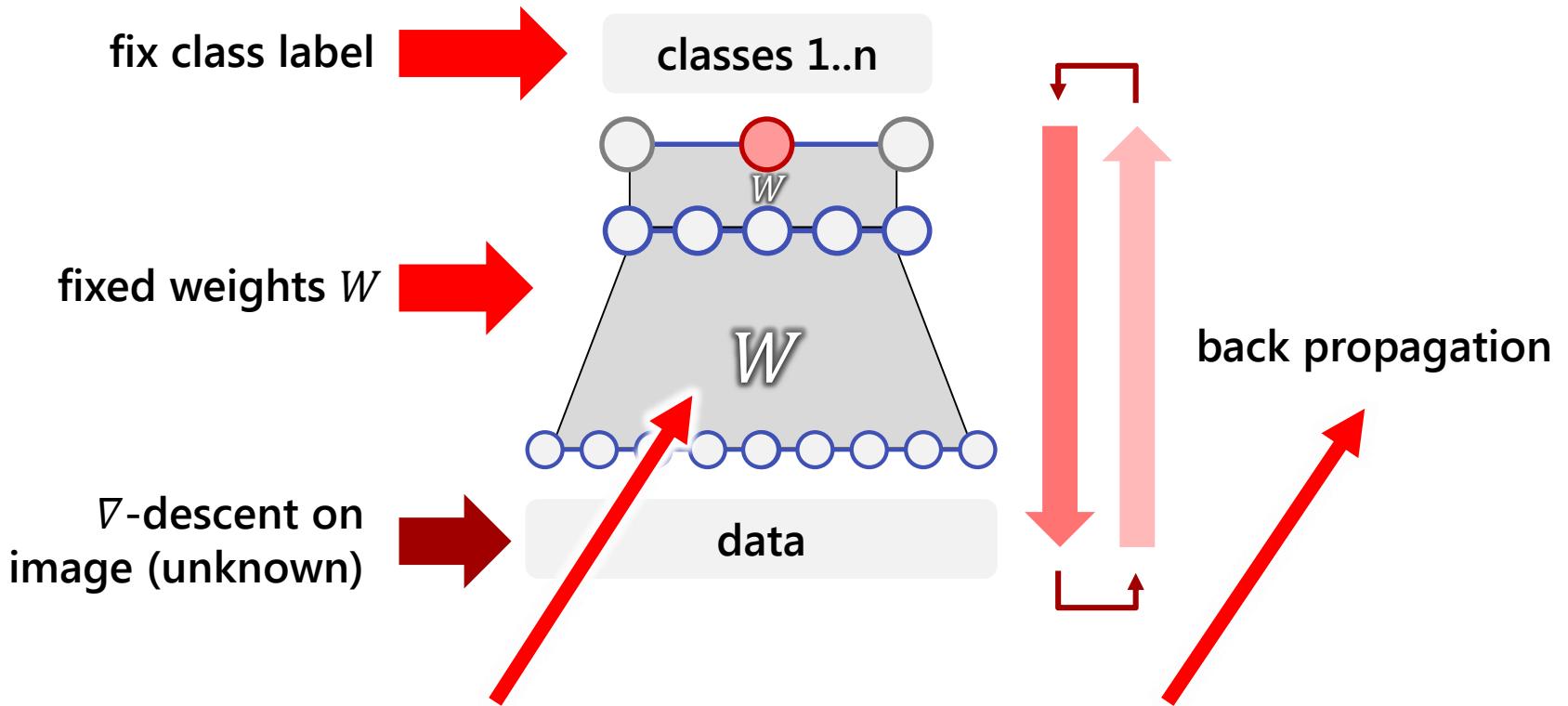
- Generalization
 - Broad object class rather than single image
 - "Faces", "Dogs", "Living Room Scenes"
- Explicit generative statistical model

Technical options

- (Variational) Autoencoders
- Generative adversarial networks

Generative Networks

So Far: Variational Inversion



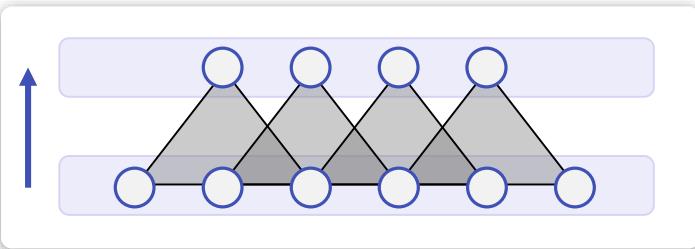
pretrained for
image classification!

(why should we do this?)

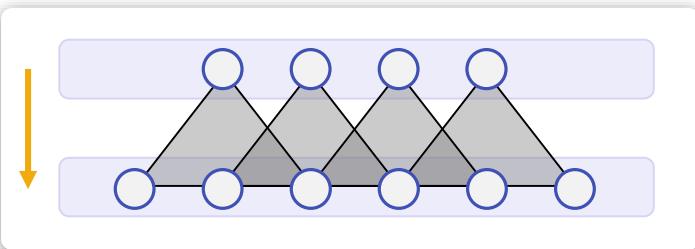
variational optimization
very expensive

(~2min for 256^2 pix)

How to Create the Data?

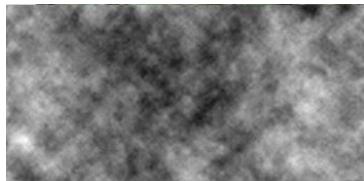


Convolutional network
Discriminative network



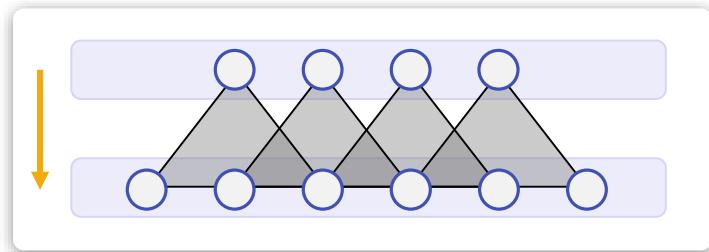
Convolutional network
Generative network

How to Create the Data?



Input

(for example noise)



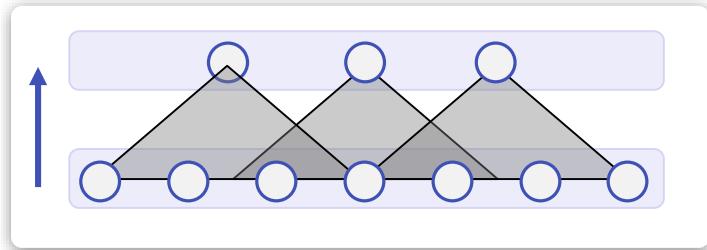
Convolutional network
Generative network



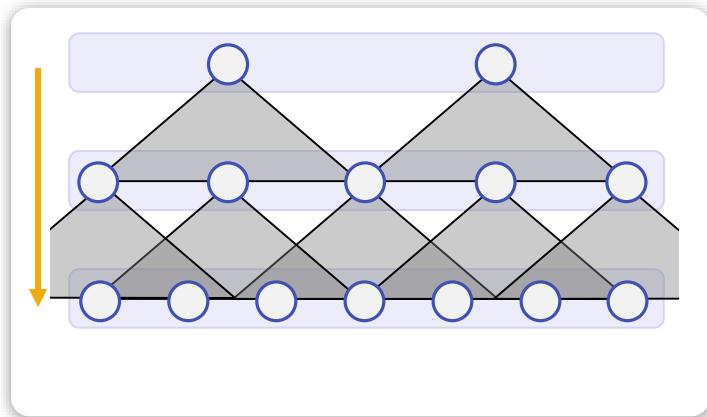
Synthesis

(after many layers...)

How to Create the Data?



Convolution with stride
(un)-pooling effect

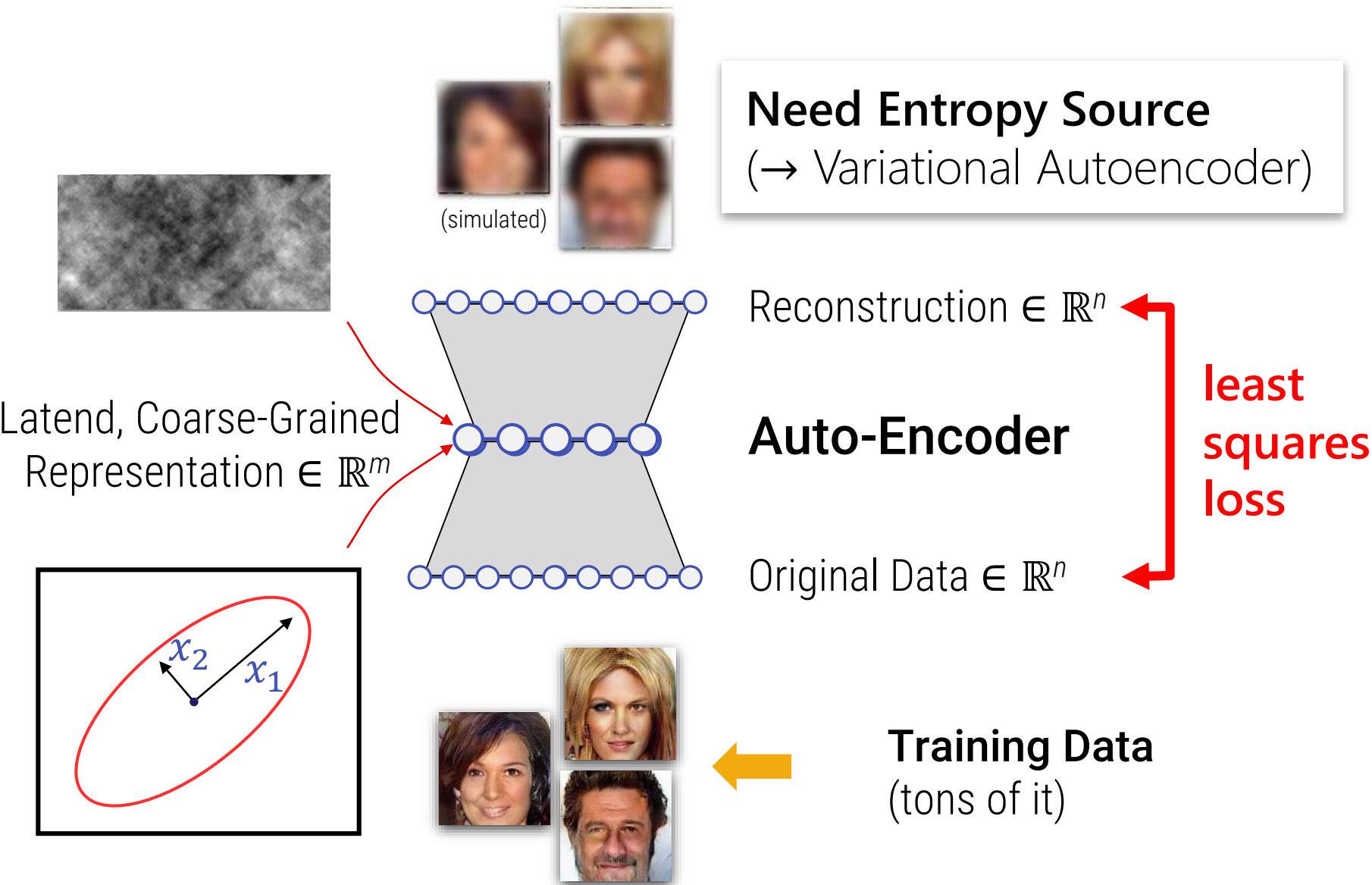


Fully convolution generator
many layers
some with stride

Great! How do we train it?

Autoencoder

Auto-Encoder: Non-linear PCA



Nature: Correlated Noise



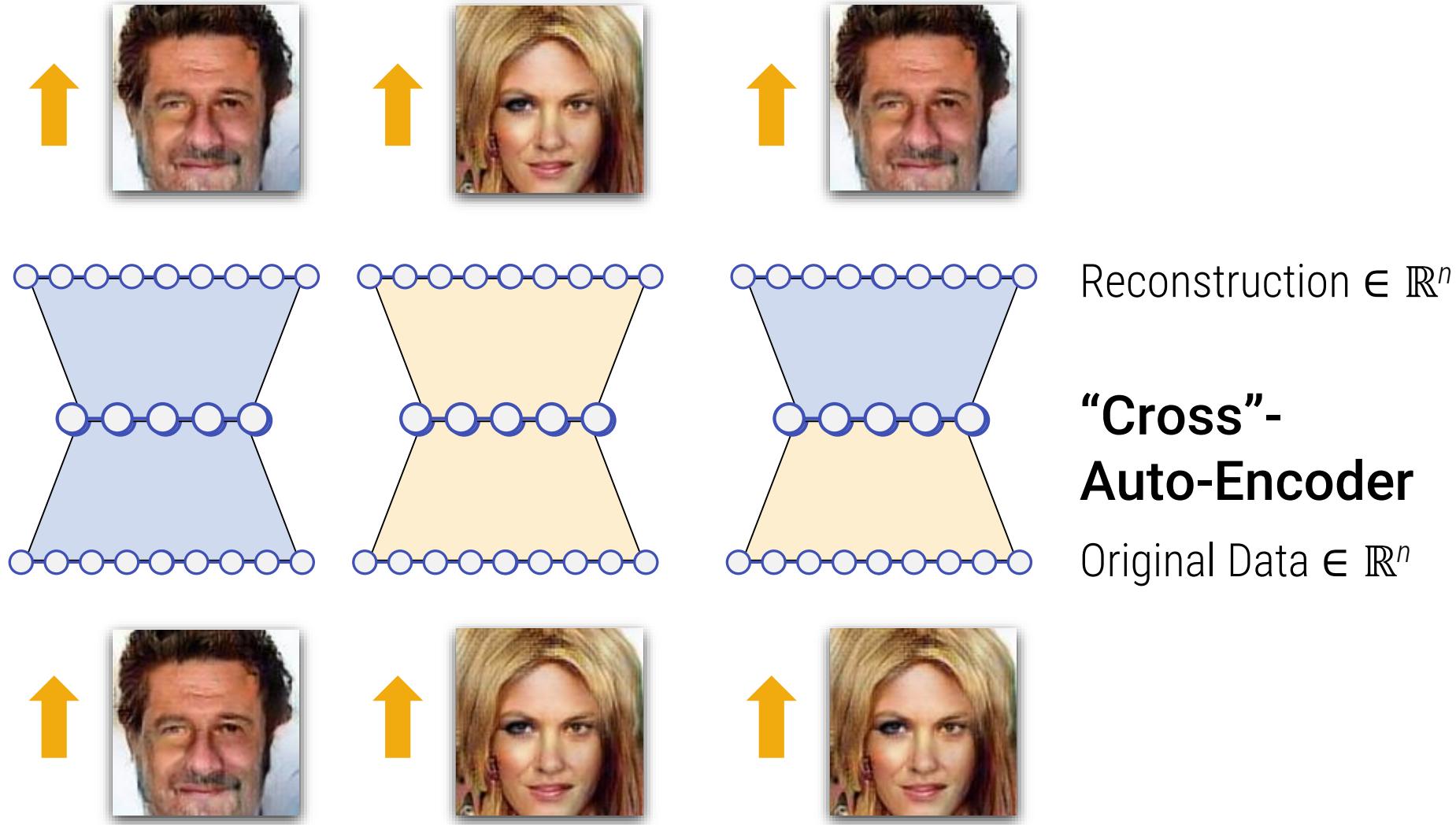
Samples

[CelebA data set]

Natural phenomena

- Most of the information (entropy) is noise
- Correlated noise, not independent pixel noise

Cross Auto-Encoder

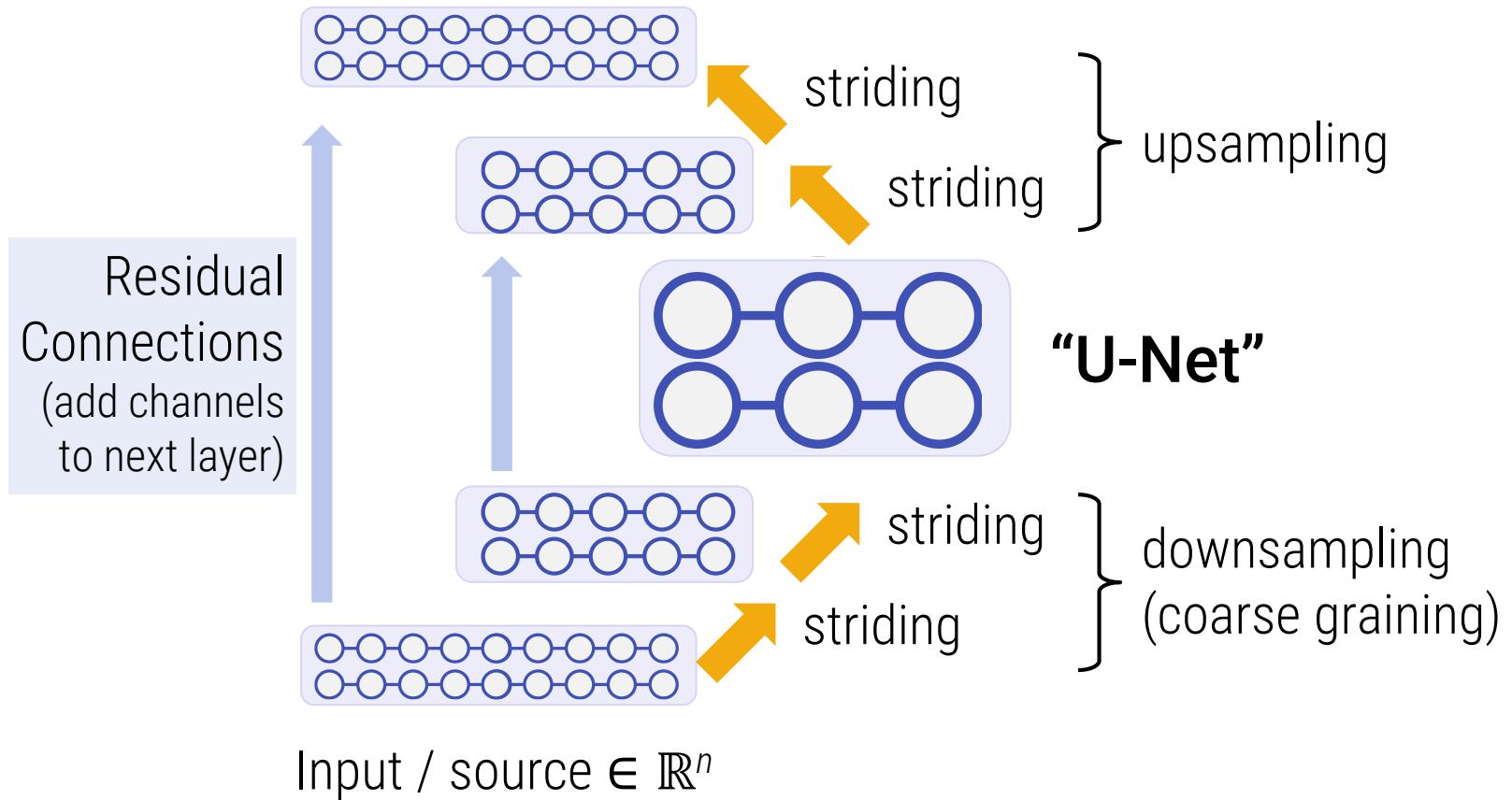


“Deep Fakes”

https://www.reddit.com/r/SFWdeepfakes/comments/7tcddy/nicolas_cage_deepfaked_into_superman/

U-Net

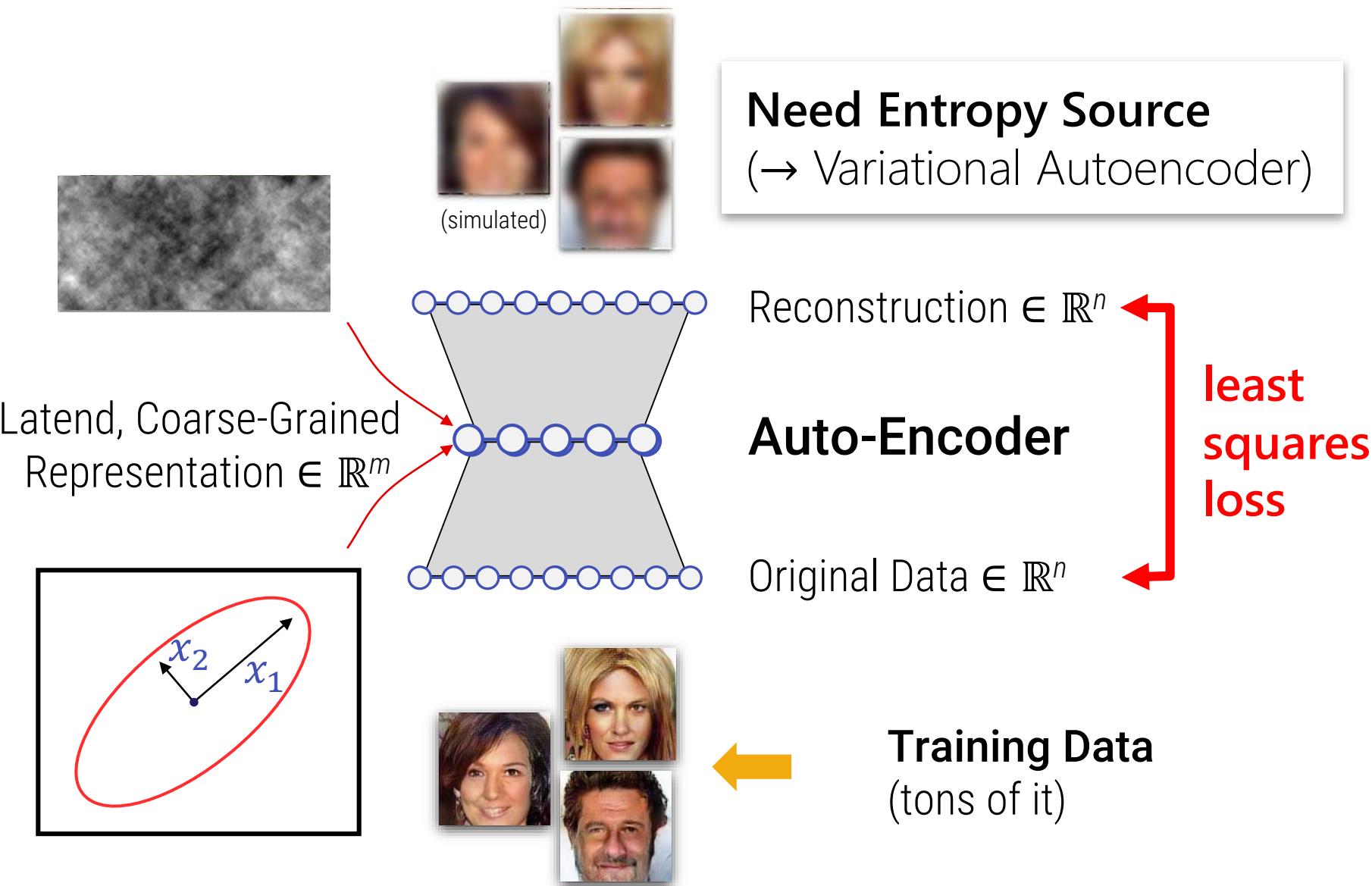
Regression target $\in \mathbb{R}^n$



Example: Segmentation

<https://towardsdatascience.com/training-road-scene-segmentation-on-cityscapes-with-supervised-tensorflow-and-unet-1232314781a8>

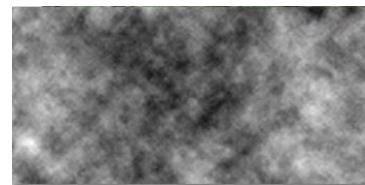
Auto-Encoder: Non-linear PCA



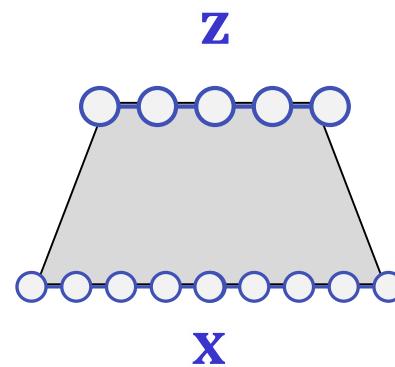
Probabilistic Generative Models

Learning Schemes

Gaussian Noise $\in \mathbb{R}^m$

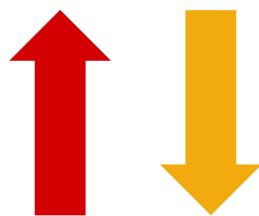


Original Data $\in \mathbb{R}^n$



**Generative
Network**

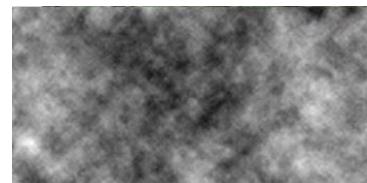
Training Data



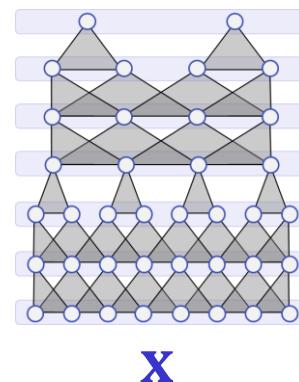
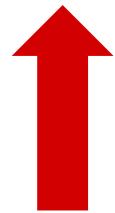
New Samples

Learning Schemes

Gaussian Noise $\in \mathbb{R}^m$



Original Data $\in \mathbb{R}^n$



**Generative
Network**

Training Data

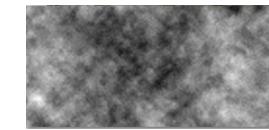
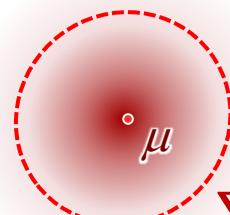


New Samples

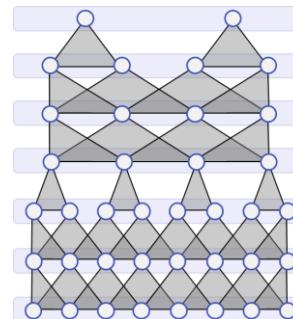
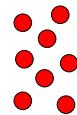
Learning Schemes

Gaussian Noise $\in \mathbb{R}^m$

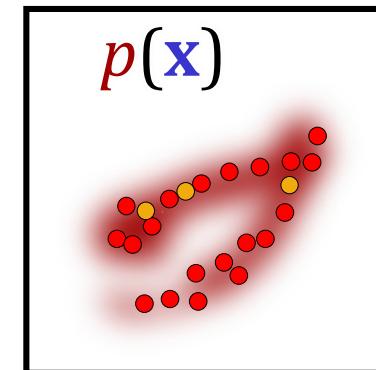
$$N_{\mathbf{0}, \mathbf{I}}(\mathbf{z})$$



Original Data $\in \mathbb{R}^n$



\mathbf{x}



**Generative
Network**

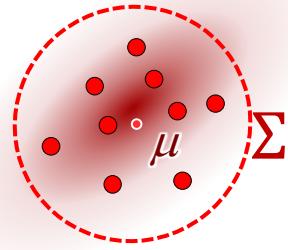


Training Data

New Samples

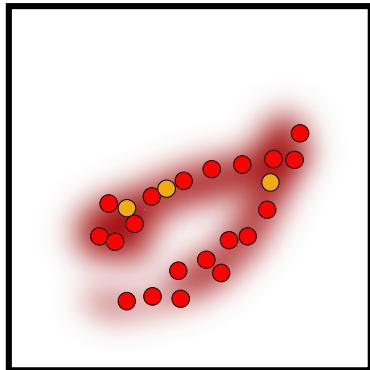
Problem: Need Normalized Density!

$$N_{\mu, \Sigma}(\mathbf{z})$$

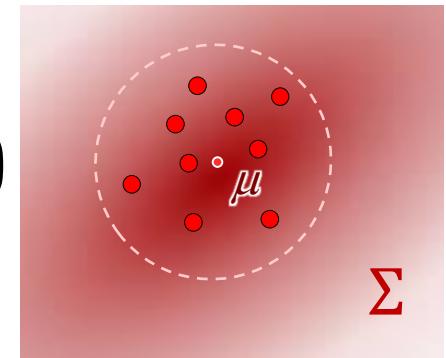


correct
(normalized)

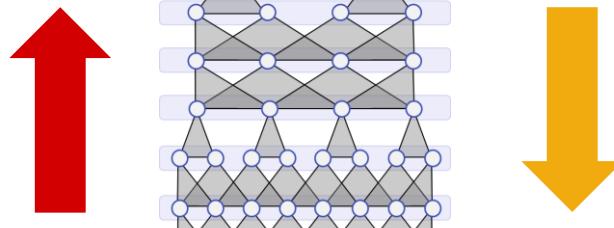
$$p(\mathbf{x})$$



$$N_{\mu, \Sigma}(\mathbf{z})$$

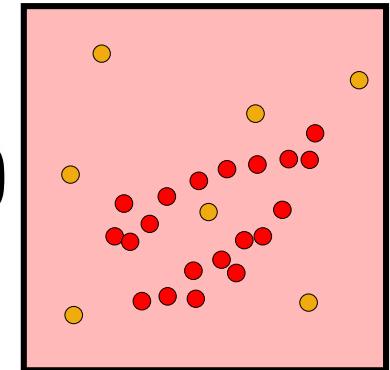


incorrect
(unnormalized)



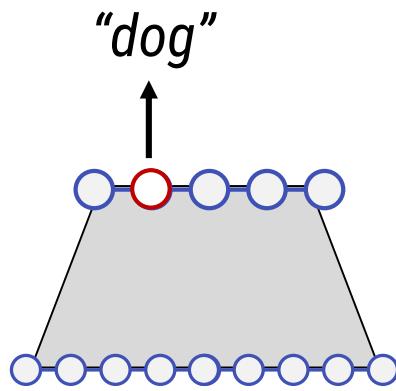
Problems:
inversion
difficult
normalization
intractable

$$p(\mathbf{x})$$



Generative Adversarial Networks (GANs)

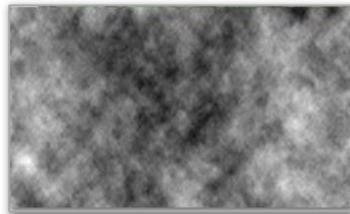
Learning Schemes



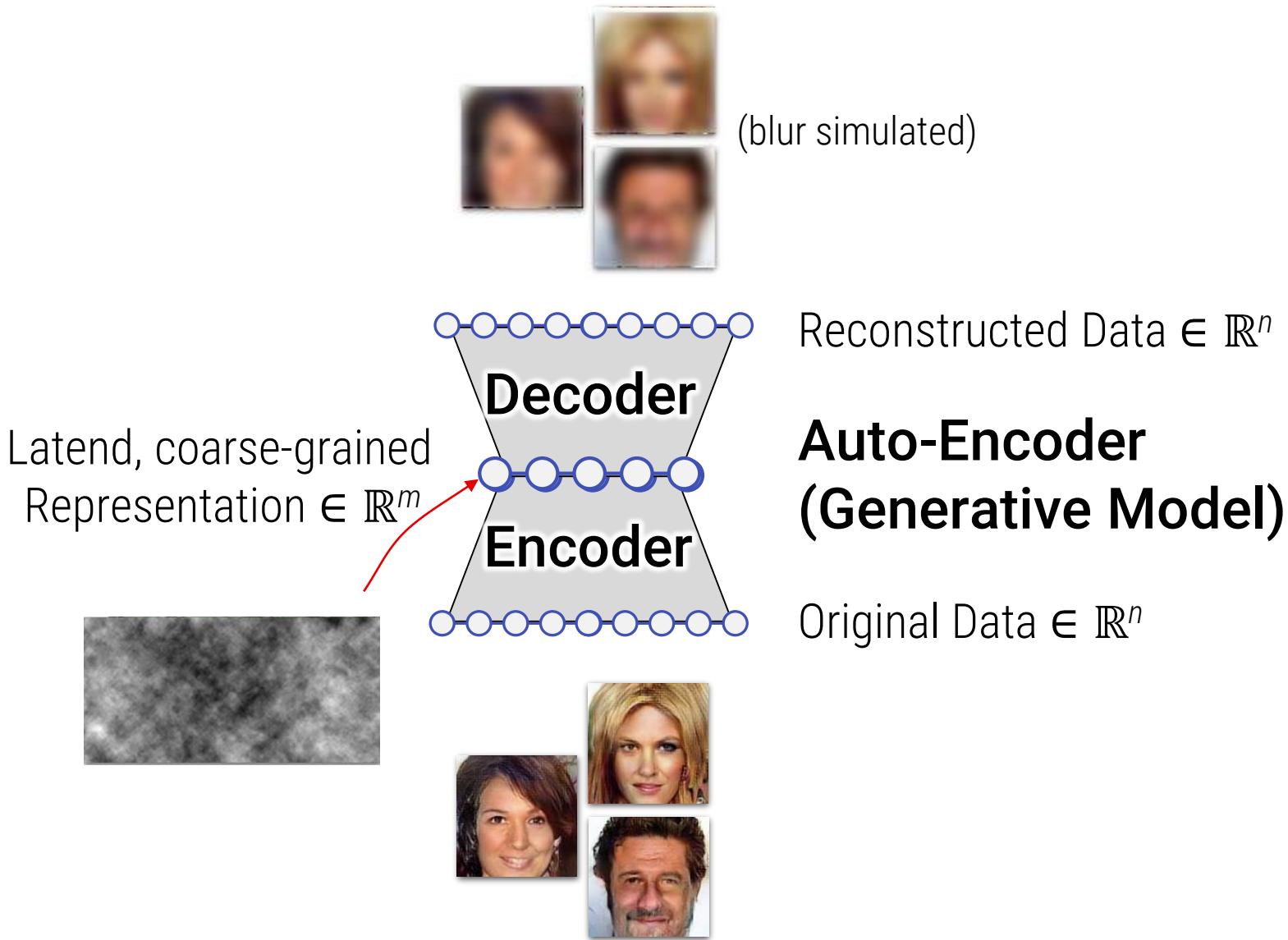
Labels, e.g. [cat?, dog?, bunny?] $\in [0,1]^m$

Discriminator

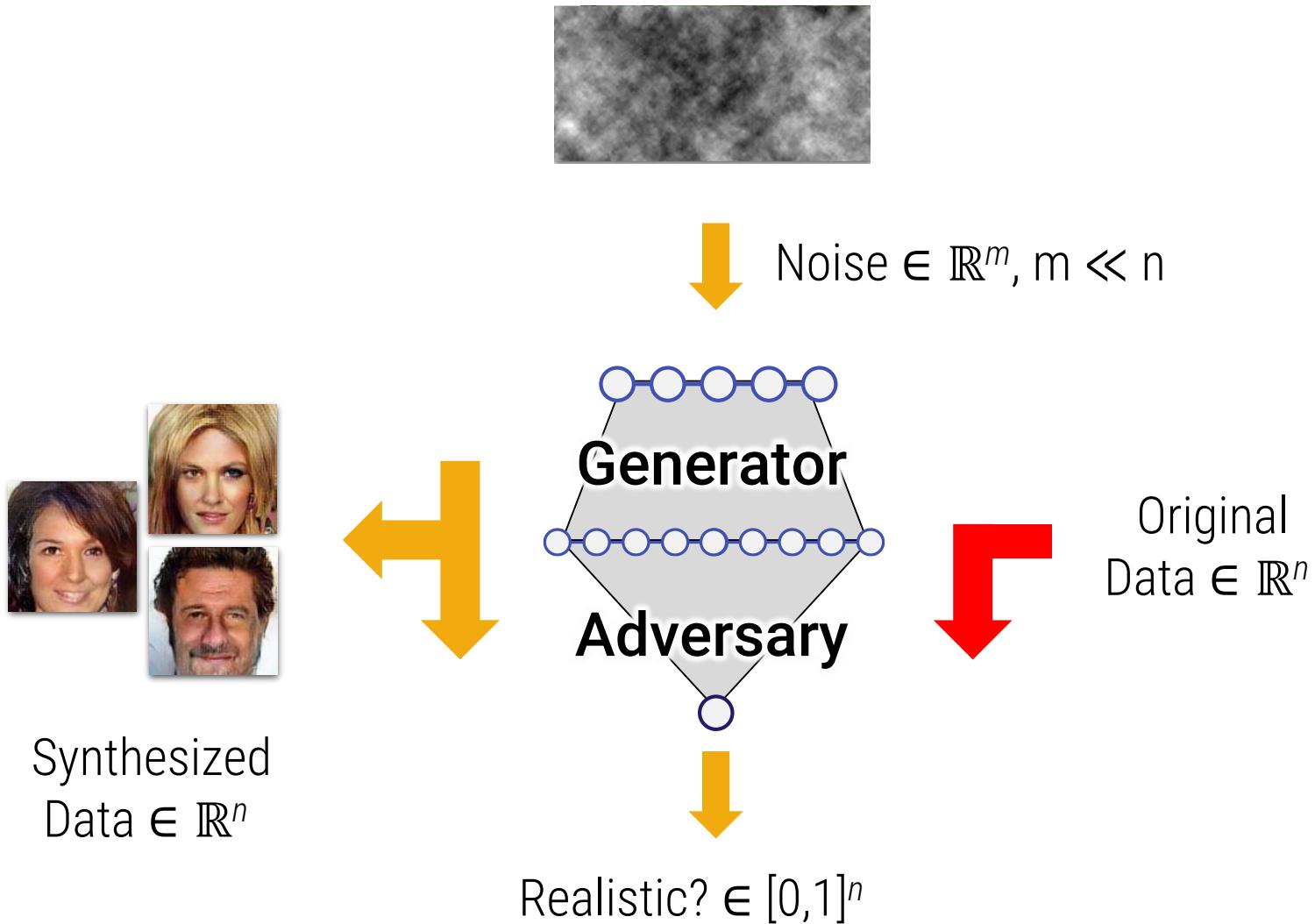
Data $\in \mathbb{R}^n$



Learning Schemes



Learning Schemes



Optimization

Training

- Discriminator tries to distinguish **real** / **fake**
 - Maximize prediction accuracy
- Generator tries to fool discriminator
 - Minimizes prediction accuracy
- Minimax game
- Nash equilibrium at true distribution

Issues

- Gradient descent instead of min-max
- Training unstable

Mode Collapse Problem

Good result
(W-DCGAN)

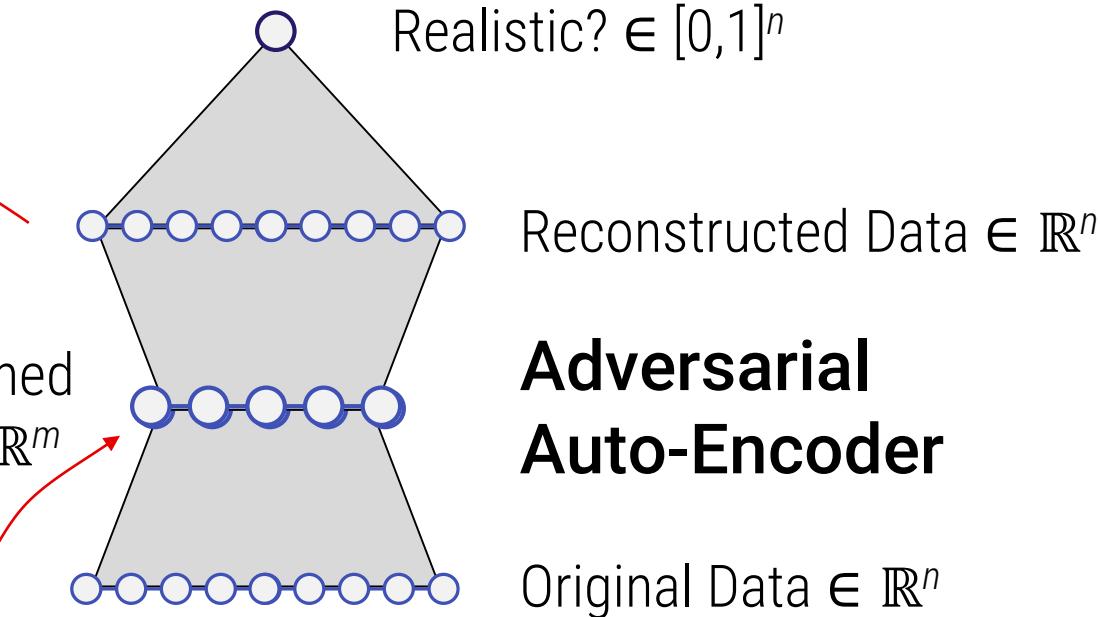
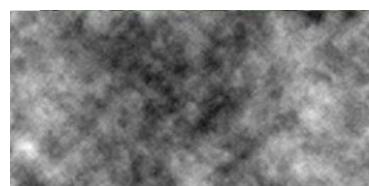
Mode collapse
(Std. GAN)

Results from [Arjovsky et al. 2017]

Simple Solution

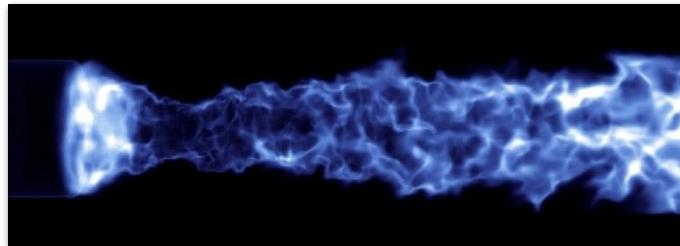


Latend, Coarse-Grained
Representation $\in \mathbb{R}^m$



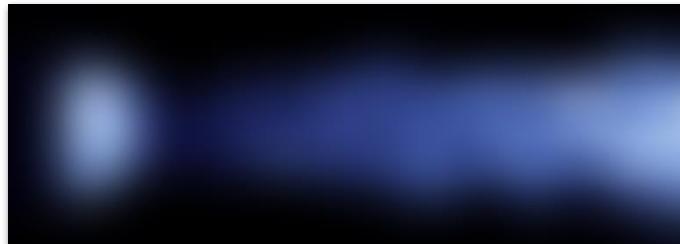
**Adversarial
Auto-Encoder**

Learning Schemes



Details

Latent, Coarse-Grained
Representation $\in \mathbb{R}^m$



Coarse Phenomenon

Realistic? $\in [0,1]^n$

Reconstructed Data $\in \mathbb{R}^n$

**Adversarial Auto-Encoder
(Unexplained Entropy)**

Original Data $\in \mathbb{R}^n$

MGANs: Noise → Images



[MGANs: Chuan Li; Training data: CelebA, University of Hong Kong]